

**NON-RENORMALISATION THEOREMS IN GLOBAL  
SUPERSYMMETRY**

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Invited talk at the Conference on "30 Years of Supersymmetry"  
Minneapolis, Minnesota, Oct. 13-15, 2000

**ABSTRACT**

We review the history of non-renormalisation theorems in global supersymmetry, as well as their importance in all attempts to apply supersymmetry to the real world.

Supersymmetry in four dimensions is thirty years old [1], [2]. It started as a rather esoteric subject, but, for the last twenty years, it has occupied a unique position in elementary particle physics: It has received no experimental support, yet it has dominated most theoretical and much of the experimental work. Each one of us has his own motivations to study supersymmetry, but we are all fascinated by the aesthetic appeal of the theory. I have always considered supersymmetry as the natural extension to gauge theories. Let me explain:

We are all convinced that gauge theories have come to stay. They provide the unique framework, based on deep geometrical ideas, to describe all interactions among elementary particles. However, they have a number of shortcomings which show that they need completion. The particular one I want to mention here is the fact that, to our present understanding, they contain three independent worlds: The world of radiation consists of, initially, massless vector bosons. Their number, their properties and their interactions are uniquely determined by the gauge group, they are purely geometrical objects. In all our present models the world of matter consists of spin one-half fermions. Their number as well as their group-theory properties are arbitrary, but, once assumed, they uniquely determine the interaction with radiation. The third world is that of Higgs scalars. They are essential for mass generation but they are the ones which bring most of the arbitrariness in the theory. In the Standard Model most free parameters are connected with the Higgs sector. Furthermore, their quadratic mass divergences tend to mix the various scales of the theory. Much effort has been devoted to constructing gauge models with Higgs scalars replaced by a dynamical symmetry breaking mechanism, but with no great success until now. It is therefore natural to seek a symmetry principle to relate the three worlds and obtain a trully unified theory, with no distinction between matter and radiation, in which all fundamental fields have a geometrical meaning. One is thus led to supersymmetry.

Supersymmetric field theories are "improved" field theories. The "improvement" is connected with the ultraviolet properties of the theory and depends on whether one considers theories with global or local supersymmetry. In this lecture I will review some of the early work on the non-renormalisation theorems in global supersymmetry. They are the ones which offer the possibility to solve the technical part of the gauge hierarchy problem.

The first indication that supersymmetric theories have special properties under renormalisation was obtained by J. Wess and B. Zumino. In their first paper on supersymmetry [2] they introduced a very simple field theory model containing a Majorana spinor, a scalar and a pseudoscalar field. The

Lagrangian density can be written as:

$$\begin{aligned}
\mathcal{L} &= \mathcal{L}_0 + \mathcal{L}_m + \mathcal{L}_{int} \\
\mathcal{L}_0 &= -\frac{1}{2}(\partial A)^2 - \frac{1}{2}(\partial B)^2 - \frac{i}{2}\bar{\psi}\not{\partial}\psi + \frac{1}{2}F^2 + \frac{1}{2}G^2 \\
\mathcal{L}_m &= m(FA + GB - \frac{i}{2}\bar{\psi}\psi) \\
\mathcal{L}_{int} &= g(FA^2 - GB^2 + 2GAB - i\bar{\psi}\psi A + i\bar{\psi}\gamma_5\psi B)
\end{aligned} \tag{1}$$

where  $F$  and  $G$  are auxiliary fields. Under the supersymmetry transformations

$$\begin{aligned}
\delta A &= i\bar{\alpha}\psi \\
\delta B &= i\bar{\alpha}\gamma_5\psi \\
\delta\psi &= \partial_\mu(A - \gamma_5 B)\gamma^\mu\alpha + (F + \gamma_5 G)\alpha \\
\delta F &= i\bar{\alpha}\not{\partial}\psi \\
\delta G &= i\bar{\alpha}\gamma_5\not{\partial}\psi
\end{aligned} \tag{2}$$

the action derived from (1) remains invariant. In (2),  $\alpha$ , the parameter of the transformation, is a constant, anticommuting, Majorana spinor.

Upon elimination of the auxiliary fields, the model describes a superposition of Yukawa,  $\phi^4$  and  $\phi^3$  couplings; it is therefore renormalisable by power counting. Supersymmetry is manifest by means of relations between the masses and coupling constants of the model. Wess and Zumino tried to check by explicit calculation whether renormalisation at the level of one loop respects these relations [3]. To their surprise, they discovered that it did much more: The only necessary counterterm was a single wave function renormalisation common to all fields. Neither mass nor coupling constant renormalisations were needed.

I was very sceptical when I first heard there results. I was inclined to believe that they were accidents of one loop and they would not survive at higher orders. *Par acquit de conscience* we decided with B. Zumino to check the two loop level. You guess the answer: The same result holds, although, this time the cancellation involves diagrammes with different topologies. It was clear that a general proof should exist. Indeed, it turned out to be rather simple [4].

As I said before, the model is renormalisable by power counting. Furthermore, because of the fact that the transformations (2) are global ( $\alpha$  constant), one can find easily supersymmetry preserving regularisation schemes. For example, a higher derivative kinetic term will do [4]. It follows that renormalisation will preserve supersymmetry, in other words one will need, at most, three counterterms,  $Z$ ,  $\delta m$  and  $Z_g$ , one for each term in (1). The surprising result was that only  $Z$  was needed. These extra cancellations

that give  $\delta m = 0$  and  $Z_g = 1$  clearly go beyond symmetry alone since the corresponding terms  $\mathcal{L}_m$  and  $\mathcal{L}_{int}$  are allowed by supersymmetry.

The particular property of (1) which is relevant for the proof is [4]:

$$\frac{\partial}{\partial m} \mathcal{L}_m = \frac{1}{2g} \frac{\partial}{\partial A} \mathcal{L}_{int} \quad (3)$$

This property has an immediate analogue in terms of the 1P-I functions: Let  $\Gamma[R]$  be the generating functional where  $R$  denotes, collectively, the classical fields, the conjugate variables under Legendre transformation of the external sources. We obtain:

$$\frac{\partial}{\partial m} \Gamma[R] = -\frac{m}{2g} \int R_F(y) d^4 y + \frac{1}{2g} \int \frac{\delta \Gamma[R]}{\delta R_A(y)} d^4 y \quad (4)$$

which means that, for every vertex function other than the 1P-I part of  $\langle F \rangle_0$ , the derivative with respect to the bare mass gives an insertion of a zero momentum  $A$  field. On the other hand, using the supersymmetry Ward identities and the equations of motion of the regularized theory, it is easy to prove [4] that the vacuum expectation values of all fields vanish. We now take the functional derivative of (4) with respect to  $R_F$  and then put all  $R$ 's equal to zero. Using the vanishing of  $\langle F \rangle_0$  we obtain:

$$m = Z^{-1} \Gamma_{FA}(p^2 = 0) \quad (5)$$

which implies

$$m_r = Zm \quad (6)$$

i.e.  $\delta m = 0$ . Similarly we obtain

$$g_r = Z^{\frac{3}{2}} g \quad (7)$$

i.e.  $Z_g = 1$ . This completes the proof of the non-renormalisation theorem.

In terms of the renormalisation group functions (7) has an interesting consequence [5]:

$$\beta(g) = 3g\gamma(g) \quad (8)$$

Using (8), it is easy to show that the  $\beta$  function of this model cannot have a non-trivial fixed point. Indeed, let us consider the massless case. A fixed point  $g_0$  satisfies  $\beta(g_0) = 0$ . But then (8) implies that  $\gamma(g_0)$  also vanishes, i.e. all fields have canonical dimensions and all Green functions satisfy free-field theory renormalisation group equations. This is enough to show that the model is in fact free. But  $g$  is defined as the value of the three point function at zero external momenta and cannot be non-zero for a free field theory. Turning to the massive case we can write the corresponding Callan-Symanzik equation:

$$[m\frac{\partial}{\partial m} + \beta(g) - n\gamma(g)]\Gamma_{\phi_1\ldots\phi_n}(p_i; m, g) = \frac{m}{2g}\delta(g)\Gamma_{A,\phi_1\ldots\phi_n}(0, p_i; m, g) \quad (9)$$

where  $m$  and  $g$  denote the renormalised quantities and

$$\beta(g) = \frac{3}{2}g\frac{f}{1+f} \quad , \quad \gamma(g) = \frac{1}{2}\frac{f}{1+f} \quad , \quad \delta(g) = \frac{1}{1+f} \quad (10)$$

Equation (9) has some interesting features [5] : First, all three functions usually appearing, namely  $\beta$ ,  $\gamma$  and  $\delta$ , are expressed in terms of the single function  $f$ . This is a direct consequence of the non-renormalisation theorem. In perturbation  $f$  has a power series expansion in  $g$ :

$$f(g) = \frac{g^2}{4\pi^2} + \dots \quad (11)$$

Second, at the right hand side of (9), instead of the familiar mass insertion, there appears an insertion of a zero momentum  $A$  field. Notice that, since the added line carries zero momentum, the Green function in the left hand side still dominates in the deep Euclidean region.

At this stage these divergence cancellations appeared to be miraculous. We had no deeper understanding of their origin and we could only speculate. The first question was whether the remaining divergence, the wave function counterterm, was really present to all orders, in other words the question was whether the theory was in fact superrenormalisable. Our explicit calculation showed that, at least up to two loops, this did not seem to be the case, although a partial cancellation did occur [4]. A related question was whether supersymmetry could turn a theory which is non-renormalisable by power counting into a renormalisable one. We could find no examples. Today we know the precise answer to such questions. We use a new formulation of supersymmetry [6], in which the base space is eight dimensional. Four are the usual Minkowski coordinates  $x_\mu$ ,  $\mu = 0, 1, 2, 3$  and the remaining four can be viewed as forming, under Lorentz transformations, a complex two-component Weyl spinor  $\theta_\alpha$  together with its conjugate  $\bar{\theta}_{\dot{\alpha}}$ ,  $\alpha, \dot{\alpha} = 1, 2$ . These components are taken to be totally anti-commuting elements of a Grassmann algebra. This space is called "superspace". We can show that supersymmetry transformations act on superspace as generalised translations. The important point is that, because of the anti-commutation properties of the components of  $\theta$ , any function in superspace is, in fact, a polynomial in  $\theta$  and  $\bar{\theta}$  with coefficients which are functions of  $x$ . In other words, a field in superspace, called "superfield", is equivalent to a finite multiplet of ordinary fields.

$$\Phi(x, \theta, \bar{\theta}) = A(x) + \theta\psi(x) + \bar{\theta}\bar{\chi} + \dots + \theta\theta\bar{\theta}\bar{\theta}R(x) \quad (12)$$

The fields  $A(x)$ ,  $\psi(x)$ , etc which appear as coefficients in the expansion (12), have well-defined Lorentz transformation properties and transform among themselves and their derivatives under supersymmetry. Therefore, they form a representation, in general reducible. It is possible to find a complete set of covariant restrictions on superfields to obtain the irreducible representations. A particular example of such restrictions is given by the equation:

$$\frac{\partial}{\partial \theta_\alpha} \Phi(x, \theta, \bar{\theta}) = 0 \quad (13)$$

A superfield that satisfies (13) is a function of  $x$  and  $\theta$  only and is called "chiral". Its expansion in powers of  $\theta$  is given by:

$$\phi(x, \theta) = A(x) + \theta\psi(x) + \theta\theta F(x) \quad (14)$$

It is precisely the multiplet we considered in (1) written in complex notation.

These observations provide the basis for the representation theory of supersymmetry. Since the product of two superfields is again a superfield, they also provide the elements of a tensor calculus. The Lagrangian densities which were initially constructed by trial and error can be obtained now as superfields in superspace. The corresponding actions are eight dimensional integrals of the Lagrangian superfields. Integrals over Grassmann variables have unusual properties. In particular, they satisfy:

$$\int d\theta = 0 \quad , \quad \int \theta d\theta = 1 \quad (15)$$

which means that only the last term in the expansion of a superfield survives. With these results we can reformulate perturbation theory using Feynman rules directly in superspace [7]. It follows that, although we can use a chiral superfield as part of a Lagrangian and integrate this piece only over  $\theta$  to obtain the action, only integrals over the entire superspace appear as counterterms. Thus we can understand the origin of the non-renormalisation theorems. Going back to (1), we can show that both  $\mathcal{L}_m$  and  $\mathcal{L}_{int}$  are chiral superfields and depend only on  $\theta$ , while  $\mathcal{L}_0$  depends on both  $\theta$  and  $\bar{\theta}$ . Therefore only a wave function counterterm will appear.

Before leaving the scalar model I want to address the following question: After all, the supersymmetric model (1) is just a particular combination of Yukawa and scalar couplings. Are there any other combinations with similar remarkable properties? As an example, let us consider the massless Lagrangian [8]:

$$\begin{aligned} \mathcal{L} = & - \frac{1}{2}(\partial A)^2 - \frac{1}{2}(\partial B)^2 - \frac{i}{2}\bar{\psi}\not{\partial}\psi \\ & - ig\bar{\psi}\psi A + ig\bar{\psi}\gamma_5\psi B \end{aligned} \quad (16)$$

$$- \frac{1}{2}\lambda(A^4 + B^4) - fA^2B^2$$

Invariance under supersymmetry is obtained for

$$\lambda = f = g^2 \tag{17}$$

At one loop we can compute the counterterms of this model [8] with the following results: (i) Only under the supersymmetric relation (17) we obtain the non-renormalisation theorem. (ii) As expected, this relation is a fixed point of the renormalisation group flow. (iii) This fixed point is an infrared attractor, i.e. if we start at high energies somewhere in its vicinity, we shall be driven towards it at larger and larger distances.

The superfield techniques have been used to derive more general non-renormalisation theorems and they will be reviewed elsewhere. In the rest of my time I want to describe some early results on supersymmetry breaking.

In Nature we see no degeneracy between fermions and bosons. So it was immediately recognised that supersymmetry, if at all relevant, must be broken. In our first paper with Zumino [4] we addressed the question for the simple model of equation (1). An ordinary internal symmetry is spontaneously broken if an operator, usually one of the canonical fields, which transforms non trivially under the symmetry transformations, is allowed to take a non-zero vacuum expectation value. This is often achieved by choosing a negative value for the mass square term of a scalar field. In supersymmetry the situation turns out to be different. The masses of scalars and spinors are degenerate and the classical potential for any scalar field never becomes negative. In our model the only fields which can take non-vanishing vacuum expectation values without breaking Lorentz invariance or parity are  $A$  and  $F$ . However the first one does not help because  $A$  appears only in the transformation law of  $\psi$  through its derivative (2). Therefore, as long as we do not break translational invariance, we can shift it with a constant value without breaking supersymmetry. We are left with the  $F$  field. It transforms by a total derivative (2) and therefore, we can add to the Lagrangian (1) a term linear in  $F$  without breaking supersymmetry explicitly. But even this term does not help because it is straightforward to verify that it can always be eliminated by a shift of the  $A$  field. We thus showed that there was no spontaneous breaking of supersymmetry, for any choice of the parameters of the model. We also asked the general question of the possibility of spontaneous breaking and we gave the wrong answer. We argued that, since the hamiltonian of a supersymmetric system can be expressed as the anti-commutator of two fermionic generators, the energy of an eigenstate which is annihilated by the generators is zero. On the other hand, the same relation shows that the spectrum of the hamiltonian is positive semi-definite. Therefore we concluded that the supersymmetric invariant state will be always the ground state. We were aware of the fact that the statement was not rigorous and we said so, but we believed the

result to be correct. I shall come back to the fate of spontaneous breaking in a moment, but let me examine first the consequences of a soft, explicit breaking for the model of equation (1).

The simplest breaking term is one linear in the field  $A$  [4]:

$$\mathcal{L} \rightarrow \mathcal{L} - cA \tag{18}$$

This term can be eliminated by a simultaneous shift of the fields  $A$  and  $F$ ,  $A \rightarrow A + a$ ,  $F \rightarrow F + f$  with  $a$  and  $f$  constants given in terms of the original parameters  $m$ ,  $g$  and  $c$ . The shift in  $F$  breaks supersymmetry and induces a mass-splitting in the multiplet:



$$\begin{aligned}
m_\psi &= m + 2ga = c/f \\
m_A^2 &= m_\psi^2 - 2fg \\
m_B^2 &= m_\psi^2 + 2fg
\end{aligned}
\tag{19}$$

The masses are no longer equal but, in the tree approximation, they satisfy the relation:

$$m_A^2 + m_B^2 = 2m_\psi^2 \tag{20}$$

The remnant of the non-renormalisation theorem presented above, guarantees that this relation will receive no divergent corrections in higher orders.

If one eliminates  $f$ , one finds an equation of third degree for  $a$ . For small but finite  $c$ , its solutions correspond to the extrema of the potential for the field  $A$ :

$$V(a) = \tfrac{1}{2}a^2(m + ga)^2 + ca \tag{21}$$

As  $c \rightarrow 0$ , the three solutions become

$$a_1 = 0 \quad , \quad a_2 = -\frac{m}{g} \quad , \quad a_3 = -\frac{m}{2g} \tag{22}$$

and the potential becomes symmetric around the value  $a_3$ .  $a_1$  and  $a_2$  correspond to the two minima of the potential and give two, stable, supersymmetric, physically equivalent solutions.  $a_3$  corresponds to a local maximum and it is unstable. It is instructive to notice that if one could choose this unstable solution, one would have  $m_\psi = 0$ , i.e. the  $\psi$  field would become a Goldstone spinor and supersymmetry would be spontaneously broken [4]. In this case the relation (20) shows that one of the bosons would have a negative square mass. This is the sign of instability.

This mass relation which shows an equal splitting among the levels in broken supersymmetry turns out to be very general in the breaking of both global and local supersymmetries [9]. In fact it poses severe constraints in model building. Although, in general, quantum corrections are expected to modify it, it turns out that it is remarkably robust [10].

I shall end with a short review of the mechanism of spontaneous breaking of global supersymmetry. As I explained before, the particular connection between supersymmetry generators and translations, shows that a supersymmetric invariant state is always a ground state [4]. This was initially interpreted as an indication for the existence of a no-go theorem as regards to spontaneous supersymmetry breaking. In fact the situation is different: It is correct that a supersymmetric invariant state, if it exists, is always a ground state and global supersymmetry is unbroken. But, contrary to what happens in ordinary symmetries, a supersymmetric state may not exist at

all. In this case, and in this case only, spontaneous breaking occurs. The first example [11] was that of the supersymmetric extension of a  $U(1)$  gauge theory [12]. The model describes the interaction of a charged scalar multiplet and a gauge vector multiplet. In a particular family of gauge choices! , ! the Wess-Zumino gauge [?], the Lagrangian is polynomial and renormalisable by power counting. In terms of physical fields, the gauge multiplet consists of the photon field  $\mathcal{V}_\mu(x)$  and its supersymmetric partner which is a neutral Majorana spinor  $\lambda(x)$ . The matter multiplet consists of a Dirac spinor  $\psi(x)$  (the electron) and two charged spin zero fields, a scalar  $A(x)$  and a pseudoscalar  $B(x)$ . The photon has the usual electromagnetic couplings with the charged fields, characterised by a coupling constant  $e$  and supersymmetry induces new, Yukawa type couplings between  $\lambda$ ,  $\psi$  and  $A$  and  $B$ , with a coupling constant which is again equal to  $e$ . As with eq.(1), the transformations are simpler if one includes auxiliary fields, a charged scalar  $F$ , a charged pseudoscalar  $G$  and a neutral pseudoscalar  $D$ . The first two are associated with the matter multiplet and the last one with the photon. Under supersymmetry transformations  $D$  has properties! similar to those of  $F$  and  $G$  of eq.(2), i.e. it transforms by a four derivative and it appears without derivative in the transformation of  $\lambda$ . Therefore, we can add to the Lagrangian a term linear in the field  $D$ . This term preserves supersymmetry and gauge invariance and violates parity explicitly but softly. On the other hand, a non zero vacuum expectation value for  $D$  breaks supersymmetry spontaneously. The classical potential for the spin zero fields is given by:

$$\begin{aligned} V = & \frac{1}{2}[F_1^2 + F_2^2 + G_1^2 + G_2^2 + D^2] \\ & + m(F_1 A_1 + F_2 A_2 + G_1 B_1 + G_2 B_2) \\ & + eD(A_1 B_2 - A_2 B_1) + \xi D \end{aligned} \quad (23)$$

where  $F_1$ ,  $F_2$  etc are the real and imaginary parts of the fields. The novel feature here is that the linear term  $\xi D$  cannot be absorbed by a shift of an  $A$  or  $B$  field and, therefore, we expect supersymmetry to be spontaneously broken [11]. Indeed, after elimination of the auxiliary fields and diagonalisation of the resulting mass terms, we obtain:

$$\mathcal{L}_m = -\frac{1}{2}(m^2 + e\xi)(\tilde{A}_1^2 + \tilde{B}_1^2) - \frac{1}{2}(m^2 - e\xi)(\tilde{A}_2^2 + \tilde{B}_2^2) - im\bar{\psi}\psi \quad (24)$$

where  $\tilde{A}_i$  etc are linear combinations of the old fields.  $\mathcal{V}_\mu$  and  $\lambda$  remain massless. In fact it is easy to show that  $\lambda$  is the Goldstone spinor one expects after spontaneous breaking of a symmetry whose conserved current has spin equal to  $3/2$ . We can verify this result explicitly by studying the transformation properties of the fields under infinitesimal supersymmetry transformations. A Goldstone field is the one which has in its transformation law a constant term which is not proportional to any other field.

The relations (24) show that we can distinguish two cases depending on the sign of  $m^2 - e\xi$ . (We assume, without loss of generality,  $e\xi > 0$ ). The positive sign means that supersymmetry is spontaneously broken but gauge symmetry is not. In the opposite case they are both spontaneously broken and the photon becomes massive by the usual Brout-Englert-Higgs mechanism. The Goldstone fermion is now a linear combination of  $\lambda$  and  $\psi$ .

This simple example shows the general mechanism for spontaneous supersymmetry breaking. In fact, it would have been impossible to have such a breaking, if it were not for the peculiar property we mentioned earlier, namely the possibility of adding to the Lagrangian a term linear in the auxiliary fields without breaking supersymmetry explicitly. If we restrict ourselves to renormalisable theories, we can use only scalar and vector multiplets with auxiliary fields we have called before  $F$ ,  $G$ , and  $D$ . The first is scalar, the other two pseudoscalar. Let  $\phi$  denote, collectively, all other physical, spin zero fields. We shall assume that Lorentz invariance is not broken, consequently all other fields have zero vacuum expectation values. The potential of the scalar fields in the tree approximation has the form:

$$V(\phi) = -\frac{1}{2}[\Sigma F_i^2 + \Sigma G_i^2 + \Sigma D_i^2] + [\Sigma F_i F_i(\phi) + \Sigma G_i G_i(\phi) + \Sigma D_i D_i(\phi)] \quad (25)$$

where the functions  $F_i(\phi)$ ,  $G_i(\phi)$  and  $D_i(\phi)$  are polynomials in the physical fields  $\phi$  of degree not higher than second. The equations of motion which eliminate the auxiliary fields are

$$F_i = F_i(\phi) ; G_i = G_i(\phi) ; D_i = D_i(\phi) \quad (26)$$

so the potential in terms of the physical fields reads:

$$V(\phi) = \frac{1}{2}[\Sigma F_i^2(\phi) + \Sigma G_i^2(\phi) + \Sigma D_i^2(\phi)] \quad (27)$$

The important point is that  $V$  is non-negative and vanishes only when

$$F_i(\phi) = 0 ; G_i(\phi) = 0 ; D_i(\phi) = 0 \quad (28)$$

i.e. when all auxiliary fields have zero vacuum expectation values and supersymmetry is unbroken. For spontaneous breaking we must arrange so that the system of the second degree algebraic equations (28) has no real solution. This was the case in the supersymmetric extension of Q.E.D. we presented before. We can also construct models with more than one scalar multiplets [13]. A final remark: The non-renormalisation theorems we presented before show that, if global supersymmetry is unbroken in the tree approximation, it will remain unbroken to all orders in perturbation theory. This also puts severe restrictions in model building where non-perturbative breaking mechanisms must be invented [14].

As we saw in the previous example and as we know from general theorems, spontaneous breaking of supersymmetry results in the appearance of a zero mass Goldstone spinor. It satisfies the standard low-energy theorem, known as “Adler’s zero”. It states that the amplitude for the emission (or absorption) of a Goldstone particle of momentum  $k$  vanishes at low energies linear in  $k$ . This means that this fermion cannot be identified with one of the neutrinos of the Standard Model, even if they have exactly zero mass [15]. Although we have no experimental hint of any kind, the predominant philosophy to-day is to believe that such a Goldstone fermion is absorbed in a super-Higgs mechanism in the framework of a supergravity theory [16].

It is still too early to take bets on the final place that supersymmetry will occupy in particle physics. It is amusing to notice that several times in recent years, whenever experimental results appeared to depart from the Standard Model predictions, the first reaction of both theorists and experimentalists was to try to interpret them as indications of supersymmetry. Few theories have exercised so much fascination to so many physicists for so long. Looking for supersymmetric particles will be an important part of experimental research in the years to come. I hope that it will be both exciting and rewarding and that the fortieth anniversary Conference will be that of supersymmetric phenomenology.

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