Basic Math for Physics

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1 Quadratic Equation - Phương trình bậc 2

Với phương trình $ax^2 + bx + c = 0 \ (a \neq 0)$.

Ta có
$$\Delta = b^2 - 4ac$$
.

TH1. $\Delta < 0$ phương trình vô nghiệm

TH2. $\Delta=0$ phương trình có nghiệm kép $x_1=x_2=-\frac{b}{2ac}$

TH3. $\Delta > 0$ phương trình có hai nghiệm phân biệt $x_{1;2} = \frac{-b \pm \sqrt{\Delta}}{2a}$

2 Common Formulae of Algebra - Hằng đẳng thức đáng nhớ

(i)
$$(a+b)^2 = a^2 + b^2 + 2ab$$

(ii)
$$(a-b)^2 = a^2 + b^2 - 2ab$$

(iii)
$$(a+b+c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca$$

(iv)
$$(a+b)(a-b) = a^2 - b^2$$

(v)
$$(a+b)^3 = a^3 + b^3 + 3ab(a+b)$$

(vi)
$$(a-b)^3 = a^3 - b^3 - 3ab(a-b)$$

(vii)
$$(a+b)^2 - (a-b)^2 = 4ab$$

(viii)
$$(a+b)^2 + (a-b)^2 = 2(a^2+b^2)$$

(ix)
$$a^3 - b^3 = (a - b)(a^2 + b^2 + ab)$$

(x)
$$a^3 + b^3 = (a+b)(a^2+b^2-ab)$$

3 Arithmetic Progression - Tiến trình số học

(i) n^{th} term of arithmetic progression

$$a_n = a_0 + (n-1)d$$

 $a_0 = \text{First term},$

n = Number of terms,

d =Common difference

$$= (a_1 - a_0)$$
 or $(a_2 - a_1)$ or $(a_3 - a_2)$

(ii) Sum of arithmetic progression

$$S_n = \frac{n}{2}[2a_0 + (n-1)d] = \frac{n}{2}[a_0 + a_n]$$

 $a_n = \text{last term}$

4 Geometric Progression - Tiến trình hình học

Here a =first term, r =common ratio (tỷ lệ chung)

(i) Sum of 'n' terms of G.P

$$S_n = \frac{a(1-r^n)}{1-r} \quad \text{if} \quad r < 1$$

$$S_n = \frac{a(r^n - 1)}{r - 1} \quad \text{if} \quad r > 1$$

(ii) Sum of infinite terms of G.P

$$S_{\infty} = \frac{a}{1 - r} \quad \text{if} \quad r < 1$$

$$S_{\infty} = \frac{a}{r-1} \quad \text{if} \quad r > 1$$

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5 Trigonometry Angle

Hình 1: Length of chord $l = \frac{\pi Rn}{180}$

$$Angle(\theta) = \frac{ArcLength}{Radius} = \frac{L}{r}$$
 (formula true for radian only)

6 Trigonometry Ratio

$$\begin{split} \sin(\theta) &= \frac{Perpendicular}{Hypotenuse} = \frac{p}{h} = \text{di hoc} \\ \cos(\theta) &= \frac{Base}{Hypotenuse} = \frac{b}{h} = \text{không hư} \\ \tan(\theta) &= \frac{\sin(\theta)}{\cos(\theta)} = \frac{Perpendicular}{Base} = \frac{p}{b} = \text{đoàn kết} \\ \cos(\theta) &= \frac{1}{\sin(\theta)}; \qquad \sec(\theta) = \frac{1}{\cos(\theta)}; \qquad \cot(\theta) = \frac{1}{\tan(\theta)} \end{split}$$

7 Trigonometry values of Larger Angles

$$\begin{array}{ll} \sin(180^o-\theta)=\sin(\theta) & \sin(360^o-\theta)=-\sin(\theta) \\ \cos(180^o-\theta)=-\cos(\theta) & \cos(360^o-\theta)=\cos(\theta) \\ \tan(180^o-\theta)=-\tan(\theta) & \tan(360^o-\theta)=-\tan(\theta) \\ \sin(180^o+\theta)=-\sin(\theta) & \sin(360n^o+\theta)=\sin(\theta) \\ \cos(180^o+\theta)=-\cos(\theta) & \cos(360n^o+\theta)=\cos(\theta) \\ \tan(180^o+\theta)=\tan(\theta) & \tan(360n^o+\theta)=\tan(\theta) \end{array}$$

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8 Trigonometrical Indentities

(i)
$$sin^2(\theta) + cos^2(\theta) = 1$$

(ii)
$$sec^2(\theta) - tan^2(\theta) = 1$$

(iii)
$$cosec^2(\theta) + cot^2(\theta) = 1$$

9 Trigonometry Formulae

$$\begin{split} \sin(A+B) &= \sin(A)\cos(B) + \cos(A)\sin(B) \\ \sin(A-B) &= \sin(A)\cos(B) - \cos(A)\sin(B) \\ \cos(A+B) &= \cos(A)\cos(B) - \sin(A)\sin(B) \\ \cos(A-B) &= \cos(A)\cos(B) + \sin(A)\sin(B) \\ \tan(A+B) &= \frac{\tan(A) + \tan(B)}{1 - \tan(A)\tan(B)} \\ \tan(A-B) &= \frac{\tan(A) - \tan(B)}{1 + \tan(A)\tan(B)} \\ \sin(2\theta) &= 2\sin(\theta)\cos(\theta) \\ \cos(2\theta) &= \cos^2(\theta) - \sin^2(\theta) = 2\cos^2(\theta-1) = 1 - 2\sin^2(\theta) \\ \tan(2\theta) &= \frac{2\tan(\theta)}{1 - \tan^2(\theta)} \end{split}$$

10 Logarithm

If $a^x = N$ then $log_a(N) = x$ Conversion of natural log into common log:

$$log_e(x) = ln(x) = 2.3026log_{10}(x)$$

11 Important formulae of logarithm

- (i) $log_a(m.n) = log_a(m) + log_a(n)$
- (ii) $log_a(m/n) = log_a(m) log_a(n)$
- (iii) $log_a(m^n) = nlog_a(m)$

12 Differential Calculus

$y = x^n$	$\frac{dy}{dx} = nx^{n-1}$	y = sin(x)	$\frac{dy}{dx} = \cos(x)$
y = kx	$\frac{dy}{dx} = k \frac{dx}{dx} = k$	y = cos(x)	$\frac{dy}{dx} = -\sin(x)$
y = k	$\frac{dy}{dx} = 0$	y = tan(x)	$\frac{dy}{dx} = sec^2(x)$
$y = \frac{1}{x}$	$\frac{dy}{dx} = -\frac{1}{x^2}$	y = coses(x)	$\frac{dy}{dx} = -cot(x)cosec(x)$
$y = \sqrt{x}$	$\frac{dy}{dx} = \frac{1}{2\sqrt{x}}$	y = sec(x)	$\frac{dy}{dx} = sec(x)tan(x)$
y = ln(x)	$\frac{dy}{dx} = \frac{1}{x}$	y = cot(x)	$\frac{dy}{dx} = -cosec^2(x)$
$y = log_a(x)$	$\frac{dy}{dx} = \frac{1}{x}log_a(e)$		
$y = e^x$	$\frac{dy}{dx} = e^x$		
$y = a^x$	$\frac{dy}{dx} = a^x log_e(a)$		

(u+v)' = u' + v'	(u-v)' = u' - v'	(u.v)' = u'v + v'u	$\left(\frac{u}{v}\right)' = \frac{u'.v - v'.u}{v^2}$
$(e^u)' = u'.e^u$	$ln(u)' = \frac{u'}{u}$	$(u^{\alpha})' = \alpha.u^{\alpha - 1}.u'$	$(\sqrt{u})' = \frac{u'}{2\sqrt{u}}$
$(\sqrt[n]{u})' = \frac{u'}{n\sqrt[n]{u^{n-1}}}$	$(\sin(u))' = u' \cdot \cos(u)$	$(\cos(u))' = -u' \cdot \sin(u)$	$(a^u)' = u'.a^u.ln(a)$
$(log_a(u))' = \frac{u'}{u \cdot ln(a)}$			

$$(\tan(u))' = \frac{u'}{\cos^2(u)}$$

$$(\cot(u))' = -\frac{u'}{\sin^2(u)}$$

$$\left[(x^m)^n \right]' = (m \ge n) \quad ? \quad m(m-1)(m-2)(m-n+1)x^{m-n} : 0$$

$$(\log_a(x))^n = (-1)^{n-1} \cdot \frac{(n-1)!}{\ln(a)} \frac{1}{x^n}$$

$$(\ln(x))^n = (-1)^{n-1} \cdot (n-1)! \cdot x^{-n}$$

$$(e^{kx})^n = k^n \cdot e^{kx}$$

$$(a^x)^n = (\ln(a))^n \cdot a^x$$

$$(\sin(ax))^n = a^n \cdot \sin(ax + n \cdot \pi/2)$$

$$(\cos(ax))^n = a^n \cdot \cos(ax + n \cdot \pi/2)$$

$$\left(\frac{1}{ax+b} \right)^n = (-1)^n \cdot a^n \cdot n! \cdot \frac{1}{(ax+b)^{n+1}}$$

$$(\arcsin(x))' = \frac{1}{\sqrt{1-x^2}}$$

$$(\arccos(x))' = \frac{-1}{\sqrt{1-x^2}}$$

$$(\arctan(x))' = \frac{1}{1+x^2}$$

Chain rule

$$\left[f\Big(g(x)\Big)\right]' = f'\Big(g(x)\Big).g'(x)$$

13 Integral Calculus

$y = x^n$	$\int x^n dx = \frac{x^{n+1}}{n+1} + c$	y = sin(x)	$\int \sin(x)dx = -\cos(x)$
y = k	$\int kdx = kx + c$	y = cos(x)	$\int \cos(x)dx = \sin(x)$
y = 1	$\int dx = x + c$	$y = sec^2(x)$	$\int sec^2(x)dx = tan(x)$
$y = \frac{1}{x}$	$\int \frac{1}{x} dx = \ln(x) + c$	y = sec(x)tan(x)	$\int sec(x)tan(x)dx = sec(x)$
$y = e^x$	$\int e^x dx = e^x + c$	$y = cosec^2(x)$	$\int cosec^2(x)dx = -cot(x)$
$y = a^x$	$\int a^x dx = \frac{a^x}{\log_e(a)} + c$	y = cosec(x)cot(x)	$\int cosec(x)cot(x)dx = -cosec(x)$

14 Circumferences

- 1. Circumderence of circle: $C=2\pi R$
- 2. Circumderence of triangle: P = a + b + c

15 Formulae for Area and Volume

- 1. Area of square = $(side)^2$
- 2. Area of rectangle = $length \times length$
- 3. Area of triangle = $\frac{1}{2} \times base \times height$
- 4. Area of equilateral triangle = $\frac{\sqrt{3}}{4}a^2$
- 5. Are enclosed by a circle = πr^2
- 6. Surface area of sphere = $4\pi r^2$
- 7. Surface area of cube = $6L^2$

- 8. Surface area of cuboid $= 2[L \times b + b \times h + h \times L]$
- 9. Area of curved surface of cylinder = $2\pi rl$
- 10. Volume of cube = L^3
- 11. Volume of cuboid = $L \times b \times h$
- 12. Volume of sphere = $\frac{4}{3}\pi r^3$
- 13. Volume of cylinder = $\pi r^3 l$
- 14. Volume of cone = $\frac{1}{2}\pi r^2 h$