

Life Contingencies: The Mathematics, Statistics, and Economics of Life Insurance

An open text authored by the Actuarial Community

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Preface

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Book Description

How will the text be used?

Why is this good for the profession?

Life Contingent Calculations

Project Goal

Acknowledgements

Contributors

For our Readers

Chapter 1

Introduction

Placeholder

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