

Assignment No. 10: Depth-first search

Allocated time: 2 hours

Implementation

You are required to implement correctly and efficiently the *căutare în* depth-first search algorithm (DFS) (Chapter 22.3 from the book). For graph representation, you should use adjacency lists. You also have to:

- Implement the Tarjan algorithm for detecting strongly connected components (https://en.wikipedia.org/wiki/Tarjan's_strongly_connected_components_algorithm)
- Implement topological sorting (described in chapter 22.4)

Evaluation

!! Before you start to work on the algorithm evaluation code, make sure you have a correct algorithm! Prove the correctness of your algorithm/implementation by running it on a smaller graph:

- Printing the initial graph (the adjacency lists)
- Printing all strongly connected components of the graph
- A list of nodes sorted topologically (should this list be non-empty/if it is - why so?)

Since, for a graph, both $|V|$ and $|E|$ may vary, and the running time of DFS depends on both (how?), we will make each analysis in turn:

1. Set $|V| = 100$ and vary $|E|$ between 1000 and 5000, using a 100 increment. Generate the input graphs randomly – make sure you don't generate the same edge twice for the same graph. Run the DFS algorithm for each $\langle |V|, |E| \rangle$ pair value and count the number of operations performed; generate the corresponding chart (i.e. the variation of the number of operations with $|E|$).
2. Set $|E| = 9000$ and vary $|V|$ between 100 and 200, using an increment equal to 10. Repeat the procedure above to generate the chart which gives the variation of the number of operations with $|V|$.
3. Interpret your charts.