

Homework #1 MME 529

1. Use Euclid's Algorithm to find the gcd of each pair
a) 24,138 b) 159 , 414 c) 272 and 1479 d) 4144 and 7696
2. Use the prime factorization of the numbers in Problem 1 to find their gcd's.
(feel free to use software for the prime factorization)
3. a) If $a|b$ and $a|c$ prove that $a|(b+c)$.
b) prove $\gcd(ta,tb) = t \gcd(a,b)$
4. A student claims that $(2n+1, 2n^2 + 2n, 2n^2 + 2n + 1)$ give Pythagorean Triples
 - a) verify it *does* generate Pythagorean Triples (i.e satisfy the Pythagorean Theorem)
 - b) can you find one triple that it does *not* generate? (this would then prove that it only produces a proper subset)
5. Argue that the sum of the squares of two odd numbers must always be even.
6. What is the sum of

$$100+103+106+ \dots + 1399 \quad ?$$

7. For a general arithmetic series with $n+1$ terms $a + (a+d) + (a+2d) + \dots (a+nd)$
Can you work out a formula for the sum?
8. Can you prove the arithmetic series formula $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$ by *induction*?
9. What are the possible values of $\gcd(n,n+2)$ where n is any possible positive integer ?
10. a) Use Geometric series to sum the first n powers of 2 $1 + 2 + 2^2 + \dots + 2^{n-1}$
a) What is the *binary* form of $2^7 - 1$? $2^9 - 1$? $2^n - 1$? (by *binary* is meant base 2)
11. Consider numbers of the form $2^{pq} - 1$ where p and q are integers greater than 1. See if you can factor this. (hint: use Geometric Series)
12. Write Maple or Matlab code to generate a list of PTs as discussed in **Problem #4**. Do a screen shot and include it in your work turned in. Which ones are PPTs ?