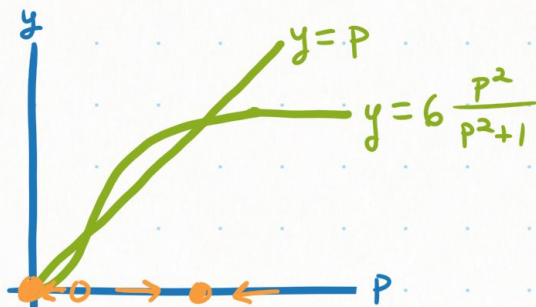


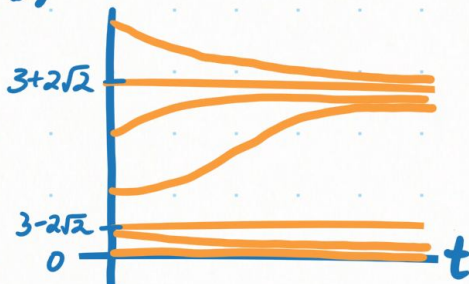
$$1 \dot{p} = -p + A \frac{p^2}{p^2+1}, \quad p(t) \geq 0, \quad A > 0$$

a) $A = 6$

$$p^* = 0, 3 \pm 2\sqrt{2}$$

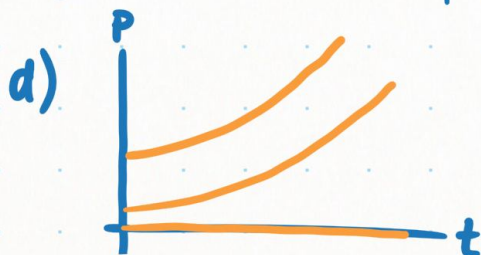
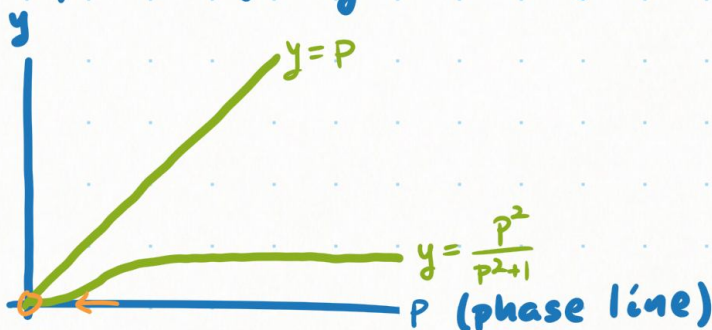


b) P



c) $A = 1$

$$p^* = 0 \text{ (only 1 real fixed point)}$$



e) Choose $A = 6$ since the system has nonzero steady states for $A = 6$ but not $A = 1$. You must also start with $p(0) \geq 3 - 2\sqrt{2}$.

2 In order to exhibit the behavior seen in the video, there must be 3 real p^* .

$$0 = -p + A \frac{p^2}{p^2 + 1}$$

$$0 = p(p^2 - Ap + 1)$$

$$p^* = 0, \frac{A \pm \sqrt{A^2 - 4}}{2}$$

There are 3 real p^* if $A^2 > 4 \rightarrow A > 2$.