

Hwk 4

February 1, 2018

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```
In [1]: import numpy as np
import scipy.stats as stats

# Graphics
import matplotlib as mpl
import matplotlib.pyplot as plt
import seaborn as sns
from matplotlib import rc

rc('text', usetex=True)
rc('text.latex', preamble=r'\usepackage{cmbright}')
rc('font', **{'family': 'sans-serif', 'sans-serif': ['Helvetica']})

# Magic function to make matplotlib inline;
%matplotlib inline

# This enables SVG graphics inline.
# There is a bug, so uncomment if it works.
%config InlineBackend.figure_formats = {'png', 'retina'}

# JB's favorite Seaborn settings for notebooks
rc = {'lines.linewidth': 2,
      'axes.labelsize': 18,
      'axes.titlesize': 18,
      'axes.facecolor': 'DFDFE5'}
sns.set_context('notebook', rc=rc)
sns.set_style("dark")

mpl.rcParams['xtick.labelsize'] = 16
mpl.rcParams['ytick.labelsize'] = 16
mpl.rcParams['legend.fontsize'] = 14
```

2 Implementation of Needleman Wunsch algorithm

The algorithm below works but is a little incomplete. At the moment it will fail if there are multiple optimal alignments, but this could be easily solved by choosing one optimal alignment at random. Alternatively, I could modify it by presenting all possible alignments, but I started this morning and ran out of time. All work below is my own.

```
In [9]: class needle:
        def __init__(self, a, b):
            """Initialize needle object"""
            self.a = ' ' + a
            self.b = ' ' + b
            self.m, self.x, self.g = 10, -1, -5
            self.make_mat()
            self.histories = {}

        def make_mat(self):
            """Initialize alignment matrix"""
            n, n2 = len(self.a), len(self.b)
            mat = np.zeros(shape=(n, n2))
            mat[:,0] = np.linspace(0, (n-1)*self.g, n)
            mat[0,:] = np.linspace(0, (n2-1)*self.g, n2)
            self.mat = mat

        def matcher(self, c1, c2):
            """For a pair of coordinates, if the pair matches,
            figure out whether they should be aligned or not"""
            if self.a[c1] == self.b[c2]:
                return self.m
            else:
                return self.x

        def submat(self, c1, c2):
            """Returns a 2x2 submatrix"""
            smat = self.mat[c1-1:c1+1, c2-1:c2+1]
            return smat

        def next_square(self, c1, c2):
            """Fill in the next 2x2 square"""
            smat = self.submat(c1, c2)
            # (c1,c2)-1 -> (c1, c2) is a possible match
            s00 = smat[0, 0] + self.matcher(c1, c2)
            # other two are gaps
            s10 = smat[1, 0] + self.g
            s01 = smat[0, 1] + self.g

            array = np.array([s00, s10, s01])
            score = np.max(array)
```

```

self.mat[c1, c2] = score
self.histories[(c1, c2)] = np.where(array == score)[0]

def fill_in(self):
    """Fill in the matrix"""
    for c1 in range(1, len(self.a)):
        for c2 in range(1, len(self.b)):
            self.next_square(c1, c2)

def init_traceback(self):
    """Initialize the traceback parameters"""
    # coordinates of the maximum score(s)
    # note, np.where returns an x-coord array and a y-coord
    # array in a tuple if there is more than one entry
    c = np.where(np.max(self.mat[:,len(self.b)-1]) == self.mat)
    if len(c[0]) > 1:
        # there are multiple alignments
        print('uhoh')
    else:
        self.initial_coords = (c[0][0], c[1][0])
        begin = self.histories[self.initial_coords]

    self.begin = begin

def trace(self, c1, c2, trace, Sa, Sb):
    """Figures out whether it is a gap or a mismatch or what"""
    if len(trace) == 1:
        if trace[0] == 0:
            return c1-1, c2-1, self.a[c1-1]+Sa, self.b[c1-1]+Sb
        if trace[0] == 1:
            return c1-1, c2, self.a[c1-1]+Sa, '-' +Sb
        else:
            return c1, c2 -1, '-' +Sa, self.b[c2-1]+Sb
    else:
        print('uhoh')

def traceback(self):
    """
    Trace an alignment path.
    This function currently only works if there is a SINGLE
    allowable alignment...
    I could easily fix this by choosing a random alignment out of
    the multiple optimal ones
    """

    self.init_traceback()
    c = np.where(np.max(self.mat[:,len(self.b)-1]) == self.mat)
    c1_init = c[0][0]

```

```

c2_init = c[1][0]
C1, C2 = np.array([c1_init]), np.array([c2_init])
F = True
c1, c2 = c1_init, c2_init
Sa = self.a[c1]
Sb = self.b[c2]
while F:
    if (c1, c2) not in self.histories.keys():
        F = False
        continue
    c1, c2, Sa, Sb = self.trace(c1, c2, self.histories[(c1, c2)], Sa, Sb)
    C1, C2 = np.append(C1, [c1]), np.append(C2, [c2])
self.C1 = C1
self.C2 = C2

def draw_alignments(self):
    """Draw the alignment as a matrix of zeros and 1's"""
    self.m = np.zeros(shape=(len(self.a), len(self.b)))
    for coord in zip(self.C1, self.C2):
        self.m[coord[0], coord[1]] = 1
    print(self.m)

```

```

In [3]: wunsch = needle('atcg', 'atc')
        wunsch.fill_in()
        wunsch.mat

```

```

Out[3]: array([[ 0., -5., -10., -15.],
               [-5., 10., 5., 0.],
               [-10., 5., 20., 15.],
               [-15., 0., 15., 30.],
               [-20., -5., 10., 25.]])

```

Here, I perform the traceback, and then draw the alignment as a matrix of zeros and ones.

```

In [4]: wunsch.traceback()
        wunsch.draw_alignments()

```

```

[[ 1.  0.  0.  0.]
 [ 0.  1.  0.  0.]
 [ 0.  0.  1.  0.]
 [ 0.  0.  0.  1.]
 [ 0.  0.  0.  0.]]

```

3 Implementation of a random number generator with a negative binomial distribution

For this problem, I relied heavily on this [PDF](#), page 21.

A geometric random variable, Y_N can be generated from a $\text{geom}(p)$ distribution by using the generator:

$$Y_i = \lfloor 1 + \frac{\log u_i}{\log 1-p} \rfloor$$

The PDF I used claims that the negative binomial distribution with parameters p and n can be generated by calculating:

$$r + \sum_i^r Y_i(p)$$

However, when I compare my generator with the scipy generator, the functions are shifted and the correction that matches the curves exactly is:

$$\sum_i^r Y_i(p) - r$$

```
In [5]: # define parameters to use
        n = 10
        p = .1

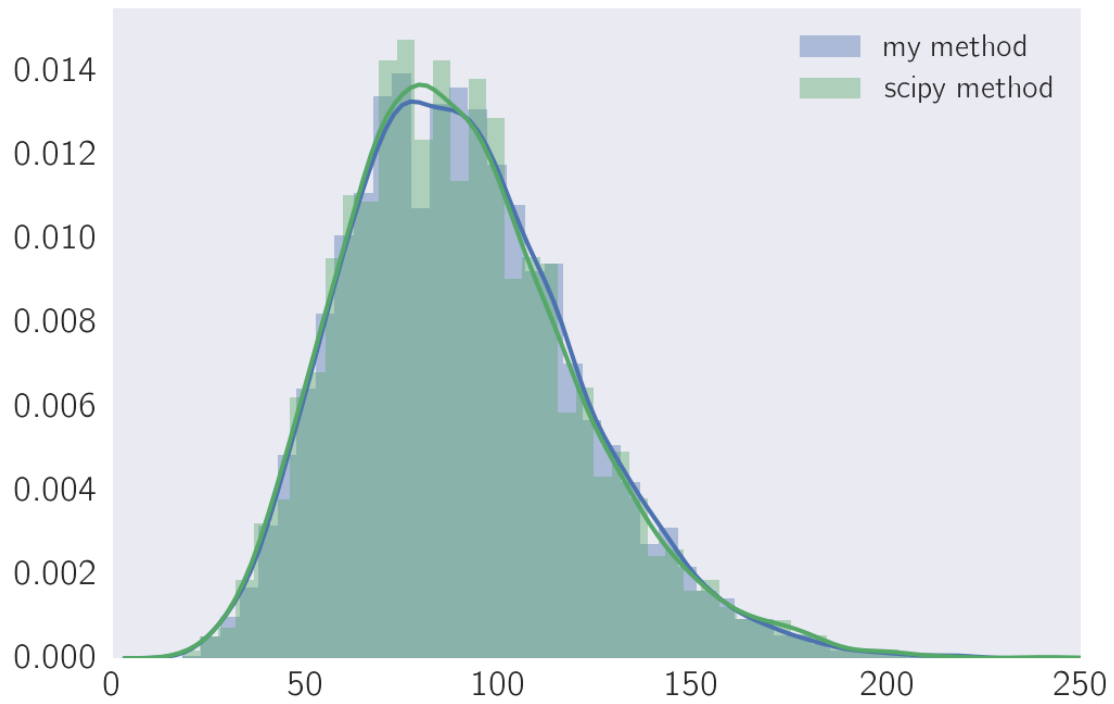
In [6]: def bernoulli_generator(p):
        """Given a probability `p`, returns a geometrically distributed variable"""
        u = np.random.random()
        return np.floor(1 + np.log(u)/np.log(1-p))

        def neg_binom_generator(n, p):
            """Generates random numbers with a negative binomial distribution.
            The method used is to add `n` random bernoulli variables, then subtracts
            `n`."""
            return np.sum(np.array([bernoulli_generator(p) for i in range(n)])) - n

In [7]: # make arrays for histograms
        iters = 10**4
        # my function
        x = np.array([neg_binom_generator(n, p) for i in range(iters)])
        # scipy function
        y = np.array([stats.nbinom.rvs(n, p, size=1) for i in range(iters)])

In [8]: # plot
        ax = sns.distplot(x, label='my method')
        ax = sns.distplot(y, label='scipy method')
        plt.xlim(0, 250)
        plt.legend()

Out[8]: <matplotlib.legend.Legend at 0x105df3710>
```



In []: