$$\vec{F}(x,y) = \langle M, N \rangle$$

$$\vec{F}(x,y) = M(x,y)\hat{i} + N(x,y)\hat{j}$$

$$\operatorname{curl} \vec{F} = N_x - M_y$$

$$\operatorname{div} \vec{F} = M_x + N_y$$