# Interacting with the external world using comodels (aka runners)

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## The plan

- Computational effects and external resources in PL
- Runners a natural model for top-level runtime
- T-runners for also modelling non-top-level runtimes
- Turning **T**-runners into a **useful programming construct**
- Some programming examples
- Some implementation details

# Computational effects and external resources

• Using monads (as in HASKELL)

```
type St a = String \rightarrow (a,String)

f :: St a \rightarrow St (a,a)

f c = c \Rightarrow (\x \rightarrow c \Rightarrow (\y \rightarrow return (x,y)))
```

• Using monads (as in HASKELL)

```
type St a = String \rightarrow (a,String)

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f c = c >>= (\x \rightarrow c >>= (\y \rightarrow return (x,y)))
```

• Using alg. effects and handlers (as in EFF, FRANK, KOKA)

```
effect Get : int effect Put : int \rightarrow unit let g (c:Unit \rightarrow a!{Get,Put}) = with state_handler handle (perform (Put 42); c ()) (*:int \rightarrow a * int *)
```

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effect Get : int
effect Put : int → unit

let g (c:Unit → a!{Get,Put}) =
   with state_handler handle (perform (Put 42); c ()) (* : int → a * int *)
```

Both are good for faking comp. effects in a pure language!
 But what about effects that need access to the external world?

### **External resources in PL**

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• Declare a signature of monads or algebraic effects, e.g.,

```
(* System.IO *)

type IO a

openFile :: FilePath \rightarrow IOMode \rightarrow IO Handle
```

```
(* pervasives.eff *)

effect RandomInt : int → int

effect RandomFloat : float → float
```

And then treat them specially in the compiler, e.g.,

```
(* eff/src/backends/eval.ml *)
let rec top_handle op =
  match op with
  | ...
```

#### **External resources in PL**

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And then treat them specially in the compiler, e.g.,

but there are some issues with that approach . . .

- Difficult to cover all possible use cases
  - external resources hard-coded into the top-level runtime
  - non-trivial to change what's available and how it's implemented

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```
Ohad 4 8:35 PM
So here's the hack I added We should do something a bit more principled
In pervasives.eff:
 effect Write : (string*string) -> unit
in eval.ml under let rec top handle op = add the case:
     | "Write" ->
        (match v with
         | V.Tuple vs ->
            let (file_name :: str :: _) = List.map V.to_str vs in
            let file_handle = open_out_gen
                                 [Open_wronly
                                 :Open append
                                 ;Open_creat
                                 ;Open_text
                                 1 0o666 file_name in
            Printf.fprintf file handle "%s" str:
            close_out file_handle;
            top_handle (k V.unit_value)
```

- Difficult to cover all possible use cases
  - external resources hard-coded into the top-level runtime
  - non-trivial to change what's available and how it's implemented



This talk — a principled modular (co)algebraic approach!

• Lack of linearity for external resources

```
let f (s:string) =
  let fh = fopen "foo.txt" in
  fwrite (fh,s^s);
  fclose fh;
  return fh

let g s =
  let fh = f s in fread fh
```

• Lack of linearity for external resources

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- We shall address these kinds of issues indirectly,
  - by **not** introducing a linear typing discipline
  - but instead make it convenient to hide external resources

• Excessive generality of effect handlers

```
let f (s:string) =
let f = fopen "foo.txt" in
fwrite (fh,s^s);
fclose fh

let f = handler f fwrite f = handler f = handler f = handle f = ha
```

• Excessive generality of effect handlers

```
let f (s:string) =
  let fh = fopen "foo.txt" in
  fwrite (fh,s^s);
  fclose fh
let h = \text{handler} \{ \text{ fwrite (fh,s) } k \rightarrow \text{return () } \}
let f' s = handle (f "bar") with h
where misuse of external resources can also be purely accidental
let g (s:string) =
  let fh = fopen "foo.txt" in
  let b = choose () in
  if b then (fwrite (fh,s)) else (fwrite (fh,s^s));
  fclose fh
let nondet handler =
  handler { choose () k \rightarrow return (k true ++ k false) }
```

• Excessive generality of effect handlers

```
let f (s:string) =
let fh = fopen "foo.txt" in
fwrite (fh,s^s);
fclose fh

let h = handler { fwrite (fh,s) k → return () }

let f' s = handle (f "bar") with h
```

- We shall address these kinds of issues directly,
  - by proposing a restricted form of handlers for resources
  - that support controlled initialisation and finalisation,
  - and limit how general handlers can be used

# Runners enter the spotlight

• Given a **signature**<sup>1</sup>  $\Sigma$  of operation symbols  $(A_{op}, B_{op} \text{ countable})$ 

$$op: A_{op} \leadsto B_{op}$$

a runner<sup>2</sup>  $\mathcal{R}$  for  $\Sigma$  is given by a carrier  $|\mathcal{R}|$  and co-operations

$$\left(\overline{\operatorname{op}}_{\mathcal{R}}: A_{\operatorname{op}} \times |\mathcal{R}| \longrightarrow B_{\operatorname{op}} \times |\mathcal{R}|\right)_{\operatorname{op} \in \Sigma}$$

<sup>&</sup>lt;sup>1</sup>We consider runners for signatures, but the work generalises to alg. theories.

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 $\bullet$  For example, a natural runner  $\mathcal{R}$  for S-valued state

get : 
$$\mathbb{1} \rightsquigarrow S$$
 set :  $S \rightsquigarrow \mathbb{1}$ 

is given by

$$|\mathcal{R}| \stackrel{\text{def}}{=} S$$
  $\overline{\text{get}}_{\mathcal{R}}(\star, s) \stackrel{\text{def}}{=} (s, s)$   $\overline{\text{set}}_{\mathcal{R}}(s, s) \stackrel{\text{def}}{=} (\star, s)$ 

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- Runners/comodels have been used for
  - operational semantics using tensors of models and comodels
     [Plotkin and Power '08]
     and
  - stateful running of algebraic effects [Uustalu '15]
  - linear-use state-passing translation

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     and
  - **stateful running** of algebraic effects

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• linear-use state-passing translation

[Møgelberg and Staton '11, '14]

- The latter explicitly rely on one-to-one correspondence between
  - $\bullet$  runners  $\mathcal{R}$
  - ullet monad morphisms<sup>3</sup>  $r: \mathsf{Free}_{\Sigma}(-) \longrightarrow \mathsf{St}_{|\mathcal{R}|}$

where

$$\mathbf{St}_{C}X \stackrel{\mathsf{def}}{=} C \Rightarrow X \times C$$

 $<sup>{}^{3}</sup>Free_{\Sigma}(X)$  is the free monad ind. defined with leaves val x and nodes op(a,  $\kappa$ ).

• For our purposes, we see runners

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  - hardware vs OS
  - OS vs VMs
  - VMs vs sandboxes

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- Unfortunately, runners, as defined above, are not readily able to
  - use external resources
  - signal failure caused by unavoidable circumstances
- But is there a useful generalisation that would achieve this?

• Møgelberg and Staton usefully observed that a runner  $\mathcal{R}$  is equivalently simply a family of **generic effects** for  $\mathbf{St}_{|\mathcal{R}|}$ , i.e.,

$$\left(\overline{\operatorname{op}}_{\mathcal{R}}:A_{\operatorname{op}}\longrightarrow\operatorname{\mathbf{St}}_{|\mathcal{R}|}B_{\operatorname{op}}\right)_{\operatorname{op}\in\Sigma}$$

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• Building on this, we define a **T-runner**  $\mathcal{R}$  for  $\Sigma$  to be given by

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• The one-to-one correspondence with monad morphisms

$$r: \mathbf{Free}_{\Sigma}(-) \longrightarrow \mathbf{T}$$

now simply amounts to the univ. property of free models, e.g.,

$$\mathsf{r}_X \, (\mathsf{val} \, x) = \eta_X \, x \qquad \qquad \mathsf{r}_X \, (\mathsf{op}(\mathsf{a}, \kappa)) = (\mathsf{r}_X \circ \kappa)^\dagger (\overline{\mathsf{op}}_\mathcal{R} \, \mathsf{a})$$

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• Observe that  $\kappa$  appears in a **tail call position** on the right!

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- Algebraically (and pragmatically), this amounts to taking
  - (i) getenv :  $\mathbb{1} \rightsquigarrow C$ , setenv :  $C \rightsquigarrow \mathbb{1}$
  - (ii) op :  $A_{op} \leadsto B_{op}$  (op  $\in \Sigma'$ , for some external  $\Sigma'$ )
  - (iii) kill :  $S \leadsto \mathbb{O}$
  - s.t., (i) satisfy state equations; and (i) commute with (ii) and (iii)

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  - s.t., (i) satisfy state equations; and (i) commute with (ii) and (iii)
- The induced monad is then isomorphic to

$$\mathsf{T} X \stackrel{\mathsf{def}}{=} C \Rightarrow \mathsf{Free}_{\Sigma'} \big( (X \times C) + S \big)$$

• The corresponding **T-runners**  $\mathcal{R}$  for  $\Sigma$  are then of the form

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• With this, our **T-runners**  $\mathcal{R}$  for  $\Sigma$  are (with "primitive" excs.)

$$\left(\overline{\operatorname{op}}_{\mathcal{R}}: A_{\operatorname{op}} \longrightarrow \mathbf{K}_{C}^{\Sigma'!E_{\operatorname{op}} \notin S} B_{\operatorname{op}}\right)_{\operatorname{op} \in \Sigma}$$

where we call  $\mathbf{K}_{C}^{\Sigma!E \downarrow S}$  a **kernel monad**, given by

$$\mathbf{K}_{C}^{\Sigma!E \notin S} X \stackrel{\text{def}}{=} C \Rightarrow \mathbf{Free}_{\Sigma} (((X+E) \times C) + S)$$

# T-runners as a programming construct

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we can easily accommodate them in a programming language as

let 
$$R = runner \{ op_1 x_1 \rightarrow K_1 , ... , op_n x_n \rightarrow K_n \} @ C$$

where  $K_i$  are **kernel code**, modelled using  $\mathbf{K}_C^{\Sigma'!E_{op_i} \notin S}$ 

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For instance, we can implement a write-only file handle as

 $IOError \in S$ 

```
where \left(\mathsf{fwrite}:\mathsf{FileHandle}\times\mathsf{String}\leadsto 1+E\right)\in\Sigma' \Sigma\stackrel{\mathsf{def}}{=} \left\{\;\mathsf{write}:\mathsf{String}\leadsto 1+E\cup\{\mathsf{WriteSizeExceeded}\}\;\right\}
```

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• We make use of it, to accommodate running user code:

```
using R @ M_{init} run M finally {return x @ c \rightarrow M<sub>ret</sub> , ... raise e @ c \rightarrow M<sub>e</sub> ... , ... kill s \rightarrow M<sub>s</sub> ...}
```

where (a user monad)

• Ms are user code, modelled using  $\mathbf{U}^{\Sigma ! E} X \stackrel{\text{def}}{=} \mathbf{Free}_{\Sigma} (X + E)$ 

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```
 \begin{tabular}{ll} \textbf{using} & R & @ & M_{init} \\ \textbf{run} & M \\ \textbf{finally} & \{ \textbf{return} \times \textbf{@} & c \rightarrow M_{ret} \ , \ ... \ \textbf{raise} \ e & @ & c \rightarrow M_e \ ... \ , \ ... \ \textbf{kill} \ s \rightarrow M_s \ ... \} \\ \end{tabular}
```

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- M<sub>init</sub> produces the initial kernel state
- M is the user code being run using the runner R
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- M<sub>init</sub> produces the initial kernel state
- M is the user code being run using the runner R
- M<sub>ret</sub>, M<sub>e</sub>, M<sub>s</sub> finalise for return values, exceptions, and signals
- M<sub>ret</sub> and M<sub>e</sub> depend on the final state c, but M<sub>s</sub> does not

For instance, we can define a PYTHON-like with-file construct

```
with fileName do M = using R<sub>FH</sub> @ (fopen fileName) run M finally { return \times @ fh \rightarrow fclose fh; return \times , raise e @ fh \rightarrow fclose fh; raise e , kill s \rightarrow return () }
```

- Importantly, here
  - the file handle is hidden from M
  - M can only use write but not fopen and fclose
  - fopen and fclose are limited to initialisation-finalisation

## A core calculus for programming with runners

## Core calculus (syntax)

## **Core calculus (syntax)**

• Ground types (types of ops. and kernel state)

$$A, B, C ::= B \mid 1 \mid 0 \mid A \times B \mid A + B$$

Types

$$X, Y ::= B \mid 1 \mid 0 \mid X \times Y \mid X + Y$$

$$\mid X \xrightarrow{\Sigma} Y \mid E$$

$$\mid X \xrightarrow{\Sigma} Y \mid E \not\downarrow S \otimes C$$

$$\mid \Sigma \Rightarrow \Sigma' \not\downarrow S \otimes C$$

Values

$$\Gamma \vdash V : X$$

• User computations

$$\Gamma \stackrel{\Sigma}{\vdash} M : X ! E$$

Kernel computations

$$\Gamma \stackrel{\Sigma}{\vdash} K : X ! E \nleq S @ C$$

```
M ::= \mathbf{return} \ V \mid \mathbf{try} \ M \ \mathbf{with} \ \{ \ \mathbf{return} \ x \mapsto N_{val} \ , \ (\mathbf{raise} \ e \mapsto N_e)_{e \in E} \ \}
            VW \mid \mathbf{match} \ V \ \mathbf{with} \ \{ \langle x_1, x_2 \rangle \mapsto N \ \}
            match V with \{\}_X \mid \text{match } V \text{ with } \{ \text{ inl } x_1 \mapsto N_1 \text{ , inr } x_2 \mapsto N_2 \}
          \operatorname{op}_{X} V(x.M)(N_{e})_{e \in E_{\operatorname{op}}} \mid \operatorname{raise}_{X} e
           using V @ W run M finally { return x @ c \mapsto N_{val},
                                                                        (\mathbf{raise}\ e\ @\ c\mapsto N_e)_{e\in F},
                                                                        \{\text{kill } s \mapsto N_s\}_{s \in S} \}
            exec K @ W finally { return x @ c \mapsto N_{val},
                                                        (\mathbf{raise}\ e\ @\ c\mapsto N_e)_{e\in F},
                                                        \{\text{kill } s \mapsto N_s\}
K ::= \mathbf{return}_C V \mid \mathbf{try} \ K \ \mathbf{with} \ \{ \ \mathbf{return} \ x \mapsto L_{val} \ , \ (\mathbf{raise} \ e \mapsto L_e)_{e \in E} \ \}
           VW \mid \mathbf{match} \ V \ \mathbf{with} \ \{ \langle x_1, x_2 \rangle \mapsto L \ \}
            match V with \{\}_{X@C} \mid \text{match } V \text{ with } \{ \text{ inl } x_1 \mapsto L_1 \text{ , inr } x_2 \mapsto L_2 \}
       | \operatorname{op}_{X \odot C} V(x.K)(L_e)_{e \in E_{op}} | \operatorname{raise}_{X \odot C} e | \operatorname{kill}_{X \odot C} s
       \mid \operatorname{getenv}_{C}(c.K) \mid \operatorname{setenv} V K
           exec M finally { return x \mapsto L_{val}, (raise e \mapsto L_e)
```

Fig. 1. Syntax of user and kernel computations



### Core calculus (type system and eq. theory)

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```
\Gamma \vdash V : \Sigma \Rightarrow \Sigma' \not \downarrow S @ C \qquad \Gamma \vdash W : C
\Gamma \vdash M : X ! E \qquad \Gamma, x : X, c : C \vdash N_{ret} : Y ! E'
(\Gamma, c : C \vdash N_e : Y ! E')_{e \in E} \qquad (\Gamma \vdash N_s : Y ! E')_{s \in S}
\Gamma \vdash \text{using } V @ W \text{ run } M \text{ finally } \{ \text{ return } x @ c \mapsto N_{ret} ,
(\text{raise } e @ c \mapsto N_e)_{e \in E} ,
(\text{kill } s \mapsto N_s)_{s \in S} \} : Y ! E'
```

• and the main  $\beta$ -equation for running user comps. is

```
\begin{split} \Gamma &\stackrel{\Sigma'}{=} \text{using } R_C \otimes W \text{ run } (\text{op}_X \ V \ (x.M) \ (M_e)_{e \in E_{op}}) \text{ finally } F \\ &\equiv \text{exec } R_{op}[V] \otimes W \text{ finally } \{ \\ & \text{return } x \otimes c' \mapsto \text{using } R_C \otimes c' \text{ run } M \text{ finally } F \ , \\ & \left( \text{raise } e \otimes c' \mapsto \text{using } R_C \otimes c' \text{ run } M_e \text{ finally } F \right)_{e \in E_{op}}, \\ & \left( \text{kill } s \mapsto N_s \right)_{s \in S} \ \} : Y \ ! \ E' \end{split}
```

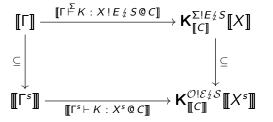
- Monadic semantics, for simplicity in **Set**, using
  - user monads  $\mathbf{U}^{\Sigma!E}X\stackrel{\text{def}}{=} \mathbf{Free}_{\Sigma}(X+E)$
  - kernel monads  $K_C^{\Sigma!E \notin S} X \stackrel{\text{def}}{=} C \Rightarrow \text{Free}_{\Sigma} (((X + E) \times C) + S)$

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(At a high level) the judgements are interpreted as

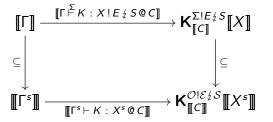
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- However, to prove coherence of the semantics (subtyping!),
   we actually give the semantics in the subset fibration
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• No essential obstacles to extending to **Sub(Cpo)** and beyond

- $\bullet \quad \llbracket V \rrbracket_{\gamma} \ = \ \mathcal{R} \ = \ \left( \overline{\mathsf{op}}_{\mathcal{R}} : \llbracket A_{\mathsf{op}} \rrbracket \ \longrightarrow \ \mathsf{K}_{\llbracket C \rrbracket}^{\Sigma' \mid E_{\mathsf{op}} \notin S} \ \llbracket B_{\mathsf{op}} \rrbracket \right)_{\mathsf{op} \in \Sigma}$
- $\llbracket W \rrbracket_{\gamma} \in \llbracket C \rrbracket$
- $\llbracket M \rrbracket_{\gamma} \in \mathbf{U}^{\Sigma!E} \llbracket A \rrbracket$
- [return  $\times$  0 c o  $N_{ret}$ ] $_{\gamma} \in$  [A]  $\times$  [C]  $\Rightarrow$   $\mathbf{U}^{\Sigma'!E'}$  [B]
- $[\![ (raise e \ \mathbf{0} \ c \rightarrow N_e)_{e \in E} ]\!]_{\gamma} \in E \times [\![C]\!] \Rightarrow \mathbf{U}^{\Sigma'!E'} [\![B]\!]$
- $[\![(kill\ s o N_s)_{s \in S}]\!]_{\gamma} \in S \Rightarrow U^{\Sigma'!E'}[\![B]\!]$

- $\bullet \quad \llbracket V \rrbracket_{\gamma} \ = \ \mathcal{R} \ = \ \left( \overline{\mathsf{op}}_{\mathcal{R}} : \llbracket A_{\mathsf{op}} \rrbracket \longrightarrow \mathsf{K}_{\llbracket C \rrbracket}^{\Sigma' ! E_{\mathsf{op}} \frac{j}{2} S} \, \llbracket B_{\mathsf{op}} \rrbracket \right)_{\mathsf{op} \in \Sigma}$
- $[W]_{\gamma} \in [C]$
- $\llbracket M \rrbracket_{\gamma} \in \mathbf{U}^{\Sigma!E} \llbracket A \rrbracket$
- $[\![ return \times @ c \rightarrow N_{ret} ]\!]_{\gamma} \in [\![ A ]\!] \times [\![ C ]\!] \Rightarrow \mathbf{U}^{\Sigma'!E'} [\![ B ]\!]$
- $[\![ (raise e \ \mathbf{0} \ c \rightarrow N_e)_{e \in E} ]\!]_{\gamma} \in E \times [\![C]\!] \Rightarrow \mathbf{U}^{\Sigma'!E'} [\![B]\!]$
- $\llbracket (\mathbf{kill} \ \mathsf{s} \to N_s)_{s \in S} \rrbracket_{\gamma} \in S \Rightarrow \mathbf{U}^{\Sigma'!E'} \llbracket B \rrbracket$
- allowing us to use the free model property to get

$$\mathbf{U}^{\Sigma \mid E} \llbracket A \rrbracket \xrightarrow{\mathsf{r}_{\llbracket A \rrbracket + E}} \mathbf{K}_{\llbracket C \rrbracket}^{\Sigma' \mid E_{\frac{J}{2}} S} \llbracket A \rrbracket \xrightarrow{(\lambda \llbracket M_3 \rrbracket_{\gamma})^{\ddagger}} \llbracket C \rrbracket \Rightarrow \mathbf{U}^{\Sigma' \mid E'} \llbracket B \rrbracket$$

and then apply the resulting composite to  $[\![M]\!]_\gamma$  and  $[\![W]\!]_\gamma$ 

### **Runners in action**

### Runners can be vertically nested

### Runners can be vertically nested

```
• using R<sub>FH</sub> @ (fopen fileName) run ( using R<sub>FC</sub> @ (return "") run M finally { return \times @ str \rightarrow write str; return \times , raise e @ str \rightarrow write str; raise e } ) ) finally { return \times @ fh \rightarrow fclose fh; return \times , raise e @ fh \rightarrow fclose fh; raise e , kill s \rightarrow return ()}
```

where the **file contents runner** (with  $\Sigma' = 0$ ) is defined as

#### Runners can be horizontally paired

# Runners can be horizontally paired

ullet Given a runner for  $\Sigma$ 

```
let R_1 = \text{runner} \{ ... , op_{1i} x \rightarrow k_{1i} , ... \} @ C_1
and a runner for \Sigma'
let R_2 = \text{runner} \{ ... , op_{2i} x \rightarrow k_{2i} , ... \} @ C_2
we can pair them to get a runner for \Sigma \cup \Sigma'
 let R_{\otimes} = runner {
   op_{1i} \times \rightarrow let (c,c') = getenv () in
                let (x,c^{II}) = k_{1i} \times in
                setenv (c<sup>11</sup>,c<sup>1</sup>);
                return x,
   op_{2j} x \rightarrow ... (* analogously to above *),
 \{ \bigcirc C_1 * C_2 \}
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                return x,
```

• For instance, this way we can build a runner for multiple files

 $op_{2j} x \rightarrow ... (* analogously to above *)$ ,

# Vertical nesting for instrumentation

### Vertical nesting for instrumentation

```
using R<sub>Sniffer</sub> ② (return 0)
run M
finally {
  return x ② c →
    let fh = fopen "nsa.txt" in fwrite (fh,nat_to_str c); fclose fh }
```

where the **instrumenting runner** is defined as

```
\begin{tabular}{lll} \textbf{let} & R_{Sniffer} = \textbf{runner} & \{ & \dots & , \\ & op & a & \rightarrow \textbf{let} & c = \textbf{getenv} & () & \textbf{in} \\ & & & \textbf{setenv} & (c+1); \\ & & op & a & , \\ & & \dots & \\ & & 0 & \textbf{Nat} \\ \end{tabular}
```

- ullet The runner  $R_{Sniffer}$  implements the same sig.  $\Sigma$  that M is using
- As a result, the runner R<sub>Sniffer</sub> is **invisible** from M 's viewpoint

• **type** IntHeap =  $\{$  memory : Nat  $\rightarrow$  Option Int ; next : Nat  $\}$ 

```
let R_{IntState} = runner {
 alloc x \rightarrow \dots
 deref r \rightarrow let h = getenv () in
             match (heapSel h r) with
               Some x \rightarrow return x
               None → kill ReferenceDoesNotExistSignal,
 assign r y \rightarrow let h = getenv () in
                match (heapUpd h r y) with
                  Some h' \rightarrow if (rel \times y)
                                then (setenv h')
                                else (raise MonotonicityException)
                | None \rightarrow kill ReferenceDoesNotExistSignal
} 👩 IntHeap
```

• type IntHeap = { memory : Nat → Option Int; next : Nat }

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• This is runtime verification for rel -monotonic integer state

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- This is runtime verification for rel-monotonic integer state
- Also possible with vertical nesting: MLState 
   ← Monotonicity

#### Other examples

- More general forms of (ML-style) state (for general Ref A)
  - if the host language allows it, we use GADTs, etc for safety
  - some examples extract a footprint from a larger memory
- Combinations of different effects and runners
  - in particular the combination of IO and state
  - good use case for both vertical and horizontal composition
- Koka-style ambient values and ambient functions
  - ambient values are essentially mutable variables/parameters
  - ambient functions are executed in their lexical context
  - a runner for amb. funs. treats fun. application as a co-operation
  - amb. funs. are stored in a context-sensitive heap
  - the appl. co-operation restores the heap to the lexical context

# **Implementing runners**

- A small experimental language Coop<sup>4</sup>
  - Implements the core calculus with few extras
  - The interpreter is directly based on the denotational semantics
  - Top-level containers for running external (OCaml) code

<sup>&</sup>lt;sup>4</sup>coop [/ku:p/] – a cage where small animals are kept, especially chickens

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- A HASKELL library HASKELL-COOP
  - A shallow-embedding of the core calculus in HASKELL
  - Uses one of the Freer monad implementations underneath
  - Again, the operational aspects implement the denot. semantics
  - Top-level containers for arbitrary HASKELL monads
  - Examples make use of HASKELL's features (GADTs, ...)

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  - Examples make use of HASKELL's features (GADTs, ...)
- Both still need some finishing touches, but will be public soon

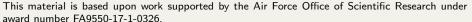
<sup>&</sup>lt;sup>4</sup>coop [/ku:p/] - a cage where small animals are kept, especially chickens

```
module AmbientsTests where
import Control.Runner
import Control.Runner.Ambients
ambFun :: AmbVal Int -> Int -> AmbEff Int
ambFun x y =
  do x <- getVal x;</pre>
     return (x + y)
test1 :: AmbEff Int
test1 =
  withAmbVal
    (4 :: Int)
    (\ x ->
      withAmbFun
        (ambFun x)
        (\ f ->
          do rebindVal x 2:
             applyFun f 1))
test2 = ambTopLevel test1
```

### Wrapping up

- Runners are a natural model of top-level runtime
- We propose **T-runners** to also model **non-top-level runtimes**
- We have turned **T**-runners into a **(practical ?) programming construct**, that supports controlled initialisation and finalisation
- I showed you some combinators and programming examples
- Two implementations in the works, COOP & HASKELL-COOP
- Future: handlers, case studies, refinement typing, compilation, ...

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# Thank you!

