

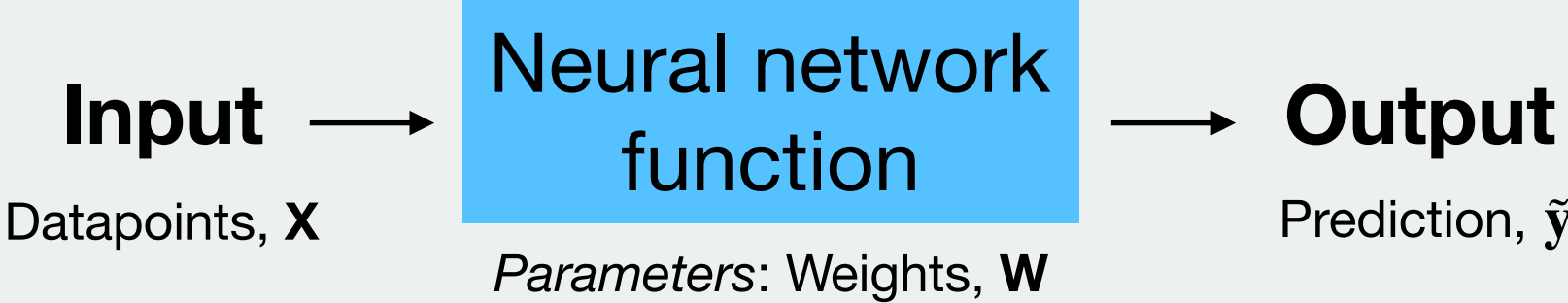
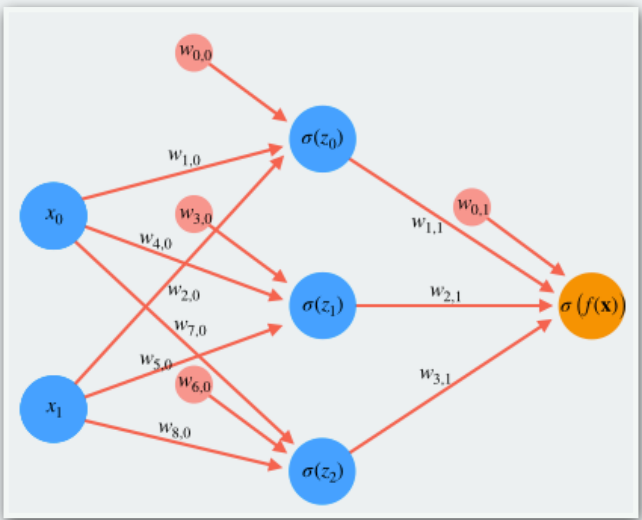
Artificial Neural Networks and Deep Learning

Week 4

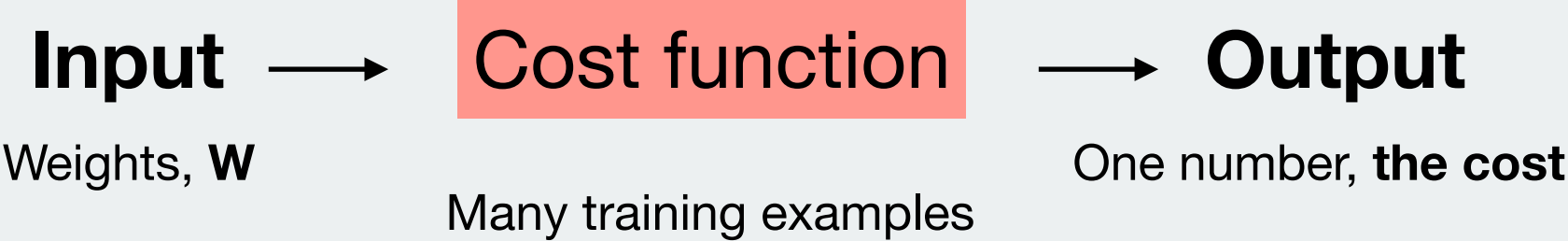
Convolutional neural networks

Quick recap...

(1) The model



(2) Its performance



$$\begin{aligned} C(\mathbf{W}) &= \frac{1}{N} \sum_i (\tilde{y}_i - y_i)^2 \\ &= (0.96 - 1)^2 \\ &\quad + (0.10 - 0)^2 \\ &\quad + (0.04 - 0)^2 \\ &\quad + \dots \\ &\quad + (0.70 - 1)^2 \\ &\quad + (0.02 - 0)^2 \\ &\quad + (0.99 - 1)^2 \end{aligned}$$

(3) The cost function gradient in \mathbf{W}

$$-\nabla C(\mathbf{W}) = \begin{bmatrix} -0.23 \\ 1.32 \\ 0.20 \\ 0.38 \\ -1.23 \\ 0.01 \\ 1.20 \\ -2.12 \\ 0.73 \\ 2.17 \\ 0.54 \\ -0.23 \\ -0.93 \\ 0.45 \end{bmatrix}$$

Find the gradients with
Backpropagation
... this week

(4) Updating \mathbf{W}

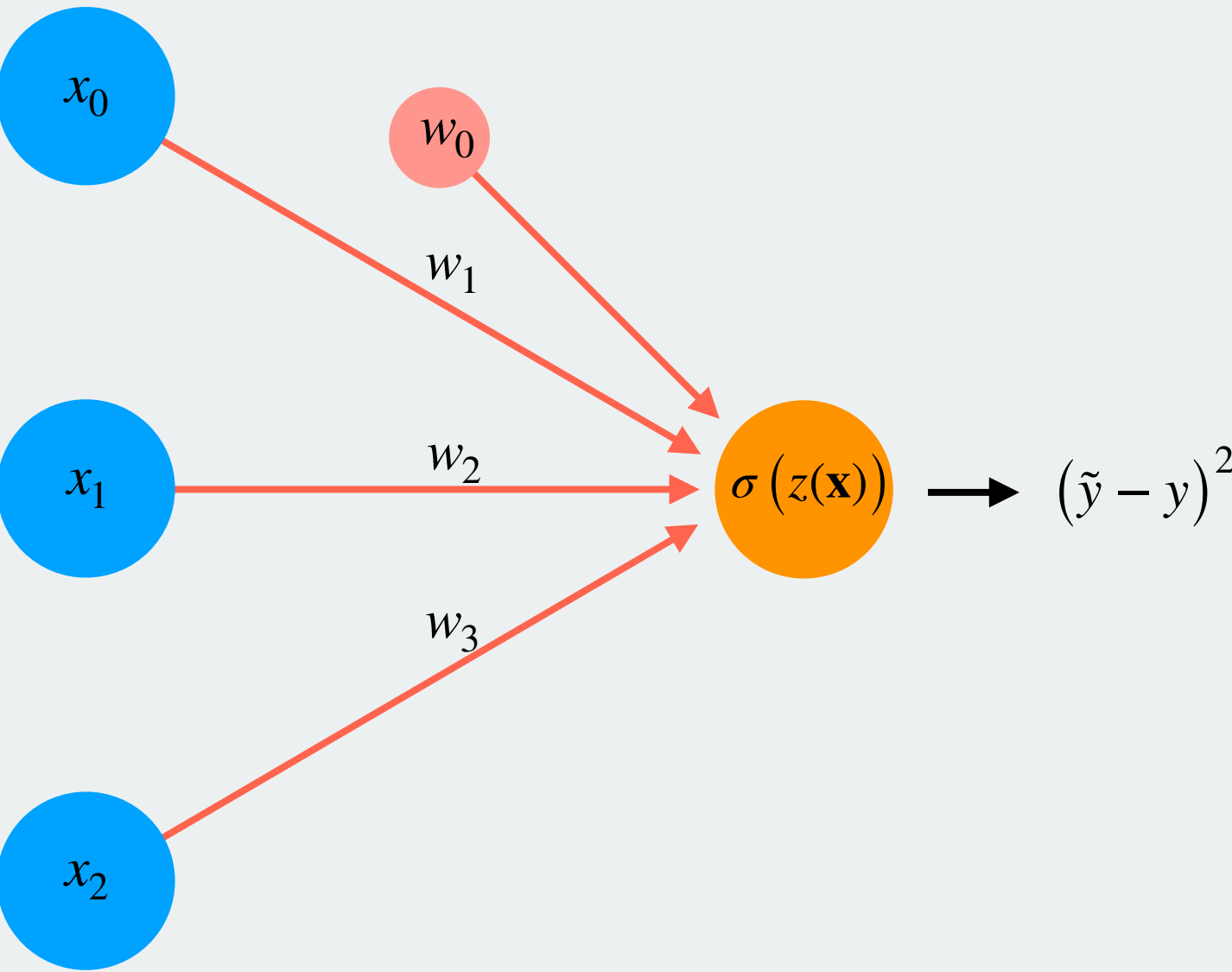
$$\mathbf{W} = \mathbf{W}^{\text{old}} + r (-\nabla C(\mathbf{W}^{\text{old}}))$$

(5) Repeat 3 and 4

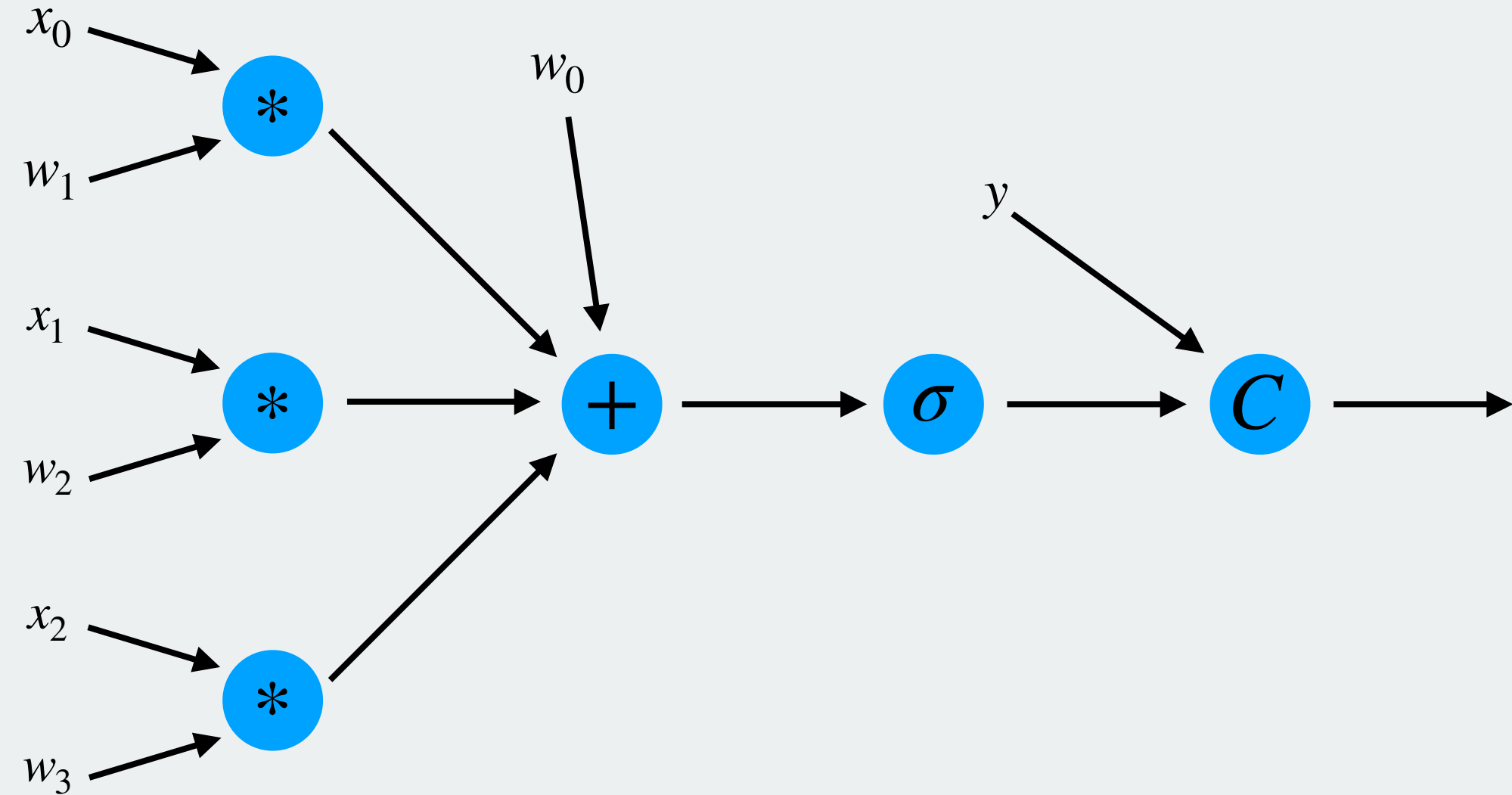
r is usually called the *learning rate*

Quick recap...

Neural network

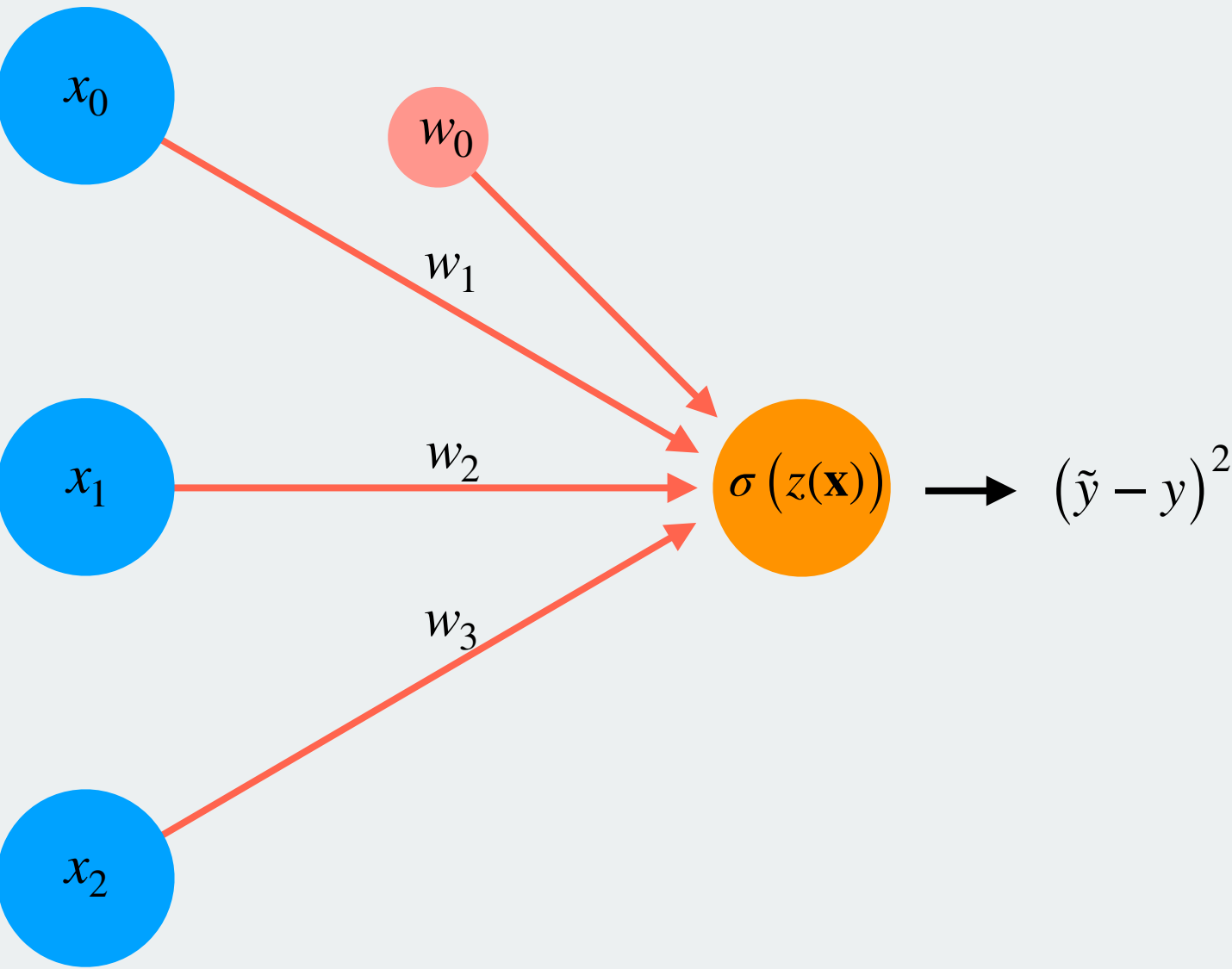


Computational graph

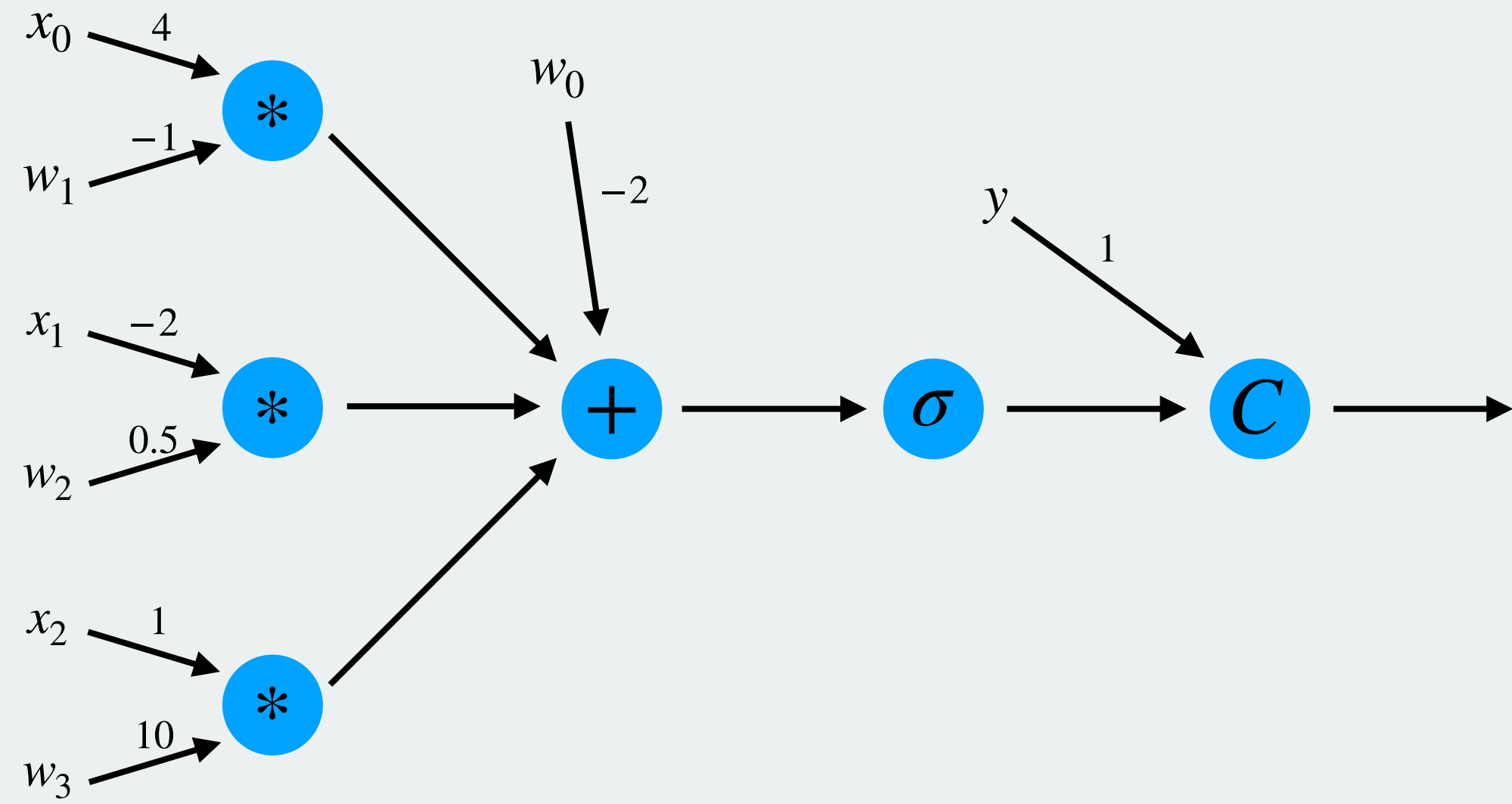


Quick recap...

Neural network

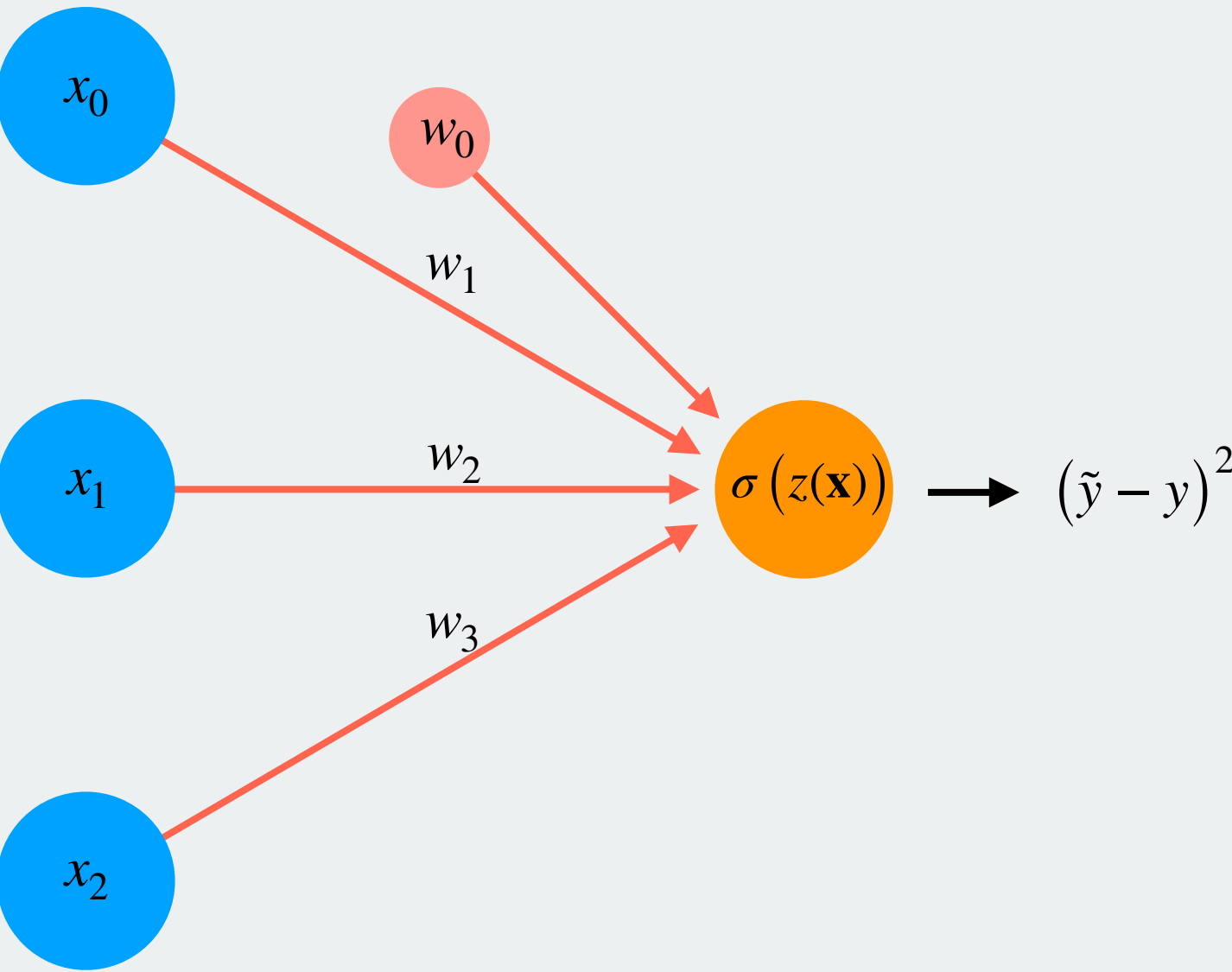


Computational graph



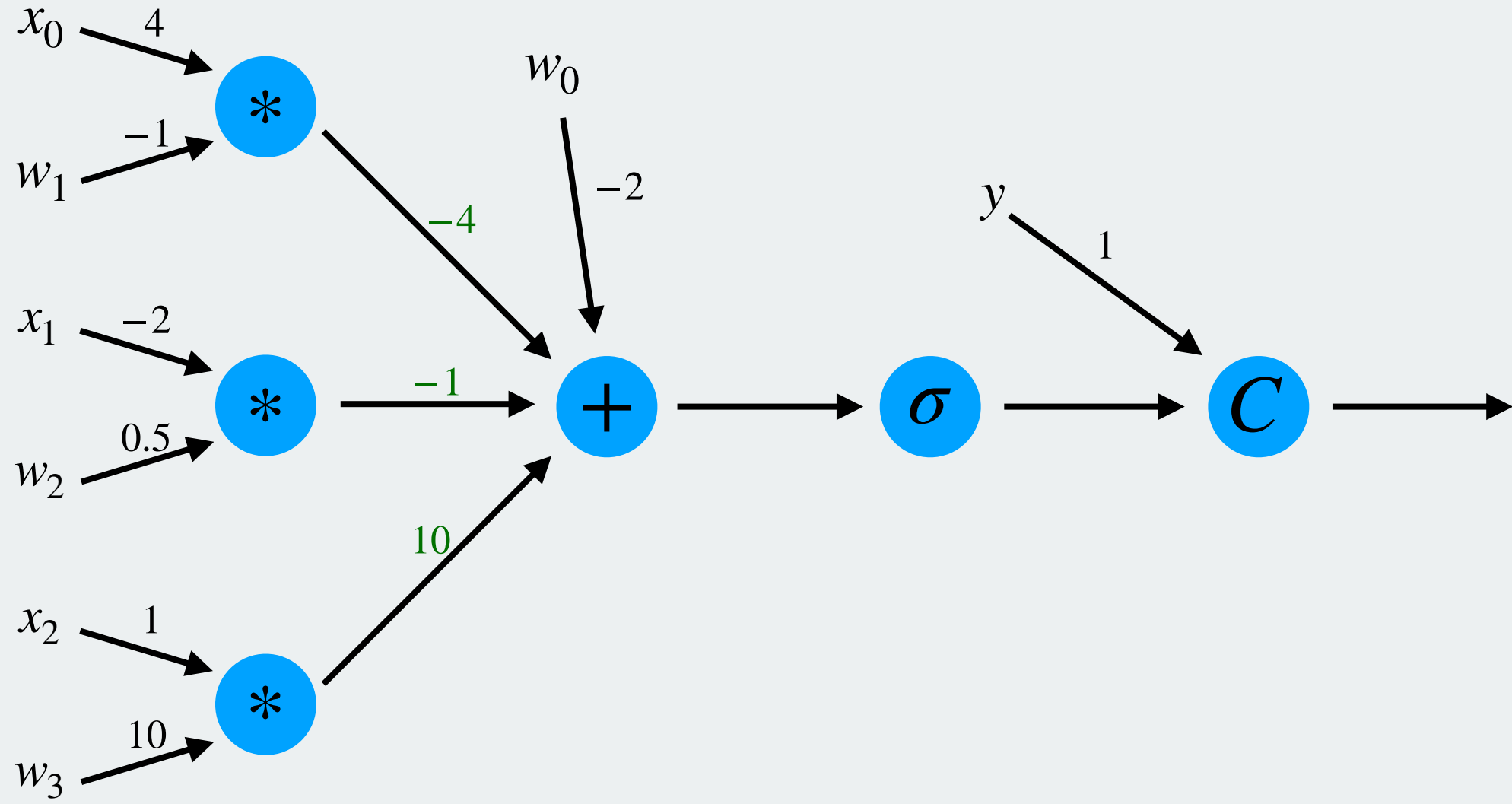
Quick recap...

Neural network



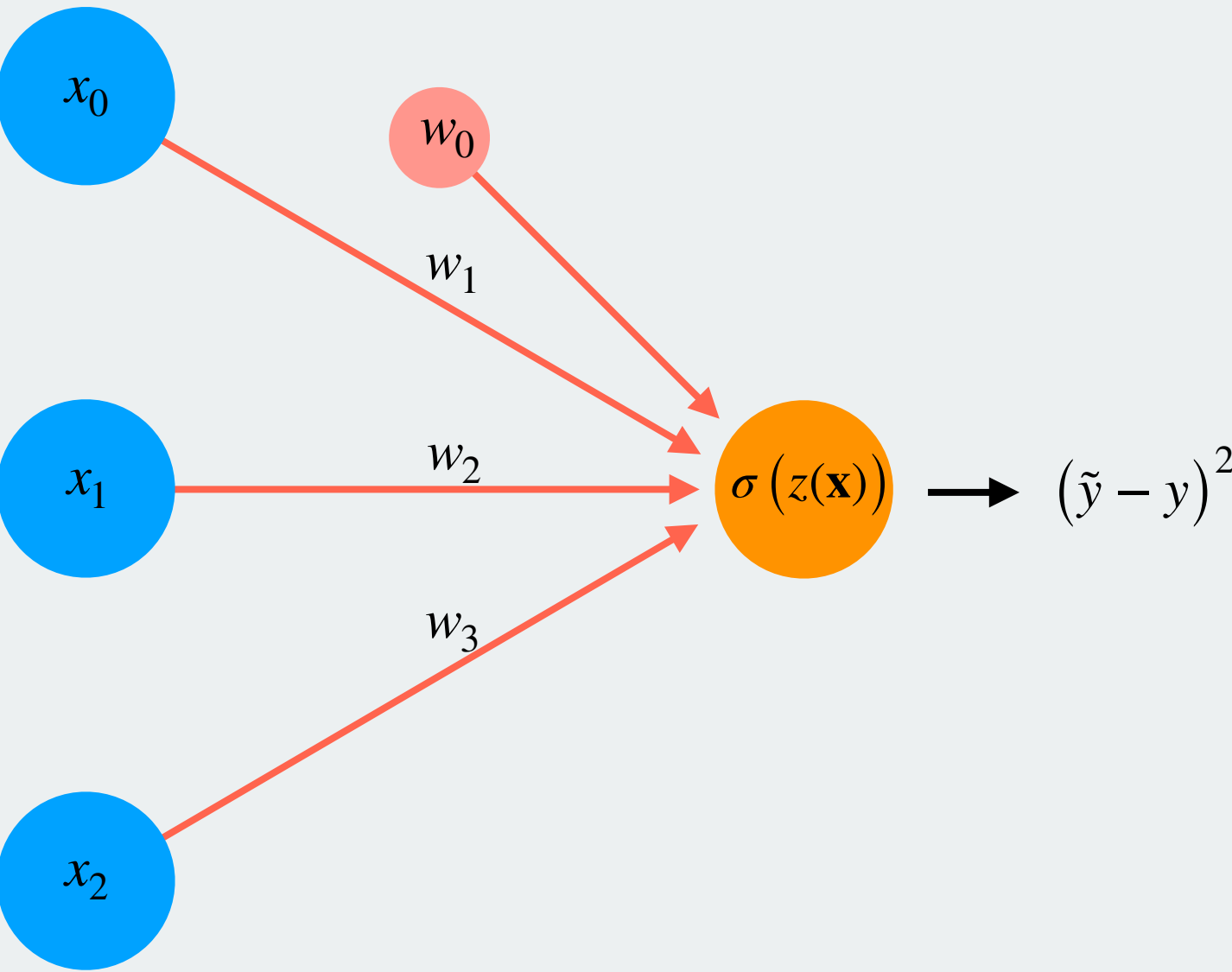
Computational graph

Forward pass



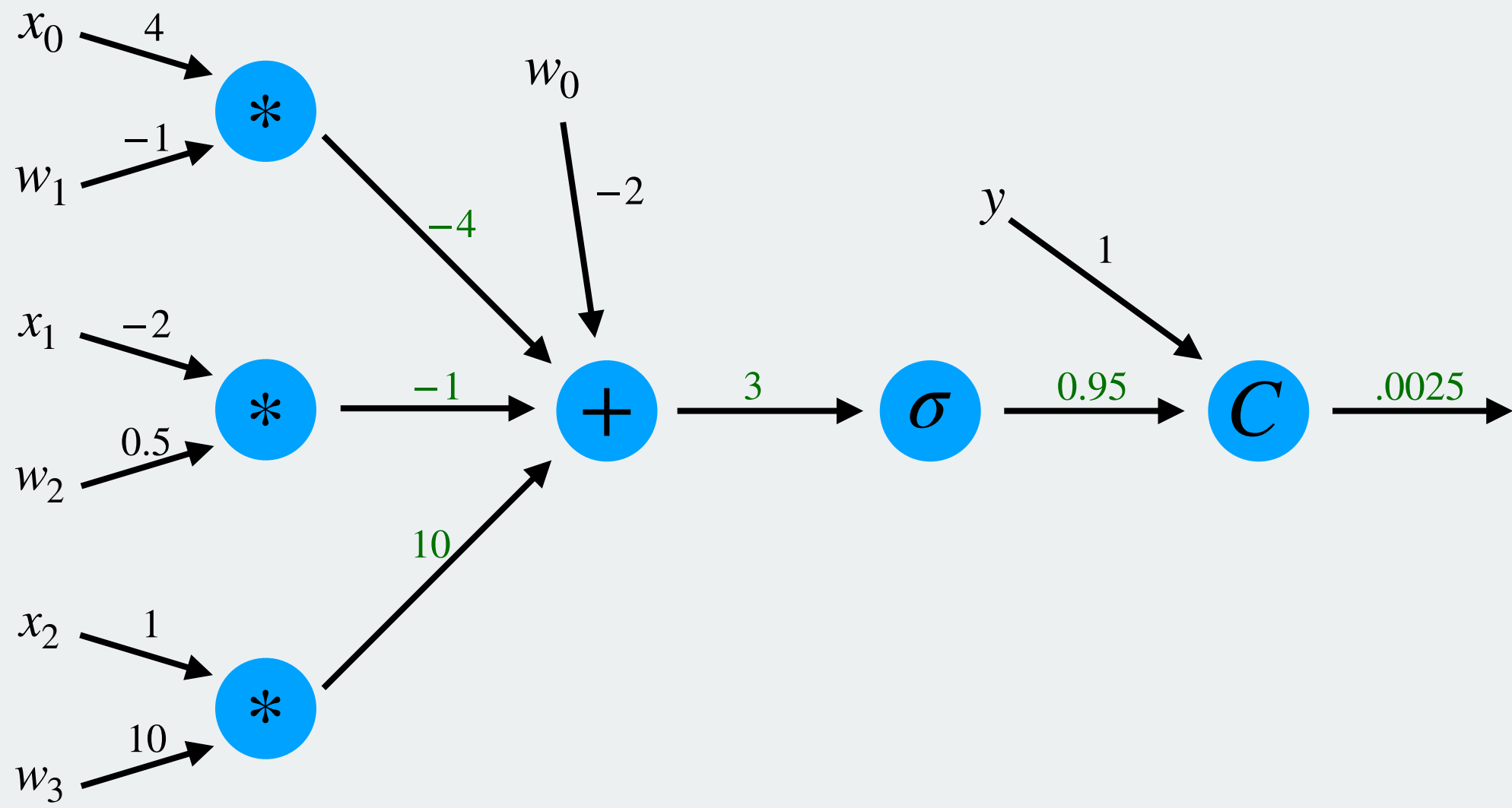
Quick recap...

Neural network



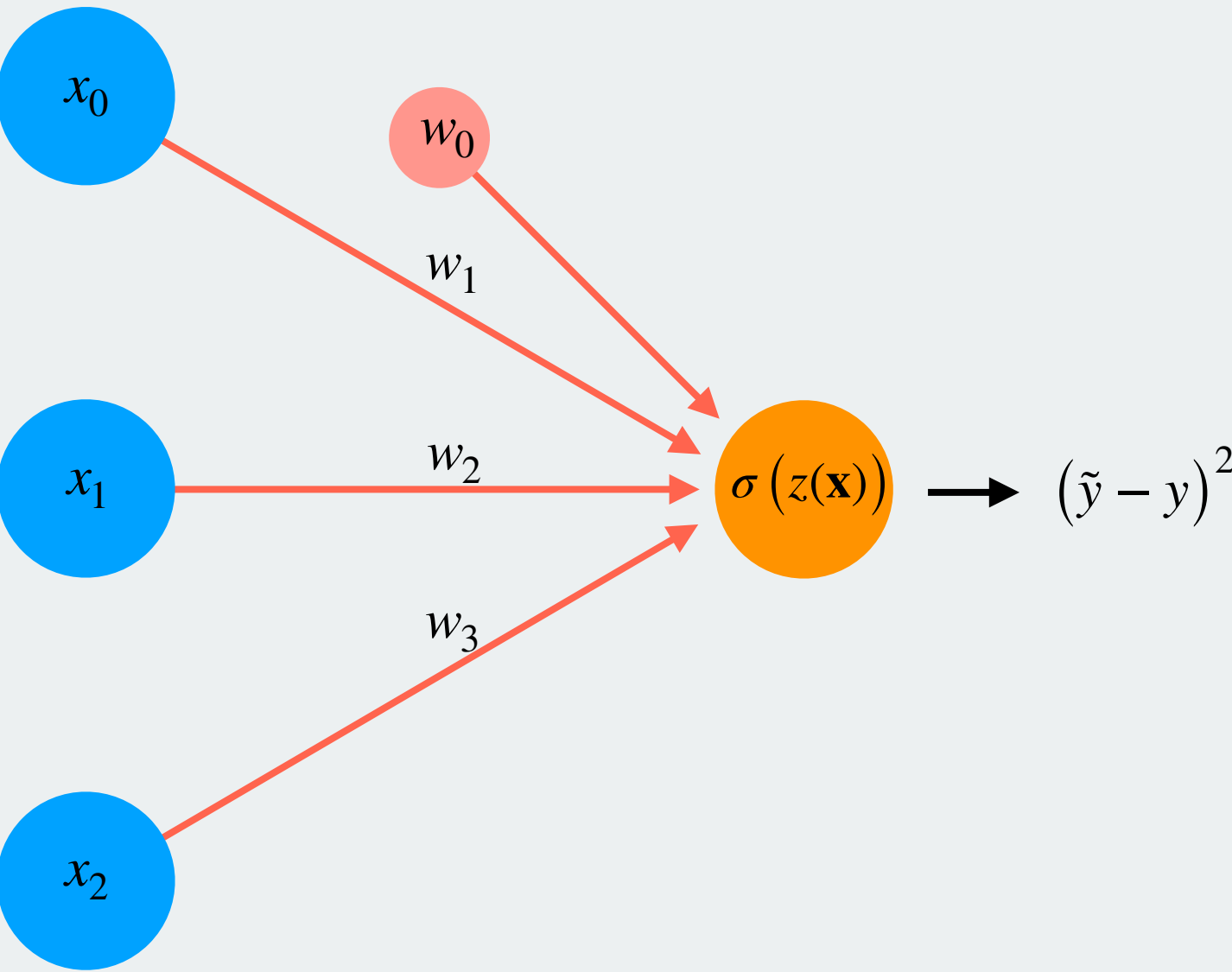
Computational graph

Forward pass



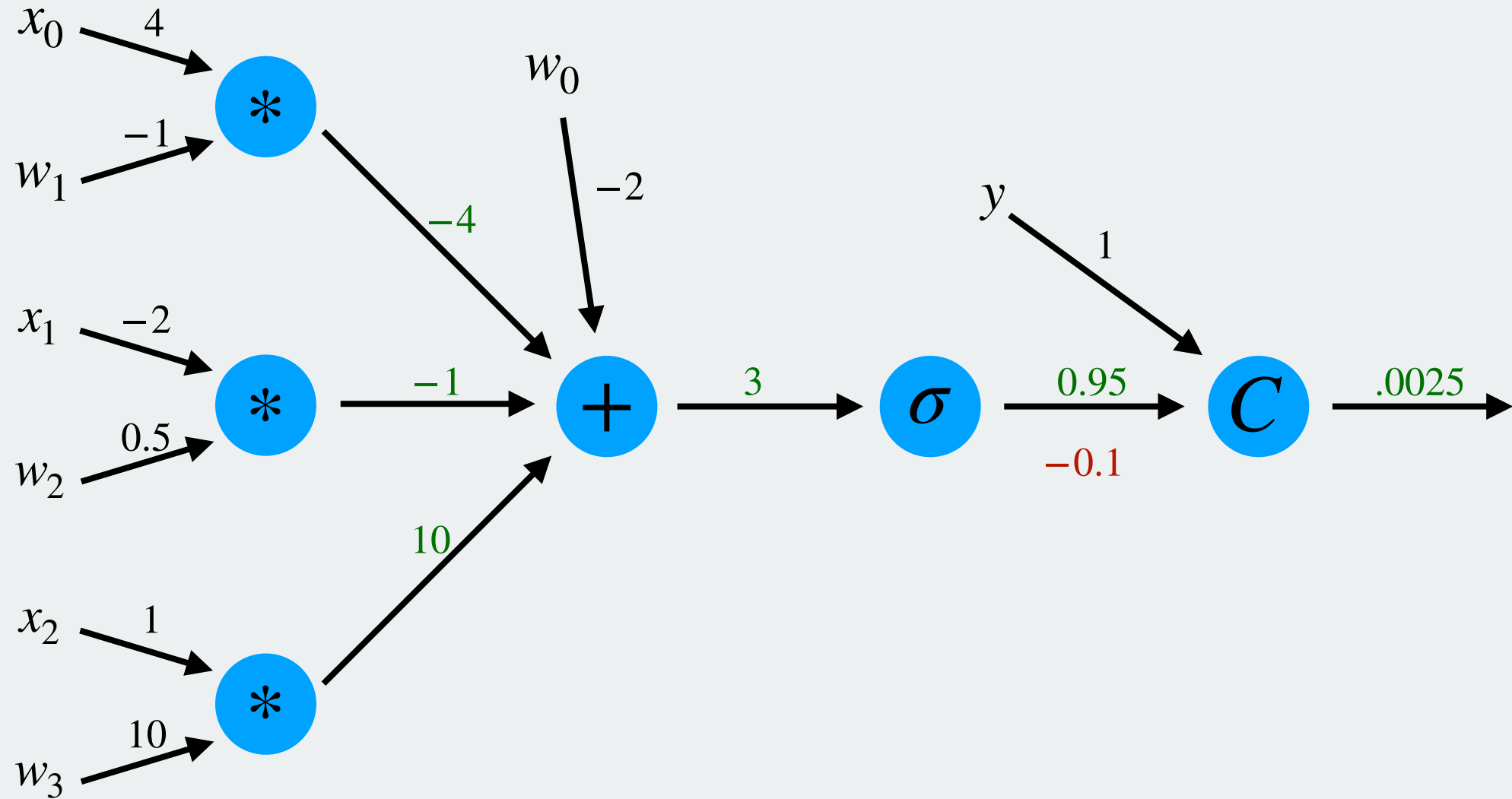
Quick recap...

Neural network

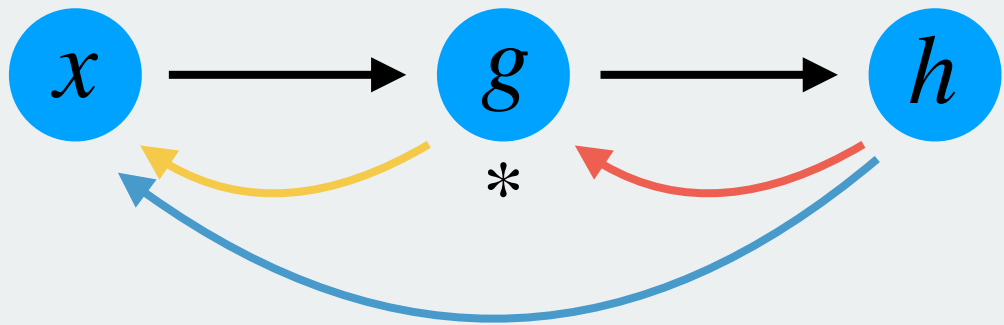


Computational graph

Backward pass



$h(g(x))$

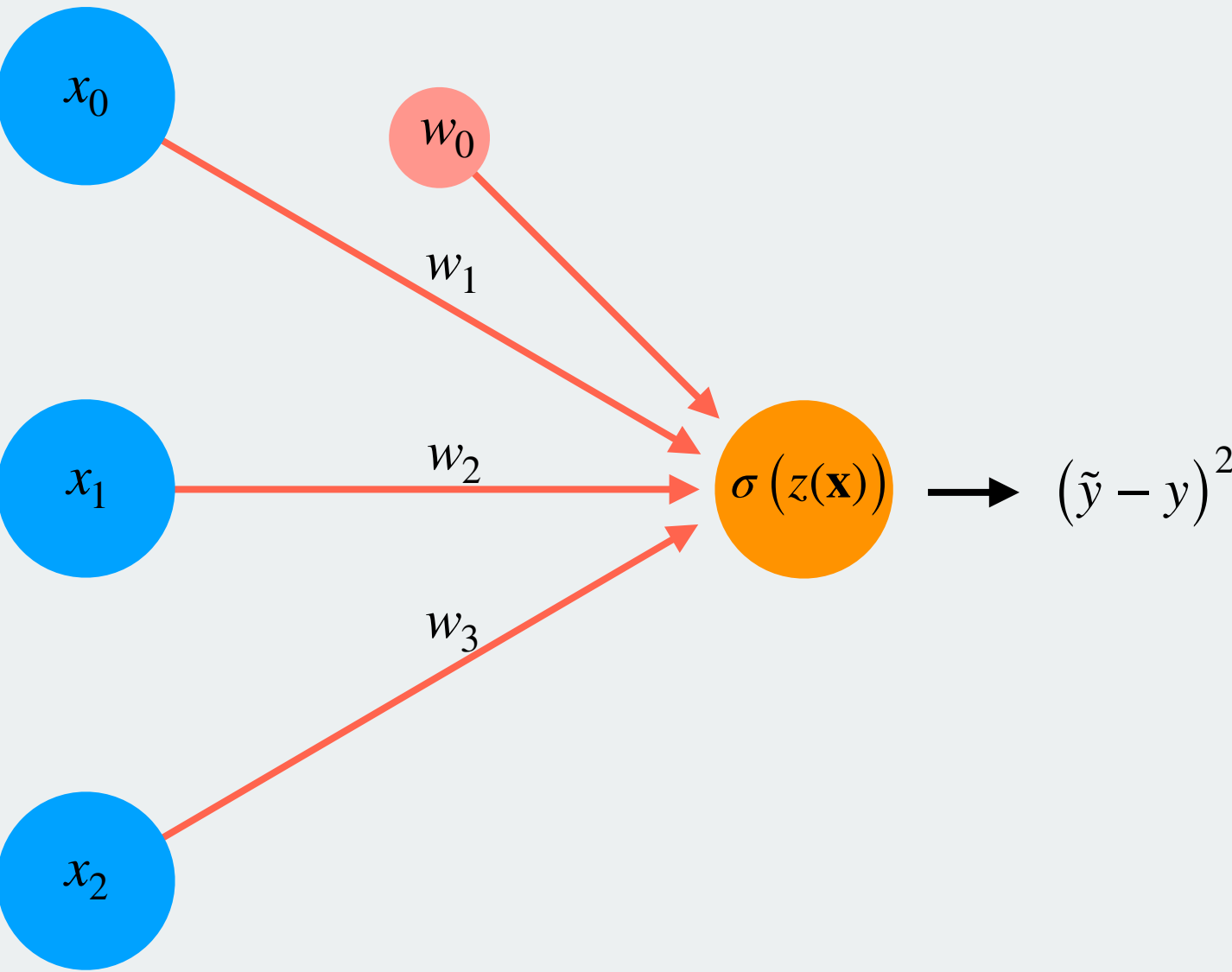


Chain rule says:

$$\frac{dh}{dx} = \frac{dh}{dg} \frac{dg}{dx}$$

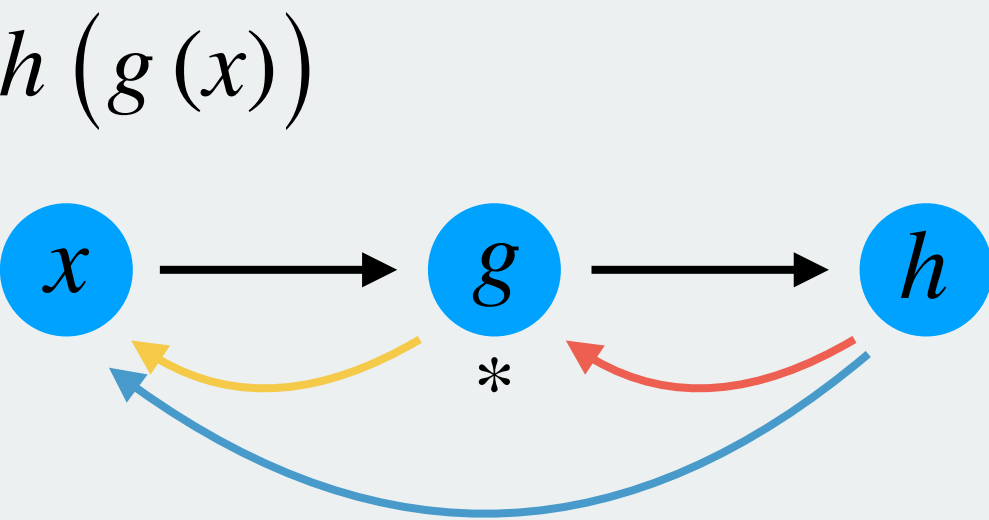
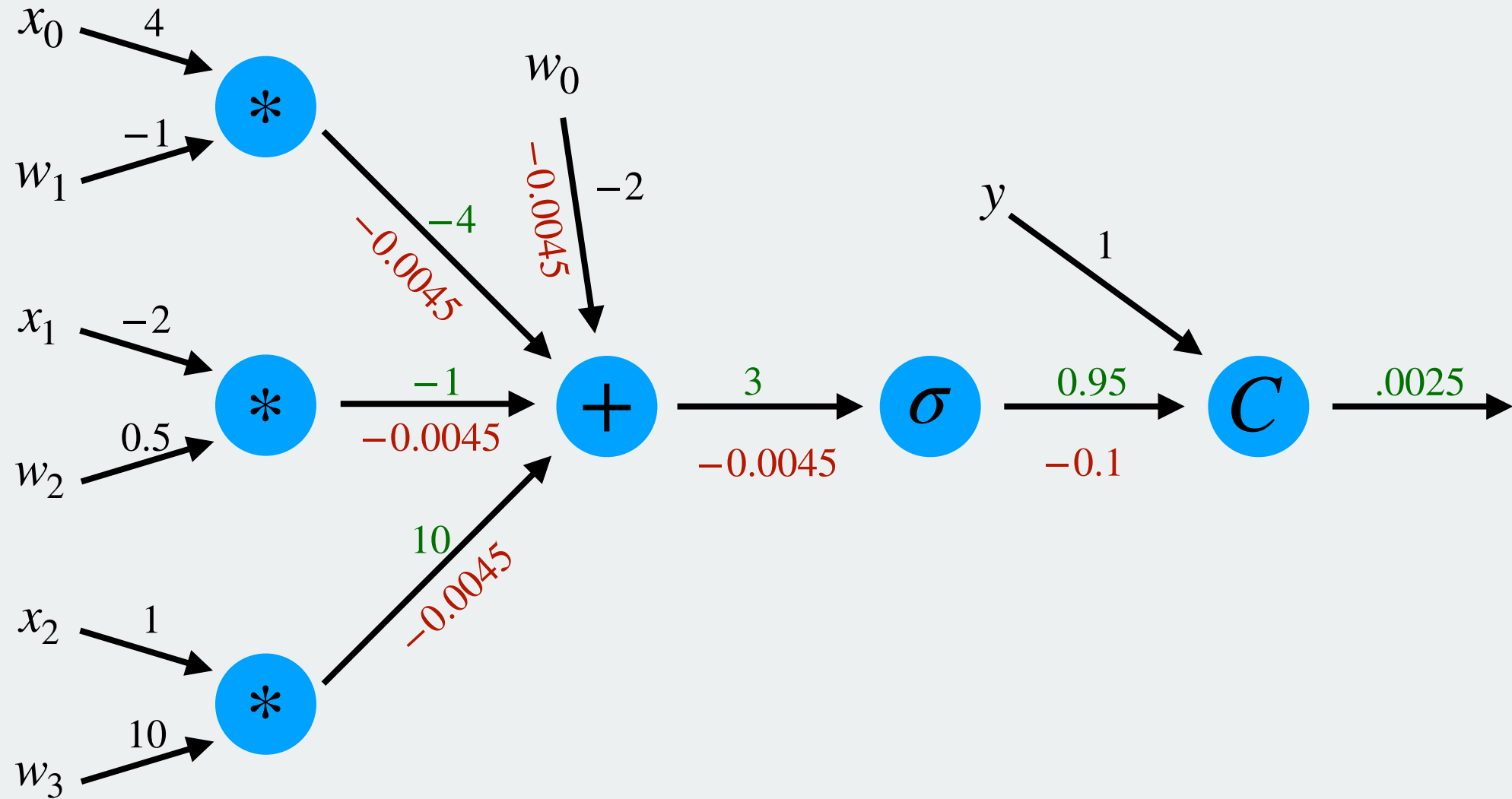
Quick recap...

Neural network



Computational graph

Backward pass

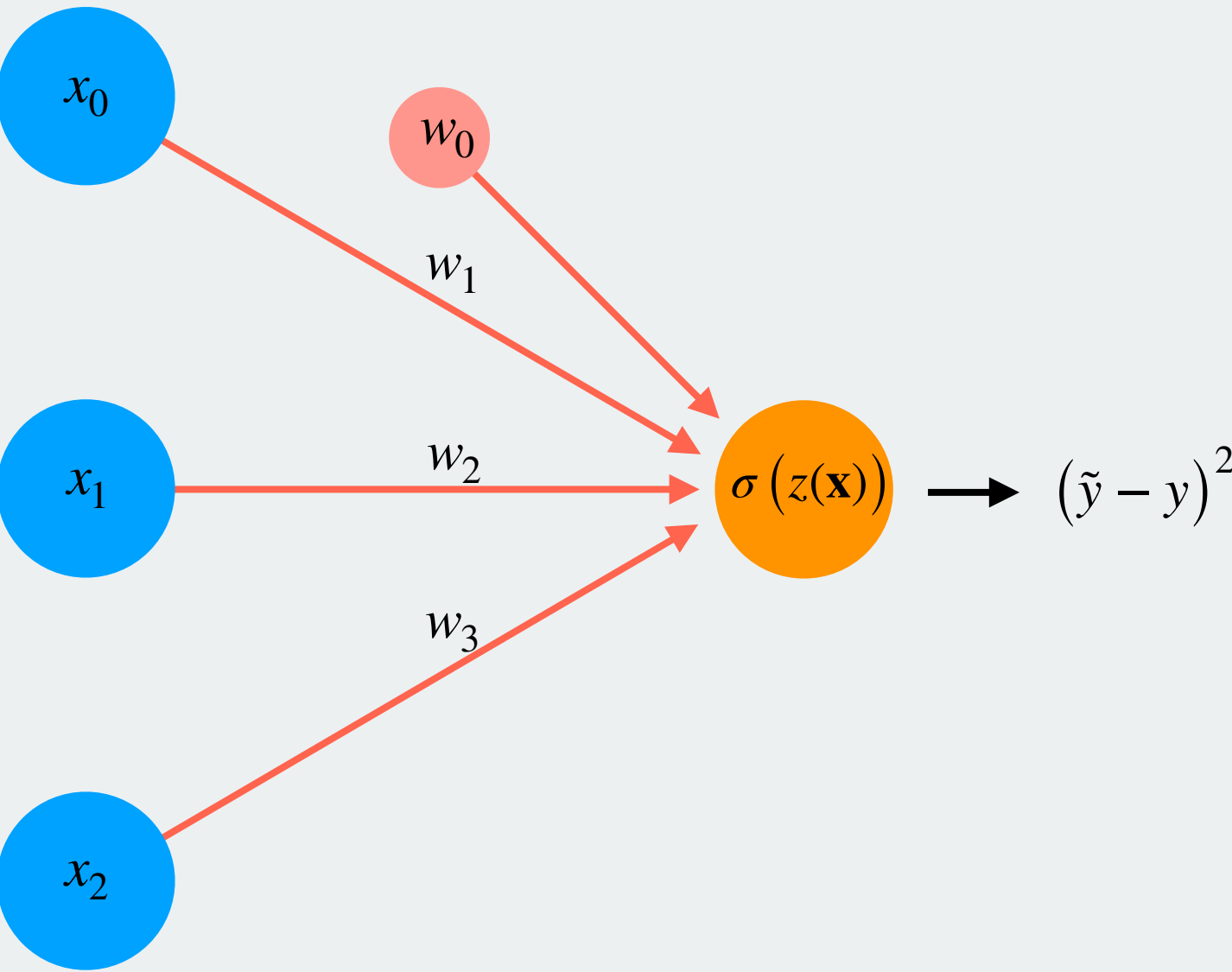


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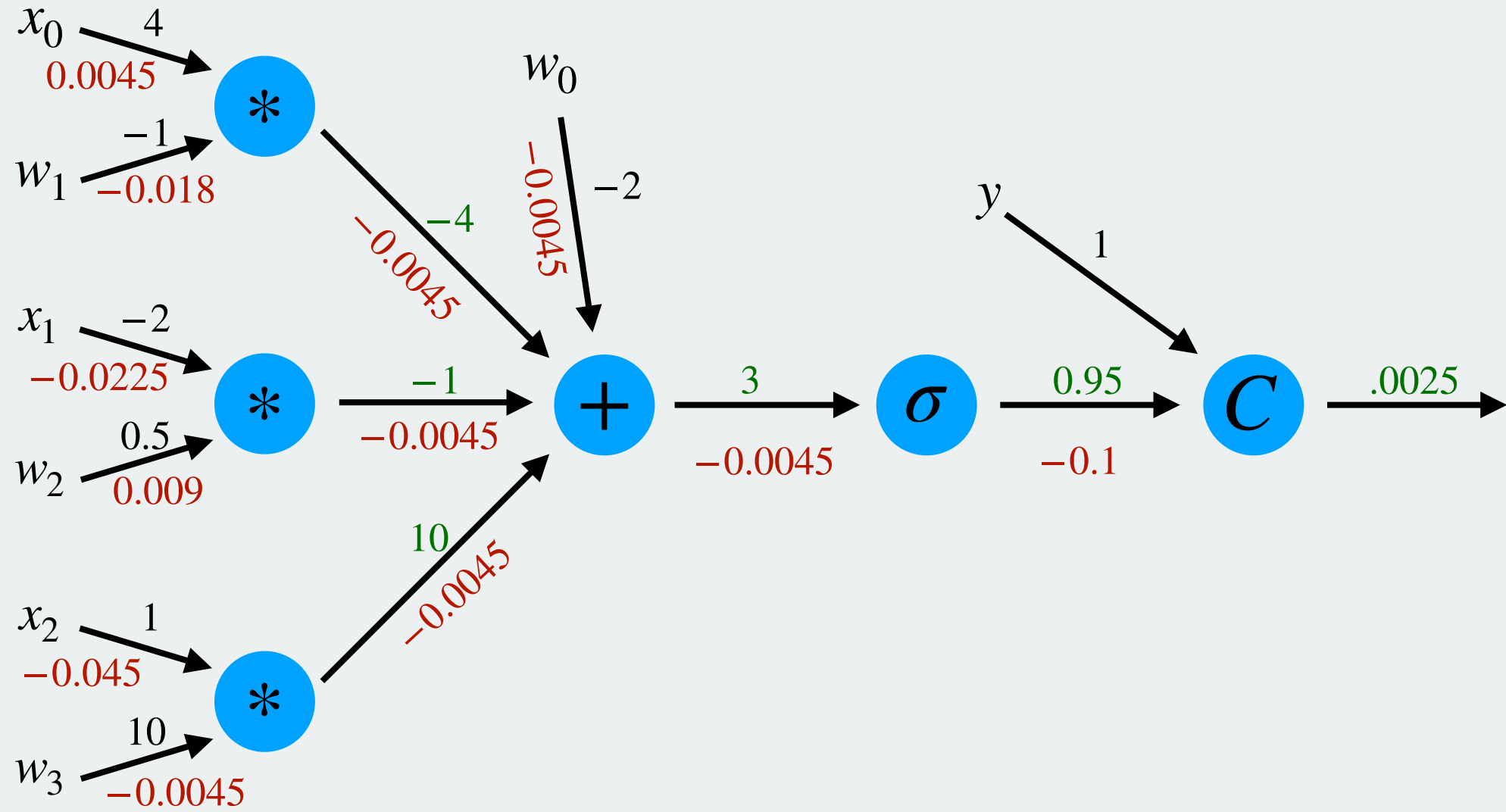
Quick recap...

Neural network

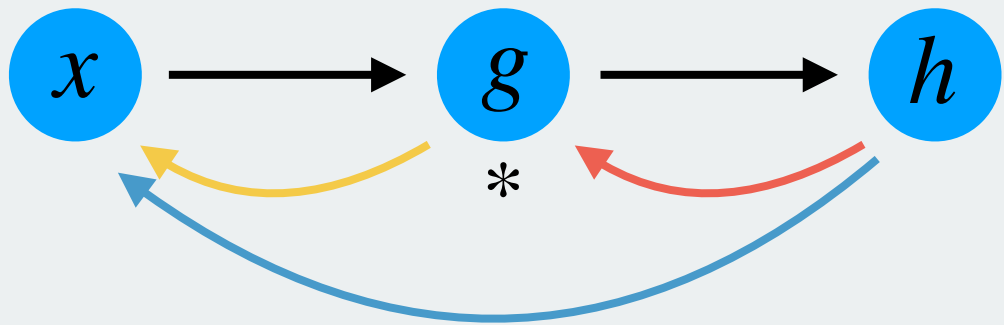


Computational graph

Backward pass









$h(g(x))$



Chain rule says:

$$\frac{dh}{dx} = \frac{dh}{dg} \frac{dg}{dx}$$

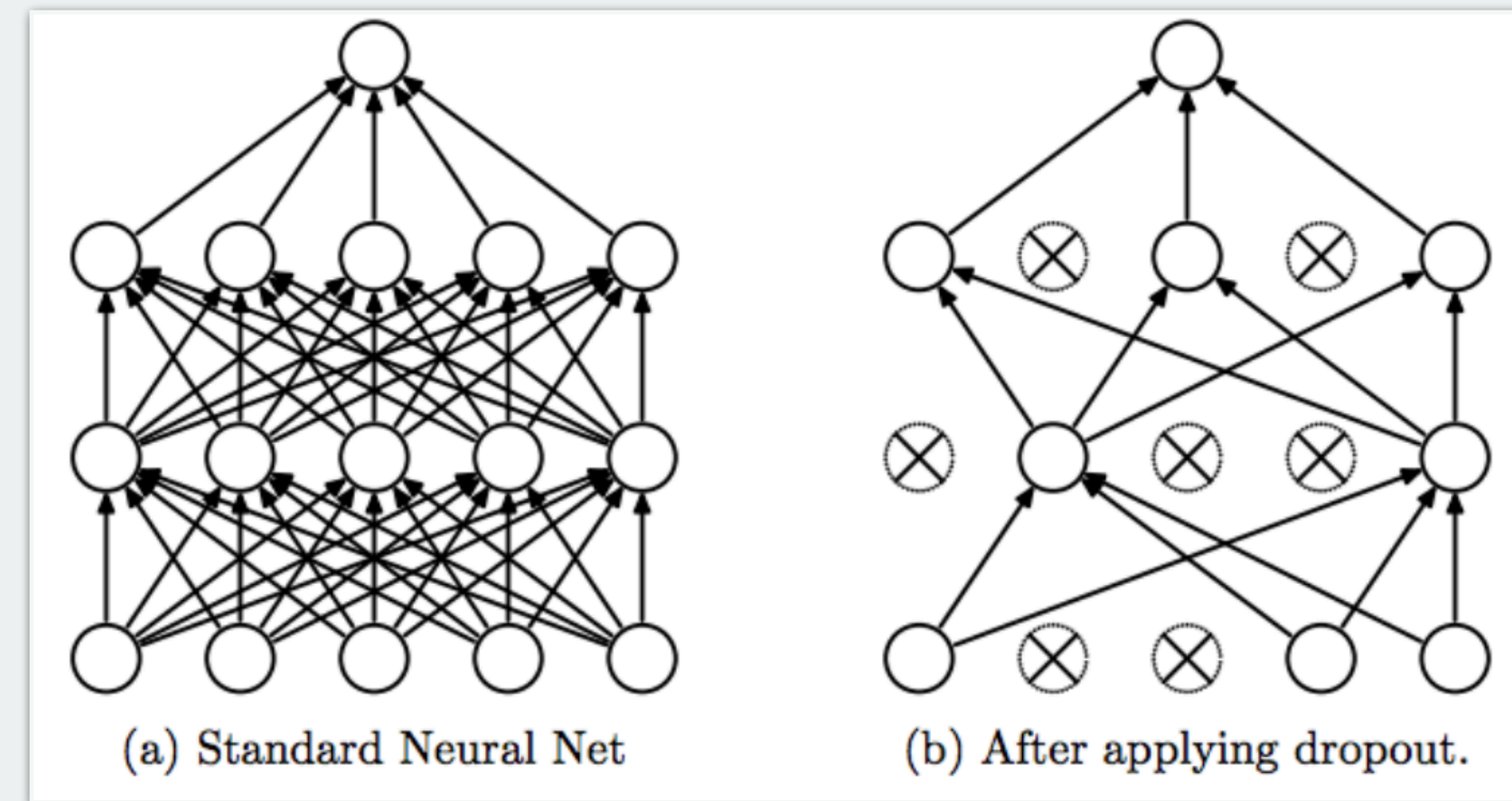
Quick recap...

							Average over all training data ...
w_0	-0.08	+0.02	-0.02	+0.11	-0.05	-0.14	... → -0.08
w_1	-0.11	+0.11	+0.07	+0.02	+0.09	+0.05	...
w_2	-0.07	-0.04	-0.01	+0.02	+0.13	-0.15	...
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
$w_{13,001}$	+0.13	+0.08	-0.06	-0.09	-0.02	+0.04	...

Quick recap...

Dropout:

“In each SGD step, randomly ignore a fraction p of neurons”



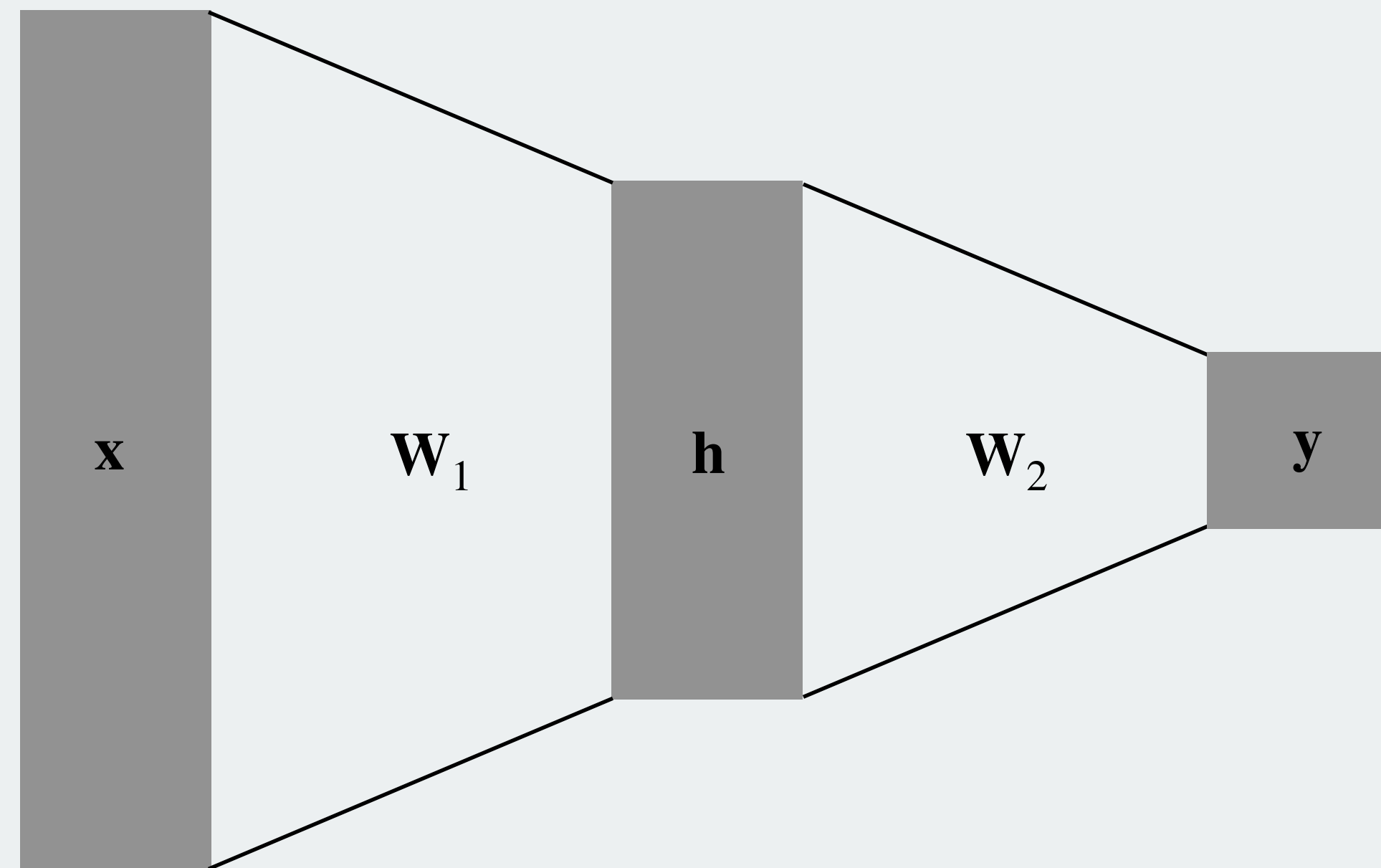
Srivastava, Nitish, et al. "Dropout: a simple way to prevent neural networks from overfitting", JMLR 2014

- Can select p in wide range. Typical is 0.2 – 0.8, dependent on size of ANN
- Can apply only in specific layers. It is typical to only do dropout in a designated “dropout layer” somewhere close to output.

Convolutional Neural Networks

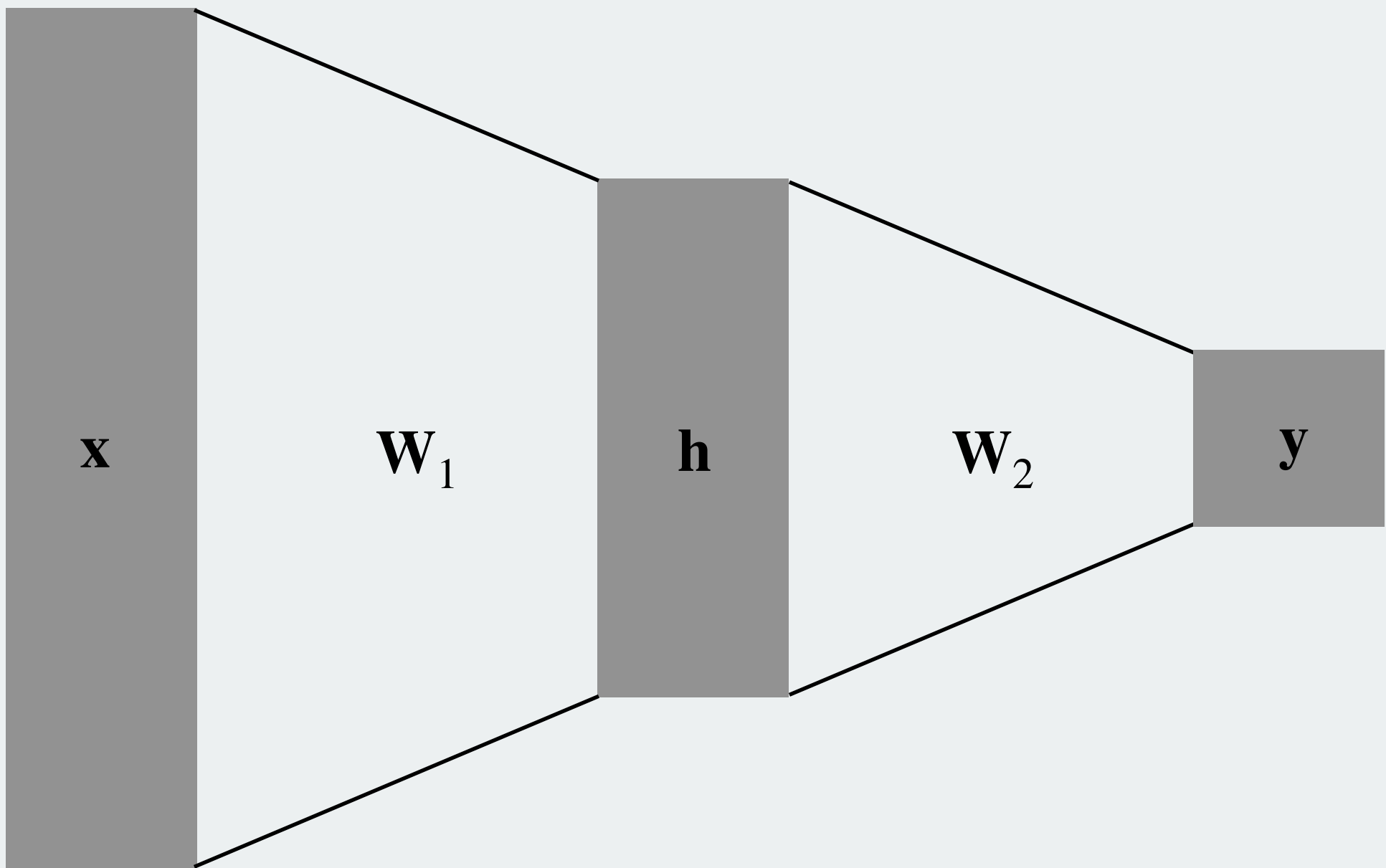
THE neural network architecture to use for image data

The problem with vanilla neural networks

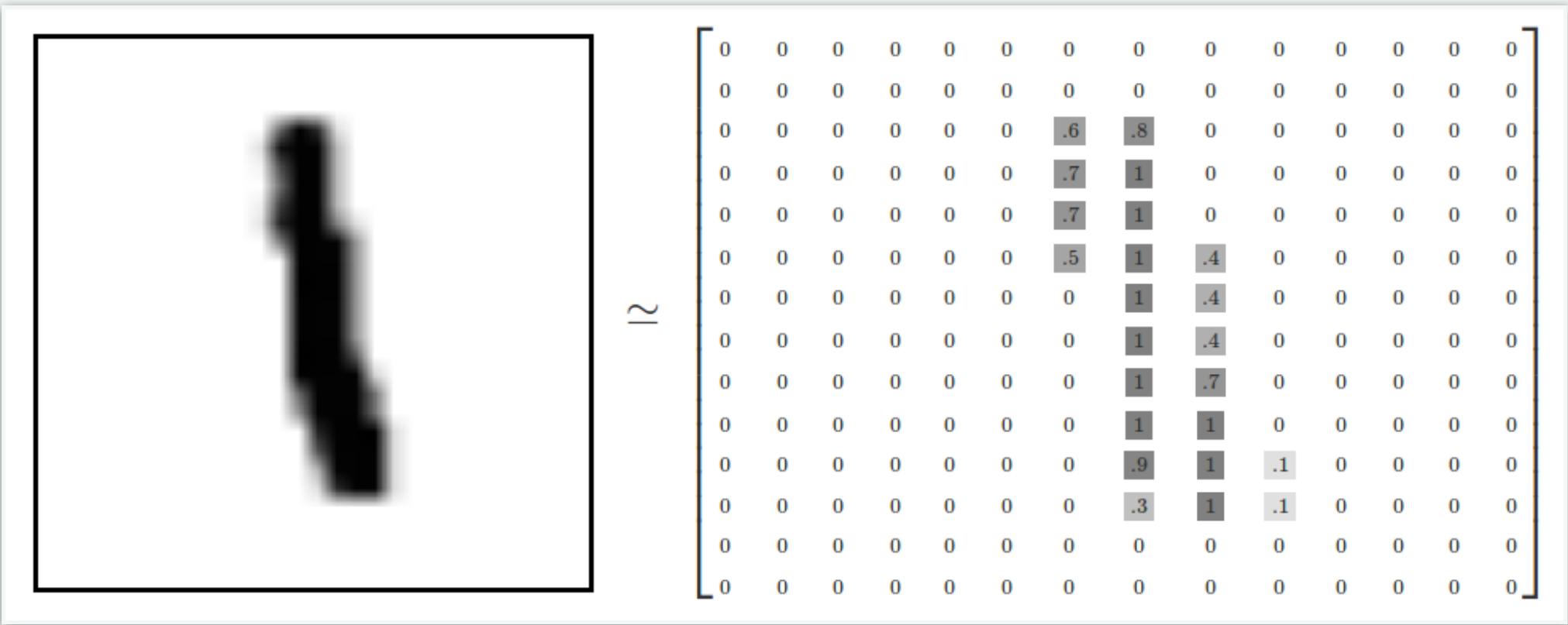


- Single operation on whole input
- Each neuron reacts to specific inputs

The problem with vanilla neural networks

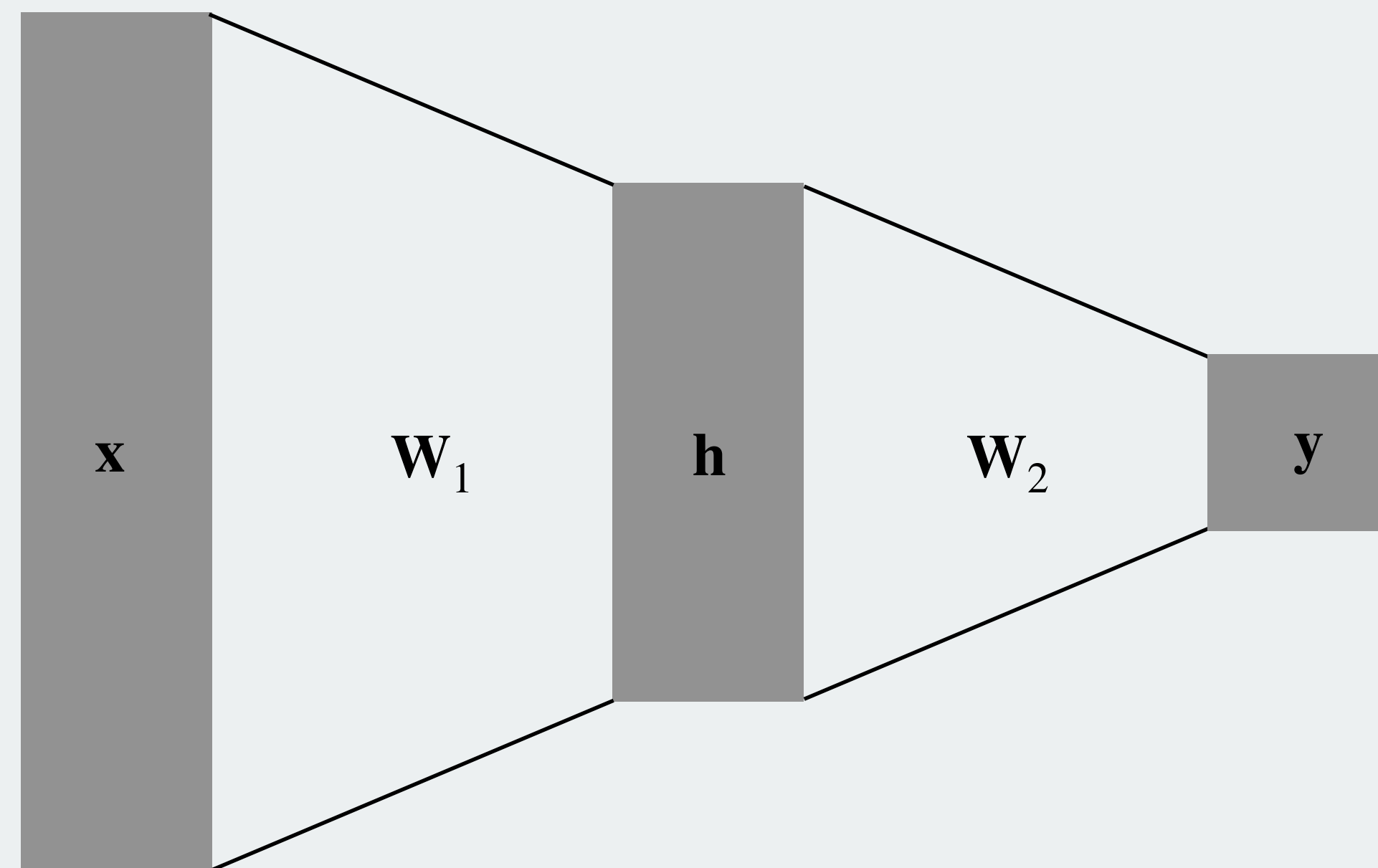


- Single operation on whole input
- Each neuron reacts to specific inputs
- Bad for images: objects move around
- No attention to spatial adjacency



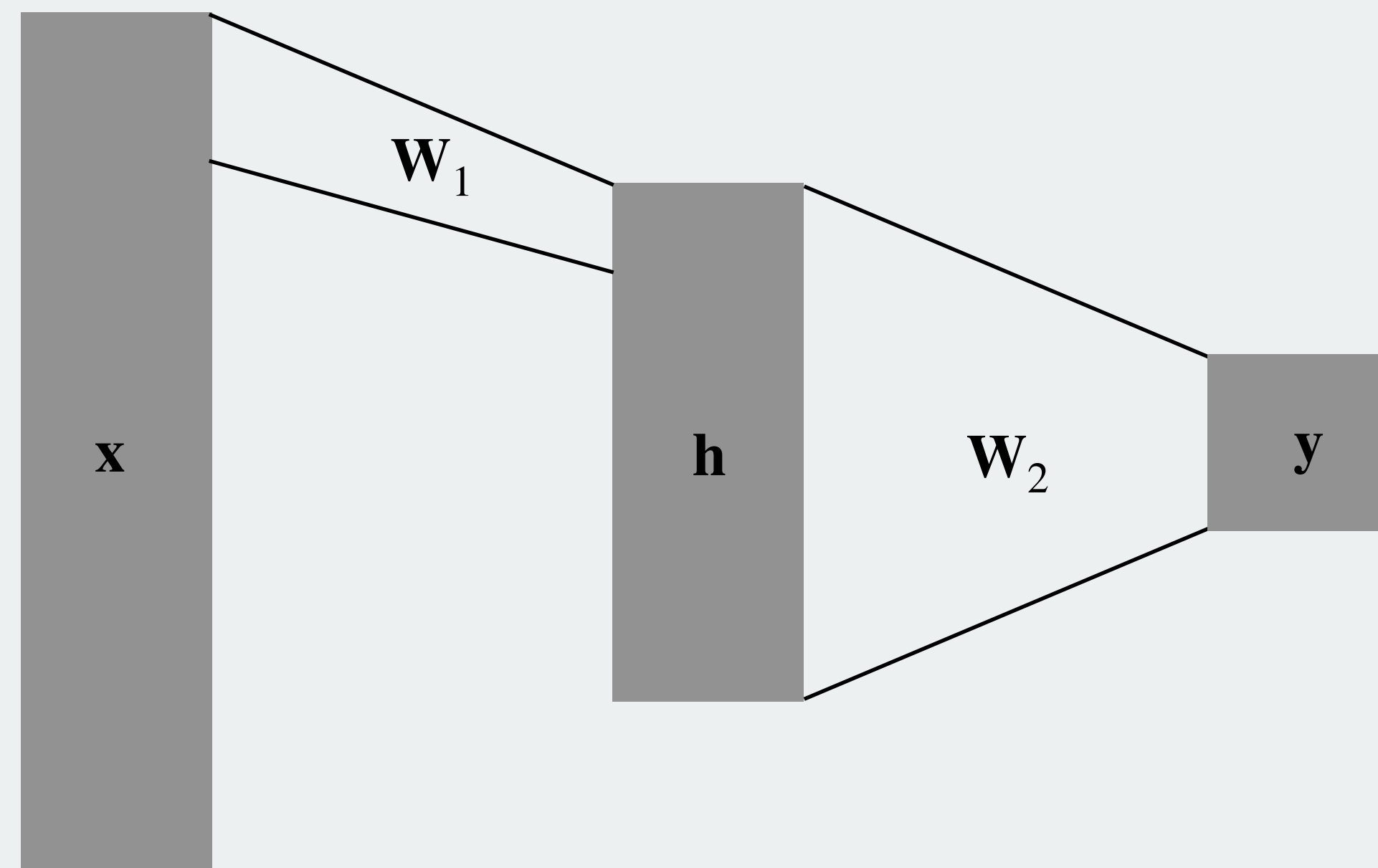
The problem with vanilla neural networks

> Solution: “slide” the weight matrix over the input



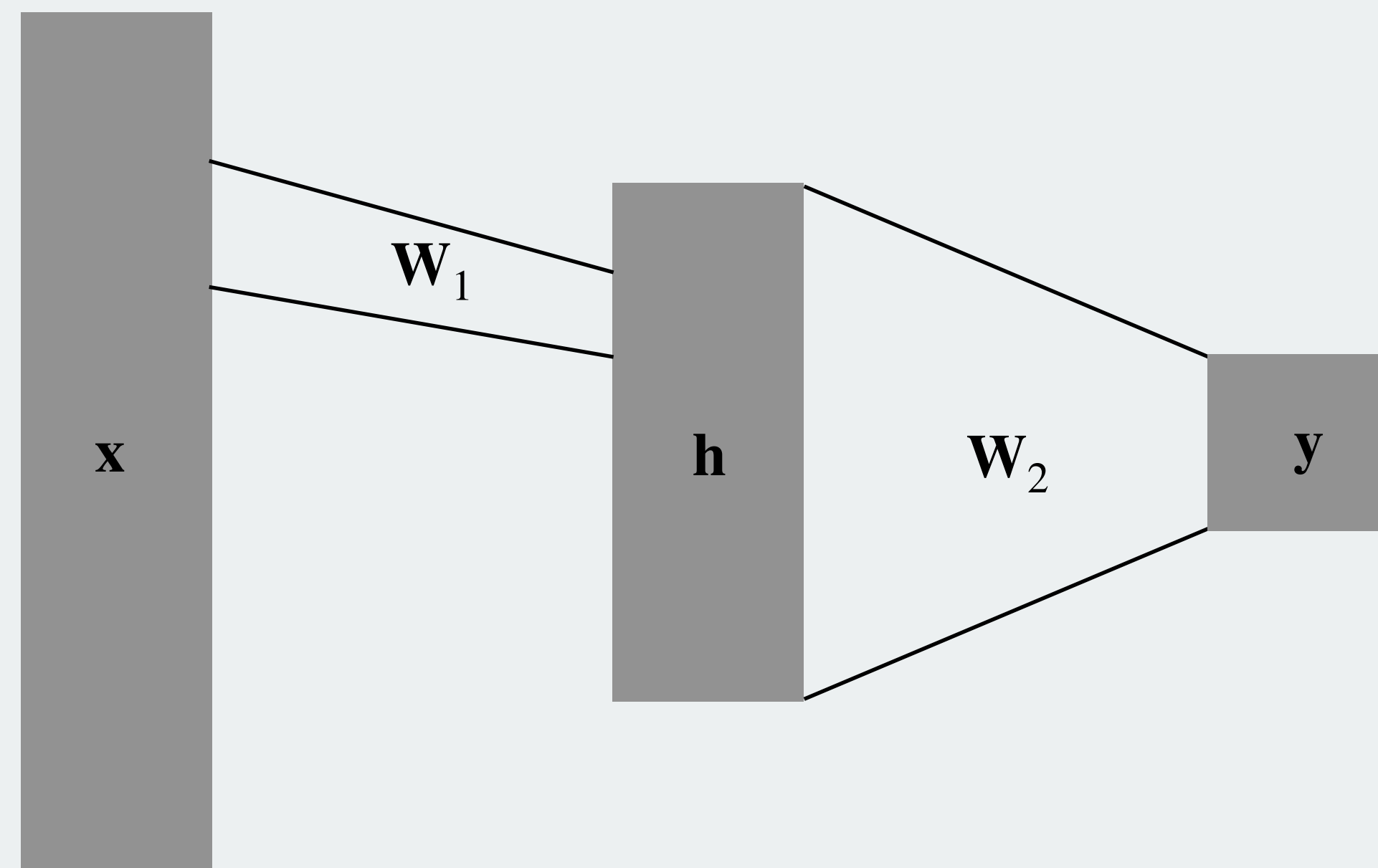
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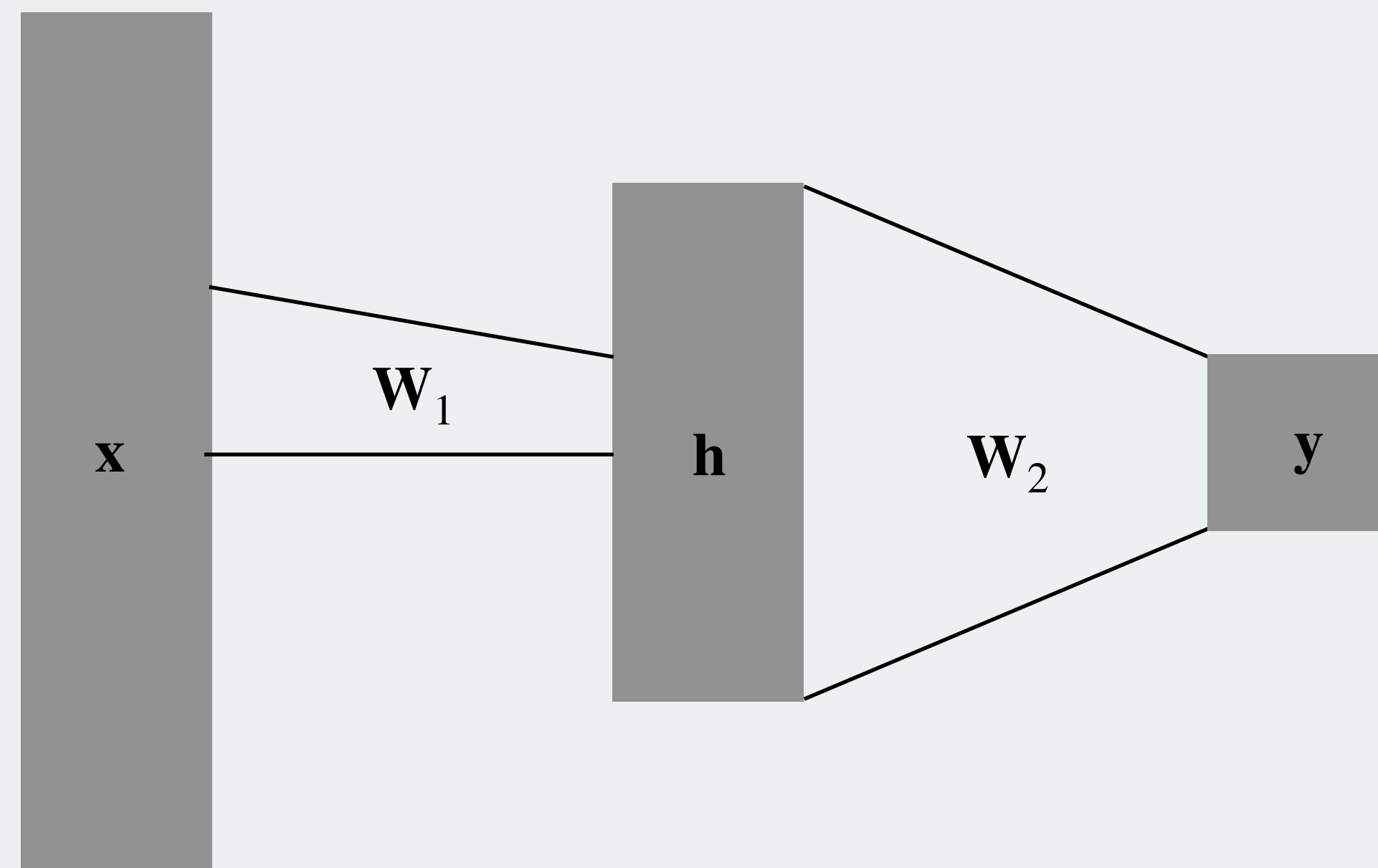
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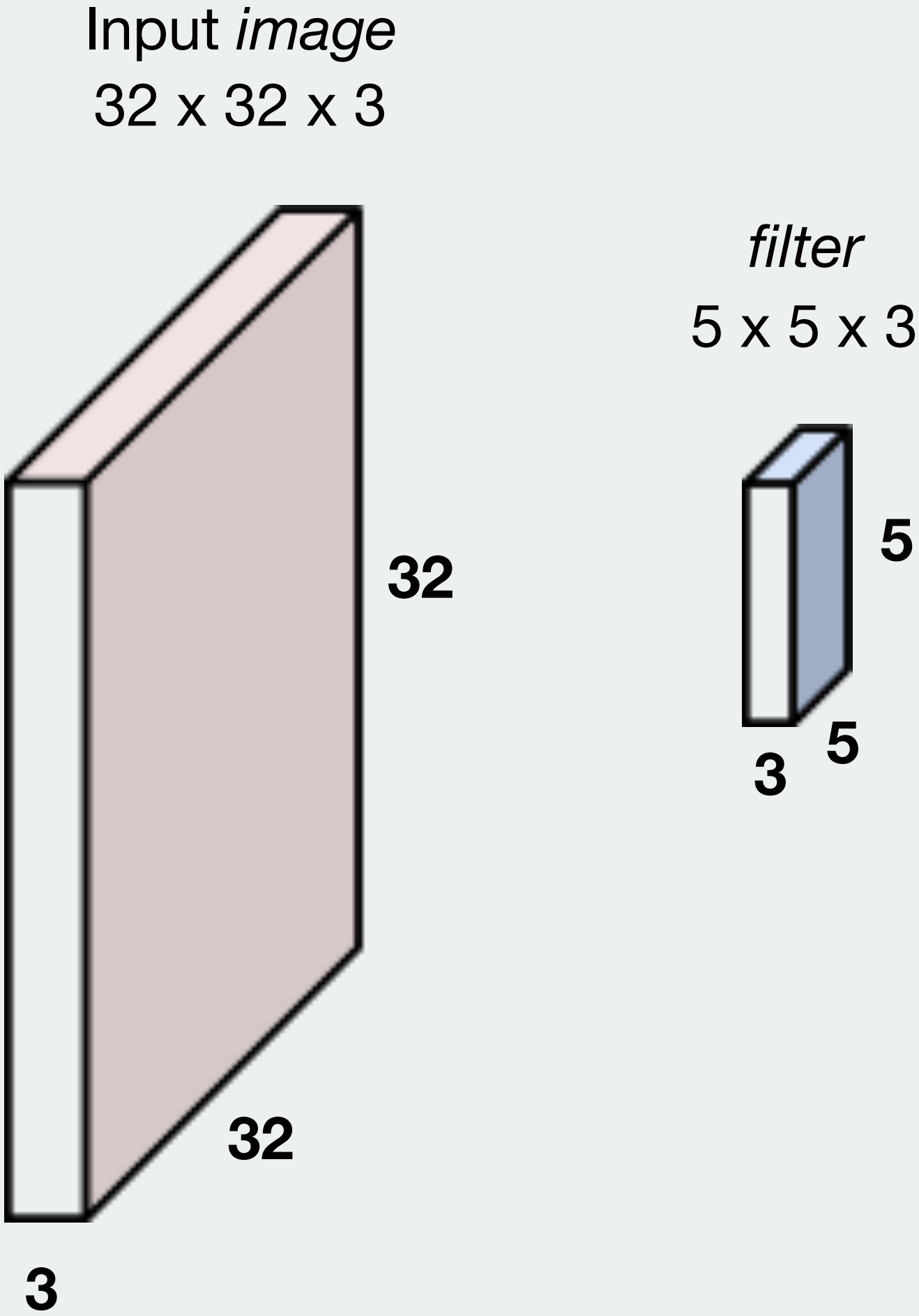


The problem with vanilla neural networks

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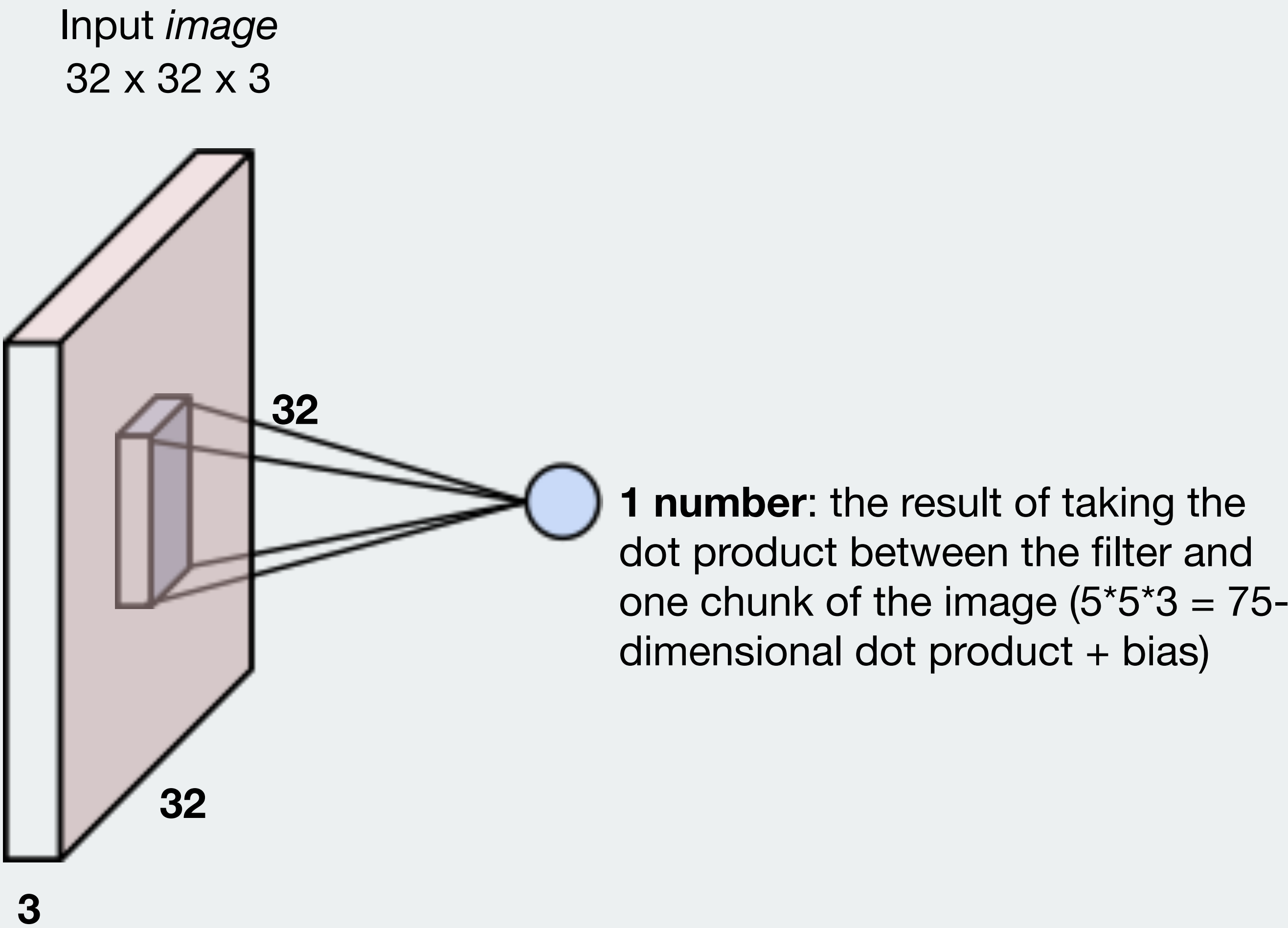


Convolutional neural networks



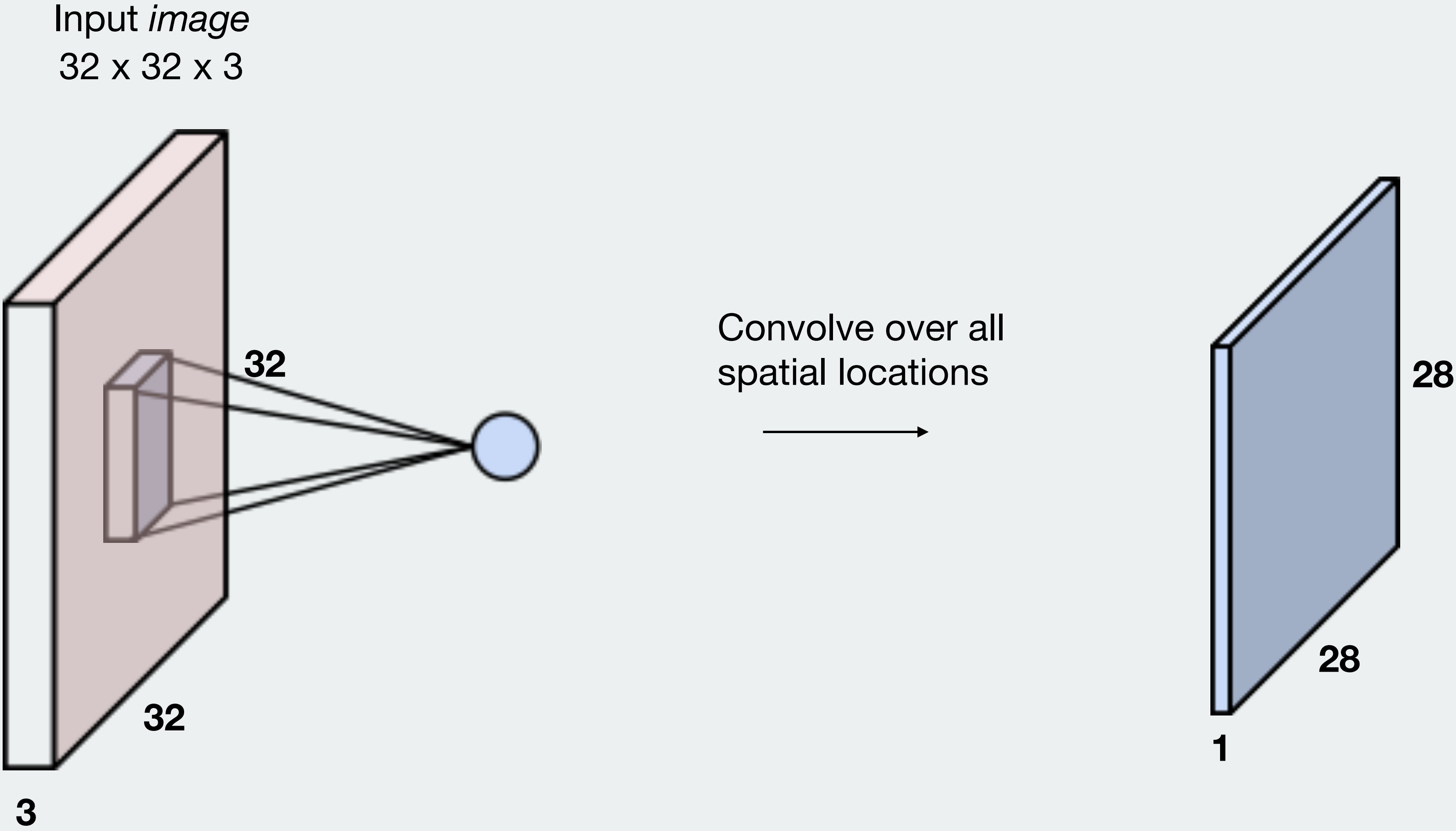
Convolutional neural networks

> Convolve the filter across the input image to computing dot products



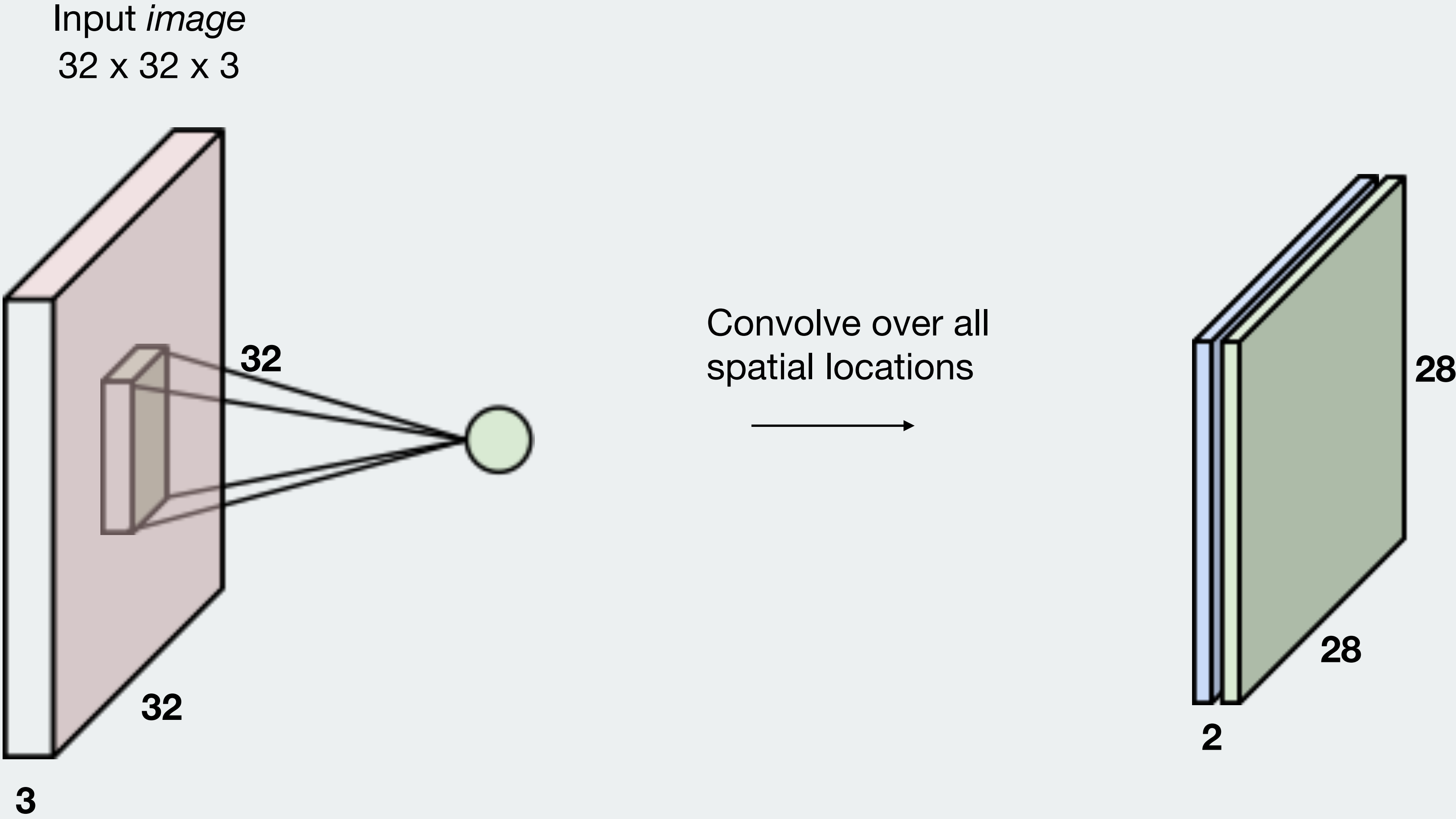
Convolutional neural networks

> Convolution by 1 filter produces new *activation map* of depth 1



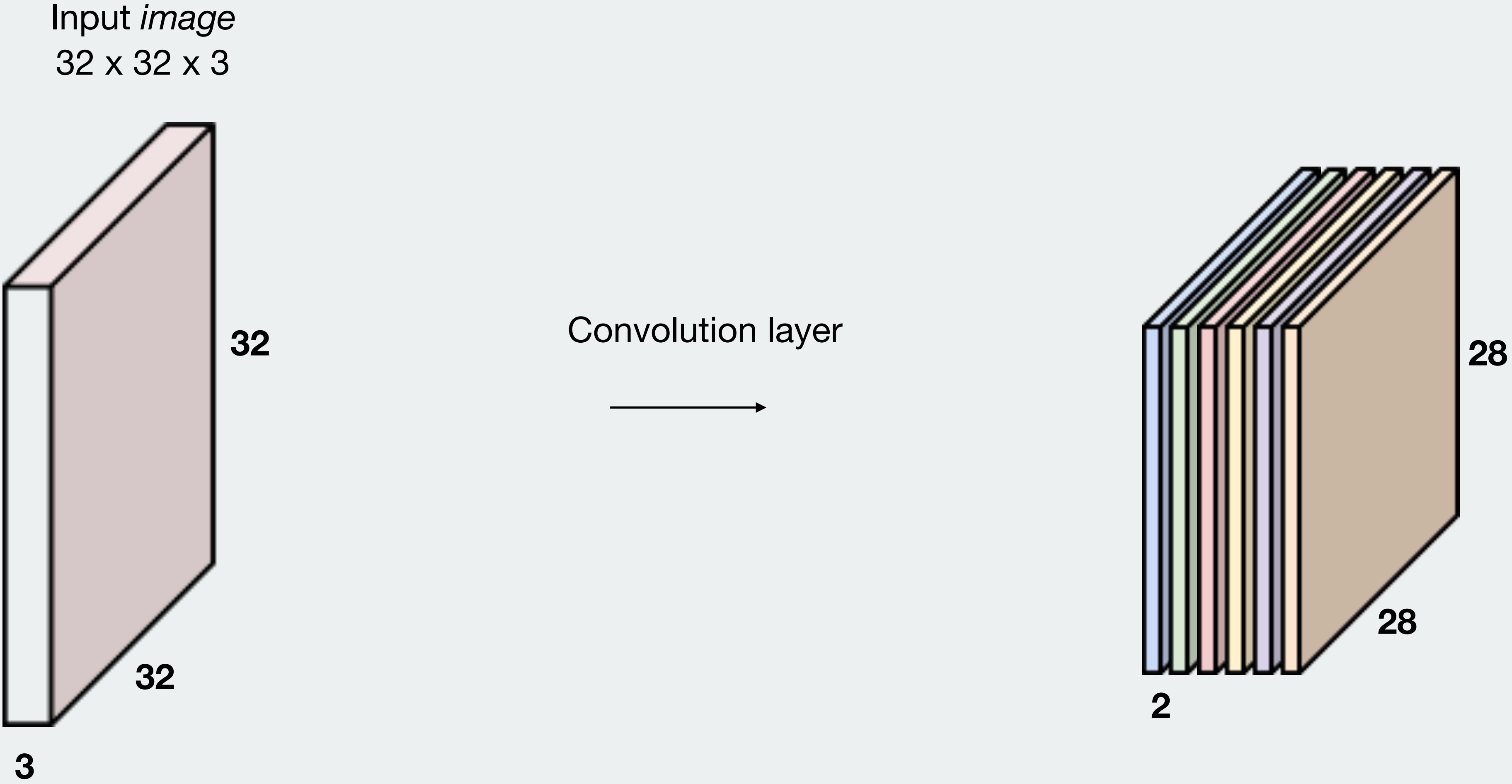
Convolutional neural networks

> Convolution by 2 filters produces new *activation map* of depth 2



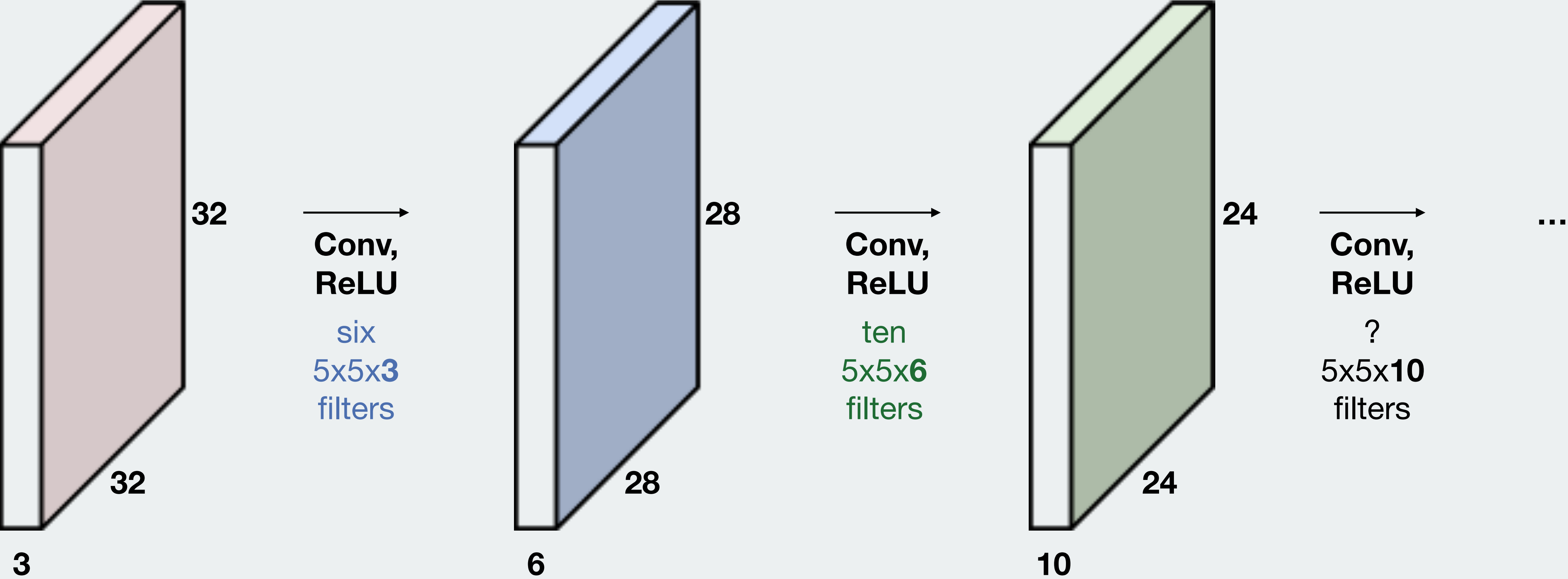
Convolutional neural networks

> Convolution by n filters produces new *activation map* of depth n



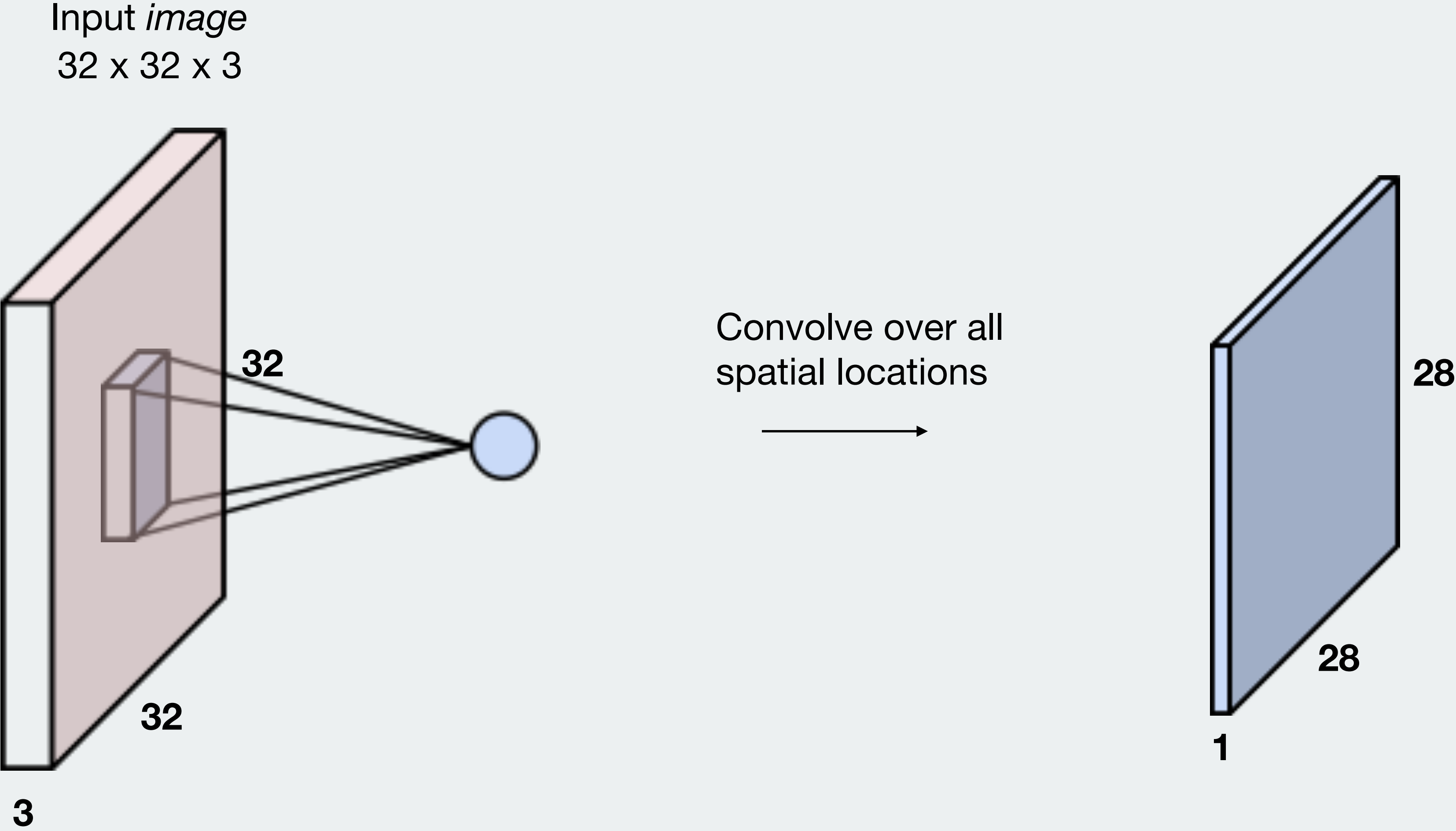
Convolutional neural networks

> Stack these operations



Convolutional neural networks

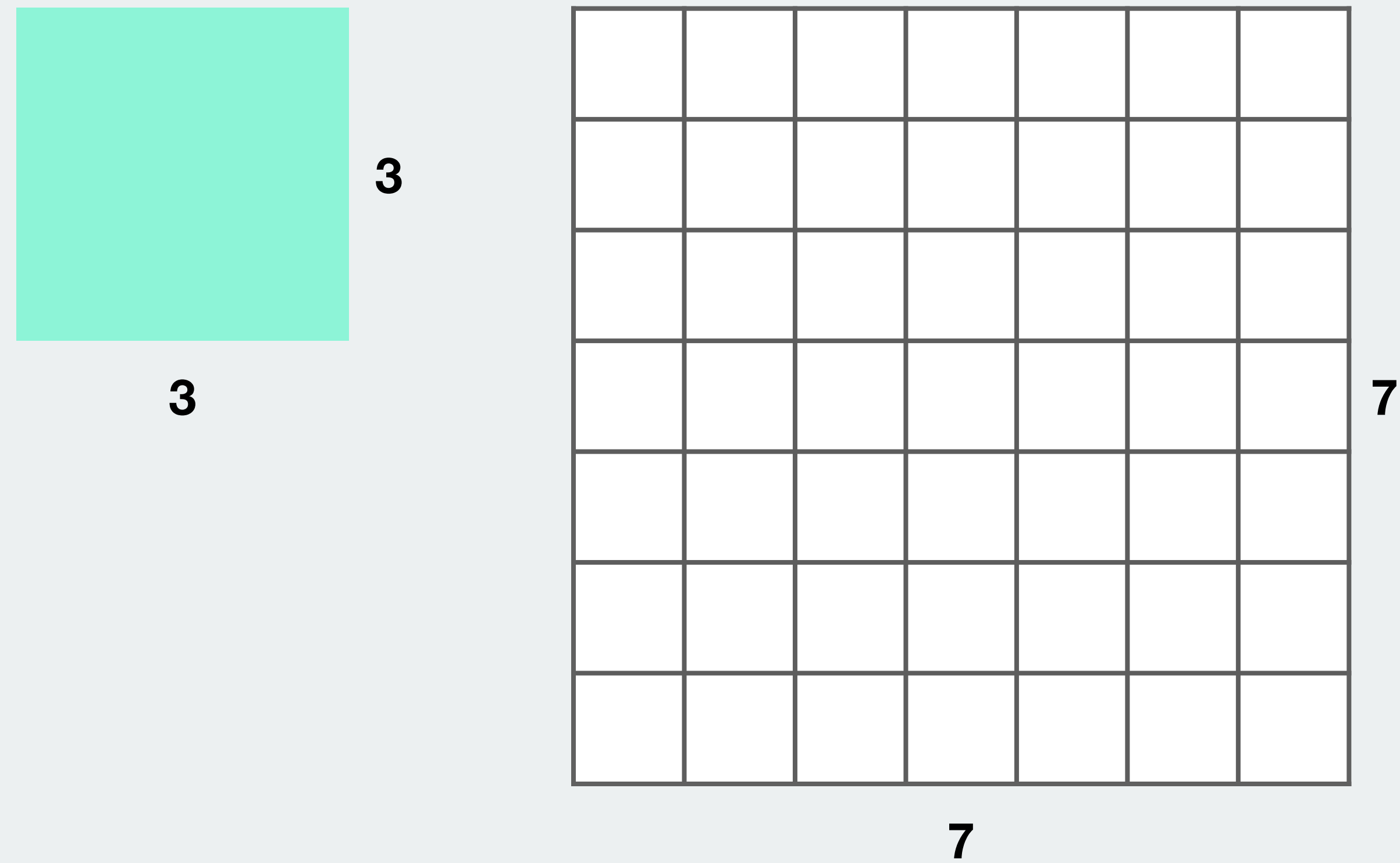
> Dimensions



Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter



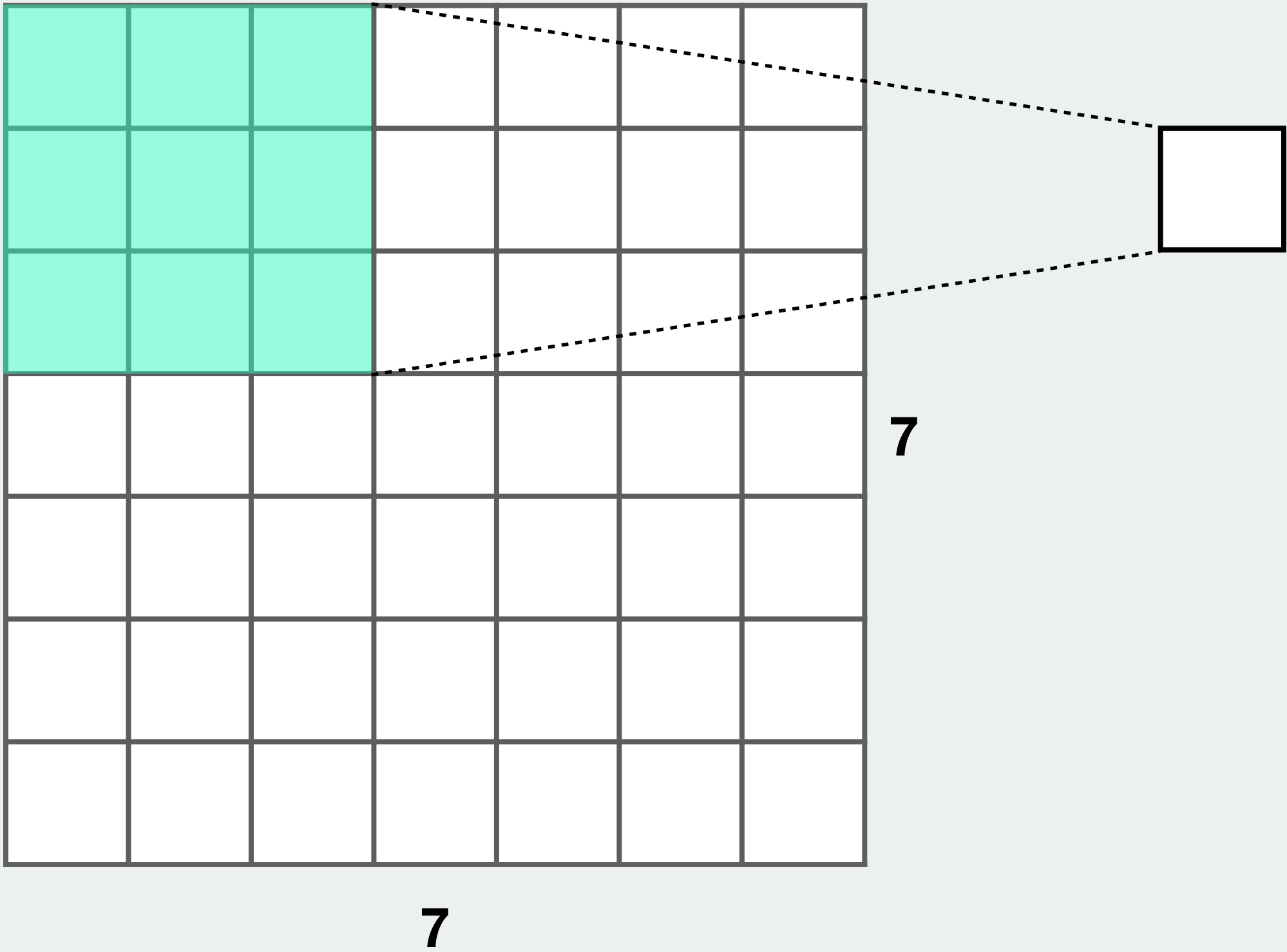
Question: What is the dimensions of the resulting activation map?

Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: What is the
dimensions of the resulting
activation map?

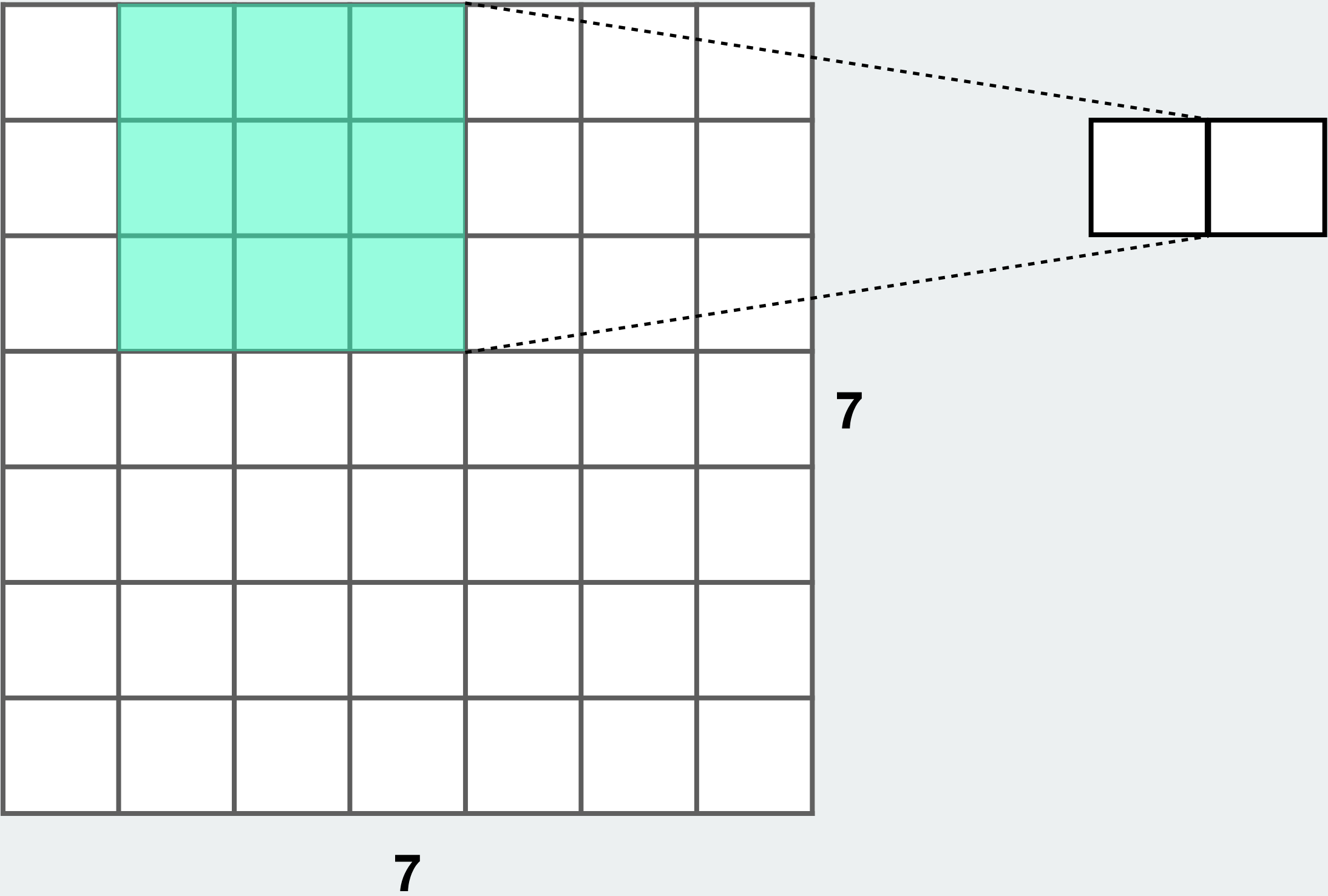


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: What is the
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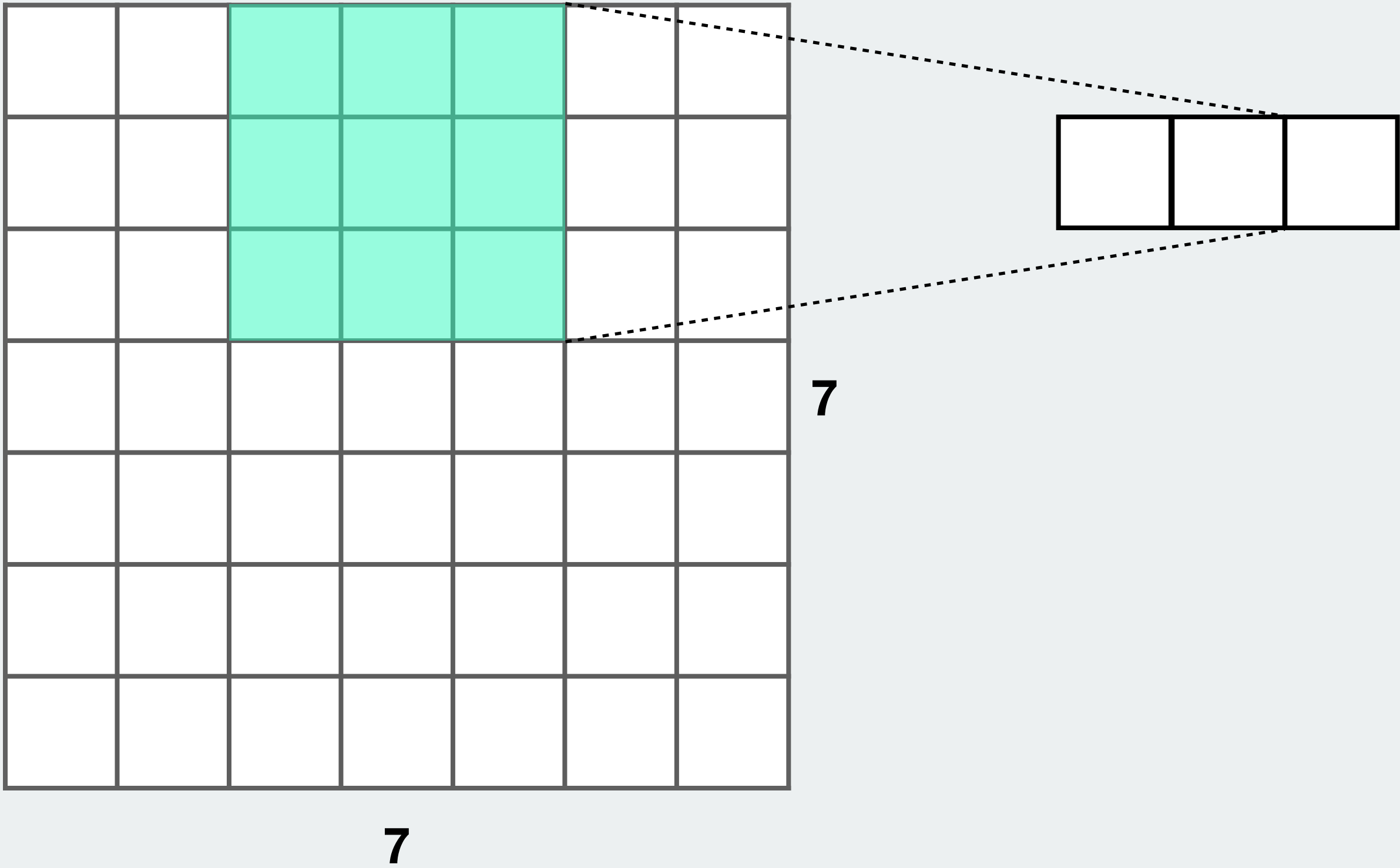


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
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Question: What is the
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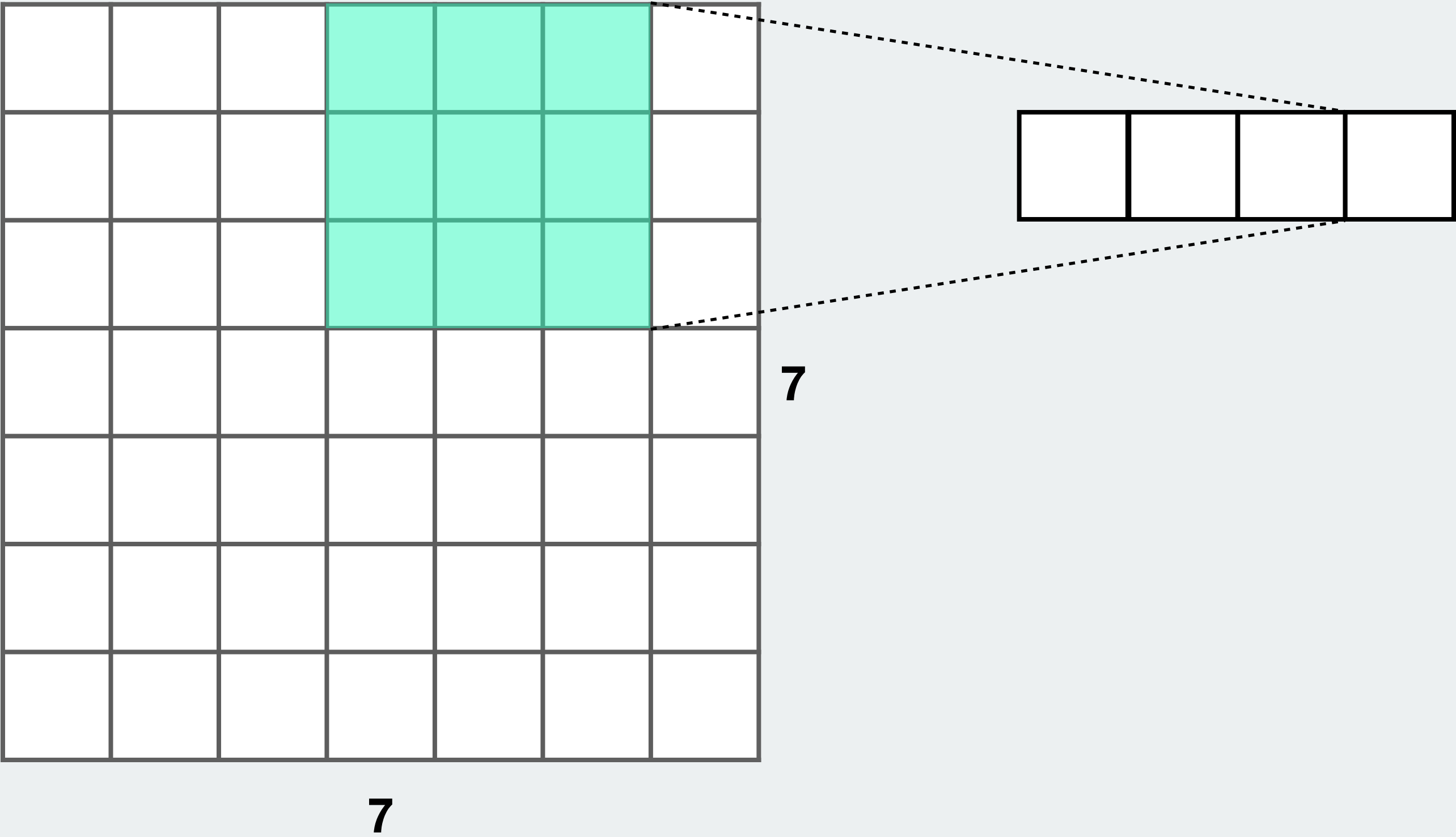


Convolutional neural networks

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Example: 7 x 7 input
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Question: What is the
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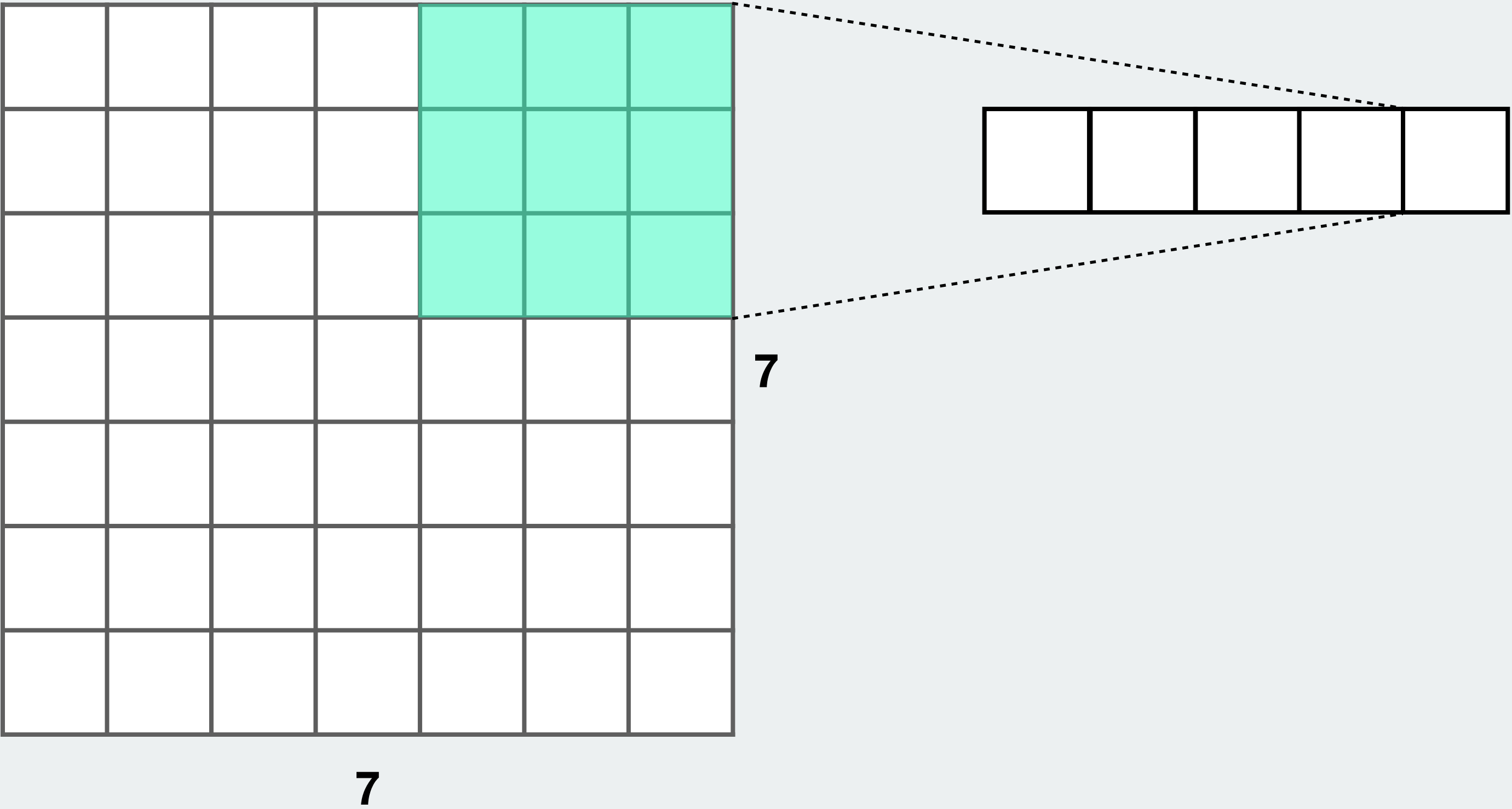


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
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Question: What is the
dimensions of the resulting
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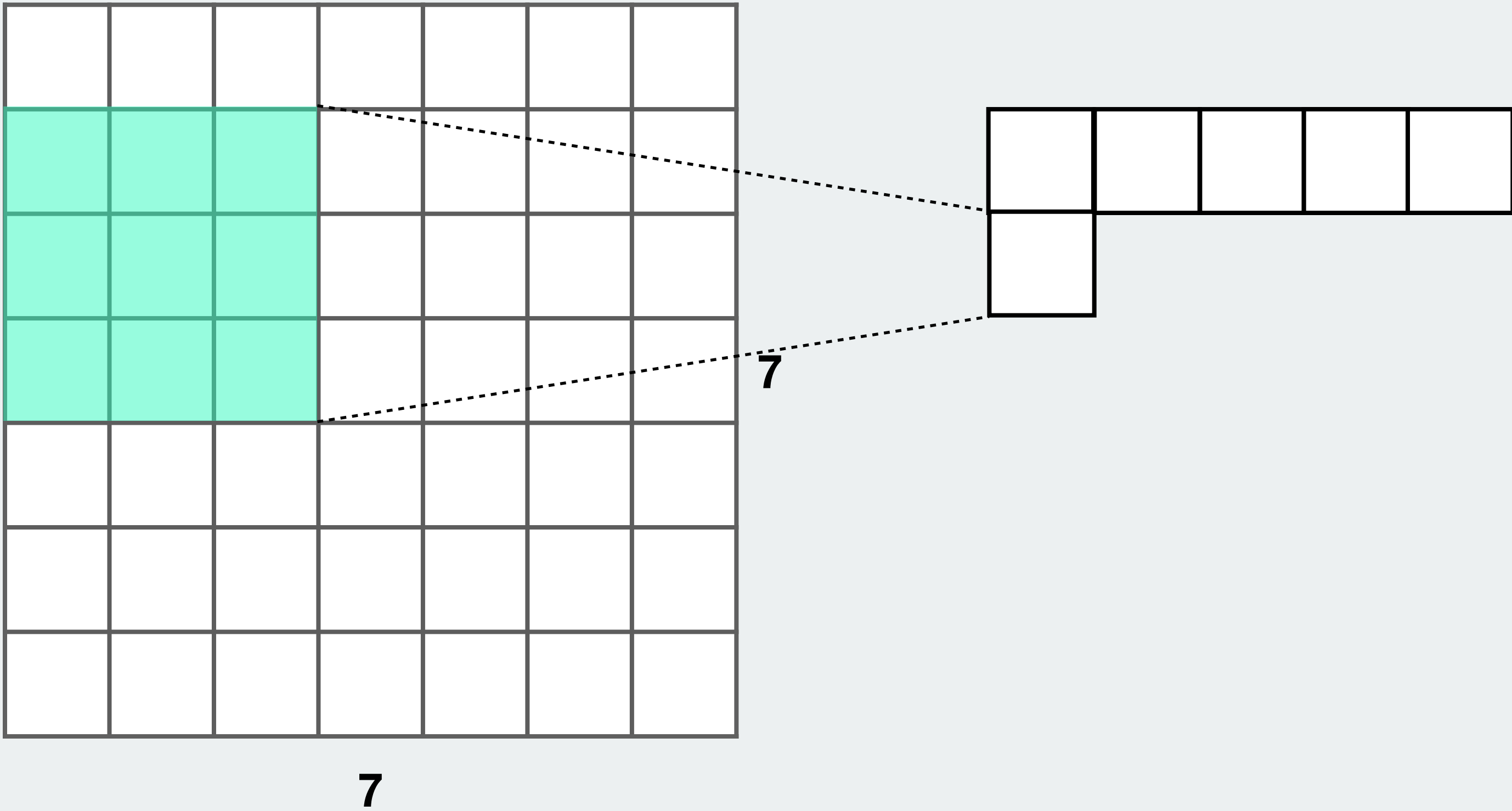


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: What is the
dimensions of the resulting
activation map?

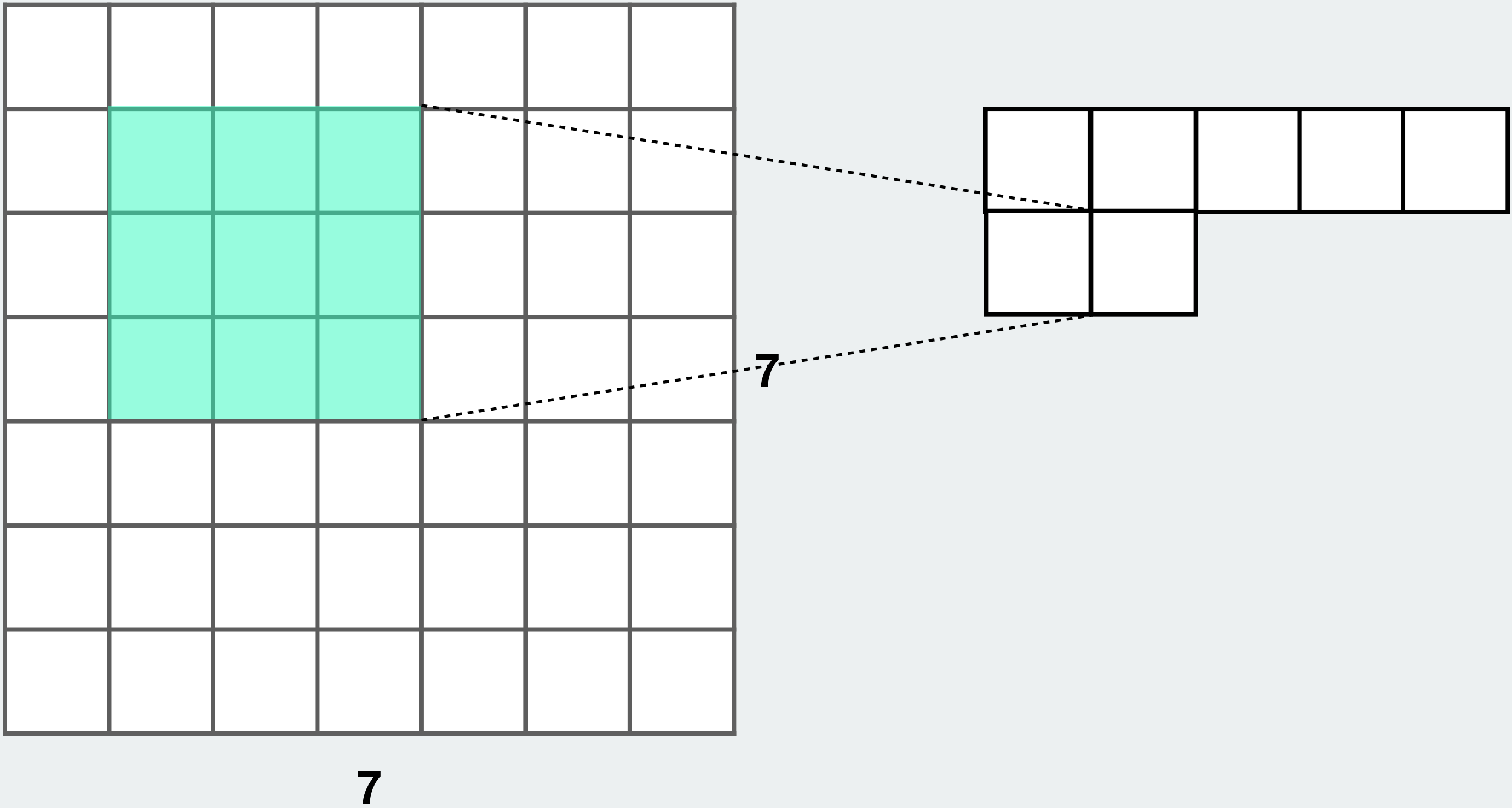


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: What is the
dimensions of the resulting
activation map?



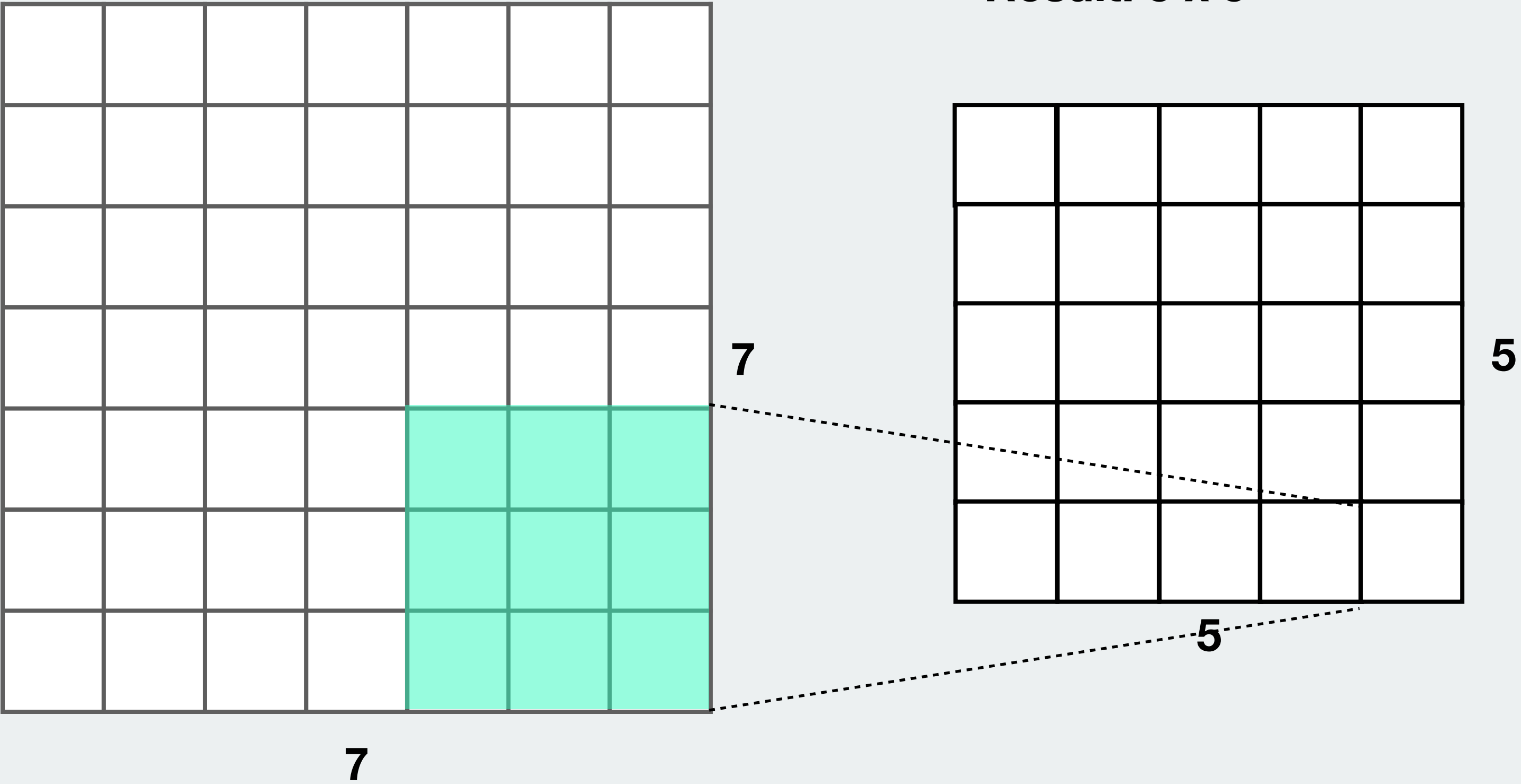
Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: What is the dimensions of the resulting activation map?

Result: 5 x 5

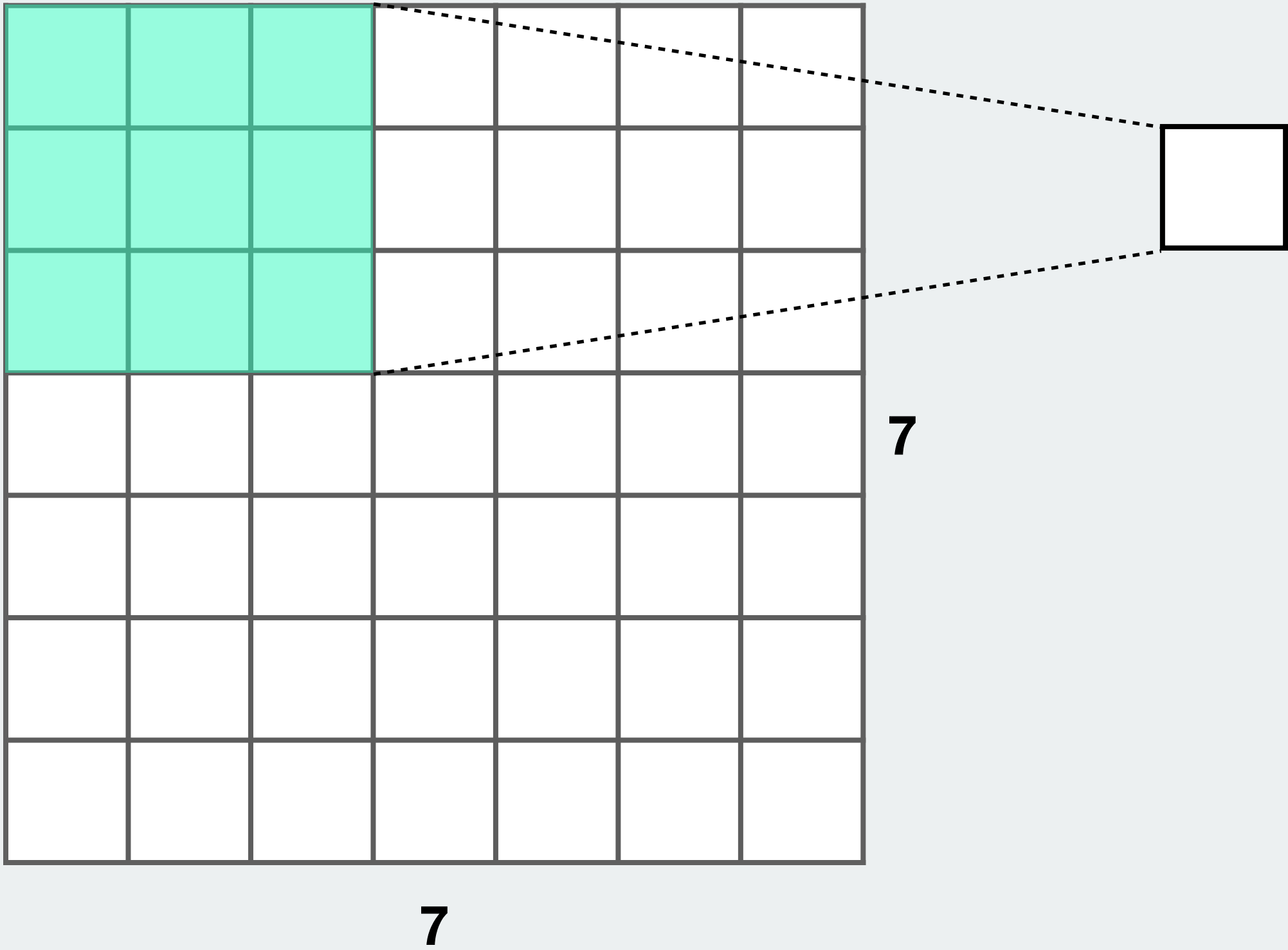


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: What if we use
stride 2?

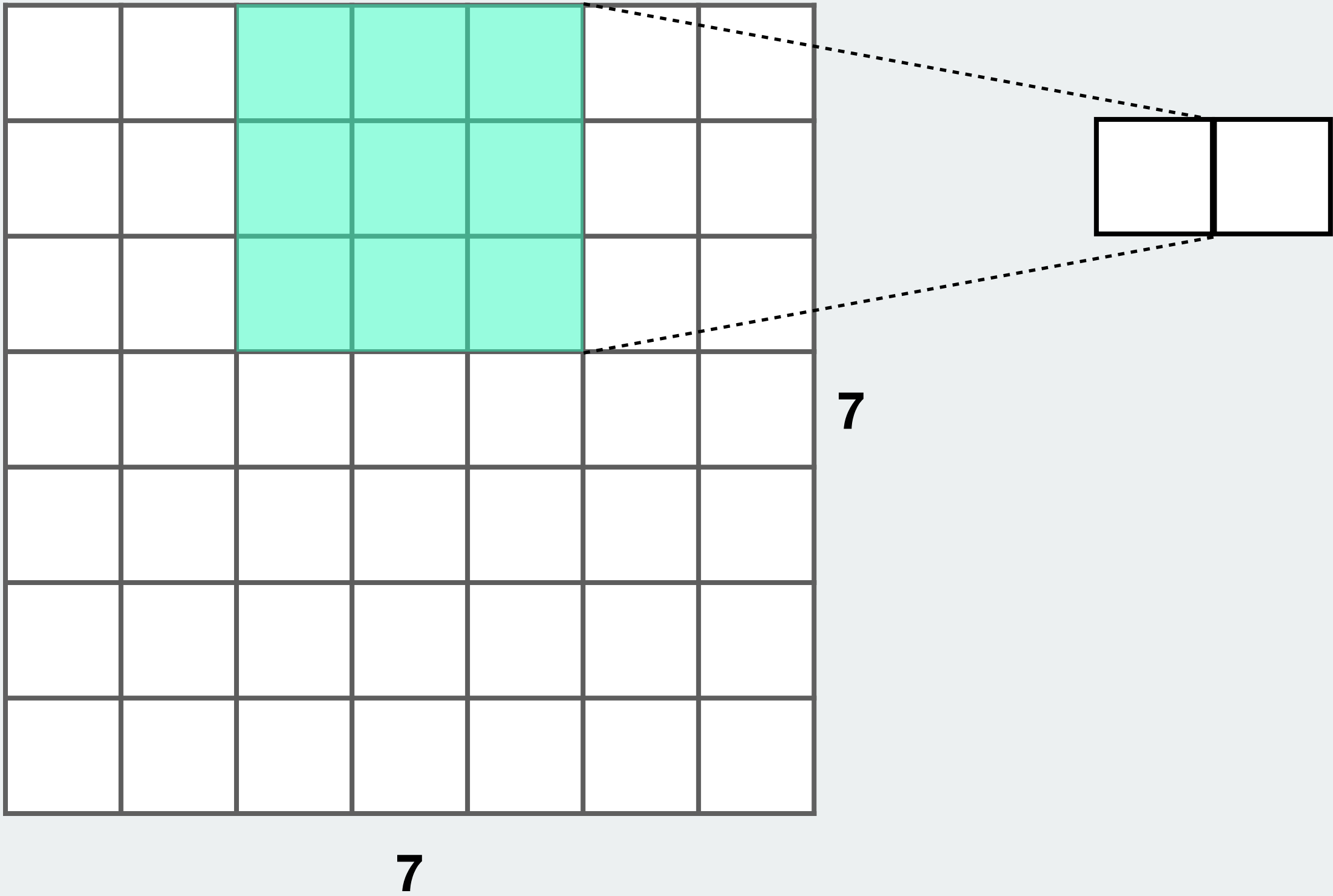


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: What if we use
stride 2?



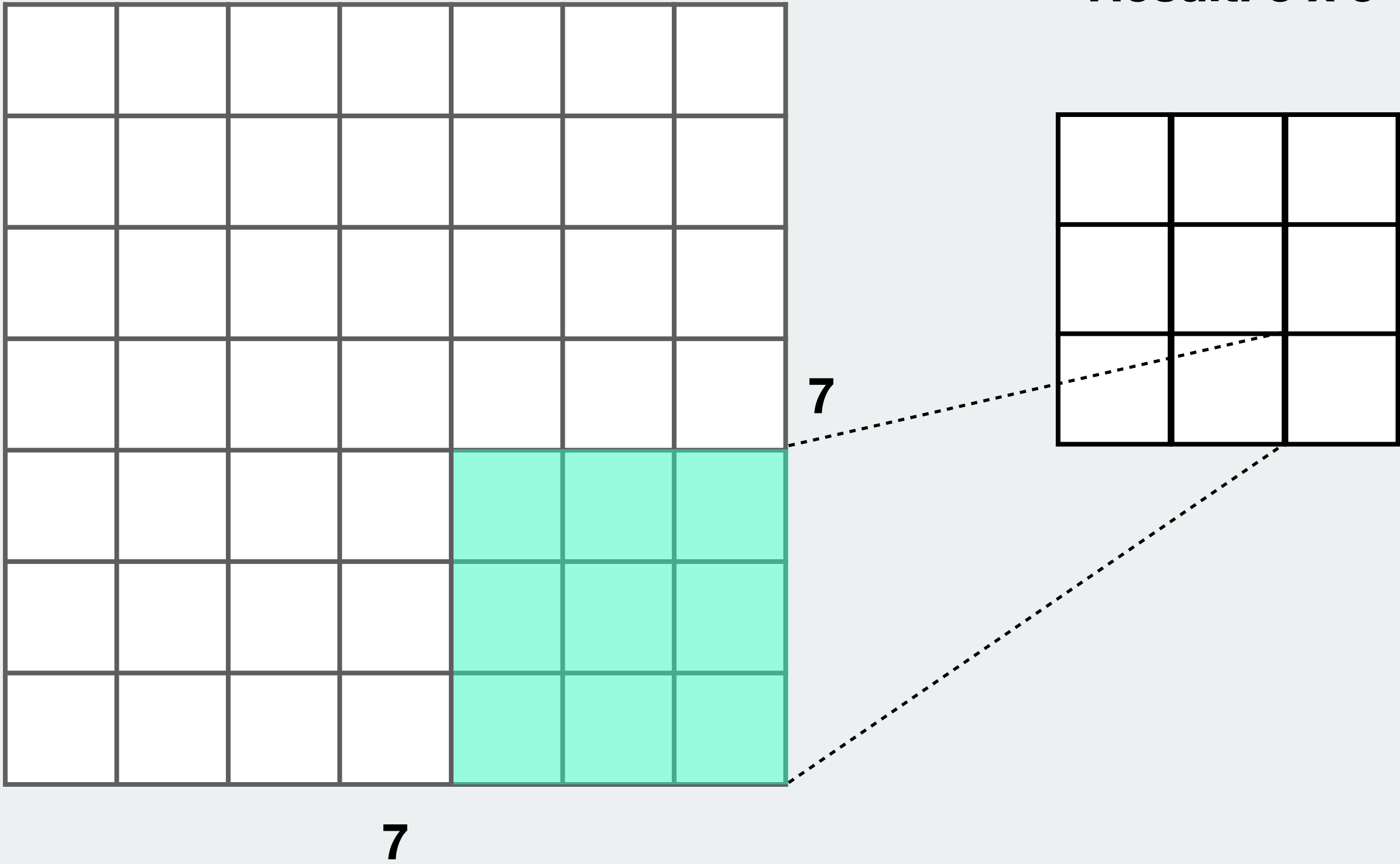
Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: What if we use
stride 2?

Result: 3 x 3

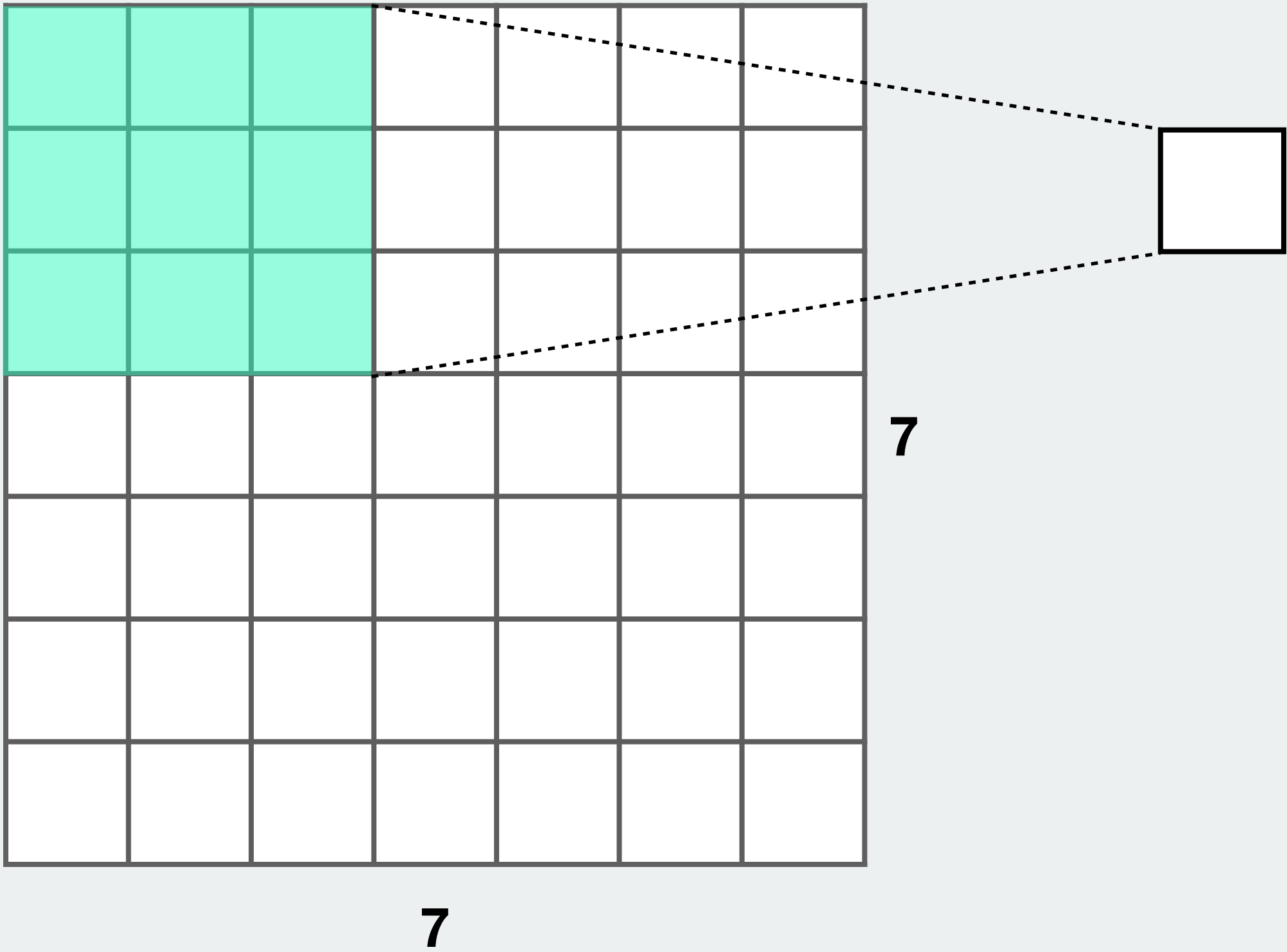


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: Stride 3?

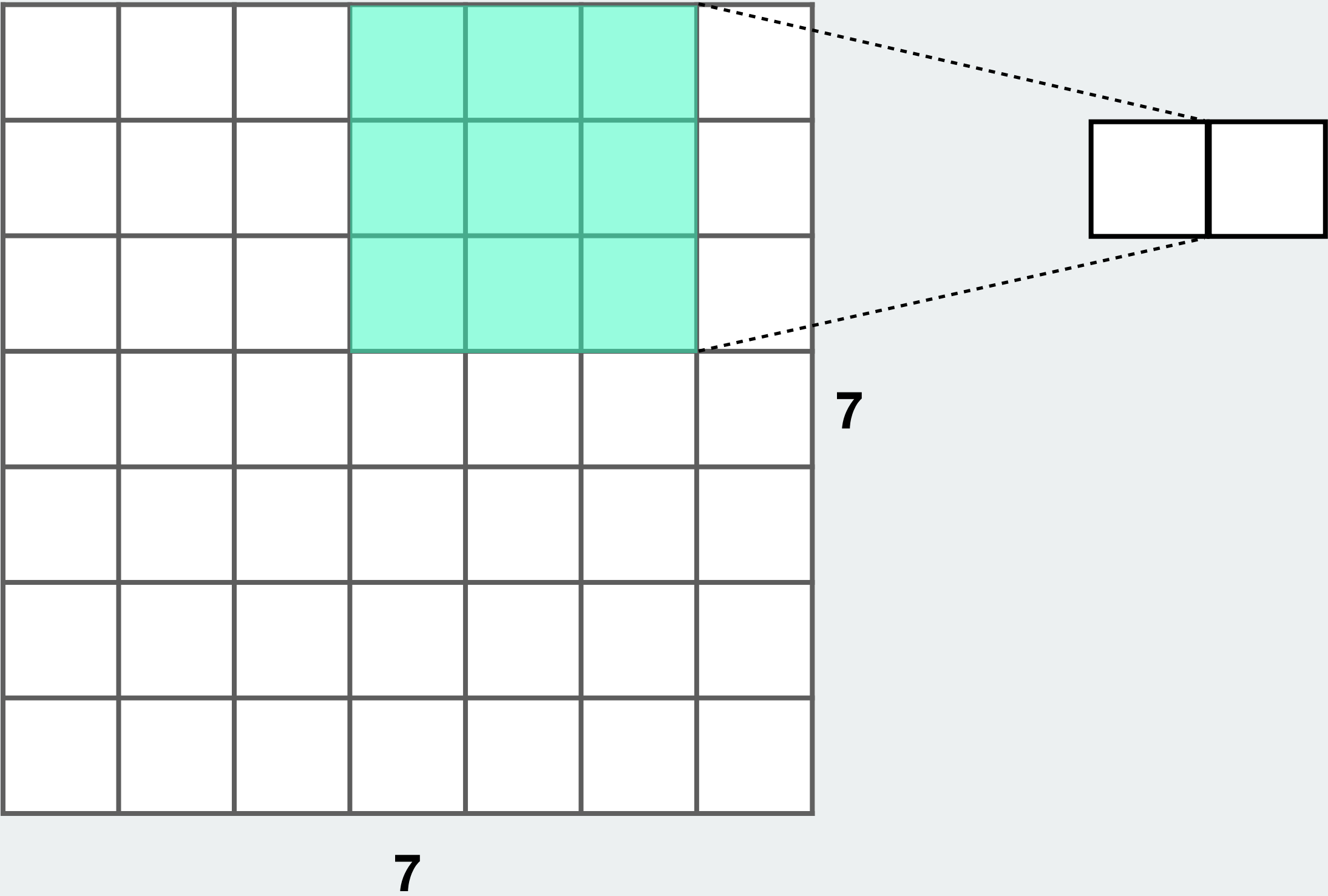


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: Stride 3?

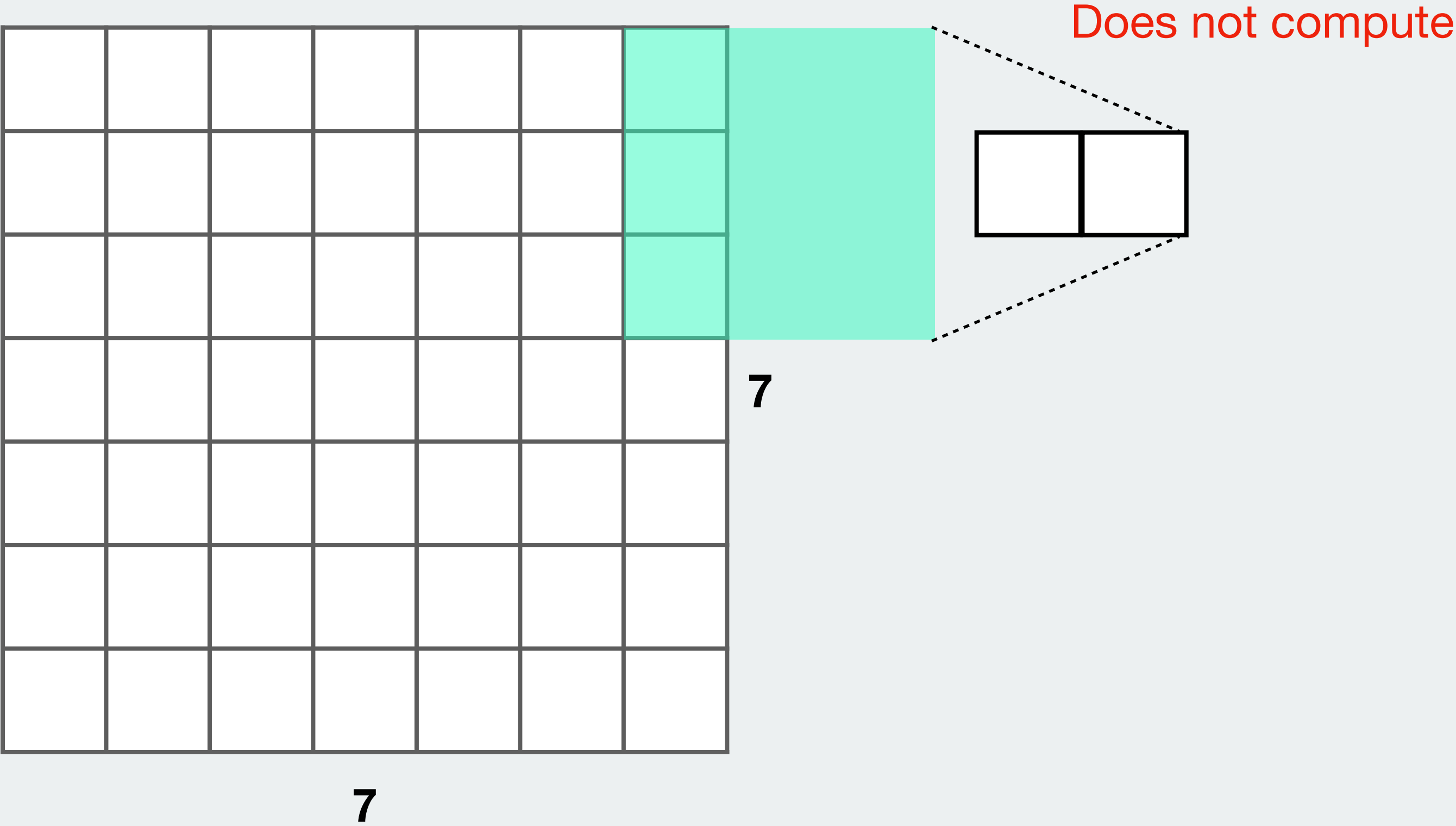


Convolutional neural networks

> Dimensions

Example: 7 x 7 input
3 x 3 filter

Question: Stride 3?

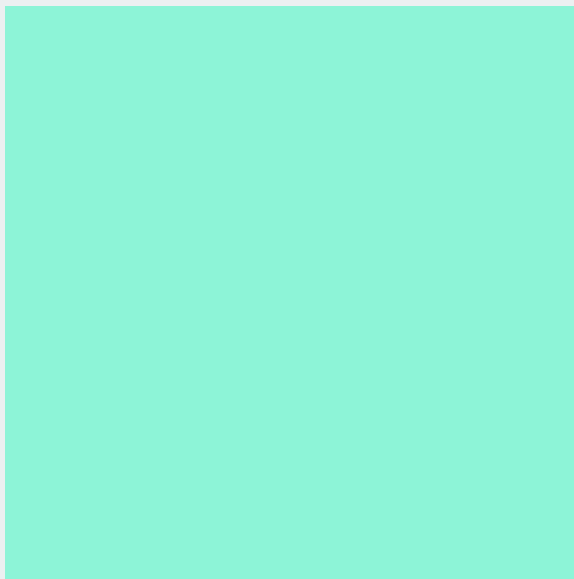


Convolutional neural networks

> Dimensions

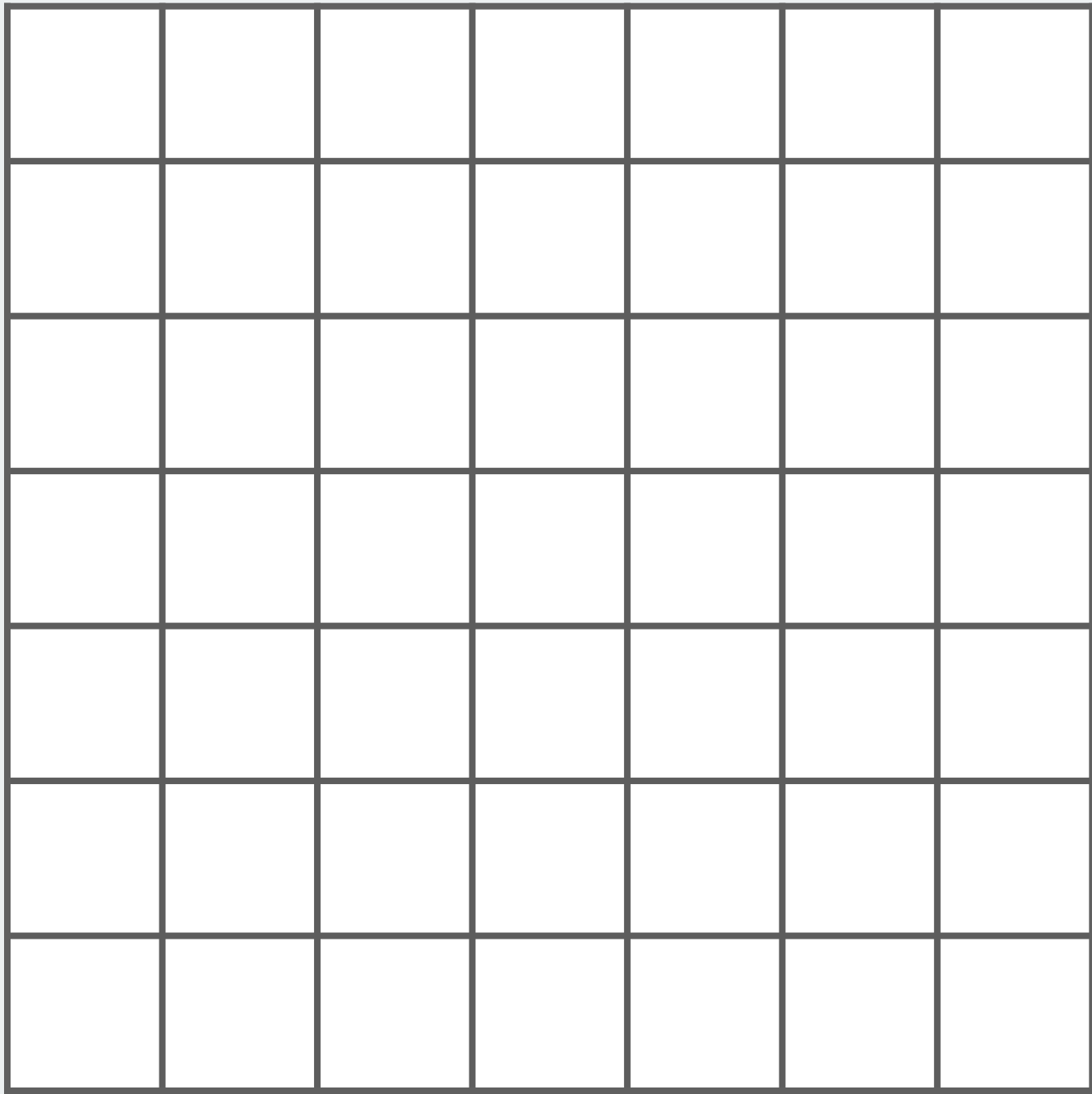
Problem: The image *shrinks*

$7 \times 7 \Rightarrow 5 \times 5$



3

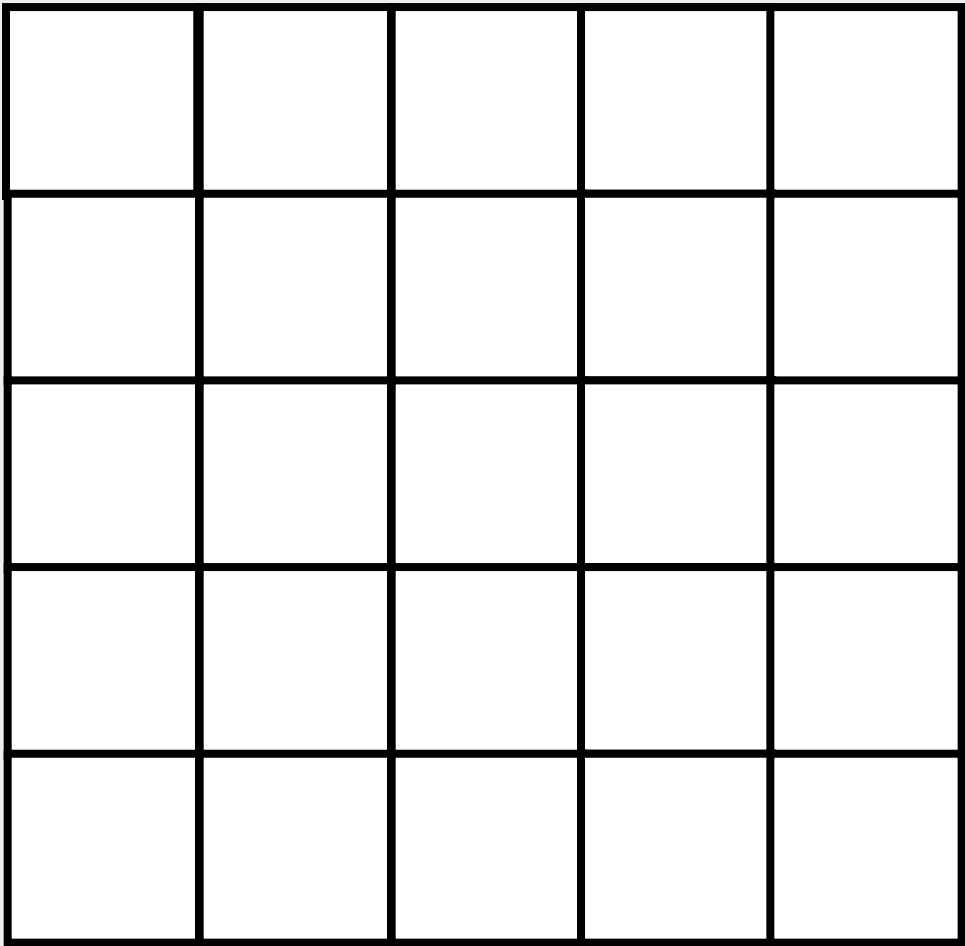
3



7

7

Convolution
→



5

5

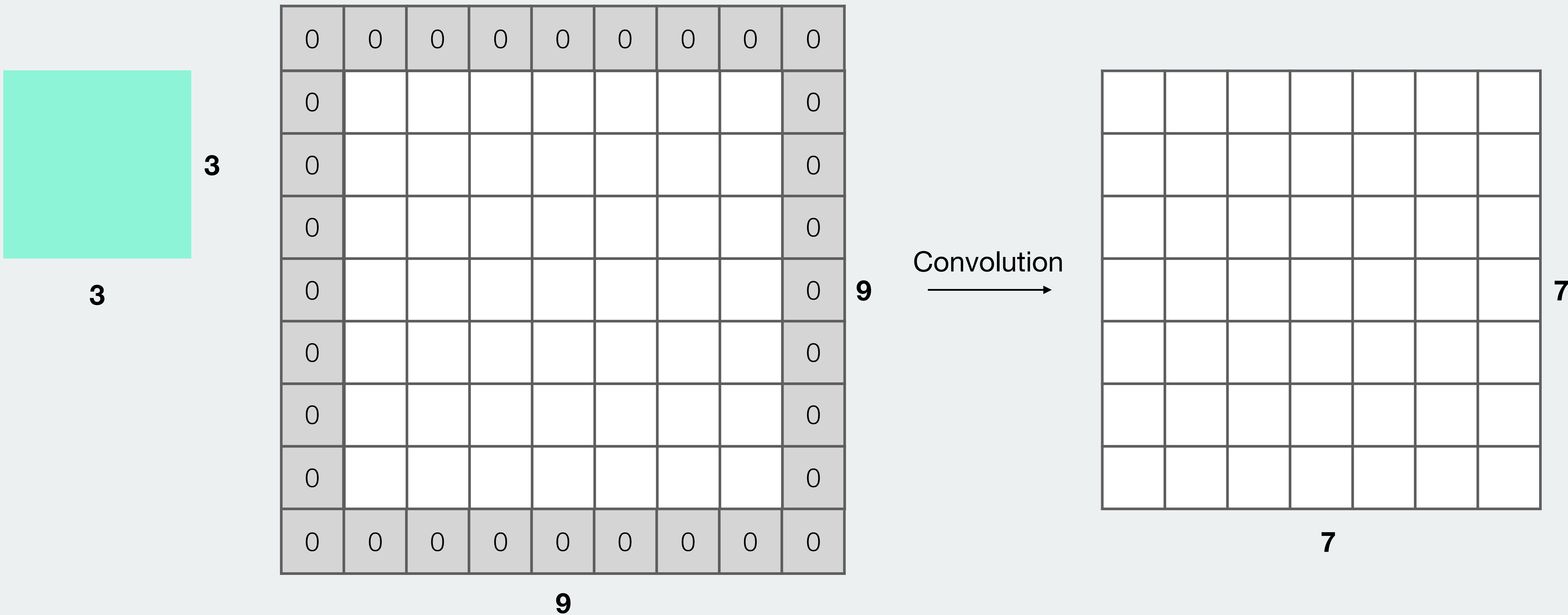
Convolutional neural networks

> Dimensions

Problem: The image *shrinks*

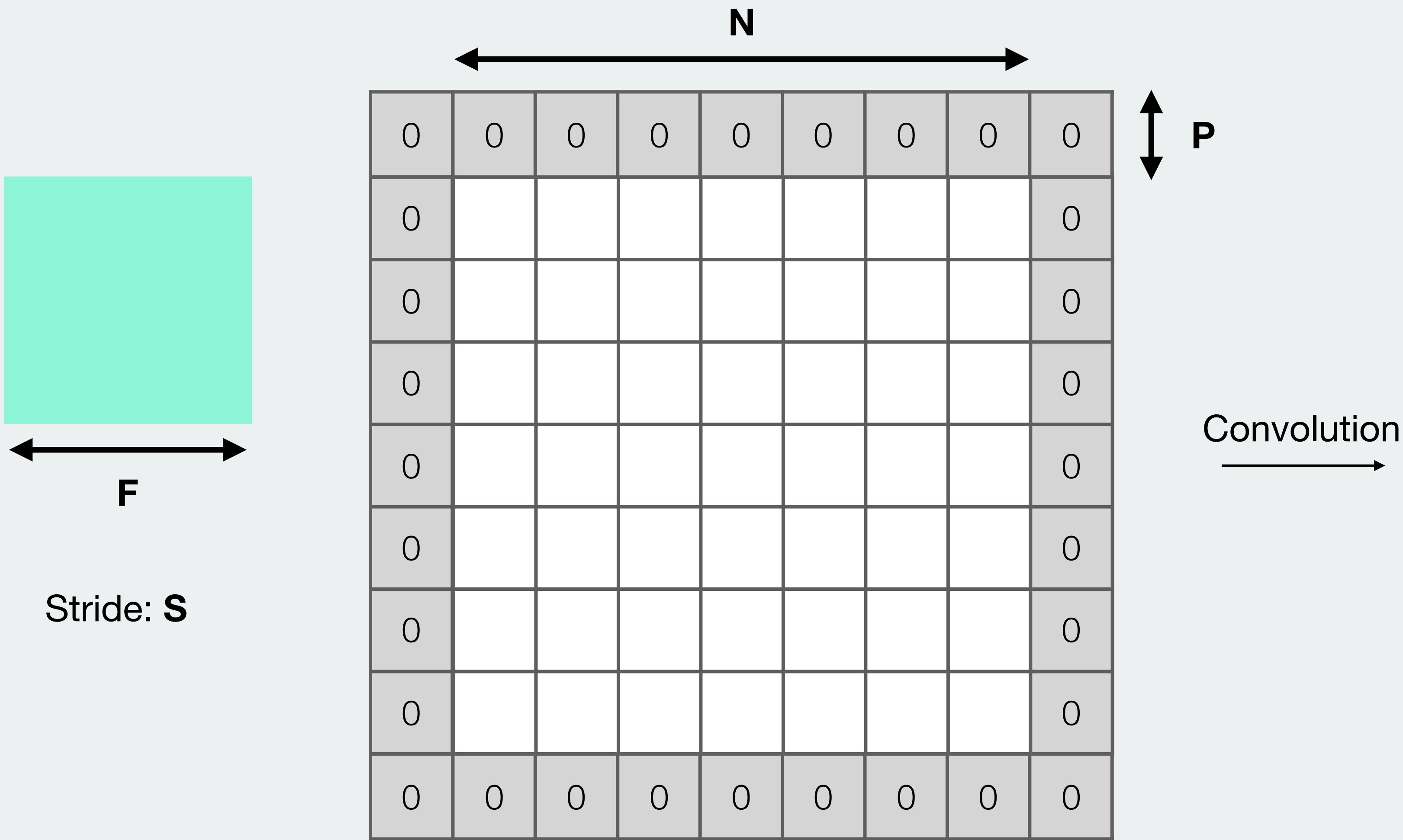
Solution: *Padding!*

$7 \times 7 \Rightarrow 5 \times 5$



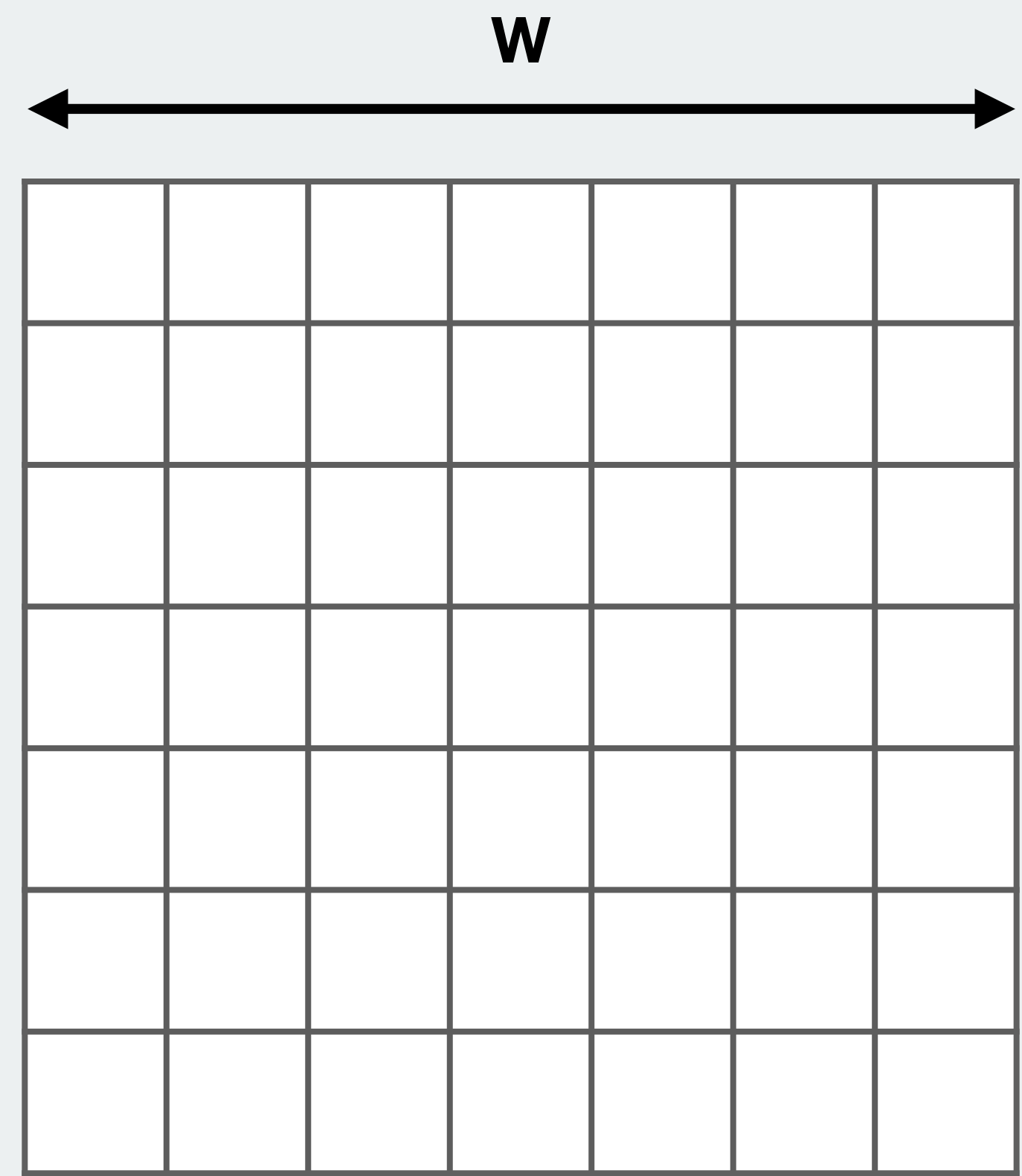
Convolutional neural networks

> Dimensions



General formula

$$W = \frac{N + 2P - F}{S} + 1$$



Animations

Convolutional neural networks

> Quiz

Given: 128 x 128 x 3 input

Ten 5 x 5 x 3 filters

Padding: 2

Stride: 1

Question 1: What are the output dimensions?

Question 2: What is the number of parameters?

Question 3: What if $F = N + 2P$?

Given: 128 x 128 x 3 input

Ten 5 x 5 x 3 filters

Padding: 2

Stride: 1

Question 1: What are the output dimensions?

Question 2: What is the number of parameters?

Question 3: What if $F = N + 2P$?

Answer 1:

$$W = \frac{128 + 2 \cdot 2 - 5}{1} + 1 = 128$$

Answer 2:

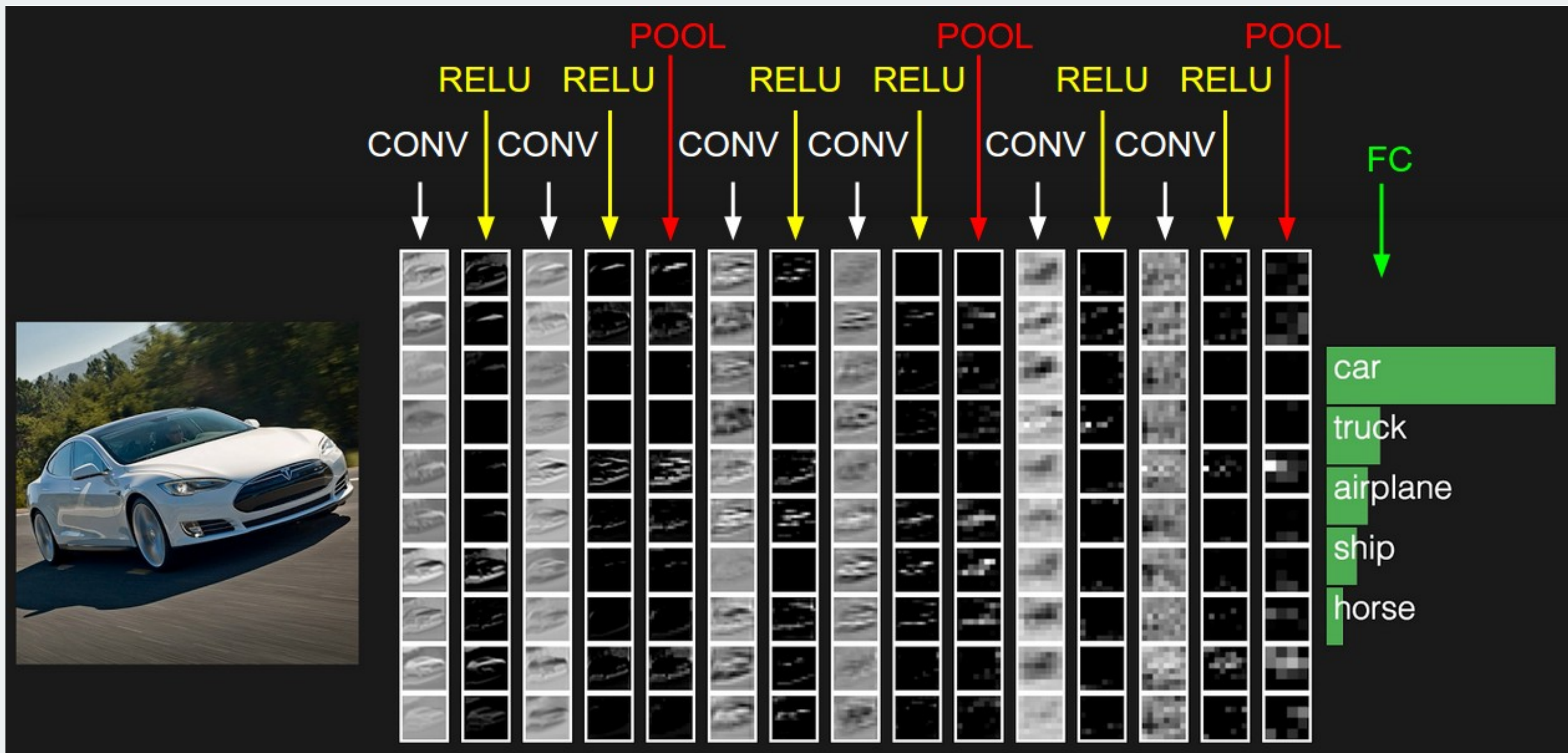
$$5 \cdot 5 \cdot 3 \cdot 10 + 10 = 760$$

Answer 3:

Then it's just a VNN!

Convolutional neural networks

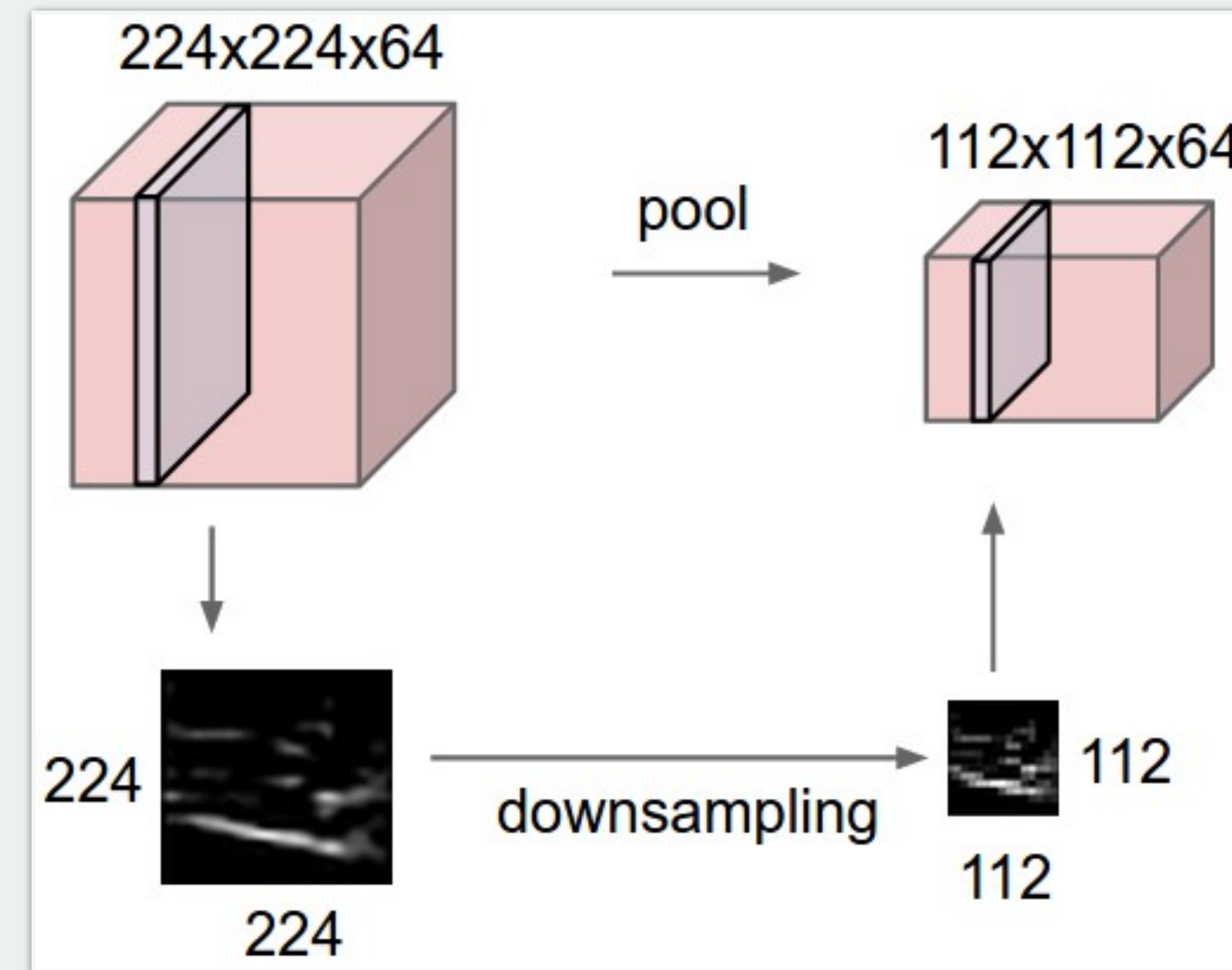
> Example of a bigger network



Convolutional neural networks

> Pooling

- Method used for downsampling
- Reduces number of parameters and computations
- Lowers width and height of volume by an integer factor
- Preserved depth



Convolutional neural networks

> Pooling

- Method used for downsampling
- Reduces number of parameters and computations
- Lowers width and height of volume by an integer factor
- Preserved depth

