

Solution 1

- (a) I won't draw a solution here, but will provide an explanation. Picture a triangle. If you pictured it in 2 dimensions then try picturing it again in three dimensions. Now replace the sides of the triangle which you probably visualized as lines to infinite planes. Notice how each of these planes intersect at the vertices of previously visualized triangle which are now lines in 3d.

Also notice how these lines are distinct from each other yet they do not intersect hence parallel.

- (b) The normal vectors n_1, n_2, n_3 are also normal to lines l_1, l_2, l_3 respectively. Since $l_1 // l_2 // l_3$ we can cut through them in a single plane hence the vectors n_1, n_2, n_3 all lie on the same plane.
- (c) Equation of plane i is $x \cdot n_i = a_i$. But since the planes do not intersect. There is no solution. Hence, $\det(A) = 0$. This implies $n_1 \cdot n_2 \times n_3 = 0$.

Solution 2

solution

$$(a) \ A = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 3 & 5 \\ 3 & 5 & 8 \end{bmatrix}$$

$$Ax = P$$