## 1 Modeling

Formal specification of a buffer with an infinite number of states.

### 1.1 Rigid data types

**Example 1.** Specification of lists of arbitrary elements:

```
spec! LISTS
pr BOOL
sorts Elt List .
op empty : -> List .
op _%_ : Elt List -> List .
op _in_ : Elt List -> Bool .
vars E E' : Elt .
var L : List .

(1) ∀E·E in empty = false
(2) ∀E, E'·(E in E'%L) if E = E'
(3) ∀E, E'·E in E'%L = E in L if ¬(E = E')
```

### 1.2 Nominals

**Example 2.** Specification of nominals:

```
spec! NOMINAL
sort Nominal .
op init : -> Nominal .
op next : Nominal -> Nominal .
```

#### 1.3 Flexible data types

Example 3. Specification of the attributes read and del:

# 2 Formal verification

The property we are interested in proving formally is  $\Gamma \vdash_{\Sigma} \forall L, E \cdot \exists Z \cdot (@_Z \operatorname{read})(L) = E \operatorname{if} (E \operatorname{in} L) = \operatorname{true}$ , where  $\Sigma = \operatorname{Sig}(\mathsf{BUFFER})$  and  $\Gamma = \operatorname{Sen}(\mathsf{BUFFER})$ . We proceed by induction on the structure of L.

- $\bullet \ \, \mathrm{ind.\ base:}\ \Gamma \vdash \forall \mathtt{E} \cdot \exists \mathtt{Z} \cdot (@_{\mathtt{Z}} \, \mathtt{read})(\mathtt{empty}) = \mathtt{E} \, \, \mathtt{if} \, \, (\mathtt{E} \, \mathtt{in} \, \mathtt{empty}) = \mathtt{true}, \, \mathtt{which} \, \mathtt{is} \, \mathtt{true} \, \mathtt{since} \, \mathtt{E} \, \mathtt{in} \, \mathtt{empty} = \mathtt{false} \, (\texttt{E} \, \mathtt{in} \, \mathtt{empty}) = \mathtt{false}$
- ind. step:  $\Gamma \cup \{ \forall E \cdot \exists Z \cdot \texttt{read}(Z, 1) \text{ if } (E \text{ in } 1) = \texttt{true} \} \vdash_{\mathsf{Sig}[1,e]} \forall E \cdot \exists Z \cdot \texttt{read}(Z, 1 \circ e) = E \text{ if } (E \text{ in } 1 \circ e) = \texttt{true},$  where  $e \colon \to \mathsf{Elt}$  and  $1 \colon \to \mathsf{List}$