## Exercitii suplimentare

1 Déterminati multimea pet de acumulare A

(xw)men , xw= m/ w/r on terment besigns

lim san = lim 3/1 . 3/1/2 = lam 3/2 < 1, m>2, m+2, m+2 = lam m+2 < 1, m>2,

deci conform Crit. Raportului pt. sirvei (Verzi Ex. 3, Sem.4)

lim xm = +00. Deci A'= {+03.

B) A=(0,2) 1 Q. → m. ivationale dim (0,2).

Tre y E (012). Cum ouce mr. real e limita unui ya de

m. ivationale (veri Ext, Som. 1) =)

] (om) E A) 149 a.c. lim om=y, deci ye A).

y orbital => A'= (0,2).

3) Det. pet. de extrem local si valorile extreme ale fc:

$$\xi(x) = \int -x(x-x) = -x^2 + x^2, x > 0$$

! O mi Bliebovinub s um f

$$\int_{0}^{x} (0) = \lim_{x \to 0} \frac{x}{x(x-1)} = \lim_{x \to 0} \frac{x}{x(x-1)} = \lim_{x \to 0} \frac{x}{x(x-1)}$$

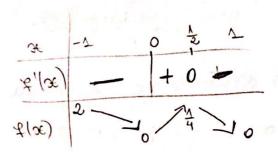
$$\lim_{x \to 0} \frac{x}{x(x-1)} = \lim_{x \to 0} \frac{x}{x(x-1)}$$

$$(a'(0) = \lim_{x \to 0} \frac{x(-x+4)}{x} = \lim_{x \to 0} \frac{x(-x+4)}{x} = 1$$

$$f'(x) = \begin{cases} 2x-1, & x < 0 \\ -2x+1, & x > 0 \end{cases}$$

$$2x-1 = 0 = 3x = \frac{1}{2} > 0, \text{ mu convine}$$

$$-2x+1 = 0 = 3x = \frac{1}{2} \text{ convine}.$$



$$(2) = \frac{1}{2} = 0 = \frac{1}{2}$$

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$$4(-1)=2$$
 $4(0)=0$ 
 $-1,\frac{1}{2}$  pct. de

 $4(\frac{1}{2})=\frac{1}{4}$ 
 $4(\frac{1}{2})=0$ 
 $0,1$  pct. de minim

 $100$ 

$$f: (0,0) \rightarrow \mathbb{R}, \quad f(x) = \frac{1 \ln x}{\sqrt{x}}, \quad x \in (0,1),$$

$$\frac{\ln x}{\sqrt{x}}, \quad x \neq 1.$$

 $\varphi'(x) = \begin{cases} \frac{2x\sqrt{x}}{2x\sqrt{x}}, & x \in (0,1) \\ \frac{2x\sqrt{x}}{2x\sqrt{x}}, & x \in (0,1) \end{cases}$ 

I mu e derivable in 1!

$$\lim_{x \to 0} \varphi(x) = \lim_{x \to 0} \frac{-\ln x}{\sqrt{x}} = \frac{1}{\sqrt{x}}$$

$$= \lim_{x \to 0} \frac{1}{\sqrt{x}} \cdot \ln x = \frac{1}{\sqrt{x}} \cdot \frac{1}{\sqrt{x}}$$

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 $\sup_{A} \varphi(A) = +\infty \text{ (mu is atimgs)}$   $\lim_{A} \varphi(A) = 0 = \varphi(A)$ 

$$4(x) = 0$$

$$4(x) = \lim_{x \to \infty} \frac{x - x}{x} = \lim_{x \to \infty} \frac{x}{x} = \lim_{x \to \infty} \frac{x}{x}$$

$$\lim_{x \to \infty} 4(x) = \lim_{x \to \infty} \frac{x - x}{x} = \lim_{x \to \infty} \frac{x}{x} = \lim_{x \to \infty} \frac{x}{x}$$

$$\lim_{x \to \infty} 4(x) = 0$$

$$\lim_{x \to \infty} 4(x) = \lim_{x \to \infty} 1 = \lim_{x \to \infty} \frac{x}{x} = \lim_{x \to \infty} \frac{x}{x}$$

$$\lim_{x \to \infty} 4(x) = 0$$

$$\lim_{x \to \infty} 4(x) = \lim_{x \to \infty} 1 = \lim$$

=> 1 pt. de minim local Q e 2 pt. marsim local

$$\frac{2}{2} = \frac{2}{2} = \frac{2}$$

b) 
$$\lim_{x \to 0} x^d \cdot \ln(\lim_{x \to 0} x)$$
,  $d > 0$ .

 $\lim_{x \to 0} \lim_{x \to 0} \lim_{x \to 0} \lim_{x \to 0} \lim_{x \to 0} \frac{\log x}{\log x} = \lim_{x \to 0} \frac{\log x}{2^{d+1}} = \lim$ 

 $=-\frac{7}{7}\cdot 0\cdot 7=0$ 

@ Fie ASR m 7: ATA o fc. au proprietatile: i) & derivabilà pe A

ii) Ig ( 1 a.i. 14'(2) / 19, 4 gec A.

ii) 3 a & A a a . 7 (a) = Q.

Definim recursio virel sents= glown, 4 m EM voj seo EA. Justificati:

a) lames-al & g. lam-al, smen

6) (son) e convergent ni are limita a. Construiti o fc. si un six neconstant cu proprietatile de mai sus.

Aplicam T. dagrange pe int. [a, sm ] (sau [sm. 19]) Jee (a, xm.) (nou (xn., a)) a.c.

$$\delta_{1}(c) = \frac{xw-\sigma}{\delta(xw)-\delta(\sigma)} \frac{xw-\sigma}{x^{w+2}-\delta(xw)} \frac{xw-\sigma}{x^{w+2}-\sigma}$$

=) cxm+1-a = 2,(c) (xm-a) =)

12m+1-a1=12'co). /2m-a/ L g. /2m-a/ A=>+, B=1 (3) \$1 (3)

w) |xm-a| = g|xm-2-a| = g.g. |xm-2-a| ≤ g3 |xm-3-a| ≤ ... 29 /240-a/ →0, deposece g41.

over (xm-al-) 0=) (xm) consequent cu limita a.

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- \* 4 desirabla pe [1,00)
- \* D=[1,0), Im & = [2,0)

$$\delta_1(x) = 0$$
 (=)  $x = T$ .  
 $\delta_1(x) = \frac{3}{7} \left(1 - \frac{x_5}{1}\right) = \frac{3}{7} \cdot \frac{x_5}{x_5 - T}$ 

$$\frac{2}{2} |x| = 1$$

$$\frac{2}{2} |x$$

\* 
$$| \varphi^{(1)}(x) | = \frac{1}{2} \cdot | \frac{x^2 - 1}{x^2} | < \frac{1}{2}$$

Deci  $3g = \frac{1}{2} < 1$ .

$$\Re_{\Lambda} = \frac{1}{2} \left( \infty + \frac{1}{36} \right) = \frac{1}{2} \left( 2 + \frac{1}{2} \right) = \frac{5}{4}$$

$$\Re_{\Lambda} = \frac{1}{2} \left( \infty_{\Lambda} + \frac{1}{34} \right) = \frac{1}{2} \left( \frac{5}{4} + \frac{1}{5} \right) = \frac{14}{40}$$

$$\mathfrak{X}_{m+1} = \frac{1}{2} \left( \mathfrak{X}_m + \frac{1}{\mathfrak{X}_m} \right)$$

Limb va avea limita 1.