Heimadæmi 2

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1 Spurning 1

1.1 Dæmi 1

- 1. Dæmi 1
- 2. litarinn



Mynd 1: triangle_dæmi1

2.1 Dæmi 1

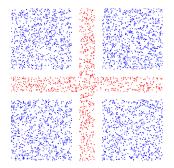
- 1. Dæmi 1
- 2. litarinn



Mynd 2: fallingPoints_dæmi1

2.2 Dæmi 2

- 1. Dæmi 2
- 2. litarinn



Mynd 3: fallingPoints_dæmi2

3.1 Dæmi 1

- 1. $M = \begin{bmatrix} -\frac{1}{3} & \frac{2}{3} \\ \frac{2}{3} & -\frac{1}{3} \end{bmatrix}$
- 2. [0, 1]

3.2 Dæmi 2

- $1. \ M = \begin{bmatrix} 1 & 1 \\ -1 & 1 \end{bmatrix}$
- 2. <u>[3, -1]</u>

4.1 Dæmi 1

1. $\vec{p}=(a,b)$ $\vec{q}=(-b,a)$ $\vec{p}\cdot\vec{q}=\vec{p}_x\vec{q}_x+\vec{p}_y\vec{q}_y$ a*-b+a*b=-ba+ba $\underline{-ba+ba=0}$ $\underline{\text{petta er hornrætt,}}$ Vegna ef svarið er 0 þá er það hornrétt

4.2 Dæmi 2

1.
$$\vec{c} = \vec{a} \times \vec{b} = [\vec{a}_y \vec{b}_z - \vec{a}_z \vec{b}_y, \quad \vec{a}_z \vec{b}_x - \vec{a}_x \vec{b}_z, \quad \vec{a}_x \vec{b}_y - \vec{a}_y \vec{b}_x]$$

$$\begin{array}{ll} 2. \ \, \vec{c} = \vec{v} \times \vec{w} = [\vec{v}_y \vec{w}_z - \vec{v}_z \vec{w}_y, \quad \vec{v}_z \vec{w}_x - \vec{v}_x \vec{w}_z, \quad \vec{v}_x \vec{w}_y - \vec{v}_y \vec{w}_x] \\ \underline{[0,0,1]} = \vec{v} \times \vec{w} = [0*0-0*1, \quad 0*0-1*0, \quad 1*1-0*0] \end{array}$$

$$\begin{array}{ll} 3. \ \, \vec{c} = \vec{w} \times \vec{v} = [\vec{w}_y \vec{v}_z - \vec{w}_z \vec{v}_y, \quad \vec{w}_z \vec{v}_x - \vec{w}_x \vec{v}_z, \quad \vec{w}_x \vec{v}_y - \vec{w}_y \vec{v}_x] \\ \underline{[0,0,-1]} = \vec{w} \times \vec{v} = [1*0-0*0, \quad 0*1-0*0, \quad 0*0-1*1] \end{array}$$

4.3 Dæmi 3

1.
$$\vec{c} = \vec{a} \times \vec{b} = [\vec{a}_y \vec{b}_z - \vec{a}_z \vec{b}_y, \quad \vec{a}_z \vec{b}_x - \vec{a}_x \vec{b}_z, \quad \vec{a}_x \vec{b}_y - \vec{a}_y \vec{b}_x]$$

$$\begin{aligned} 2. & \ \vec{c} = \vec{a} \times \vec{a} = [\vec{a}_y \vec{a}_z - \vec{a}_z \vec{a}_y, & \ \vec{a}_z \vec{a}_x - \vec{a}_x \vec{a}_z, & \ \vec{a}_x \vec{a}_y - \vec{a}_y \vec{a}_x] \\ & \ \vec{a}_y \vec{a}_z - \vec{a}_z \vec{a}_y = 0 \\ & \ \vec{a}_x \vec{a}_y - \vec{a}_y \vec{a}_x = 0 \\ & \ \vec{a}_x \vec{a}_y - \vec{a}_y \vec{a}_x = 0 \\ & \ \vec{c} = [0, 0, 0] \end{aligned}$$

4.4 Dæmi 4

1.
$$\vec{c} = \vec{a} \times \vec{b} = [\vec{a}_y \vec{b}_z - \vec{a}_z \vec{b}_y, \quad \vec{a}_z \vec{b}_x - \vec{a}_x \vec{b}_z, \quad \vec{a}_x \vec{b}_y - \vec{a}_y \vec{b}_x]$$

$$\begin{aligned} 2. & \ \vec{s} = \vec{v} \times \vec{w} = \underline{ \left[\vec{v}_y \vec{w}_z - \vec{v}_z \vec{w}_y, \quad \vec{v}_z \vec{w}_x - \vec{v}_x \vec{w}_z, \quad \vec{v}_x \vec{w}_y - \vec{v}_y \vec{w}_x \right] } \\ & \ \vec{t} = \vec{v} \times \vec{s} = \underline{ \left[\overline{\vec{v}_y \vec{s}_z - \vec{v}_z \vec{s}_y, \quad \vec{v}_z \vec{s}_x - \vec{v}_x \vec{s}_z, \quad \vec{v}_x \vec{s}_y - \vec{v}_y \vec{s}_x \right] } \end{aligned}$$

3. let say $\vec{v} = [1, 0, 0]$ and $\vec{w} = [2, 1, 0]$.

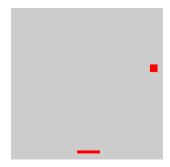
then

$$\begin{array}{l} [0,0,1] = \vec{s} = \vec{v} \times \vec{w} = [0*0-0*0, \quad 0*2-1*0, \quad 1*1-0*2] \\ [0,-1,0] = \vec{t} = \vec{v} \times \vec{s} = [0*1-1*0, \quad 0*0-1*1, \quad 1*0-0*0] \\ \end{array}$$

$$\begin{split} \vec{v} \cdot \vec{s} &= \vec{v}_x \vec{s}_x + \vec{v}_y \vec{s}_y + \vec{v}_z \vec{s}_z \\ 0 &= \vec{v} \cdot \vec{s} = 1*0+0*0+0*1 \\ 0 &= \vec{v} \cdot \vec{t} = 1*0+0*-1+0*0 \\ \text{then } \vec{v}, \vec{s}, \vec{t} \text{ eru allir hornréttir} \end{split}$$

5.1 Dæmi 1

1. Dæmi 1



Mynd 4: box-bounce_dæmi1

Heimildir

- [1] Daníel Ágúst. Heimadæmi 3. URL: https://danielagust.github.io/TOL105M-Tolvugrafik-Daniel/Code/Heimad%C3%A6mi/heimad%C3%A6mi_3/heimad%C3%A6mi_3_index.html.
- [2] Daníel Ágúst. Heimadæmi 3 myndir. URL: https://danielagust.github.io/TOL105M-Tolvugrafik-Daniel/Code/Heimad%C3%A6mi/heimad%C3%A6mi_3/img.html.