# CARNEGIE MELLON UNIVERSITY APPLIED STOCHASTIC PROCESSES (COURSE 18-751) HOMEWORK 13

Daniel Marew

December 6, 2017

I collaborated with :  $\,$ 

Nebyou Yismaw Daniel Nkemelu Agatha Niwomugizi

## **2.**b

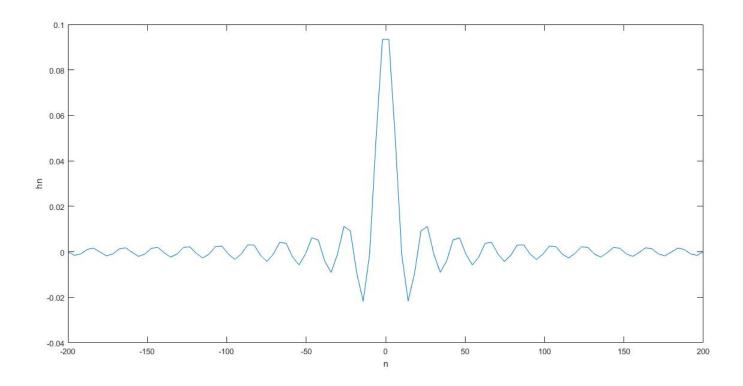


Figure 1:  $h_n$ 

### 2.c

Comment on the apparent bandwidth of the system in all three cases. The bandwidth increases as we consider more and more parts of the impulse response(filter) i.e as c increases.

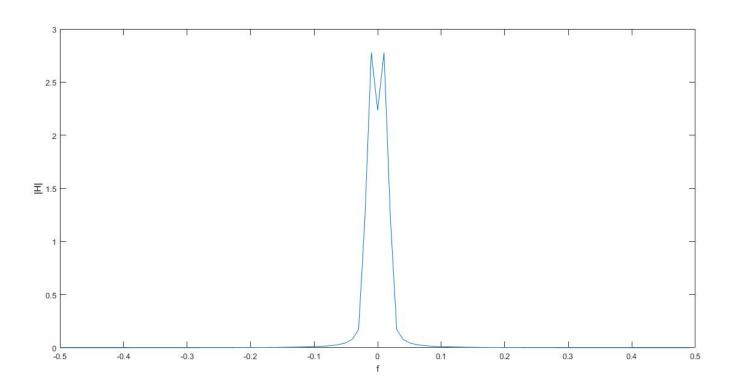


Figure 2: random sequence of impulses

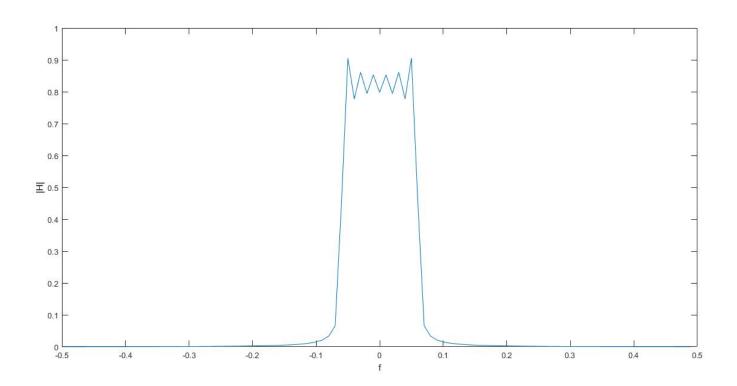


Figure 3: random sequence of impulses

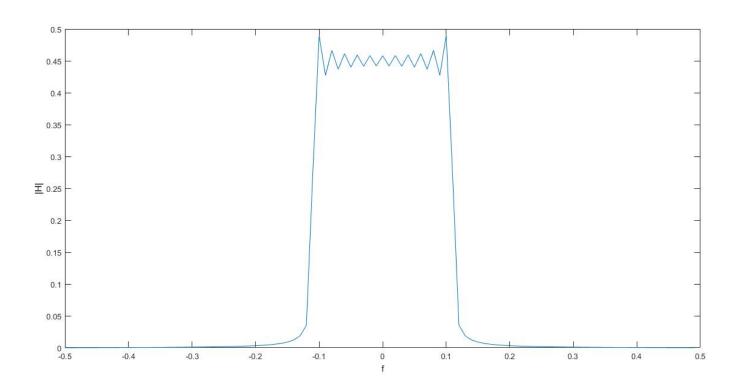


Figure 4: random sequence of impulses

# **2.**d

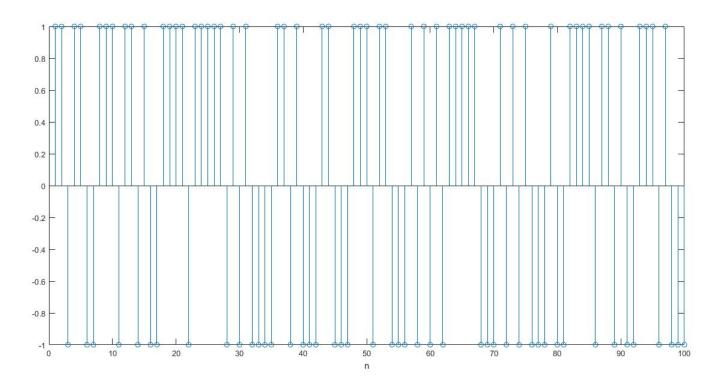


Figure 5: random sequence of impulses

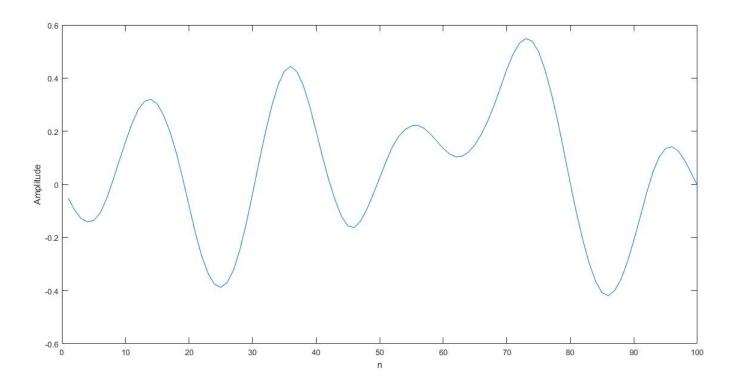


Figure 6: random sequence of pulses

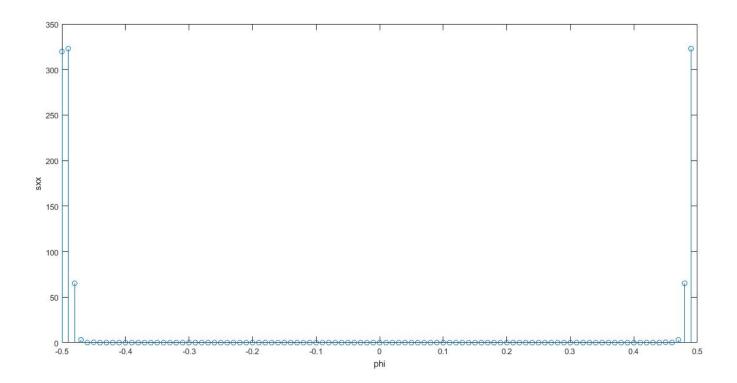


Figure 7:  $SXX(\phi)$  c=2

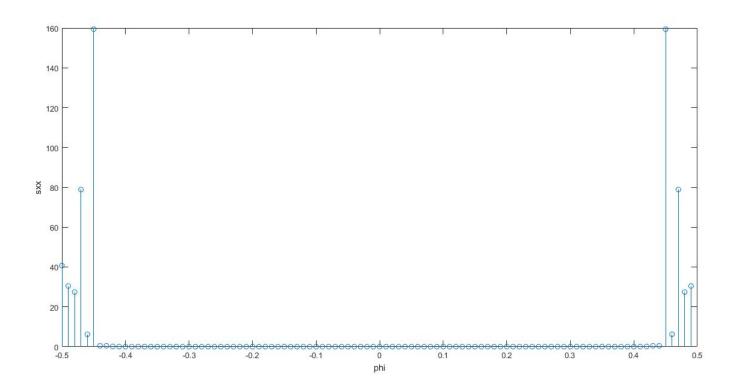


Figure 8:  $SXX(\phi)$  c=5

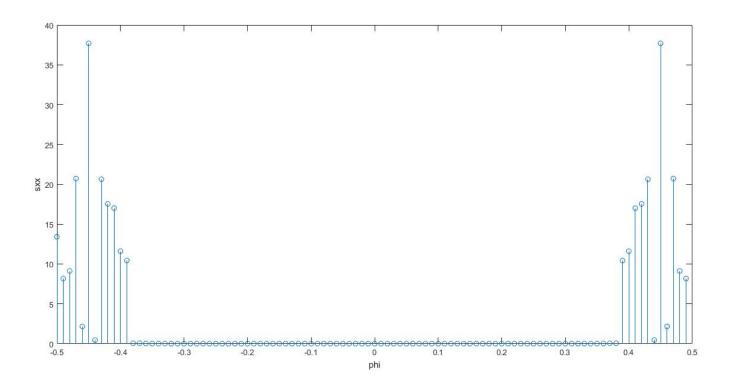


Figure 9:  $SXX(\phi)$  c = 10

### Code Appendix

```
clear;
2 clc;
з close all;
5 \text{ fe} = 0.05;
n = linspace(-200,200);
7 h = 2*fe*sinc(2*fe*n);
8 figure;
9 plot (n,h);
10 xlabel('n')
11 ylabel ('hn')
12 \%c = 2
n = linspace(-20,20);
14 h = 2*fe*sinc(2*fe*n);
15 figure;
16 plot (n,h);
17 xlabel('n')
18 ylabel ('hn')
dtft = fft (h);
dtft = fftshift (abs(dtft));
21 fc = (-\text{numel}(\text{dtft})/2:\text{numel}(\text{dtft})/2-1)./\text{numel}(\text{dtft});
22 figure;
23 plot(fc,dtft);
24 xlabel('f');
25 ylabel('|H|');
26 \% c = 5
n = linspace(-60,60);
h = 2*fe*sinc(2*fe*n);
19 figure;
plot(n,h);
31 xlabel('n')
32 ylabel ('hn')
dtft = fft (h);
dtft = fftshift (abs(dtft));
35 fc = (-\text{numel}(\text{dtft})/2:\text{numel}(\text{dtft})/2-1)./\text{numel}(\text{dtft});
36 figure;
37 plot (fc , dtft);
38 xlabel('f');
39 ylabel(', |H|');
40 \% c = 10
n = linspace(-110,110);
h = 2*fe*sinc(2*fe*n);
43 figure;
44 plot (n,h);
45 xlabel('n')
46 ylabel ('hn',)
dtft = fft (h);
48 dtft = fftshift (abs(dtft));
49 fc = (-numel(dtft)/2:numel(dtft)/2-1)./numel(dtft);
50 figure;
plot (fc , dtft);
```

```
52 xlabel('f');
53 ylabel('|H|');
54 %last part
55 \text{ iidp} = \mathbf{zeros}(1,100);
56 for i = 1:100
flip = discrete([1,1]);
if (flip == 2)
59 iidp(i) = 1;
60 else
61 \text{ iidp (i)} = -1;
62 end
63 end
64
65 %c=5
n = linspace(-60,60);
67 h = 2*fe*sinc(2*fe*n);
68 figure;
69 stem (iidp)
70 xlabel('n');
71 \text{ iidpft} = \text{fft}(\text{iidp});
filterdFt = iidpft.*fft(h);
73 filteredDt = ifft (filterdFt);
74 figure;
75 plot (filteredDt);
76 xlabel('n');
77 ylabel('Amplitude')
78
79 \%c=2
so n = linspace(-20,20);
h = 2*fe*sinc(2*fe*n);
82 figure;
83 stem (iidp)
84 xlabel('n');
85 \text{ iidpft} = \text{fft}(\text{iidp});
86 filterdFt = iidpft.*fft(h);
87 filteredDt = ifft (filterdFt);
88 figure;
89 plot(filteredDt);
90 sxx = (abs(iidpft).^2).*(abs(fft(h))).^2;
\mathbf{x} = -0.5:0.01:0.49;
92 figure;
93 stem(x, sxx);
94 xlabel('phi');
95 ylabel('sxx');
96
97 %c=5
98 n = linspace(-60,60);
99 h = 2*fe*sinc(2*fe*n);
100 figure;
101 stem (iidp)
102 xlabel('n');
iidpft = fft(iidp);
filterdFt = iidpft.* fft(h);
filteredDt = ifft(filterdFt);
```

```
106 figure;
plot (filteredDt);
 xx = (abs(iidpft).^2).*(abs(fft(h))).^2; 
x = -0.5:0.01:0.49;
110 figure;
stem(x, sxx);
112 xlabel('phi');
113 ylabel('sxx');
114 \% c = 10
n = linspace(-110,110);
_{116} h = 2*fe*sinc(2*fe*n);
117 figure;
118 stem (iidp)
119 xlabel('n');
iidpft = fft(iidp);
filterdFt = iidpft.*fft(h);
122 filteredDt = ifft (filterdFt);
123 figure;
plot (filteredDt);
127 figure;
128 stem(x,sxx);
129 xlabel('phi');
130 ylabel('sxx');
```