For each observation i of species j, we assumed that the timing of phenological events were generated from the following sampling distribution:

$$y_{i,j} \sim \mathcal{N}(\mu_i, \sigma_e^2)$$
 (1)

where

$$\mu_j = \alpha_j + \beta_{chill,j} X_{chill} + \beta_{force,j} X_{force} + \beta_{photo,j} X_{photo}$$
 (2)

and σ_e^2 represents random error unrelated to the phylogeny.

Predictors X_{chill} , X_{force} , X_{photo} are standardized chilling, forcing, and photoperiod, and their effects on the phenology of species j are determined by parameters $\beta_{chill,j}$, $\beta_{force,j}$, $\beta_{photo,j}$, representing species' responses (or sensitivities) to each of the cues. These responses, including the species-specific intercept α_j , are elements of the following normal random vectors:

$$\boldsymbol{\alpha} = [\alpha_1, \dots, \alpha_n]^T \text{ such that } \boldsymbol{\alpha} \sim \mathcal{N}(\mu_{\alpha}, \boldsymbol{\Sigma}_{\alpha})$$
(3)
$$\boldsymbol{\beta_{chill}} = [\beta_{1,1}, \dots, \beta_{chill,n}]^T \text{ such that } \boldsymbol{\beta_{chill}} \sim \mathcal{N}(\mu_{\beta_{chill}}, \boldsymbol{\Sigma}_{\beta_{chill}})$$

$$\boldsymbol{\beta_{force}} = [\beta_{2,1}, \dots, \beta_{force,n}]^T \text{ such that } \boldsymbol{\beta_{force}} \sim \mathcal{N}(\mu_{\beta_{force}}, \boldsymbol{\Sigma}_{\beta_{force}})$$

$$\boldsymbol{\beta_{photo}} = [\beta_{3,1}, \dots, \beta_{photo,n}]^T \text{ such that } \boldsymbol{\beta_{photo}} \sim \mathcal{N}(\mu_{\beta_{nhoto}}, \boldsymbol{\Sigma}_{\beta_{nhoto}})$$

where the means of the multivariate normal distributions are root trait values (i.e., values of cue responses prior to evolving across a phylogenetic tree) and Σ_i are $n \times n$ phylogenetic variance-covariance matrices of the form:

$$\begin{bmatrix} \sigma_i^2 & \lambda_i \times \sigma_i \times \rho_{12} & \dots & \lambda_i \times \sigma_i \times \rho_{1n} \\ \lambda_i \times \sigma_i \times \rho_{21} & \sigma_i^2 & \dots & \lambda_i \times \sigma_i \times \rho_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ \lambda_i \times \sigma_i \times \rho_{n1} & \lambda_i \times \sigma_i \times \rho_{n2} & \dots & \sigma_i^2 \end{bmatrix}$$

$$(4)$$

where σ_i^2 is the rate of evolution across a tree for trait i (here assumed to be constant along all branches), λ_i scales branch lengths and therefore is a measure of the "phylogenetic signal" or extent of phylogenetic relatedness on each model parameter (i.e., α_j , $\beta_{force,j}$, $\beta_{force,j}$, $\beta_{photo,j}$), and ρ_{xy} is the phylogenetic correlation between species x and y, or the fraction of the tree shared by the two species.

The above specification is equivalent to writing equation ?? in terms of root trait values and residuals, such that:

$$\mu_j = \mu_{\alpha} + \mu_{\beta_{chill}} X_{chill} + \mu_{\beta_{force}} X_{force} + \mu_{\beta_{photo}} X_{photo} + e_{\alpha_j} + e_{\beta_{force,j}} + e_{\beta_{chill,j}} + e_{\beta_{photo,j}}$$
 (5)

where the residual phylogenetic error terms (e.g., e_{α_j}) are elements of normal random vectors from multivariate normal distributions centered on 0 with the same phylogenetic variance-covariance matrices as in equation ??. Model code, including priors used here, are given in the supplement.