Homomorphic Encryption Implementation for Small SWaP Platforms

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PROJECT INTRODUCTION & BACKGROUND

What is homomorphic encryption?

- Homomorphic encryption:
 - An encryption scheme that allows the processing of data in its encrypted form without access to the secret key
 - Preserves the structure of the underlying data
 - Some developed using public asymmetric key systems, such as
 - RSA
 - ElGamal
 - Paillier
- Encryption schemes can be fully homomorphic or partially homomorphic, with respect to one type of data operation (i.e. multiplication, addition)

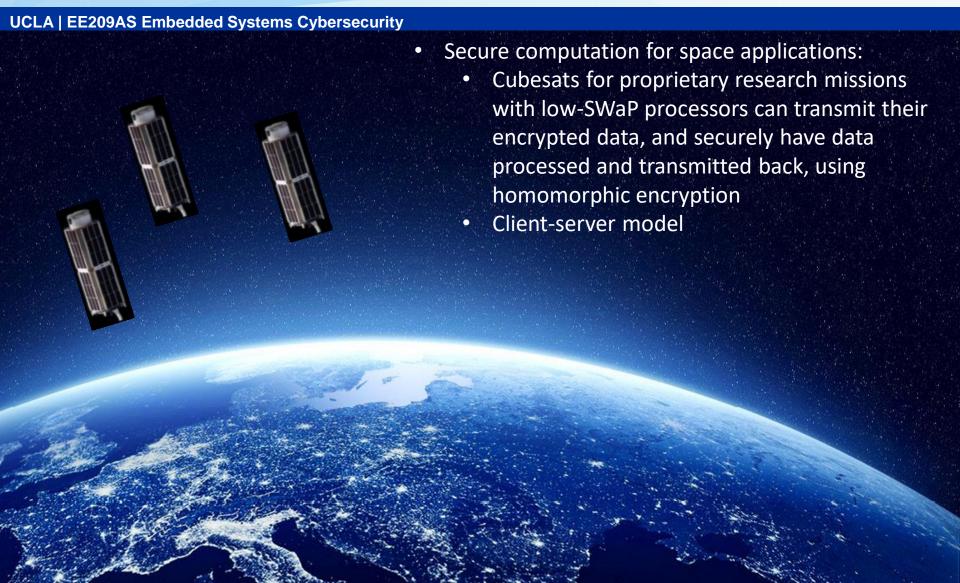
Types of Homomorphic Encryption

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Year	Acronym	Name	Description
2011	BGV	Brakerski-Gentry- Vaikuntanathan	RLWE lattice-based FHE
2011	BFV	Brakerski-Fan- Vercauteren	RLWE lattice-based FHE
2016	CKKS	Cheon-Kim-Kim-Song	Supports approx. arithmetics over complex numbers. Exploits ring isomorphism.

There are many homomorphic encryption schemes, including Enhanced Homomorphic Cryptosystem (EHC), Algebra Homomorphic Encryption (AHEE), and Non-interactive Exponential Homomorphic Encryption Scheme (NEHE); however, we focused most on BFV and CKKS, as they had the most materials available to researchers for free.

Project Motivation: Space Applications, IoT Devices



Project Objectives

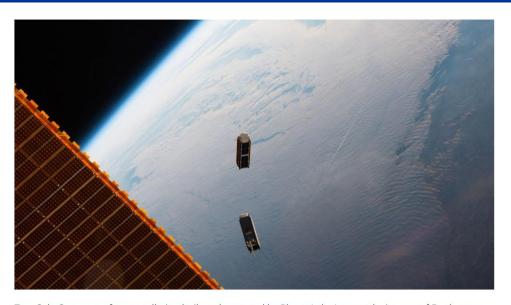
- 1. Analyze and implement a series of homomorphic encryption functions
 - Small SWaP Platform:
 - small SoCFPGA
 - FPGA-only
 - ARM processor only
- 2. Benchmark homomorphic encryption algorithms on cloud computing service
 - Amazon AWS EC2 cloud computing service
- 3. Implement client-server model
 - Modification of SEAL libraries to split computing requirements for implementation
 - Uses a combination of small SWaP device and a cloud computing service

Homomorphic Encryption Library: Microsoft SEAL (MIT)

- Simple Encrypted Arithmetic Library (SEAL):
 - Open-source software library developed by Microsoft
 - Implements various forms of homomorphic encryption
 - Standard C/C++ (no external dependencies)
 - Supports both asymmetric and symmetric encryption algorithms
 - Supports both BFV and CKKS encryption schemes

Technical Approach

- Implement a low-SWaP clientserver model for expanded use of homomorphic encryption schemes
 - Some existing experiments for IoT devices and high-performance computing platforms
 - Limited implementations achievable with Raspberry Pi in literature
 - No current literature on low-SWaP space applications
 - Desire for better encryption for cubesat and small sats, resistance to quantum computing for forced decryption
 - No library of functions for FPGA implementation commercially available
 - Some in-work at IBM, pay for access



Two CubeSats, part of a constellation built and operated by Planet Labs Inc. to take images of Earth, were launched from the International Space Station on May 17, 2016. (Image: © NASA)

- Relevant current solicitation for research FY2020 FY2023:
 - AFRL BAA Capabilities for Cyber Resiliency
 - AFRL BAA Foundations of Trusted Computational Information Systems
 - NAVAIR BAA Cyber Warfare Detachment
 - AFRL BAA Next Generation Intelligence Collection and Analysis
 - AFRL BAA Measurement and Signatures Intelligence Exploitation

Related Work

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- Simulated WBAN through OMNET++ and Castalia
 - 30s interval for reading and writing encrypted data
 - Simulation time 3600 s
 - Simulation with Helib and SEAL
 - Measured packet delay

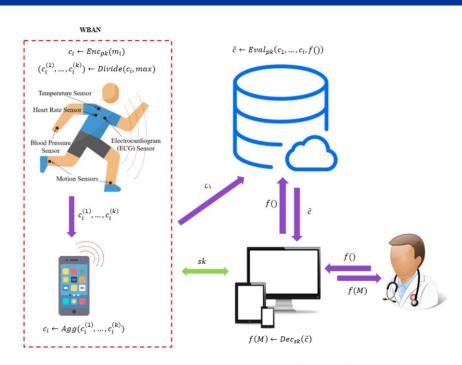


Table 5. The running time (Milliseconds)

vices in healthcare systems.

		KeyGen	Encryption	Decryption	Addition	Multiplication	Bootstrapping
PC	HElib	0.760058	0.032094	0.013368	0.000094	0.066178	85.323830
I C	SEAL	1.930100	2.342723	0.177101	0.005329	2.187750	-
Raspberry Pi	HElib	79.933075	2.084733	1.258043	0.006370	4.707492	7,846.207000
Raspocity 11	SEAL	181.319900	229.979548	46.673325	0.920642	480.622600	-

A. Prasitupparote, et. Al., "Implementation and Analysis of Fully Homomorphic Encryption in Wearable Devices", *Proceedings of 4th International Conference on Information Security and Digital Forensics, ISDF2018*, Greece, 2018.



Objective 1: Small SWaP Platform Analysis

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Item No.	Manufacturer	Device Description	Platform Type
1	Intel	DE10 Nano SoC (Cyclone V)	SoC (ARM + FPGA)
2	Intel	DE0 Nano (Cyclone IV)	FPGA
3	Xilinx	Arty A7 (Zynq 7020)	SoC (ARM + FPGA)
4	Texas Instruments	MSP430 LaunchPad	Microcontroller
5	Raspberry Pi	Rpi 4	ARM Processor

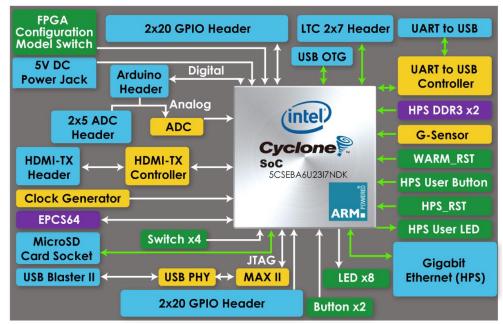
Criteria examined:

- Power consumption
- Processor type
- FPGA number of programmable logic elements
- Physical size
- Cost

Objective 1: Small SWaP Platform Selection 1

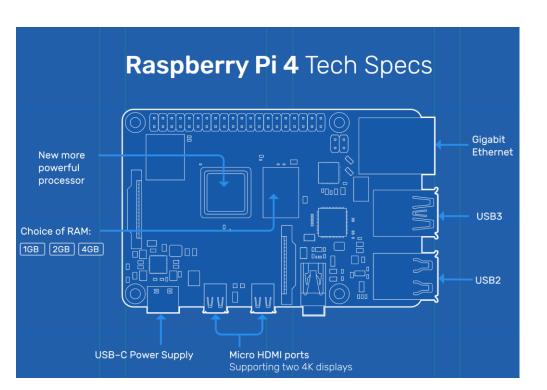
- Intel Cyclone V: DE10 Nano SoC
 - SoCFGPA
 - Dual-core Cortex A9 32-bit ARM processor
 - 110k Programmable Logic Elements
- Linux OS:
 - Yocto Poky Distro
 - Boot from 32GB SD card





Objective 1: Small SWaP Platform Selection 2

- Raspberry Pi 4
 - Cortex A72 quad-core 64-bit ARM processor
 - 4GB DDR3 memory





Objective 1: Implementation

- Using both DE10 Nano SoC and Raspberry Pi 4, we attempted to compile the SEAL library functions and run on the platform.
 - Using DE10 Nano SoC ARM processor
 - Porting C -> HDL on DE10 Nano SoC FPGA
 - Using Raspberry Pi 4 ARM processor

Objective 1: Results

- 32-bit processor incompatible with SEAL and similar available homomorphic encryption libraries.
- Requires at least 64-bit processor.
- HDL -> C implementation too large for Cyclone V FPGA
- Success with Raspberry Pi 4 Cortex A78 ARM processor
 - All instances runnable for degrees <32768

Objective 1: Results (2)

#	Parameter	SEAL BFV Degree Computation Time [ms]				
	Degree	1024	2048	4096	8192	16384
1	Average Batch	0.233	0.466	0.984	2.092	4.435
2	Average Unbatch	0.186	0.344	0.740	1.569	3.373
3	Average Encrypt	3.329	6.524	22.071	64.670	219.878
4	Average Decrypt	1.566	2.417	7.137	26.089	100.465
5	Average Add	0.025	0.036	0.116	0.498	2.047
6	Average Multiply	11.460	22.102	74.159	279.802	1,146.392
7	Average Multiply Plain	1.006	2.076	8.810	37.527	158.410
8	Average Square	8.252	16.237	55.181	209.815	867.853
9	Average Relinearize	N/A	N/A	16.476	72.648	396.322
10	Average Rotate 1 step	N/A	N/A	16.613	73.975	400.704
11	Average Rotate Random	N/A	N/A	53.823	341.561	1,765.455
12	Average Rotate Columns	N/A	N/A	16.624	73.992	400.718
13	CPU Usage [%]	5.0 %	10.6%	87.7%	99.7%	100%

Objective 1: Results (3)

#	Parameter	SEAL CKKS Degree Computation Time [ms]				
	Degree	1024	2048	4096	8192	16384
1	Average Batch	1.801	2.969	7.514	20.257	61.416
2	Average Unbatch	2.594	4.250	14.735	57.825	257.827
3	Average Encrypt	3.016	4.455	21.417	66.505	232.468
4	Average Decrypt	0.148	0.215	0.842	3.325	13.085
5	Average Add	0.027	0.036	0.114	0.446	1.998
6	Average Multiply	0.427	0.729	2.951	12.627	48.889
7	Average Multiply Plain	0.186	0.316	1.243	4.921	19.506
8	Average Square	0.302	0.517	2.137	9.173	36.203
9	Average Relinearize	N/A	N/A	16.323	71.417	391.350
	Average Rescale	N/A	N/A	6.235	30.999	140.706
10	Average Rotate 1 step	N/A	N/A	16.734	73.160	399.765
11	Average Rotate Random	N/A	N/A	57.636	279.600	1,790.253
12	Average Complex Conjugate	N/A	N/A	16.684	73.036	398.881
13	CPU [%]	7.0%	11.6%	81.1%	98.3%	100%



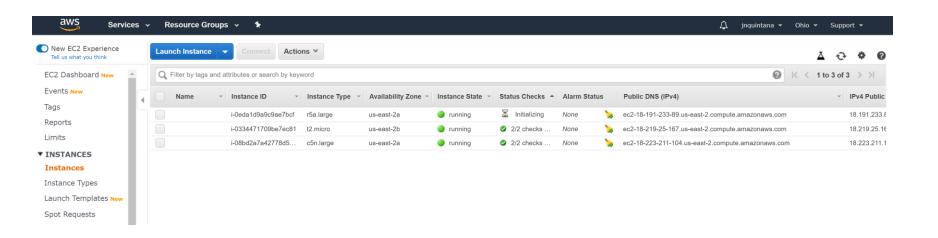
Objective 2: AWS EC2 Selection

Item No.	Instance Name	Instance Type	CPU Cores	Memory
1	t1.micro	General Purpose	1	0.5 GB
2	c5n.large	Computation Optimized	2	4 GB
3	t2.micro	General Purpose	1	1 GB
4	r5a.large	Memory Optimized	2	16 GB

- Selected different instances based on processing properties:
 - Large, high-capability instances
 - Small, resource-limited instances

Objective 2: Implementation (1)

- Instantiated AWS EC2:
- Ubuntu 18.04 OS used for instantiations
- SSH to EC2 to run performance metrics for different functional implementations of SEAL benchmarking



Objective 2: Results for t2_micro instance - BFV

#	Parameter	SEAL BFV Degree Computation Time [ms]				
	Degree	1024	2048	4096	8192	16384
1	Average Batch	0.024	0.050	0.129	0.273	0.539
2	Average Unbatch	0.026	0.048	0.105	0.214	0.453
3	Average Encrypt	0.537	1.034	3.034	8.262	26.371
4	Average Decrypt	0.118	0.234	0.764	2.671	11.488
5	Average Add	0.005	0.008	0.034	0.112	0.430
6	Average Multiply	1.103	2.180	7.349	27.757	116.834
7	Average Multiply Plain	0.113	0.234	0.931	4.047	19.624
8	Average Square	0.754	1.509	5.038	20.058	82.345
9	Average Relinearize	N/A	N/A	1.496	7.331	42.251
10	Average Rotate 1 step	N/A	N/A	1.549	7.354	43.365
11	Average Rotate Random	N/A	N/A	6.213	31.027	205.262
12	Average Rotate Columns	N/A	N/A	1.493	7.360	42.124
13	CPU Usage [%]	1%	2.3%	16.6%	51.8%	89.7%

Objective 2: Results for t2_micro instance - CKKS

#	Parameter	SEAL CKKS Degree Computation Time [ms]				
	Degree	1024	2048	4096	8192	16384
1	Average Batch	0.496	1.055	2.467	6.197	17.045
2	Average Unbatch	0.558	1.182	3.273	11.141	46.447
3	Average Encrypt	0.508	0.950	3.376	9.462	31.022
4	Average Decrypt	0.015	0.026	0.112	0.405	1.705
5	Average Add	0.006	0.009	0.030	0.105	0.418
6	Average Multiply	0.053	0.088	0.345	1.364	5.432
7	Average Multiply Plain	0.014	0.023	0.091	0.375	1.453
8	Average Square	0.035	0.064	0.251	1.015	4.191
9	Average Relinearize	N/A	N/A	1.530	7.811	43.702
	Average Rescale	N/A	N/A	0.733	3.516	15.965
10	Average Rotate 1 step	N/A	N/A	1.750	8.344	47.054
11	Average Rotate Random	N/A	N/A	7.205	31.284	227.630
12	Average Complex Conjugate	N/A	N/A	1.757	8.244	46.406
13	CPU [%]	1.0%	1.7%	15.0%	46.2%	100%

Objective 2: Results for c5n_large instance - BFV

#	Parameter	SEAL BFV Degree Computation Time [ms]				
	Degree	1024	2048	4096	8192	16384
1	Average Batch	0.025	0.054	0.105	0.213	0.425
2	Average Unbatch	0.023	0.039	0.083	0.168	0.352
3	Average Encrypt	0.421	0.786	2.274	6.227	19.964
4	Average Decrypt	0.082	0.165	0.541	1.920	7.527
5	Average Add	0.004	0.006	0.018	0.073	0.309
6	Average Multiply	0.747	1.571	5.255	20.001	81.804
7	Average Multiply Plain	0.081	0.169	0.712	2.999	12.707
8	Average Square	0.522	1.071	3.612	13.791	57.450
9	Average Relinearize	N/A	N/A	1.078	5.273	31.282
10	Average Rotate 1 step	N/A	N/A	1.083	5.310	31.056
11	Average Rotate Random	N/A	N/A	4.467	20.178	136.762
12	Average Rotate Columns	N/A	N/A	1.082	5.291	30.989
13	CPU Usage [%]	1.0%	1.7%	12.0%	36.7%	100%
15	CPU USage [76]	1.0%	1.7%	12.0%	50.7%	100%

Objective 2: Results for c5n_large instance - CKKS

#	Parameter	SEAL CKKS Degree Computation Time [ms]				
	Degree	1024	2048	4096	8192	16384
1	Average Batch	0.364	0.788	1.802	4.487	12.292
2	Average Unbatch	0.390	0.831	2.325	8.039	33.520
3	Average Encrypt	0.422	0.792	2.643	7.334	23.595
4	Average Decrypt	0.009	0.016	0.063	0.245	1.041
5	Average Add	0.004	0.006	0.017	0.068	0.284
6	Average Multiply	0.024	0.048	0.179	0.841	3.900
7	Average Multiply Plain	0.009	0.016	0.060	0.239	0.950
8	Average Square	0.016	0.032	0.120	0.552	2.763
9	Average Relinearize	N/A	N/A	1.097	5.357	31.338
	Average Rescale	N/A	N/A	0.519	2.574	11.756
10	Average Rotate 1 step	N/A	N/A	1.280	6.155	34.147
11	Average Rotate Random	N/A	N/A	4.458	28.515	145.624
12	Average Complex Conjugate	N/A	N/A	1.275	6.045	33.749
13	CPU [%]	0.7%	1.3%	11.0%	41.3%	100%

Objective 2: Results for r5a_large instance - BFV

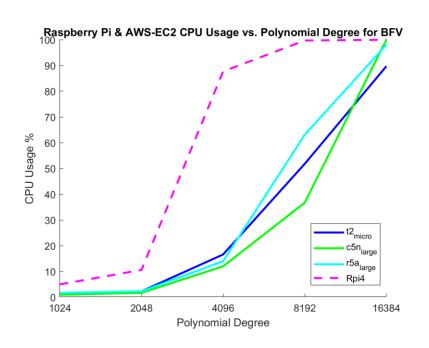
#	Parameter	SEAL BFV Degree Computation Time [ms]				
	Degree	1024	2048	4096	8192	16384
1	Average Batch	0.056	0.056	0.124	0.273	0.513
2	Average Unbatch	0.022	0.046	0.091	0.196	0.451
3	Average Encrypt	0.482	0.902	2.604	7.491	24.381
4	Average Decrypt	0.102	0.186	0.632	2.374	9.425
5	Average Add	0.005	0.007	0.020	0.083	0.327
6	Average Multiply	1.002	1.986	6.581	25.472	103.115
7	Average Multiply Plain	0.102	0.206	0.930	3.827	16.475
8	Average Square	0.676	1.390	4.609	18.096	74.667
9	Average Relinearize	N/A	N/A	1.270	6.631	39.109
10	Average Rotate 1 step	N/A	N/A	1.322	6.585	39.271
11	Average Rotate Random	N/A	N/A	4.299	24.564	162.075
12	Average Rotate Columns	N/A	N/A	1.287	6.708	39.196
13	CPU Usage [%]	1.7%	2.3%	14.0%	63.1%	98%

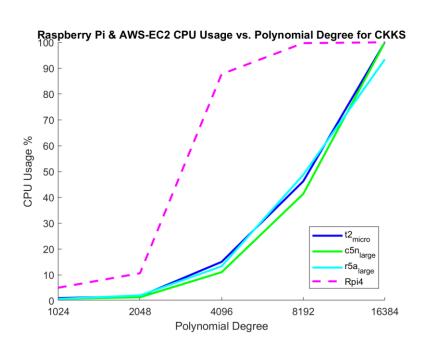
Objective 2: Results for r5a_large instance - CKKS

#	Parameter	SEAL CKKS Degree Computation Time [ms]				
	Degree	1024	2048	4096	8192	16384
1	Average Batch	0.479	1.080	2.227	5.365	14.436
2	Average Unbatch	0.536	1.102	3250	10.403	44.064
3	Average Encrypt	0.481	0.855	3.145	8.735	28.172
4	Average Decrypt	0.012	0.022	0.091	0.302	1.229
5	Average Add	0.004	0.007	0.022	0.075	0.311
6	Average Multiply	0.033	0.066	0.268	0.984	4.578
7	Average Multiply Plain	0.013	0.024	0.100	0.351	1.500
8	Average Square	0.022	0.045	0.179	0.677	3.103
9	Average Relinearize	N/A	N/A	1.449	6.599	38.316
	Average Rescale	N/A	N/A	0.667	3.164	14.578
10	Average Rotate 1 step	N/A	N/A	1.623	7.275	41.515
11	Average Rotate Random	N/A	N/A	5.934	28.260	181.675
12	Average Complex Conjugate	N/A	N/A	1.579	7.215	41.180
13	CPU [%]	0.7%	2%	13.3%	48.7%	93.4%
13	CPU [%]	0.7%	2%	13.3%	48.7%	93.4%

Objective 2 Results: CPU Usage

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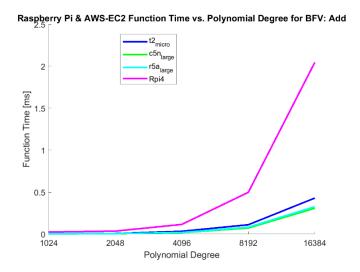


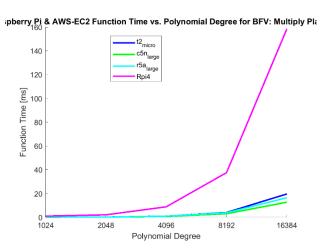


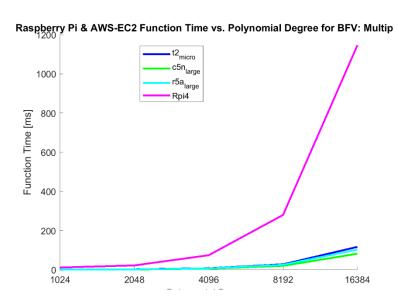
Raspberry Pi cannot complete 32k polynomial degree. AWS EC2 instances can complete without crashing but with long delay times (10s +) for each run.

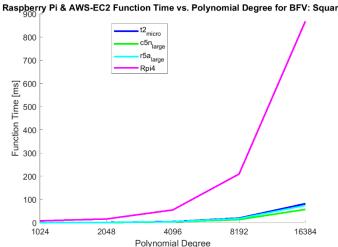
CPU utilization approaches 100% for all current platforms, including computationally optimized and memory optimized AWS EC2 instances.

Objective 2 Results: Function Computation Time











Objective 3: Client-Server Model

- Client-server model will move the bulk of the calculations from the resource-constrained Raspberry Pi to the AWS EC2 server and from micro AWS EC2 client and high performance AWS EC2 server.
 - Intended to lessen the computational cost on each device to allow a homomorphic solution for small SWaP devices

Objective 3: Implementation

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 Client BFV with 4096 default degree test and server BFV with 4096 default degree test added to SEAL library functions

```
The following examples should be executed while reading
 comments in associated files in native/examples/.
                            | Source Files

    BFV Basics

                              1 bfv basics.cpp
                             2 encoders.cpp
 Encoders
 Levels
                              3 levels.cpp
 4. CKKS Basics
                              4 ckks basics.cpp
 5. Rotation
                              5 rotation.cpp
                              6 performance.cpp
 6. Performance Test
    785 MB] Total allocation from the memory pool
 Run example (1 \sim 6) or exit (0): 6
         Example: Performance Test
Select a scheme (and optionally poly modulus degree):
 1. BFV with default degrees
 2. BFV with a custom degree
 3. CKKS with default degrees
 4. CKKS with a custom degree
 5. Client BFV with default degrees
   Server BFV with default degrees
 Run performance test (1 \sim 6) or go back (0):
```

Objective 3: Client-Server Implementation

```
Server BFV Performance Test with Degrees: 4096, 8192, 16384, and 32768
 Encryption parameters :
   scheme: BFV
   poly_modulus_degree: 4096
   coeff_modulus size: 109 (36 + 36 + 37) bits
   plain_modulus: 786433
Running tests ..... Done
Average add: 18157 microseconds
Average multiply: 61216 microseconds
Average multiply plain: 35296 microseconds
Average square: 42591 microseconds
 Encryption parameters :
   scheme: BFV
   poly_modulus_degree: 8192
   coeff modulus size: 218 (43 + 43 + 44 + 44 + 44) bits
   plain_modulus: 786433
Running tests ..... Done
Average add: 65073 microseconds
Average multiply: 228081 microseconds
Average multiply plain: 127401 microseconds
Average square: 162559 microseconds
 Encryption parameters :
   scheme: BFV
   poly_modulus_degree: 16384
   plain_modulus: 786433
Running tests ..... Done
Average add: 270092 microseconds
Average multiply: 961099 microseconds
Average multiply plain: 529304 microseconds
Average square: 683535 microseconds
```

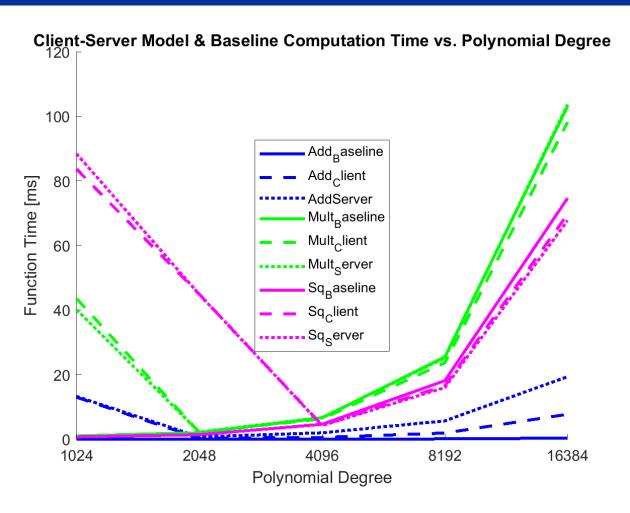
```
Client BFV Performance Test with Degrees: 4096, 8192, 16384, and 32768
  Encryption parameters :
    scheme: BFV
    poly_modulus_degree: 4096
    coeff_modulus size: 109 (36 + 36 + 37) bits
    plain_modulus: 786433
Generating secret/public keys: Done
Running tests
                + Plaintext polynomial: 2
     + Plaintext polynomial: 2x^1 + 2
     + Plaintext polynomial: 4x^1 + 2
     + Plaintext polynomial: 2x^2 + 2x^1 + 2
     + Plaintext polynomial: 4x^2 + 2
     + Plaintext polynomial: 4x^2 + 2x^1 + 2
     + Plaintext polynomial: 4x^2 + 4x^1 + 2
     + Plaintext polynomial: 2x^3 + 2x^2 + 2x^1 + 2
     + Plaintext polynomial: 4x^3 + 2
     + Plaintext polynomial: 4x^3 + 2x^1 + 2
 Done
Average add: 15929 microseconds
Average multiply: 61121 microseconds
Average multiply plain: 34737 microseconds
Average square: 43107 microseconds
  Encryption parameters :
    scheme: BFV
    poly_modulus_degree: 8192
    coeff_modulus size: 218 (43 + 43 + 44 + 44 + 44) bits
    plain_modulus: 786433
Generating secret/public keys: Done
               + Plaintext polynomial: 2
Running tests
     + Plaintext polynomial: 2x^1 + 2
     + Plaintext polynomial: 4x^1 + 2
     + Plaintext polynomial: 2x^2 + 2x^1 + 2
     + Plaintext polynomial: 4x^2 + 2
     + Plaintext polynomial: 4x^2 + 2x^1 + 2
     + Plaintext polynomial: 4x^2 + 4x^1 + 2
     + Plaintext polynomial: 2x^3 + 2x^2 + 2x^1 + 2
     + Plaintext polynomial: 4x^3 + 2
     + Plaintext polynomial: 4x^3 + 2x^1 + 2
Average add: 59338 microseconds
Average multiply: 228033 microseconds
Average multiply plain: 125155 microseconds
Average square: 164971 microseconds
```

Objective 3: Client Server Results Table (c5n shown)

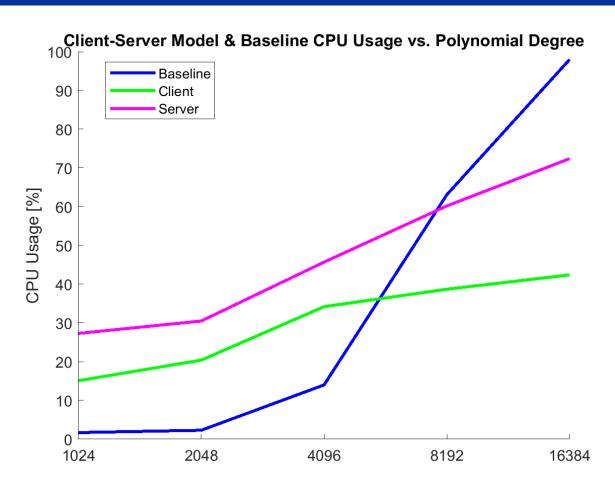
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#	Parameter			SEAL BFV Degree (Computation Time		
	Degree	1024	2048	4096	8192	16384
5	Average Add	13.002	0.226	0.539	1.895	7.71
6	Average Multiply	43.559	2.106	6.294	23.639	98.195
7	Average Multiply Plain	87.966	42.817	18.324	5.619	23.462
8	Average Square	83.679	44.901	4.321	16.539	69.679
13	CPU Usage [%]	15.1%	20.4%	34.2%	38.7%	42.4%
#	Parameter	SEAL BFV Degree (Server) Computation Time [ms]				
	Degree	1024	2048	4096	8192	16384
5	Average Add	13.245	0.712	1.971	5.667	19.364
6	Average Multiply	40.085	2.221	6.708	25.129	103.67
7	Average Multiply Plain	86.588	42.386	18.429	6.14	25.528
8	Average Square	88.393	44.865	4.19	15.996	67.72

Objective 3: Results – Function Time vs. Baseline



Objective 3: Results - CPU Usage





Future Work

- Optimization of the SEAL library functions for to improve resource freeing and reallocation
- Improvement of Raspberry Pi platform resource allocation
- Implementation on IoT device app for in-situ encrypted data usage

Summary

- Homomorphic encryption has made advancements in the past decade for implementation.
 - Understood from mathematical perspective
 - Can now optimize for resource-constrained environments
- Client-server model prototype can allow for future IoT device platforms to make use of homomorphic encryption and optimize for practical use.

GitHub File Structure

- README.txt
- 209AS_FinalPresentation.pptx
- 209AS_FinalReport.docx
- Client-Server Model <software folder>
- Console data logs <text file data folder>
- https://github.com/daniel-achee/ece209-project.git

Division of Labor

- Presentation & Report:
 - Primary: J. Quintana
 - Supporting: D. Achee
- Objective 1:
 - Primary: J. Quintana
 - Supporting: D. Achee
- Objective 2:
 - Primary: D. Achee
 - Supporting: J. Quintana
 - Initial AWS-EC2 instance implementation done by D. Achee, data shown from J. Quintana AWS-EC2 instances.
- Objective 3:
 - Server side: D. Achee
 - Client side: J. Quintana
 - Client-server model done by D. Achee, Rpi platform side done by J. Quintana

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