

# The Infinity Mirror Test for Graph Generators

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## Introduction

- Graph generative models are a way of learning the salient features of a given graph to generate similar graphs that capture the original's essence.
- However, these models make assumptions during feature extraction and generation that may not be apparent in the generated graph.
- By repeatedly fitting the same model to the graphs it generates, the model's implicit biases will be amplified and exaggerated.

## Framework

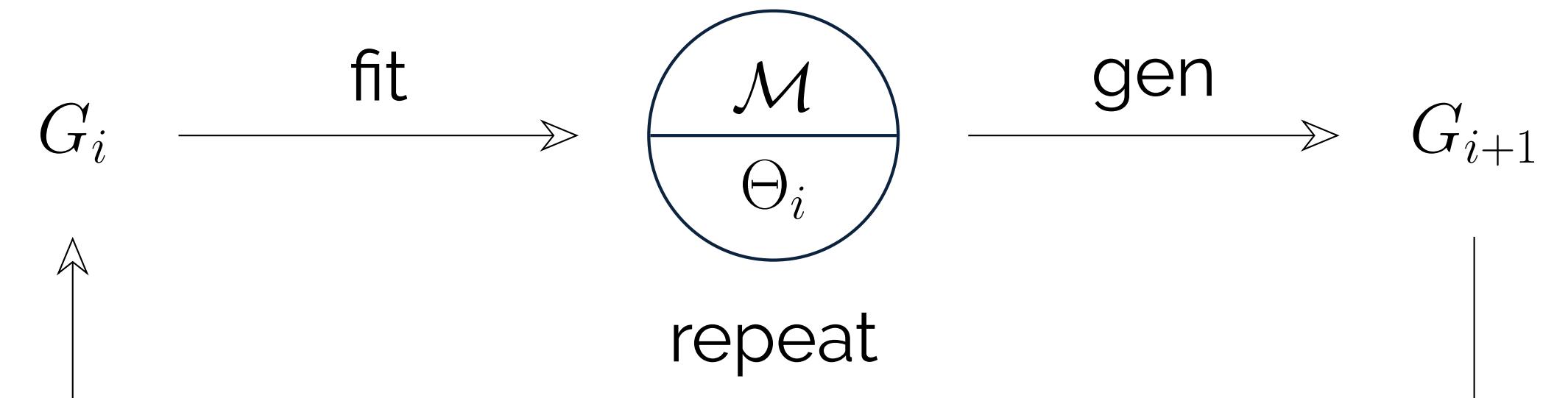
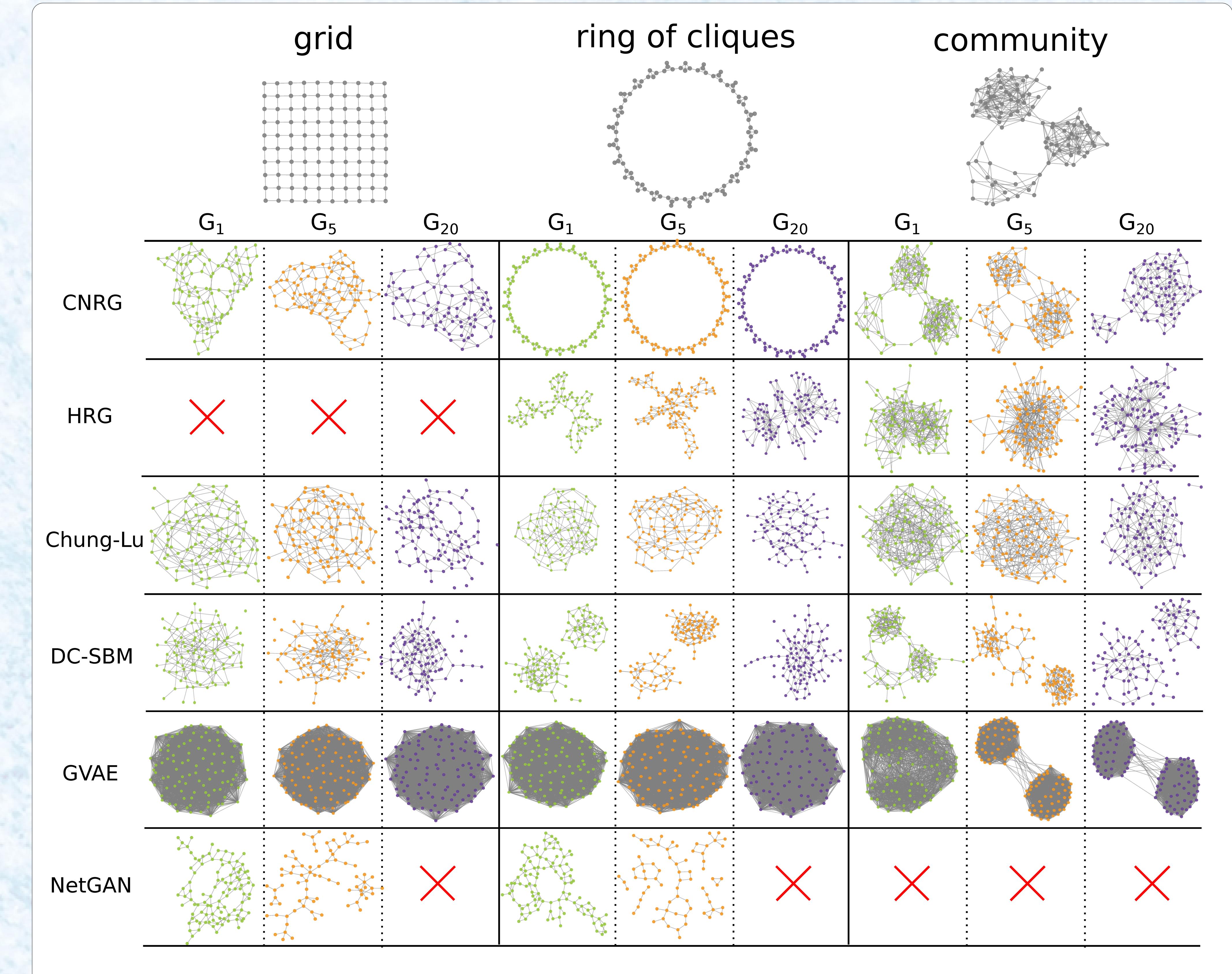


Figure 1. Fit a model  $\mathcal{M}$  on an input graph  $G_i$  to learn  $\Theta_i$  and generate  $G_{i+1}$ . Repeat the process on  $G_{i+1}$ .

## Methodology

- Given a choice of model  $\mathcal{M}$  and an initial seed graph  $G_0$ , we can use the idea in Figure 1 to generate a sequence of  $n$  graphs  $G_1, G_2, \dots, G_n$ .
- The degeneration experienced by a chain can be quantified by comparing the initial graph  $G_0$  to the last graph  $G_n$  using a graph similarity metric such as DELTACON.
- For each  $(\mathcal{M}, G_0)$  pair, we generate 50 chains, select the one with median DELTACON score, and visualize  $G_1, G_5$ , and  $G_{20}$  (i.e., the 1<sup>st</sup>, 5<sup>th</sup>, and 20<sup>th</sup> generations) in the figure to the right.



## Key Findings

- CNRG does well on graphs with community structure but not on highly-regular graphs.
- HRG's grammar extraction fails on grids and fares poorly on the other two graph types.
- Chung-Lu entirely fails to capture local and global network structure.
- SBM performs similarly to CNRG on grids and community but worse on the clique ring.
- GraphVAE produces overly dense graphs regardless of the input.
- NetGAN tends to generate increasingly sparse graphs until failure.

