

# Databases: Supervision 2

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## 2009 Paper 4 Question 8

1. (a) Define the concept of a *functional dependency*. [2]

A set of attributes  $X$  functional determines another set of attributes if, and only if, each  $X$  value is associated with precisely one  $Y$  value.

- (b) Let  $R(A, B, C, D, E, F)$  be a database schema with functional dependencies

$$A, B \rightarrow C$$

$$B, C \rightarrow A, D$$

$$D \rightarrow E$$

$$C, F \rightarrow B$$

- i. Compute the closure of  $\{A, B\}$ . [3]

$\{A, B, C, D, E\}$

- ii. Is  $A, B \rightarrow D, F$  a functional dependency over  $R$ ? Justify your answer. [1]

No, because  $F$  is not in the closure.

- (c) Define the concept of a *multivalued dependency*. [2]

A multivalued dependency on  $R$  is a constraint such that if two tuples of  $R$  agree on all the attributes of  $X$ , then their components in  $Y$  can be swapped and the result will be two tuples that are also in the relation.

- (d) Suppose the functional dependency  $X \rightarrow Y$  holds on a relational schema. Does this mean that the multivalued dependency  $X \twoheadrightarrow Y$  holds? Justify your answer. [3]

Every functional dependency is a multivalued dependency since if it is a functional dependency then swapping their components in  $y$  will result in the same tuple (since they are necessarily the same for tuples that agree on  $X$ ).

- (e) Define the concept of a *lossless-join decomposition*. [3]

A lossless-join decomposition is splitting a relation  $R$  into two relations  $R_1$  and  $R_2$  such that  $R_1 \bowtie R_2 = R$ .

- (f) Let  $R(X)$  be a database schema, where  $X$  is a set of attributes. Show that  $S(Y \cup Z)$  and  $T(Y \cup (X - Z))$  is a lossless-join decomposition of  $R(X)$  if and only if the multivalued dependency  $Y \twoheadrightarrow Z$  holds over  $R$ . [6]

- Suppose  $Z \twoheadrightarrow W$
- We know (from proof of Heath's rule) that  $R \subseteq \pi_{Z,W}(R) \bowtie \pi_{Z,Y}(R)$  so we only need to show  $\pi_{Z,W}(R) \bowtie \pi_{Z,Y}(R) \subseteq R$ .
- Suppose  $r \in \pi_{Z,W}(R) \bowtie \pi_{Z,Y}(R)$ .
- There must be a  $t \in R$  and  $u \in R$  with  $\{r\} = \pi_{Z,W}(\{t\}) \bowtie \pi_{Z,Y}(\{u\})$ .
- In other words there must be a  $t \in R$  and  $u \in R$  with  $t.Z = u.Z$
- So the MVD tells is that there must be some tuple  $v \in R$  such that
  - $v$  agrees with both  $t$  and  $u$  on the attributes of  $Z$
  - $v$  agrees with  $t$  on the attributes of  $W$ .
  - $v$  agrees with  $u$  on the attributes of  $Y$ .
- This  $v$  must be the same as  $r$ , so  $r \in R$ .
- Suppose  $R = \pi_{Z,W}(R) \bowtie \pi_{Z,Y}(R)$
- Let  $t$  and  $u$  be any records in  $R$  with  $t.Z = u.Z$ .
- Let  $v$  be defined by  $\{v\} = \pi_{Z,W}(\{t\}) \bowtie \pi_{Z,Y}(\{u\})$
- By construction we have:

$$- v.Z = t.Z = u.Z$$

$$- v.W = t.W$$

$$- v.Y = u.Y$$

Therefore,  $Z \twoheadrightarrow W$  holds.

## 2010 Paper 4 Question 5

2. (a) Suppose that  $R(A, B, C)$  is a relational schema with functional dependencies  $F = \{A, B \rightarrow C, C \rightarrow B\}$ .

- i. Is this schema in 3NF? Explain.

[2]

$A, B$  and  $A, C$  are keys for  $R$  and therefore there are no non-prime attributes.

- ii. Is this schema in BCNF? Explain.

[2]

$C$  is not a key and  $C \rightarrow B$  therefore the schema is not in BCNF.

- (b) Decomposition plays an important role in database design.

- i. Define what is meant by a *lossless-join decomposition*.

[2]

A lossless-join decomposition is splitting a relation  $R$  into two relations  $R_1$  and  $R_2$  such that  $R_1 \bowtie R_2 = R$ .

- ii. Define what is meant by a *dependency preserving decomposition*.

[2]



- (c) Let  $R(A, B, C, D, E)$  be a relational schema with the following functional dependencies.

$$A, B \rightarrow C$$

$$D, E \rightarrow C$$

$$B \rightarrow D$$

$$I$$

- i. What is the closure of  $\{A, B\}$ ?

[2]

$\{A, B, C, D\}$ 

- ii. What is the closure of  $\{B, E\}$ ?

[2]

 $\{B, C, D, E\}$ 

- iii. Decompose the schema to BCNF in two different ways. In each case, are all dependencies preserved? Explain.

[8]

**Using**  $A, B \rightarrow C, D$