# **Bare Demo of IEEEtran.cls for IEEE Computer Society Conferences**

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Abstract—The abstract goes here.

### 1. Introduction

This demo file is intended to serve as a "starter file" for IEEE Computer Society conference papers produced under LATEX using IEEEtran.cls version 1.8b and later. I wish you the best of success.

mds

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### 1.1. Subsection Heading Here

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### 2. Language

The Modal Language  $K_n$  is equivalent to its set of well-formed formulae, denoted  $WFF_{K_n}$ , which is constructed from an enumerable set of propositional symbols:

$$\mathcal{P} = \{p, q, r, \ldots\},\tag{1}$$

the negation symbol  $\neg$ , the disjunction symbol  $\vee$  and the modal connective  $\boxed{a}$ , that expresses the notion of necessity, for each index (or agent) a in a finite, fixed set:

$$\mathcal{A} = \{1, \dots, n\}, n \in \mathbb{N}$$
 (2)

The propositional symbols combined with the logic operators, represented by the symbols mentioned above, are arranged to form sentences (also, parentheses can be used to avoid ambiguity). Therefore, the set of  $WFF_{\mathbf{K}_n}$  is recursively defined as showed in 2.1.

**Definition 2.1.** The set of well-formed formulae,  $WFF_{K_n}$ , is the least set such that:

1) 
$$\mathcal{P} \subset WFF_{\mathbf{K}_n}$$

2) if  $\varphi, \psi \in WFF_{\mathbf{K}_n}$ , then so are  $\neg \varphi, (\varphi \lor \psi)$  and  $\boxed{a} \varphi$ , for each  $a \in \mathcal{A}$ 

As one might know, other logic operators may be introduced as abbreviation to formulae constructed using the operators defined as the usual. In particular, this paper considers the following abbreviations:

- 1)  $\varphi \wedge \psi = \neg(\neg \varphi \vee \neg \psi)$  (conjuction)
- 2)  $\varphi \Rightarrow \psi = \neg \varphi \lor \psi$  (implication)
- 3)  $\varphi \Leftrightarrow \psi = (\varphi \Rightarrow \psi) \land (\psi \Rightarrow \varphi)$  (equivalence)
- 4)  $\Diamond \varphi = \neg a \neg \varphi$  (possibility)
- 5) **false** =  $\varphi \land \neg \varphi$  (falsum)
- 6) **true** =  $\neg$ **false** (*verum*)

And the precedence of the operators is as follows:

- 1)  $\neg$ , a,  $\diamondsuit$
- 2) /
- 2) /\ 2) \/
- *A*) → △

Logics that involve n agents in the modal logic, with  $n \in \mathbb{N}$ , are know as Multimodal Logics. When n = 1, we often omit the index in the modal operators, i.e., we just write  $\square$  and  $\diamondsuit$ .

The maximal number of modal operators in a formula is defined as its *modal depth* and denoted mdepth. The maximal number of modal operators in which scope the formula occurs is defined as the *modal level* of that formula, and it is denoted mlevel. For instance, in  $\bigcirc p$ , mdepth(p) = 0 and mlevel(p) = 2.

#### 2.1. Semantics

**Definition 2.2.** A Kripke model for the set of propositional symbols  $\mathcal{P}$  and the agents  $\mathcal{A}$  is given by the tuple  $\mathcal{M} = (W, w_0, R_1, \dots, R_n, \pi)$ , where W is a nonempty set of possible worlds with a distinguinshed world  $w_0$ , each  $R_a, a \in \mathcal{A}$ , is a binary relation on W, and  $\pi: W \times \mathcal{P} \longrightarrow \{false, true\}$  is the valuation function that associates to each world  $w \in W$  a truth-assignment to propositional symbols.

From the definition of a Kripke model, one can define the satisfiability and validity of a formula in  $K_n$ .

**Definition 2.3.** Let  $\mathcal{M} = (W, w_0, R_1, \dots, R_n, \pi)$  be a Kripke model for  $\mathcal{P}$  and  $\mathcal{A}$ , and consider  $w \in W, p \in \mathcal{P}$  and  $\varphi, \psi \in WFF_{\mathbf{K}_n}$ . The satisfiability relation, denoted by  $\langle \mathcal{M}, w \rangle \models \varphi$ , among the world w and a formula  $\varphi$  in the model  $\mathcal{M}$ , is inductively defined by:

- 1)  $\langle \mathcal{M}, w \rangle \models p \text{ if, and only if, } \pi(w, p) = true$
- 2)  $\langle \mathcal{M}, w \rangle \models \neg \varphi \text{ if, and only if, } \langle \mathcal{M}, w \rangle \not\models \varphi$
- 3)  $\langle \mathcal{M}, w \rangle \models \varphi \lor \psi$  if, and only if,  $\langle \mathcal{M}, w \rangle \models \varphi$  or  $\langle \mathcal{M}, w \rangle \models \psi$
- 4)  $\langle \mathcal{M}, w \rangle \models \Box \varphi \text{ if, and only if, } \forall t \in W, \text{ with } a \in \mathcal{A}, (w, t) \in R_a \text{ implies } \langle \mathcal{M}, t \rangle \models \varphi$

A set of formulae  $\Gamma = \{\gamma_1, \dots, \gamma_r\}, r \in \mathbb{N}$ , is satisfiable in a world w if, and only if, each of its formulae is satisfiable in this world, i.e.,  $\langle \mathcal{M}, w \rangle \models \Gamma \Leftrightarrow \langle \mathcal{M}, w \rangle \models \gamma_1 \wedge \dots \wedge \gamma_r$ 

**Definition 2.4.** A formula  $\varphi \in WFF_{\mathsf{K}_n}$  is said to be satisfiable if exists a Kripke model  $\mathcal{M}$  such that  $\langle \mathcal{M}, w_0 \rangle \models \varphi$ .

**Definition 2.5.** A formula  $\varphi \in WFF_{\mathbb{K}_n}$  is said to be valid if for all Kripke model  $\mathcal{M}$ , we have that  $\langle \mathcal{M}, w_0 \rangle \models \varphi$ .

When one is considering a set of formulae instead of a single one, both definitions of satisfiability and validity holds similarly to the definition of satisfiability relation.

# 3. Calculus

# 4. Related Work

# 5. Conclusion

The conclusion goes here.

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## References

 H. Kopka and P. W. Daly, A Guide to BTEX, 3rd ed. Harlow, England: Addison-Wesley, 1999.