## Homework #2 MME 529

Page 37 Burton please do problems 1,2,3,5,6

## additionally:

- 1. Suppose x is an integer and someone has applied the Fundamental Theorem of Arithmetic to it, obtaining  $x = p_1^{\alpha_1} p_2^{\alpha_2} ... p_n^{\alpha_n}$  What would  $x^3$  look like? What generalization can you make out of this?
- 2. If p is a prime number, does px ky = 1 have solutions? k could be any integer here.
- 3. If p is a prime number, argue why p must divide  $C_{p,r}$  (binomial coefficient)
- 4. See if you can prove the following:

if  $\mathbf{x}$  divides the product  $\mathbf{bc}$  and  $\mathbf{x}$  is prime then  $\mathbf{x}$  divides either  $\mathbf{b}$  or  $\mathbf{c}$ .

Make up a counterexample where  $\mathbf{x}$  is *not* prime and  $\mathbf{x}$  divides their product but not either one.