

exercise 1:

Let a_n be a sequence which converges to a positive number A . We showed in class that there is an N in \mathbb{N} such that for all $n > N$ in \mathbb{N} , $|a_n| > \frac{A}{2}$. From there, show that $\frac{1}{a_n}$ converges to $\frac{1}{A}$.

exercise 2:

Optional 2.6.G from Davidson - Donsig.

exercise 3:

Prove or disprove:

Let a_n be a sequence of real numbers. If $\lim_{n \rightarrow \infty} (a_{n+1} - a_n) = 0$, then a_n is convergent.

exercise 4:

Let q be a fixed positive number. Show that the sequence $a_n = \frac{q^n}{n!}$ is eventually decreasing.

exercise 5:

2.6.B from Davidson - Donsig. **Hint:** set $f(x) = \sqrt{5 + 2x}$. Solve $f(x) = x$ and the inequality $x \leq f(x)$. Prove by induction that $0 \leq a_n \leq a_{n+1} \leq 1 + \sqrt{6}$.

exercise 6:

2.7.A

exercise 7:

2.7.G. **Hint:** any integer p can be written as $3n - 1$, $3n$, or $3n + 1$.