

DAA Assignment # 1

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Q1) $7n - 2 = O(n)$

Solution:-

$$f(n) \leq g(n) \forall n \geq k$$

$$f(n) = 7n - 2$$

$$g(n) = n$$

$$c = 7$$

$$7n - 2 \leq 7n$$

$$N = 1$$

$$7(1) - 2 \leq 7(1)$$

$$5 \leq 7 \forall n \geq 1$$

$$N = 2$$

$$7(2) - 2 \leq 7(2)$$

$$12 \leq 14 \forall n > 1$$

Q2) $3n^3 + 20n^2 + 5 = O(n^6)$

Solutions :-

$$f(n) = 3n^3 + 20n^2 + 5$$

$$g(n) = n^6$$

$$f(n) \leq g(n) \forall n \geq k$$

$$3n^3 + 20n^2 + 5 \leq n^6 \forall n > k$$

$$N=1$$

$$3(1)^3 + 20(1) + 5 \leq 28(1) \forall n > 1$$

$$28 \leq 28 \quad \forall n \geq 1$$

$$N = 2$$

$$3(2)^3 + 20(2)^2 + 5 \leq 28(2)^6$$

$$109 \leq 1792 \quad \forall n \geq 1$$

$$Q) 7n - 2 = \Theta(n^2)$$

Solution:-

$$C_1 g(n) \leq f(n) \leq C_2 g(n)$$

$$F(n) = 7n - 2$$

$$g(n) = n^2$$

$$C_1 = 5$$

$$C_2 = 7$$

$$N = 1$$

$$5n^2 \leq 7n - 2 \leq 7n^2$$

$$5(1)^2 \leq 7(1) - 2 \leq 7(1)^2$$

$$5 \leq 5 \leq 7$$

$$N = 2$$

$$5(2)^2 \leq 7(2) - 2 \leq 7(2)^2$$

$$20 \leq 12 \leq 28$$

Hence it is false .

$$F(n) = n, g(n) = n^2$$

Transpose symmetric property and it satisfy Θ & Ω notation .

$$Q (3) \quad 7(n) - 2 = \Theta(n)$$

Solution:-

$$C_1 g(n) \leq f(n) \leq C_2 g(n) \forall n \geq k$$

$$f(n) = 7n - 2$$

$$g(n) = n$$

$$C_1 = 5$$

$$C_2 = 7$$

$$5n \leq 7n - 2 \leq 7n \forall n \geq k$$

$$N=1$$

$$5(1) \leq 7(1) - 2 \leq 7(1) \forall n \geq 1$$

$$5 \leq 5 \leq 7 \forall n = 1$$

$$\mathbf{N=2}$$

$$\mathbf{5(2) \leq 7(2) - 2 \leq 7(2) \, \forall \, n \geq 1}$$

$$\mathbf{10 \leq 12 \leq 14 \, \forall \, n \geq 1}$$