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Lớp: 20CTT4

8.9

b. Ta có: $(1-\alpha) \cdot 100\% = 95\% \Rightarrow \alpha = 0,05$

$$P(Z < z_{1-\alpha/2}) = 1 - \frac{\alpha}{2} = 0,975 \Rightarrow z_{1-\alpha/2} \approx 1,96$$

$$\text{Vậy } \bar{x} - z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{x} + z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$\Rightarrow 1000 - 1,96 \frac{20}{\sqrt{25}} \leq \mu \leq 1000 + 1,96 \frac{20}{\sqrt{25}}$$

$$\Rightarrow 992,16 \leq \mu \leq 1007,84$$

c. Ta có: $(1-\alpha) \cdot 100\% = 99\% \Rightarrow \alpha = 0,01$

$$P(Z < z_{1-\alpha/2}) = 1 - \frac{\alpha}{2} = 0,995 \Rightarrow z_{1-\alpha/2} = 2,576$$

$$\text{Vậy } \bar{x} - z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{x} + z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$\Rightarrow 1000 - 2,576 \frac{20}{\sqrt{10}} \leq \mu \leq 1000 + 2,576 \frac{20}{\sqrt{10}}$$

$$\Rightarrow 983,21 \leq \mu \leq 1016,78$$

d. $(1-\alpha) \cdot 100\% = 99\% \Rightarrow \alpha = 0,01$

$$P(Z < z_{1-\alpha/2}) = 1 - \frac{\alpha}{2} = 0,995 \Rightarrow z_{1-\alpha/2} = 2,576$$

$$\text{Vậy } \bar{x} - z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{x} + z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$\Rightarrow 1000 - 2,576 \frac{20}{\sqrt{25}} \leq \mu \leq 1000 + 2,576 \frac{20}{\sqrt{25}}$$

$$\Rightarrow 989,2 \leq \mu \leq 1010,8$$

e. Khi cỡ mẫu tăng thì khoảng tin cậy ngày càng gần

8.9. $\alpha = 0,01$; $\bar{x} = 1,5054$ (inch); khoảng tin cậy 99%; $n = 10$

Ta có: $(1-\alpha) \cdot 100\% = 99\% \Rightarrow \alpha = 0,01$

$$P(Z < z_{1-\alpha/2}) = 1 - \frac{\alpha}{2} = 0,995 \Rightarrow z_{1-\alpha/2} = 2,576$$

$$\text{Vậy } \bar{x} - z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{x} + z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$\Rightarrow 1,5054 - 2,576 \frac{0,01}{\sqrt{10}} \leq \mu \leq 1,5054 + 2,576 \frac{0,01}{\sqrt{10}}$$

$$\Rightarrow 1,498 \leq \mu \leq 1,5135$$

8.10. $\sigma^2 = 1000$; $n = 12$; $\bar{x} = 3250$

a. Khoảng tin cậy 95%: $(1-\alpha) \cdot 100\% = 95\% \Rightarrow \alpha = 0,05$

$$P(Z < z_{1-\alpha/2}) = 1 - \frac{0,05}{2} = 0,975 \Rightarrow z_{1-\alpha/2} \approx 1,96$$

$$\text{Vậy } \bar{x} - z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{x} + z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$\Rightarrow 3250 - 1,96 \frac{\sqrt{1000}}{\sqrt{12}} \leq \mu \leq 3250 + 1,96 \frac{\sqrt{1000}}{\sqrt{12}}$$

$$\Rightarrow 3232,11 \leq \mu \leq 3267,89$$

$$b. (1-\alpha) = 100\% = 99\% \Rightarrow \alpha = 0,01$$

$$P(Z < z_{1-\alpha/2}) = 1 - \frac{0,01}{2} = 0,995 \Rightarrow z_{1-\alpha/2} \approx 2,576$$

$$\text{Vậy } \bar{x} - z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{x} + z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$3250 - 2,576 \frac{\sqrt{1000}}{\sqrt{12}} \leq \mu \leq 3250 + 2,576 \frac{\sqrt{1000}}{\sqrt{12}}$$

$$\Rightarrow 3206,48 \leq \mu \leq 3293,52$$

c. Sai số không vượt quá 15%.

$$\Rightarrow z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}} = 15$$

$$\text{Mà } (1-\alpha) = 100\% = 99\% \Rightarrow \alpha = 0,01 \Rightarrow z_{1-\alpha/2} \approx 2,576$$

$$\Rightarrow 2,576 \frac{\sqrt{1000}}{\sqrt{n}} = 15 \Leftrightarrow n \approx 30$$

$$8.15. \bar{x} = 185,255; \sigma^2 = 1253,03$$

$$8.16. \bar{x} = 231,61; \sigma^2 = 1,82536$$

$$8.18. \bar{x} = 2,902; \sigma^2 = 9,0922 \cdot 10^{-3}$$

$$8.19. \bar{x} = 12,21; \sigma^2 = 0,0109 \quad s^2 = 0,102$$

$$8.20. \bar{x} = 156,204; \sigma^2 = 36,283 \quad s^2 = 37,68$$

$$8.21. \bar{x} = 225,15; \sigma^2 = 123,66 \quad s^2 = 175,81$$

$$8.22. \bar{x} = 132,83; \sigma^2 = 17,81$$

$$8.23. \bar{x} = 1391,41; \sigma^2 = 54535,52$$

$$8.28. \bar{x} = 21,4125; \sigma^2 = 0,2836 \quad s^2 = 0,896$$

$$9.29. \bar{x} = 325,496; \sigma^2 = 38052,14$$

$$9.30. \bar{x} = 98,649; \sigma^2 = 0,2231$$

$$9.31. \bar{x} = 129,242; \sigma^2 = 0,229$$

$$9.32. \bar{x} = 123,226; \sigma^2 = 138,41$$

$$9.33. \bar{x} = 0,9856; \sigma^2 = 4,2864 \cdot 10^{-4}$$

$$9.34. \bar{x} = 15,4; \sigma^2 = 3,36$$

$$9.35. \bar{x} = 2,639; \sigma^2 = 3,286$$

$$10.13. \text{Mẫu 1: } \bar{x} = 9,92; \sigma^2 = 0,1601$$

$$2: \bar{x} = 10,4; \sigma^2 = 0,048$$

$$10.17. 50^\circ\text{C: } \bar{x} = 0,0964; \sigma^2 = 2,1162 \cdot 10^{-3}$$

$$60^\circ\text{C: } \bar{x} = 0,1286; \sigma^2 = 2,2851 \cdot 10^{-3}$$

$$10.18. \text{Cty 1: } \bar{x} = 92,4; \sigma^2 = 63,04$$

$$\text{Cty 2: } \bar{x} = 110; \sigma^2 = 782,857$$

$$10.19. \text{K' h'at: } \bar{x} = 0,9158; \sigma^2 = 0,044$$

$$\text{H'at: } \bar{x} = 0,92625; \sigma^2 = 0,1341$$

$$10.20. \text{Tham 1: } \bar{x} = 9892,5; \sigma^2 = 58129243$$

$$2: \bar{x} = 4120,83; \sigma^2 = 56356,08$$

$$10.21. \text{V' Rad'at: } \bar{x} = 52,5; \sigma^2 = 1,0158$$

$$\text{V' b'at: } \bar{x} = 6,6083; \sigma^2 = 0,906$$