Problem 19.1: Compute the determinant of:

$$A = \left[egin{array}{cccc} 0 & 0 & 0 & 1 \ 1 & 0 & 0 & 0 \ 0 & 1 & 0 & 0 \ 0 & 0 & 1 & 0 \end{array}
ight].$$

Which method of computing the determinant do you prefer for this problem, and why?

Problem 19.2: (5.2 #33. *Introduction to Linear Algebra:* Strang) The symmetric Pascal matrices have determinant 1. If I subtract 1 from the *n*, *n* entry, why does the determinant become zero? (Use rule 3 or cofactors.)

$$\det\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 4 \\ 1 & 3 & 6 & 10 \\ 1 & 4 & 10 & 20 \end{bmatrix} = 1 \text{ (known)} \qquad \det\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 4 \\ 1 & 3 & 6 & 10 \\ 1 & 4 & 10 & 19 \end{bmatrix} = \mathbf{0} \text{ (to explain)}.$$

19.1

$$\begin{vmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{vmatrix} = (-1)^{3} \begin{vmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{vmatrix} = (-1)^{3} (1) = 1.$$

Using row operations and properties of determinants is much simpler than cofactor expansion for this A.

19.2 By rule 3: