

Daniel Perry (dperry@cs.utah.edu)
cs6210 / Fall 2005
Homework 5

1)

I implemented newtons algorithm, and it seemed to work perfectly for almost any situation (I tried values of P (p -th root) from 2 to 30, and values of A from 2 to 15). In every case it came up with the exact same answer as the math.h function pow(), or came within $10e-7$ of it (that was the difference between iterations I used to stop iterating).

Some results:

<i>P (power)</i>	<i>A</i>	<i>$A^{(1/P)}$</i>	<i>iterations</i>
2	2	1.4142135	5
18	8	1.122462	9
20	14	1.1410545	13
29	2	1.0241896	5
29	14	1.0952712	13
30	132	1.1767544	50

2)

a) Analysis is attached to back (handwritten paper).

summary:

g1 – diverges

g2 – converges

g3 – converges

g4 - converges

b) By implementing the four fixed point problems I found the implementation matched my analysis. I found that g1 diverged, g2 would converge, g3 would converge about half the time of g2, and g4 would converge just under half the time of g3.

Results:

<i>x_0</i>	<i>g1 iterations</i>	<i>g2 iterations</i>	<i>g3 iterations</i>	<i>g4 iterations</i>
5	diverges	45	20	7
10	diverges	46	20	8
20	diverges	46	20	9

3)

In this implementation I found that both types of sampling (a-uniform, b-chebyshev's zeros), had similar results with the max difference between the interpolation and the original function with values of j very small. However as j increased, the uniform

Daniel Perry (dperry@cs.utah.edu)
cs6210 / Fall 2005
Homework 5

sampling slowly increased in max difference, while the chebyshev zeros sampled implementation didn't increase in difference as much.

Results.

<i>j</i>	<i>max diff w/ Uniform</i>	<i>max diff w/ Chebyshev</i>
3	0.646154	0.828912
4	0.707014	1.09565
6	0.432692	0.846387
8	0.247359	0.703027
10	0.298402	0.570512
16	2.09904	0.264316

I've attached my code as well. It can also be found at
<http://www.cs.utah.edu/~dperry/classes/cs6210/>.