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8

Sum (Spaces)

Superposition

Symmetric Matrix

 ${\bf Supremum}$ 

Supercritical Hopf Bifurcation

Supercritical Pitchfork Bifurcation

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