

Interacting with the external world using comodels (aka runners)

Danel Ahman

(joint work with Andrej Bauer)

University of Ljubljana, Slovenia

Gallinette seminar, Nantes, 14.10.2019

The plan

- **Computational effects** and **external resources** in PL
- **Runners** – a natural model for **top-level runtime**
- **T-runners** – for also modelling **non-top-level runtimes**
- Turning **T**-runners into a **useful programming construct**
- Some **programming examples**
- Some **implementation details**

Computational effects
and
external resources

Computational effects in PL

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- Using **monads** (as in HASKELL)

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type St a = String → (a,String)
```

```
f :: St a → St (a,a)
```

```
f c = c >>= (\x → c >>= (\y → return (x,y)))
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- Using **alg. effects** and **handlers** (as in EFF, FRANK, KOKA)

```
effect Get : int
```

```
effect Put : int → unit
```

```
let g (c:Unit → a){Get,Put} =
```

```
  with state_handler handle (perform (Put 42); c ()) (* : int → a * int *)
```

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effect Put : int → unit
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```
let g (c:Unit → a!{Get,Put}) =
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```
  with state_handler handle (perform (Put 42); c ()) (* : int → a * int *)
```

- Both are good for **faking comp. effects** in a pure language!
But what about effects that need access to the **external world**?

External resources in PL

External resources in PL

- Declare a **signature of monads** or **algebraic effects**, e.g.,

```
(* System.IO *)  
type IO a  
openFile :: FilePath → IOMode → IO Handle
```

```
(* pervasives.eff *)  
effect RandomInt : int → int  
effect RandomFloat : float → float
```

- And then **treat them specially** in the compiler, e.g.,

```
(* eff/src/backends/eval.ml *)  
let rec top_handle op =  
  match op with  
  | ...
```

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but there are some issues with that approach ...

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- Difficult to cover all possible use cases
 - **external resources hard-coded** into the top-level runtime
 - **non-trivial to change** what's available and how it's implemented

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Ohad 8:35 PM

So here's the hack I added. We should do something a bit more principled

In `pervasives.eff`:

```
effect Write : (string*string) -> unit
```

in `eval.ml`, under `let rec top_handle op =` add the case:

```
| "Write" ->
  (match v with
  | V.Tuple vs ->
    let (file_name :: str :: _) = List.map V.to_str vs in
    let file_handle = open_out_gen
      [Open_wronly
       ;Open_append
       ;Open_creat
       ;Open_text
       ] 0o666 file_name in
    Printf.fprintf file_handle "%s" str;
    close_out file_handle;
    top_handle (k V.unit_value)
  )
```

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This talk — a principled modular (co)algebraic approach!

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- **Lack of linearity** for external resources

```
let f (s:string) =  
  let fh = fopen "foo.txt" in  
  fwrite (fh,s^s);  
  fclose fh;  
  return fh
```

```
let g s =  
  let fh = f s in fread fh
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```

- We shall address these kinds of issues **indirectly**,
 - by **not** introducing a linear typing discipline
 - but instead make it convenient to **hide** external resources

Third issue

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- **Excessive generality** of effect handlers

```
let f (s:string) =  
  let fh = fopen "foo.txt" in  
  fwrite (fh,s^s);  
  fclose fh  
  
let h = handler { fwrite (fh,s) k → return () }  
  
let f' s = handle (f "bar") with h
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```

where misuse of external resources can also be **purely accidental**

```
let g (s:string) =  
  let fh = fopen "foo.txt" in  
  let b = choose () in  
  if b then (fwrite (fh,s)) else (fwrite (fh,s^s));  
  fclose fh  
  
let nondet_handler =  
  handler { choose () k → return (k true ++ k false) }
```

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let f (s:string) =  
  let fh = fopen "foo.txt" in  
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let h = handler { fwrite (fh,s) k → return () }  
  
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- We shall address these kinds of issues **directly**,
 - by proposing a **restricted form** of handlers for resources
 - that support **controlled initialisation** and **finalisation**,
 - and **limit** how general handlers can be used

Runners enter the spotlight

A natural model of **top-level runtime**

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- Given a **signature**¹ Σ of operation symbols ($A_{\text{op}}, B_{\text{op}}$ countable)

$$\text{op} : A_{\text{op}} \rightsquigarrow B_{\text{op}}$$

a **runner**² \mathcal{R} for Σ is given by a carrier $|\mathcal{R}|$ and co-operations

$$\left(\overline{\text{op}}_{\mathcal{R}} : A_{\text{op}} \times |\mathcal{R}| \longrightarrow B_{\text{op}} \times |\mathcal{R}| \right)_{\text{op} \in \Sigma}$$

¹We consider runners for signatures, but the work generalises to alg. theories.

²In the literature also known as **comodels** for Σ (or for an algebraic theory).

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- For example, a natural runner \mathcal{R} for **S-valued state**

$$\text{get} : \mathbb{1} \rightsquigarrow S \quad \text{set} : S \rightsquigarrow \mathbb{1}$$

is given by

$$|\mathcal{R}| \stackrel{\text{def}}{=} S \quad \overline{\text{get}}_{\mathcal{R}}(\star, s) \stackrel{\text{def}}{=} (s, s) \quad \overline{\text{set}}_{\mathcal{R}}(s, s) \stackrel{\text{def}}{=} (\star, s)$$

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A natural model of **top-level runtime** ctd.

- Runners/comodels have been used for
 - **operational semantics** using tensors of models and comodels
[Plotkin and Power '08]
and
 - **stateful running** of algebraic effects [Uustalu '15]
 - **linear-use state-passing translation**
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and
 - **stateful running** of algebraic effects [Uustalu '15]
 - **linear-use state-passing translation** [Møgelberg and Staton '11, '14]
- The latter explicitly rely on one-to-one correspondence between
 - **runners** \mathcal{R}
 - **monad morphisms**³ $r : \mathbf{Free}_\Sigma(-) \longrightarrow \mathbf{St}_{|\mathcal{R}|}$

where

$$\mathbf{St}_C X \stackrel{\text{def}}{=} C \Rightarrow X \times C$$

³ $\mathbf{Free}_\Sigma(X)$ is the free monad ind. defined with leaves $\text{val } x$ and nodes $\text{op}(a, \kappa)$.

A natural model of **top-level runtime** ctd.

- For our purposes, we see runners

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as describing how operations affect **runtime configurations** $|\mathcal{R}|$

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- But what if this runtime is not **the** runtime?
 - hardware vs OS
 - OS vs VMs
 - VMs vs sandboxes

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- Unfortunately, runners, as defined above, are **not readily able to**
 - use **external resources**
 - **signal failure** caused by unavoidable circumstances

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- Unfortunately, runners, as defined above, are **not readily able to**
 - use **external resources**
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- But is there a **useful generalisation** that would achieve this?

Effectful runners for modular top-levels

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- Møgelberg and Staton usefully observed that a **runner** \mathcal{R} is equivalently simply a family of **generic effects** for $\mathbf{St}_{|\mathcal{R}|}$, i.e.,

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- Building on this, we define a **T-runner** \mathcal{R} for Σ to be given by

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- The one-to-one correspondence with **monad morphisms**

$$r : \mathbf{Free}_{\Sigma}(-) \longrightarrow \mathbf{T}$$

now simply amounts to the **univ. property of free models**, e.g.,

$$r_X(\text{val } x) = \eta_X x \qquad r_X(\text{op}(a, \kappa)) = (r_X \circ \kappa)^{\dagger}(\overline{\text{op}}_{\mathcal{R}} a)$$

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- Observe that κ appears in a **tail call position** on the right!

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- What would be a **useful class of monads** \mathbf{T} to use?

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- What would be a **useful class of monads \mathbf{T}** to use?
- We want a runner to be a bit like a **kernel** of an OS, i.e., to
 - (i) provide management of **(internal) resources**
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- **Algebraically** (and pragmatically), this amounts to taking
 - (i) $\text{getenv} : \mathbb{1} \rightsquigarrow C$, $\text{setenv} : C \rightsquigarrow \mathbb{1}$
 - (ii) $\text{op} : A_{\text{op}} \rightsquigarrow B_{\text{op}}$ ($\text{op} \in \Sigma'$, for some external Σ')
 - (iii) $\text{kill} : S \rightsquigarrow \mathbb{0}$s.t., (i) satisfy state equations; and (i) commute with (ii) and (iii)

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- The **induced monad** is then isomorphic to

$$\mathbf{T} X \stackrel{\text{def}}{=} C \Rightarrow \mathbf{Free}_{\Sigma'}((X \times C) + S)$$

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- The corresponding **T-runners** \mathcal{R} for Σ are then of the form

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- With this, our **T-runners** \mathcal{R} for Σ are (with “primitive” excs.)

$$\left(\overline{\text{op}}_{\mathcal{R}} : A_{\text{op}} \longrightarrow \mathbf{K}_C^{\Sigma'!E_{\text{op}} \not\downarrow S} B_{\text{op}} \right)_{\text{op} \in \Sigma}$$

where we call $\mathbf{K}_C^{\Sigma'!E \not\downarrow S}$ a **kernel monad**, given by

$$\mathbf{K}_C^{\Sigma'!E \not\downarrow S} X \stackrel{\text{def}}{=} C \Rightarrow \mathbf{Free}_{\Sigma}(((X + E) \times C) + S)$$

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we can easily accommodate them in a programming language as

```
let R = runner { op1 x1 → K1 , ... , opn xn → Kn } @ C
```

where K_i are **kernel computations**, modelled using $\mathbf{K}_C^{\Sigma'!E_{\text{op}_i} \not\leq S}$

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- For instance, we can implement a **write-only file handle** as

```
let RFH = runner {  
  write s → if (length s > max)  
    then (raise WriteSizeExceeded)  
    else (let fh = getenv () in  
      if (valid fh) then (fwrite (fh,s)) else (kill IOError))  
} @ FileHandle
```

where

$$(\text{fwrite} : \text{FileHandle} \times \text{String} \rightsquigarrow 1 + E) \in \Sigma'$$

$$\Sigma \stackrel{\text{def}}{=} \{ \text{write} : \text{String} \rightsquigarrow 1 + E \cup \{\text{WriteSizeExceeded}\} \} \quad \text{IOError} \in S$$

Controlled **initialisation** and **finalisation**

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- We can make use of it, to accommodate **running user code**:

```
using R @ M1  
run M2  
finally { return x @ c → M3 , raise e @ c → M4 , kill s → M5 }
```

where

- M_1 is an **initialiser** producing the initial kernel state
- M_2 is the **user computation** being run using the runner R
- M_3, M_4, M_5 are **finalisers** for return values, exceptions, signals

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induced by a \mathbf{T} -runner \mathcal{R} are all **tail-recursive**

- We can make use of it, to accommodate **running user code**:

```
using R (* :  $\Sigma \Rightarrow \Sigma' \downarrow S @ C$  *) @ M1 (* :  $\mathbf{U}^{\{\Sigma' ! E\}} C$  *)  
run M2 (* :  $\mathbf{U}^{\{\Sigma ! E\}} X$  *)  
finally { return x @ c  $\rightarrow$  M3 (* :  $\mathbf{U}^{\{\Sigma' ! E\}} Y$  *) , ... , kill s  $\rightarrow$  M5 }
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Controlled **initialisation** and **finalisation** ctd.

- For instance, we can define a PYTHON-like **with-file construct**

```
with file_name do M
=
using R_FH @ (fopen file_name)
run M
finally {
  return x @ fh → fclose fh; return x ,
  raise e @ fh → fclose fh; raise e ,
  kill s → return () }
```

- Importantly, here
 - the **file handle is hidden** from M
 - M can only use **write** but not **fopen** and **fclose**
 - fopen** and **fclose** are limited to initialisation-finalisation

Controlled **initialisation** and **finalisation** ctd.

- **Semantically** (say, in the category of sets), in

| | |
|--|-------------|
| using R @ M ₁ | (* (a) *) |
| run M ₂ | (* (b) *) |
| finally { return x @ c → M ₃ , raise e @ c → M ₄ , kill s → M ₅ } | (* (c) *) |

- R denotes $\left(\overline{\text{op}}_{\mathcal{R}} : A_{\text{op}} \longrightarrow \mathbf{K}_C^{\Sigma'!E_{\text{op}} \not\vdash S} B_{\text{op}} \right)_{\text{op} \in \Sigma}$
- M₁ denotes an element of $\mathbf{U}^{\Sigma'!E'} C$
- M₂ denotes an element of $\mathbf{U}^{\Sigma!E} A$
- **return** x @ c → M₃ denotes an element of $A \times C \Rightarrow \mathbf{U}^{\Sigma'!E'} B$
- **raise** e @ c → M₄ denotes an element of $E \times C \Rightarrow \mathbf{U}^{\Sigma'!E'} B$
- **kill** e @ c → M₅ denotes an element of $S \Rightarrow \mathbf{U}^{\Sigma'!E'} B$

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- **kill** e @ c → M₅ denotes an element of $S \Rightarrow \mathbf{U}^{\Sigma'!E'} B$
- allowing us to interpret (b) and (c) using **free model properties**

$$\mathbf{U}^{\Sigma!E} A \xrightarrow[\text{(b)}]{r_{A+E}} \mathbf{K}_C^{\Sigma'!E \not\leq S} A \xrightarrow[\text{(c)}]{(\lambda M_3)^\dagger} C \Rightarrow \mathbf{U}^{\Sigma'!E'} B$$

and (a) using the **Kleisli extension** of $\mathbf{U}^{\Sigma'!E'}$

**A core calculus for
programming with runners**

Core calculus (very briefly)

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- **Ground types** (types of ops. and kernel state)

$$A, B, C ::= B \mid 1 \mid 0 \mid A \times B \mid A + B$$

- **Types**

$$X, Y ::= \dots \mid X \xrightarrow{\Sigma} Y ! E \mid X \xrightarrow{\Sigma} Y ! E \not\downarrow S @ C \mid \Sigma \Rightarrow \Sigma' \not\downarrow S @ C$$

- **Values**

$$\llbracket \Gamma \vdash V : X \rrbracket : \llbracket \Gamma \rrbracket \longrightarrow \llbracket X \rrbracket$$

- **User computations**

$$\llbracket \Gamma \stackrel{\Sigma}{\models} M : X ! E \rrbracket : \llbracket \Gamma \rrbracket \longrightarrow \mathbf{U}^{\Sigma ! E} \llbracket X \rrbracket$$

- **Kernel computations**

$$\llbracket \Gamma \stackrel{\Sigma}{\models} K : X ! E \not\downarrow S @ C \rrbracket : \llbracket \Gamma \rrbracket \longrightarrow \mathbf{K}_{[C]}^{\Sigma ! E \not\downarrow S} \llbracket X \rrbracket$$

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- To address coherence, actual semantics in subobject fibrations

Core calculus (very briefly) ctd.

$$\begin{aligned} M ::= & \text{ return } V \mid \text{ try } M \text{ with } \{ \text{ return } x \mapsto N_{val} , (\text{ raise } e \mapsto N_e)_{e \in E} \} \\ & \mid V W \mid \text{ match } V \text{ with } \{ \langle x_1, x_2 \rangle \mapsto N \} \\ & \mid \text{ match } V \text{ with } \{ \}_X \mid \text{ match } V \text{ with } \{ \text{ inl } x_1 \mapsto N_1 , \text{ inr } x_2 \mapsto N_2 \} \\ & \mid \text{ op}_X V (x.M) (N_e)_{e \in E_{\text{op}}} \mid \text{ raise}_X e \\ & \mid \text{ using } V @ W \text{ run } M \text{ finally } \{ \text{ return } x @ c \mapsto N_{val} , \\ & \quad (\text{ raise } e @ c \mapsto N_e)_{e \in E} , \\ & \quad (\text{ kill } s \mapsto N_s)_{s \in S} \} \\ & \mid \text{ exec } K @ W \text{ finally } \{ \text{ return } x @ c \mapsto N_{val} , \\ & \quad (\text{ raise } e @ c \mapsto N_e)_{e \in E} , \\ & \quad (\text{ kill } s \mapsto N_s)_{s \in S} \} \\ \\ K ::= & \text{ return}_C V \mid \text{ try } K \text{ with } \{ \text{ return } x \mapsto L_{val} , (\text{ raise } e \mapsto L_e)_{e \in E} \} \\ & \mid V W \mid \text{ match } V \text{ with } \{ \langle x_1, x_2 \rangle \mapsto L \} \\ & \mid \text{ match } V \text{ with } \{ \}_X @ C \mid \text{ match } V \text{ with } \{ \text{ inl } x_1 \mapsto L_1 , \text{ inr } x_2 \mapsto L_2 \} \\ & \mid \text{ op}_{X @ C} V (x.K) (L_e)_{e \in E_{\text{op}}} \mid \text{ raise}_{X @ C} e \mid \text{ kill}_{X @ C} s \\ & \mid \text{ getenv}_C (c.K) \mid \text{ setenv } V K \\ & \mid \text{ exec } M \text{ finally } \{ \text{ return } x \mapsto L_{val} , (\text{ raise } e \mapsto L_e)_{e \in E} \} \end{aligned}$$

Fig. 1. Syntax of user and kernel computations

Core calculus (very briefly) ctd.

- For example, the **typing rule for running user comps.** is

$$\begin{array}{c}
 \Gamma \vdash V : \Sigma \Rightarrow \Sigma' \not\downarrow S @ C \quad \Gamma \vdash W : C \\
 \Gamma \Vdash M : X ! E \quad \Gamma, x:X, c:C \Vdash' N_{ret} : Y ! E' \\
 (\Gamma, c:C \Vdash' N_e : Y ! E')_{e \in E} \quad (\Gamma \Vdash' N_s : Y ! E')_{s \in S} \\
 \hline
 \Gamma \Vdash' \text{using } V @ W \text{ run } M \text{ finally } \{ \text{return } x @ c \mapsto N_{ret} , \\
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 \text{(kill } s \mapsto N_s)_{s \in S} \} : Y ! E'
 \end{array}$$

- and the **main β -equation for running user comps.** is

$$\begin{aligned}
 &\Gamma \Vdash' \text{using } R_C @ W \text{ run } (\text{op}_X V (x.M) (M_e)_{e \in E_{\text{op}}}) \text{ finally } F \\
 &\equiv \text{exec } R_{op}[V] @ W \text{ finally } \{ \\
 &\quad \text{return } x @ c' \mapsto \text{using } R_C @ c' \text{ run } M \text{ finally } F , \\
 &\quad (\text{raise } e @ c' \mapsto \text{using } R_C @ c' \text{ run } M_e \text{ finally } F)_{e \in E_{\text{op}}} , \\
 &\quad (\text{kill } s \mapsto N_s)_{s \in S} \} : Y ! E'
 \end{aligned}$$

Runners in action

Runners can be **vertically nested**

Runners can be **vertically nested**

- ```
using RFH @ (fopen file_name)
run (
 using RFC @ (return "")
 run m
 finally {
 return x @ s → write s; return x ,
 raise e @ s → write s; raise e }
)
finally {
 return x @ fh → fclose fh; return x ,
 raise e @ fh → fclose fh; raise e }
```

where the **file contents runner** (with  $\Sigma' = \emptyset$ ) is defined as

```
let RFC = runner {
 write s → let s' = getenv () in
 if (length (s^s') > max) then (raise WriteSizeExceeded)
 else (setenv (s^s'))
} @ String
```

Runners can be horizontally paired

# Runners can be horizontally paired

- Given a runner for  $\Sigma$

```
let R1 = runner { ... , op1i x → k1i , ... } @ C1
```

and a runner for  $\Sigma'$

```
let R2 = runner { ... , op2j x → k2j , ... } @ C2
```

we can **pair them** to get a runner for  $\Sigma \cup \Sigma'$

```
let R = runner {
 ... ,
 op1i x → let (c,c') = getenv () in
 let (x,c'') = k1i x in
 setenv (c'',c');
 return x,
 ... ,
 op2j x → ... (* analogously to above *) ,
 ...
} @ C1 * C2
```

# Vertical nesting for instrumentation

# Vertical nesting for instrumentation

- ```
using RSniffer @ (return 0)
run m
finally {
  return x @ c →
    let fh = fopen "nsa.txt" in fwrite (fh,to_str c); fclose fh }
```

where the **instrumenting runner** is defined as

```
let RSniffer = runner {
  ... ,
  op a → op a;                                (* forwards op outwards *)
    let c = getenv () in
    setenv (c + 1) ,
  ...
} @ Nat
```

- The runner R_{Sniffer} implements the same sig. Σ that `m` is using
- As a result, the runner R_{Sniffer} is **invisible** from `m`'s viewpoint

Integer state **with** active monitoring

Integer state with active monitoring

- **type** IntHeap = { memory : Nat \rightarrow Option Int ; next : Nat }

```
let RIntState = runner {  
  alloc x  $\rightarrow$  ... ,  
  
  deref r  $\rightarrow$  let h = getenv () in  
    match (heap_sel h r) with  
    | Some x  $\rightarrow$  return x  
    | None  $\rightarrow$  kill ReferenceDoesNotExistSignal,  
  
  assign r y  $\rightarrow$  let h = getenv () in  
    match (heap_upd h r y) with  
    | Some h'  $\rightarrow$  if (rel x y)  
      then (setenv h')  
      else (raise MonotonicityException)  
    | None  $\rightarrow$  kill ReferenceDoesNotExistSignal  
}
```

@ IntHeap

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- This is **runtime verification** for **rel-monotonic integer state**

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}
```

@ IntHeap

- This is **runtime verification** for **rel-monotonic integer state**
- Also possible with **vertical nesting**: MLState \leftrightarrow Monotonicity

Other examples

- More general forms of **(ML-style) state** (for general Ref A)
 - if the host language allows it, we use GADTs, etc for safety
 - some examples extract a footprint from a larger memory
- **Combinations** of different effects and runners
 - in particular the combination of IO and state
 - good use case for both vertical and horizontal composition
- KOKA-style **ambient values** and **ambient functions**
 - ambient values are essentially mutable variables/parameters
 - ambient functions are executed in their lexical context
 - a runner for amb. funs. treats fun. application as a co-operation
 - amb. funs. are stored in a context-sensitive heap
 - the appl. co-operation restores the heap to the lexical context

Implementing runners

Experimenting with the **theory in practice**

Experimenting with the **theory in practice**

- A **small experimental language** COOP⁴
 - Implements the core calculus with few extras
 - The interpreter is directly based on the denotational semantics
 - Top-level containers for running external (OCaml) code

⁴coop [/ku:p/] – a cage where small animals are kept, especially chickens

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- A **HASKELL library** HASKELL-COOP
 - A shallow-embedding of the core calculus in HASKELL
 - Uses one of the Freer monad implementations underneath
 - Again, the operational aspects implement the denot. semantics
 - Top-level containers for arbitrary HASKELL monads
 - Examples make use of HASKELL's features (GADTs, ...)

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 - Examples make use of HASKELL's features (GADTs, ...)
- Both still need some finishing touches, but will be public soon

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Experimenting with the theory in practice

```
module AmbientsTests where

import Control.Runner
import Control.Runner.Ambients

ambFun :: AmbVal Int -> Int -> AmbEff Int
ambFun x y =
  do x <- getVal x;
  return (x + y)

test1 :: AmbEff Int
test1 =
  withAmbVal
    (4 :: Int)
    (\ x ->
      withAmbFun
        (ambFun x)
        (\ f ->
          do rebindVal x 2;
             applyFun f 1))

test2 = ambToplevel test1
```

Wrapping up

- **Runners** are a natural model of **top-level runtime**
- We proposed **T-runners** to also model **non-top-level runtimes**
- We turned **T-runners** into a **practical programming construct**, that supports controlled initialisation and finalisation
- We showed some **combinators** and **programming examples**
- Two **implementations** in the works, COOP and HASKELL-COOP

This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 834146.



This material is based upon work supported by the Air Force Office of Scientific Research under award number FA9550-17-1-0326.

Thank you!

