Comodels as a gateway for interacting with the external world

Danel Ahman

(joint work with Andrej Bauer)

Comodels as a gateway for interacting with the external world

Danel Ahman

(joint work with Andrej Bauer)



Shonan, 28 March 2019



Computational effects in FP

Computational effects in FP

• Using monads (as in HASKELL)

```
type St a = String \rightarrow (a, String)

f :: St a \rightarrow St (a,a)

f c = c >>= (\x \rightarrow c >>= (\y \rightarrow return (x,y)))
```

• Using alg. effects and handlers (as in Eff, Frank, Koka)

```
effect Get : int effect Put : int \rightarrow unit (*: int \rightarrow a*int!\{\} *) let g (c:unit \rightarrow a!{Get,Put}) = with st_h handle (perform (Put 42); c ())
```

Computational effects in FP

• Using monads (as in HASKELL)

```
type St a = String \rightarrow (a, String)
f :: St a \rightarrow St (a,a)
f c = c >>= (\x \rightarrow c >>= (\y \rightarrow return (x,y)))
```

• Using alg. effects and handlers (as in Eff, Frank, Koka)

```
effect Get : int effect Put : int \rightarrow unit (*: int \rightarrow a*int!\{\} *) let g (c:unit \rightarrow a!{Get,Put}) = with st_h handle (perform (Put 42); c ())
```

Both are good for faking comp. effects in a pure language!
 But what about effects that need access to the external world?

• Declare a **signature** of monads or algebraic effects

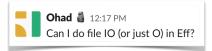
```
type IO a  \begin{array}{llll} & & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ &
```

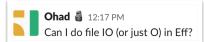
```
effect Raise : string \rightarrow empty

effect RandomInt : int \rightarrow int
effect RandomFloat : float \rightarrow float
```

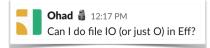
• And then treat them **specially** in the compiler, e.g.,

```
let rec top_handle op =
  match op with
  | ...
```









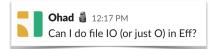


Ohad 38:35 PM
So here's the hack I added We should do something a bit more principled
In pervasives.eff:

in eval.ml, under let rec top_handle op = add the case:

effect Write : (string*string) -> unit

in eval.ml, under let rec top_handle op = add the case:



Ohad 🎒 8:35 PM



```
So here's the hack I added We should do something a bit more principled
In pervasives.eff:
 effect Write : (string*string) -> unit
in eval.ml, under let rec top_handle op = add the case:
     | "Write" ->
        (match v with
         | V.Tuple vs ->
            let (file_name :: str :: _) = List.map V.to_str vs in
            let file_handle = open_out_gen
                                 FOpen_wronly
                                 ;Open_append
                                 ;Open_creat
                                 :Open_text
                                 7 0o666 file name in
            Printf.fprintf file_handle "%s" str;
            close_out file_handle;
            top_handle (k V.unit_value)
```

This talk — a principled (co)algebraic approach!

• let f (s:string) =
 let fh = fopen "foo.txt" in
 fwrite fh (s^s);
 fclose fh;
 return fh

let g s =
 let fh = f s in fread fh

• let f (s:string) =
 let fh = fopen "foo.txt" in
 fwrite fh (s^s);
 fclose fh;
 return fh

let g s =
 let fh = f s in fread fh (* fh not open ! *)

```
• let f (s:string) =
    let fh = fopen "foo.txt" in
    fwrite fh (s^s);
    fclose fh;
    return fh

let g s =
    let fh = f s in fread fh (* fh not open! *)
```

• Even worse when we wrap f in a handler?

```
let h = handler | effect (FWrite fh s k) \rightarrow return () let g' s = with h handle f ()
```

```
• let f (s:string) =
   let fh = fopen "foo.txt" in
   fwrite fh (s^s);
   fclose fh;
   return fh

let g s =
   let fh = f s in fread fh (* fh not open! *)
```

• Even worse when we wrap f in a handler?

```
let h = handler | effect (FWrite fh s k) \rightarrow return ()

let g' s = with h handle f () (* dangling fh ! *)
```



So, how could we solve these issues?

- We could try using existing PL techniques, e.g.,
 - Modules and abstraction, e.g., System.IO

• Linear (and non-linear) types and effects

```
linear type fhandle  {\bf effect} \ \ {\sf FClose} \ : \ ({\bf linear} \ \ {\sf fhandle}) \to {\sf unit}   {\bf linear} \ \ {\bf effect} \ \ {\sf FClose} \ : \ {\sf fhandle} \to {\sf unit}
```

• Handlers with **finally clauses**

So, how could we solve these issues?

- We could try using existing PL techniques, e.g.,
 - Modules and abstraction, e.g., System.IO

• Linear (and non-linear) types and effects

```
linear type fhandle  {\bf effect} \ \ {\sf FClose} \ : \ ({\bf linear} \ \ {\sf fhandle}) \to {\sf unit}   {\bf linear} \ \ {\bf effect} \ \ {\sf FClose} \ : \ {\sf fhandle} \to {\sf unit}
```

- Handlers with **finally clauses**
- Problem: They don't really capture the essence of the problem



• Let's look at HASKELL's IO monad again

- Let's look at HASKELL's IO monad again
- A common explanation is to think of functions

$$a \rightarrow IO b$$

as

$$\mathsf{a} \to (\mathsf{RealWorld} \to (\mathsf{b}, \mathsf{RealWorld}))$$

which is the same as

$$(a, RealWorld) \rightarrow (b, RealWorld)$$

- Let's look at HASKELL's IO monad again
- A common explanation is to think of functions

$$a \rightarrow IO b$$

as

$$\mathsf{a} \to (\mathsf{RealWorld} \to (\mathsf{b}, \mathsf{RealWorld}))$$

which is the same as

$$(a, RealWorld) \rightarrow (b, RealWorld)$$

- With the System.IO module abstraction ensuring that
 - We cannot get our hands on RealWorld (no get and put)
 - We have the impression of RealWorld used linearly
 - We don't ask more from RealWorld than it can provide

- Let's look at HASKELL's IO monad again
- A common explanation is to think of functions

$$a \rightarrow IO b$$

as

$$a \rightarrow (RealWorld \rightarrow (b, RealWorld))$$

which is the same as

$$(a, RealWorld) \rightarrow (b, RealWorld)$$

But wait a minute! RealWorld looks a lot like a comodel!

 $\mathsf{hGetLine} : (\mathsf{Handle}, \mathsf{RealWorld}) \to (\mathsf{String}, \mathsf{RealWorld})$

hClose : (Handle, RealWorld) \rightarrow ((), RealWorld)

Important: co-operations (hClose) make a promise to return!

• A signature Σ is a set of operation symbols op : $A \rightsquigarrow B$

- A **signature** Σ is a set of operation symbols op : $A \rightsquigarrow B$
- A model/algebra/handler \mathcal{M} of Σ is given by

$$\mathcal{M} = \langle M : \mathsf{Set} \ , \ \{ \mathsf{op}_{\mathcal{M}} : A \times M^B \longrightarrow M \}_{\mathsf{op} \in \Sigma} \ \rangle$$

- A **signature** Σ is a set of operation symbols op : $A \rightsquigarrow B$
- A model/algebra/handler $\mathcal M$ of Σ is given by

$$\mathcal{M} = \langle \ \mathit{M} : \mathsf{Set} \ , \ \{ \mathsf{op}_{\mathcal{M}} : \mathit{A} imes \mathit{M}^\mathit{B} \longrightarrow \mathit{M} \}_{\mathsf{op} \in \Sigma} \
angle$$

• A comodel/coalgebra/cohandler ${\mathcal W}$ of Σ is given by

$$\mathcal{W} = \langle W : \mathsf{Set} , \{ \overline{\mathsf{op}}_{\mathcal{W}} : A \times W \longrightarrow B \times W \}_{\mathsf{op} \in \Sigma} \rangle$$

• Intutively, comodels describe evolution of the world W

- A **signature** Σ is a set of operation symbols op : $A \rightsquigarrow B$
- A model/algebra/handler $\mathcal M$ of Σ is given by

$$\mathcal{M} = \langle \ \mathit{M} : \mathsf{Set} \ , \ \{ \mathsf{op}_{\mathcal{M}} : \mathit{A} imes \mathit{M}^\mathit{B} \longrightarrow \mathit{M} \}_{\mathsf{op} \in \Sigma} \
angle$$

• A comodel/coalgebra/cohandler W of Σ is given by

$$\mathcal{W} = \langle \ W : \mathsf{Set} \ , \ \{ \overline{\mathsf{op}}_{\mathcal{W}} : \mathsf{A} \times W \longrightarrow \mathsf{B} \times W \}_{\mathsf{op} \in \Sigma} \ \rangle$$

- Intutively, comodels describe evolution of the world W
 - Operational semantics using a tensor of a model and a comodel (Plotkin & Power, Abou-Saleh & Pattinson)
 - <u>Stateful runners</u> of effectful programs (Uustalu)
 - Linear state-passing translation (Møgelberg and Staton)
 - Top-level behaviour of alg. effects in EFF v2 (Bauer & Pretnar)

Now external world explicit, but dangling fh etc still possible

Now **external world** explicit, but **dangling** fh etc **still possible**

Better, but have to explicitly open and thread through fh

Now **external world** explicit, but **dangling** fh etc **still possible**

Better, but have to explicitly open and thread through fh

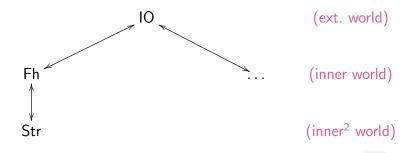
Solution: Modular treatment of external worlds

• Examples of **modularity** we might want from comodels



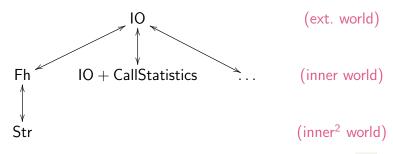
- Fh "world which consists of exactly one fh"
- ullet IO \longrightarrow Fh "call fopen with foo.txt, store returned fh"
- ullet Fh \longrightarrow IO "call fclose with stored fh"

• Examples of **modularity** we might want from comodels



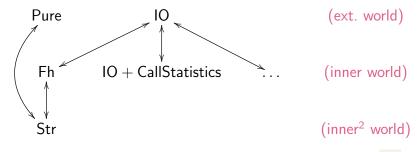
- Fh "world which consists of exactly one fh"
- Fh \longrightarrow IO "call fclose with stored fh"
- Str "world that is **blissfully unaware** of **fh**"

• Examples of **modularity** we might want from comodels



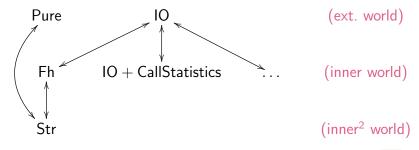
- Fh "world which consists of exactly one fh"
- Fh \longrightarrow IO "call fclose with stored fh"
- Str "world that is **blissfully unaware** of **fh**"

• Examples of **modularity** we might want from comodels



- Fh "world which consists of exactly one fh"
- Fh \longrightarrow IO "call fclose with stored fh"
- Str "world that is **blissfully unaware** of **fh**"

• Examples of **modularity** we might want from comodels



- Fh "world which consists of exactly one fh"
- Fh \longrightarrow IO "call fclose with stored fh"
- Str "world that is **blissfully unaware** of fh"
- Observation: IO ←→ Fh and other ←→ look a lot like lenses

• Our **general framework** on the file operations example

```
let f (s:string) =
    using
    Fh @ (fopen_of_io "foo.txt")
    cohandle
    fwrite_of_fh (s^s)
    finally
    x @ fh → fclose_of_io fh
```

• Our **general framework** on the file operations example

• Our **general framework** on the file operations example

```
let f(s:string) =
                                       (* in IO *)
  using
    Fh @ (fopen_of_io "foo.txt") (* in IO *)
  cohandle
                                       (* in Fh *)
    fwrite_of_fh (s^s)
  finally
    \times @ fh \rightarrow fclose_of_io fh
                                       (* in IO *)
```

where

```
Fh =
                                   (* W = fhandle *)
 { co\_fread \_ @ fh \rightarrow ...,
   co_fwrite s @ fh → fwrite_of_io s fh;
                          return ((), fh) }
     (* co\_fread : (unit * W) \rightarrow (string * W) *)
     (* co_fwrite : (string * W) \rightarrow (unit * W) *)
```

• The modularity aspect of our general framework

```
let f(s:string) =
                                        (* in IO *)
  using Fh @ (fopen_of_io "foo.txt")
  cohandle
    using Str @ (fread_of_fh ()) (* in Fh *)
    cohandle
       write_of_str (s^s)
                                      (* in Str *)
    finally
       0 \text{ s} \rightarrow \text{fwrite of fh s}
  finally
    _{-} @ fh \rightarrow fclose_of_io fh
```

where

```
Str = \{ co\_write s @ s' \rightarrow (* W = string *) \\ return ((),s'^s) \}
```

• Comodels can also **extend** the (intermediate) external world

where

• Comodels can also **extend** the (intermediate) external world

where

• Can also track **nondet./prob. choice results**, etc

• The external world could also be pure

```
let f(s:string) =
                                   (* in Pure *)
  using Str @ (return "default value")
  cohandle
    let s = read_of_str () in
    if (s = "foo")
    then (...; write_of_str "bar"; ...)
    else (...)
  finally
    \times 0 s \rightarrow return \times
```

where

• Core calculus for cohandlers (wo/ handlers ⇒ wait few slides)

- Core calculus for cohandlers (wo/ handlers ⇒ wait few slides)
- Types

$$A, B, W ::= b \mid 1 \mid A \times B \mid 0 \mid A + B \mid A \xrightarrow{\Sigma} B$$

- Core calculus for cohandlers (wo/ handlers ⇒ wait few slides)
- Types

$$A, B, W ::= b \mid 1 \mid A \times B \mid 0 \mid A + B \mid A \xrightarrow{\Sigma} B$$

• Signatures of worlds

```
\boldsymbol{\omega} ::= \{ \operatorname{op}_1 : A_1 \leadsto B_1 , \ldots , \operatorname{op}_n : A_n \leadsto B_n \}
```

- Core calculus for cohandlers (wo/ handlers ⇒ wait few slides)
- Types

$$A, B, W ::= b \mid 1 \mid A \times B \mid 0 \mid A + B \mid A \xrightarrow{\Sigma} B$$

• Signatures of worlds

$$\omega ::= \{ \mathsf{op}_1 : A_1 \leadsto B_1 , \ldots, \mathsf{op}_n : A_n \leadsto B_n \}$$

• Computation terms (value terms are unsurprising)

- Core calculus for cohandlers (wo/ handlers ⇒ wait few slides)
- Types

$$A, B, W ::= b \mid 1 \mid A \times B \mid 0 \mid A + B \mid A \xrightarrow{\Sigma} B$$

• Signatures of worlds

$$\boldsymbol{\omega} ::= \{ \operatorname{op}_1 : A_1 \leadsto B_1 , \ldots , \operatorname{op}_n : A_n \leadsto B_n \}$$

• Computation terms (value terms are unsurprising)

Comodels (cohandlers)

$$C ::= \{ \overline{op}_1 \times @ w \rightarrow c_1 , \ldots, \overline{op}_n \times @ w \rightarrow c_n \}$$

• Typing judgements

$$\Gamma \vdash v : A \qquad \Gamma \vdash c : A$$

• Typing judgements

$$\Gamma \vdash v : A \qquad \Gamma \vdash c : A$$

• The two central typing rules are

```
\Gamma \vDash D comodel of \omega' with carrier W_D \Gamma \vDash c_i : W_D
\Gamma \vDash' c : A \qquad \Gamma, x : A, w : W_D \vDash c_f : B
\Gamma \vDash \textbf{using } D @ c_i \textbf{ cohandle } c \textbf{ finally } x @ w \rightarrow c_f : B
```

• Typing judgements

$$\Gamma \vdash v : A \qquad \Gamma \nvDash c : A$$

• The two central typing rules are

$$\Gamma \nvDash D$$
 comodel of $\boldsymbol{\omega'}$ with carrier $W_D = \Gamma \nvDash c_i : W_D$

$$\Gamma \nvDash' c : A = \Gamma, x : A, w : W_D \nvDash c_f : B$$

$$\Gamma \nvDash \textbf{using } D @ c_i \textbf{ cohandle } c \textbf{ finally } x @ w \rightarrow c_f : B$$

and

$$\frac{\mathsf{op} : A \leadsto B \in \boldsymbol{\omega} \qquad \Gamma \vdash v : A}{\Gamma \stackrel{\mathsf{\mu}}{=} \widehat{\mathsf{op}} \ v : B}$$

Denotational semantics is heavily inspired by
 Møgelberg and Staton's linear state-passing translation

- Denotational semantics is heavily inspired by Møgelberg and Staton's linear state-passing translation
- Term interpretation looks very similar to alg. effects:

```
\llbracket \Gamma \vdash v : A \rrbracket : \llbracket \Gamma \rrbracket \longrightarrow \llbracket A \rrbracket \qquad \llbracket \Gamma \stackrel{\bowtie}{\vdash} c : A \rrbracket : \llbracket \Gamma \rrbracket \longrightarrow T_{\omega} \llbracket A \rrbracket
```

un-cohandled operations wait for a suitable external world!

- Denotational semantics is heavily inspired by
 Møgelberg and Staton's linear state-passing translation
- Term interpretation looks very similar to alg. effects:

$$\llbracket \Gamma \vdash v : A \rrbracket : \llbracket \Gamma \rrbracket \longrightarrow \llbracket A \rrbracket \qquad \llbracket \Gamma \stackrel{\bowtie}{\vdash} c : A \rrbracket : \llbracket \Gamma \rrbracket \longrightarrow T_{\omega} \llbracket A \rrbracket$$

- un-cohandled operations wait for a suitable external world!
- The interesting part is the interpretation of cohandling

$$\Gamma \stackrel{\bowtie}{\vdash}$$
 using D @ c_i cohandle c finally x @ $w \rightarrow c_f : B$

which is based on the linear state-passing translation, i.e.,

$$\llbracket \mathsf{D} \rrbracket \in \mathsf{Comod}_{\boldsymbol{\omega'}}(\mathsf{Kleisli}(T_{\boldsymbol{\omega}}))$$
$$\mathsf{cohandle_with}_{\llbracket \mathsf{D} \rrbracket} : T_{\boldsymbol{\omega'}} \llbracket A \rrbracket \longrightarrow \left(\llbracket W_\mathsf{D} \rrbracket \to T_{\boldsymbol{\omega}} \left(\llbracket A \rrbracket \times \llbracket W_\mathsf{D} \rrbracket \right)\right)$$

• Regarding op. semantics, e.g., consider confs. $(\overrightarrow{(C,w)}, c)$

- Regarding op. semantics, e.g., consider confs. $(\overrightarrow{(C,w)}, c)$
- For example, consider the **big-step evaluation** of **using** D ...

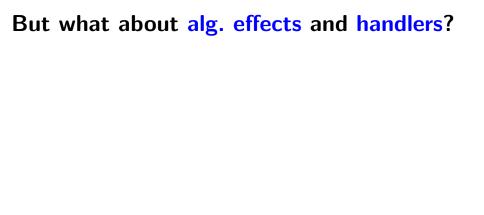
- Regarding op. semantics, e.g., consider confs. $(\overrightarrow{(C,w)}, c)$
- For example, consider the **big-step evaluation** of **using** D ...

```
 \left( \begin{array}{c} \left( (\overrightarrow{(C,w_0)},(C',w_0')) \;,\; c_i \right) \Downarrow \left( \; (\overrightarrow{(C,w_1)},(C',w_1')) \;,\; \text{return } w_0'' \; \right) \\ \\ \left( \; (\overrightarrow{(C,w_1)},(C',w_1'),(D,w_0'')) \;,\; c \; \right) \Downarrow \left( \; (\overrightarrow{(C,w_2)},(C',w_2'),(D,w_1'')) \;,\; \text{return } v \; \right) \\ \\ \left( \; (\overrightarrow{(C,w_2)},(C',w_2')) \;,\; c_f[v/x,w_1''/w] \; \right) \Downarrow \left( \; (\overrightarrow{(C,w_3)},(C',w_3')) \;,\; \text{return } v' \; \right) \\ \end{aligned}
```

- Regarding op. semantics, e.g., consider confs. $(\overrightarrow{(C,w)}, c)$
- For example, consider the **big-step evaluation** of **using** D ...

```
 \left( \begin{array}{c} \left( (\overrightarrow{(C,w_0)},(C',w_0')) \;,\; c_i \right) \Downarrow \left( \; (\overrightarrow{(C,w_1)},(C',w_1')) \;,\; \text{return } w_0'' \; \right) \\ \\ \left( \; (\overrightarrow{(C,w_1)},(C',w_1'),(D,w_0'')) \;,\; c \; \right) \Downarrow \left( \; (\overrightarrow{(C,w_2)},(C',w_2'),(D,w_1'')) \;,\; \text{return } v \; \right) \\ \\ \left( \; (\overrightarrow{(C,w_2)},(C',w_2')) \;,\; c_f[v/x,w_1''/w] \; \right) \Downarrow \left( \; (\overrightarrow{(C,w_3)},(C',w_3')) \;,\; \text{return } v' \; \right)
```

• The interpretation of **operations** uses the **co-operations** of Cs



• First: combining this with standard alg. effects and handlers

- First: combining this with standard alg. effects and handlers
- In the following

```
using C @ c_i
cohandle c
finally x @ w → c_f
```

it is natural to want that

- algebraic operations (in the sense of EFF) are allowed in c,
 but they must not be allowed to escape cohandle
- to escape, have to use the co-operations of the external world

- First: combining this with standard alg. effects and handlers
- In the following

```
using C @ c_i
cohandle c
finally x @ w → c_f
```

it is natural to want that

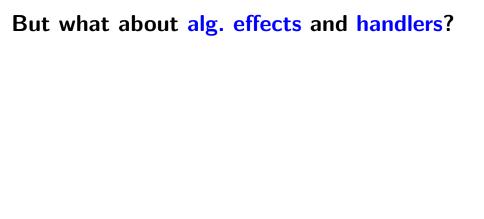
- algebraic operations (in the sense of EFF) are allowed in c,
 but they must not be allowed to escape cohandle
- to escape, have to use the co-operations of the external world
- the continuations of handlers in c are delimited by cohandle

- First: combining this with standard alg. effects and handlers
- In the following

```
using C @ c_i
cohandle c
finally x @ w → c_f
```

it is natural to want that

- algebraic operations (in the sense of EFF) are allowed in c , but they must not be allowed to escape cohandle
- to escape, have to use the co-operations of the external world
- the continuations of handlers in c are delimited by cohandle
- Where do multi-handlers fit? Co-operating handlers-cohandlers?



- Second: What if the outer comodel beaks its promise?
 - E.g., IO lost connection to the HDD where "foo.txt" was

- Second: What if the outer comodel beaks its promise?
 - E.g., IO lost connection to the HDD where "foo.txt" was

- Second: What if the outer comodel beaks its promise?
 - E.g., IO lost connection to the HDD where "foo.txt" was
- Idea:
 - Use algebraic effects to communicate downwards
 - (Algebraic ops. only allowed to appear in co-operations)
 - finally acts as a handler for broken promises

- Second: What if the outer comodel beaks its promise?
 - E.g., IO lost connection to the HDD where "foo.txt" was
- Idea:
 - Use algebraic effects to communicate downwards
 - (Algebraic ops. only allowed to appear in co-operations)
 - finally acts as a handler for broken promises

Conclusions

Conclusions

- Comodels as a gateway for interacting with the external world
- "Linearity" by leaving outer worlds implicit (via comodel ops.)
- \bullet System.IO , Koka's initially & finally , Python's with , \dots
- Convenient for general FFI

$$\frac{f:A\longrightarrow B\ \in\ \mathrm{OCamL}}{\overline{f}:A\times W_{\mathsf{OCaml}}\longrightarrow B\times W_{\mathsf{OCaml}}\ \in\ \mathsf{OCaml}}\ (\mathsf{FFI})$$

Conclusions

- Comodels as a gateway for interacting with the external world
- "Linearity" by leaving outer worlds implicit (via comodel ops.)
- \bullet System.IO , Koka's initially & finally , Python's with , \dots
- Convenient for **general FFI**

$$\frac{f:A\longrightarrow B\ \in\ \mathrm{OCamL}}{\overline{f}:A\times W_{\mathsf{OCaml}}\longrightarrow B\times W_{\mathsf{OCaml}}\ \in\ \mathsf{OCaml}}\ (\mathsf{FFI})$$

Some ongoing work

- Interaction with algebraic effects and (multi-)handlers
- Clarify the connection with (effectful) lenses
- Combinatorics of comodels and their lens-like relationships