$$\frac{d}{dt}V(t) = \frac{1}{C} \left( g_{\text{Na}}(t) \cdot (E_{\text{Na}} - V(t)) + g_{\text{K}}(t) \cdot (E_{\text{K}} - V(t)) + g_{\text{leak}} \cdot (E_{\text{leak}} - V(t)) + I_{\text{applied}} \right)$$

The potassium conductance is given by

$$g_{K}(t) = \bar{g}_{K}(n(t))^{4}$$

where  $\bar{g}_{K}$  is the maximal conductance and n is a gating variable. (The exponent characterizes the fact that four components of each channel must be in the open state in order for the channel to pass  $K^{+}$  ions.) The sodium conductance is given by

$$g_{\text{Na}}(t) = \bar{g}_{\text{Na}}(m(t))^3 h(t)$$

where  $\bar{g}_{Na}$  is the maximal conductance, m is an activation gating variable and h is an inactivation gating variable.

The gating variable dynamics are given by

$$\frac{d}{dt}n(t) = \frac{n_{\infty}(V(t)) - n(t)}{\tau_n(V(t))}$$

$$\frac{d}{dt}m(t) = \frac{m_{\infty}(V(t)) - m(t)}{\tau_m(V(t))}$$

$$\frac{d}{dt}h(t) = \frac{h_{\infty}(V(t)) - h(t)}{\tau_h(V(t))}$$

where

$$n_{\infty}(V) = \frac{0.01(V + 50)/(1 - e^{-(V + 50)/10})}{0.01(V + 50)/(1 - e^{-(V + 50)/10}) + 0.125e^{-(V + 60)/80}}$$

$$\tau_{n}(V) = \frac{1}{0.01(V + 50)/(1 - e^{-(V + 50)/10}) + 0.125e^{-(V + 60)/80}}$$

$$m_{\infty}(V) = \frac{0.1(V + 35)/(1 - e^{-(V + 35)/10})}{0.1(V + 35)/(1 - e^{-(V + 35)/10}) + 4e^{-(V + 60)/18}}$$

$$\tau_{m}(V) = \frac{1}{0.1(V + 35)/(1 - e^{-(V + 35)/10}) + 4e^{-(V + 60)/18}}$$

$$h_{\infty}(V) = \frac{0.07e^{-(V + 60)/20}}{0.07e^{-(V + 60)/20} + 1/(1 + e^{-(V + 30)/10})}$$

$$\tau_{h}(V) = \frac{1}{0.07e^{-(V + 60)/20} + 1/(1 + e^{-(V + 30)/10})}$$

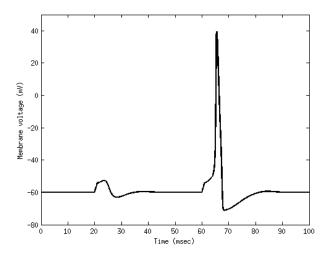
Model parameters are  $\bar{g}_{\text{Na}} = 120 \text{ mS/cm}^2$ ,  $\bar{g}_{\text{K}} = 36 \text{ mS/cm}^2$ ,  $g_{\text{leak}} = 0.3 \text{ mS/cm}^2$ ,  $E_{\text{Na}} = 55 \text{ mV}$ ,  $E_{\text{K}} = -72 \text{ mV}$ ,  $E_{\text{leak}} = -49 \text{ mV}$ , and  $C = 1 \mu \text{F/cm}^2$ .

### PROBLEMS:

 a) Simulate the system with the given parameter values, using the MATLAB script hodgkin\_huxley.m

Print the plot.

## ANS:



## **END ANS**

- b) Answer these questions, looking at the code for the MATLAB script, and at the plot:
- i) For how long an interval, and at which two times, is the current I\_applied being applied?
- ii) What is the difference between the two pulses (besides their being applied at different times, obviously)?
- ii) How did the system react to each of the two pulses?

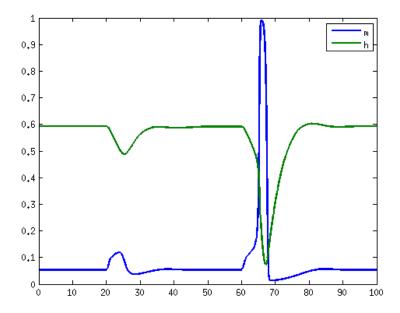
ANS: i) interval of length 1; applied at time 20 and 60; ii) first pulse has intensity -6.65, and second one -6.85; iii) no spike for the first one

c) Generate plots of m and h (on the same plot), using these commands in the MATLAB file, after the current figure:

```
figure(2)
set(gca,'fontsize',14)
plot(t,s(:,2), t,s(:,3), 'Linewidth', 2)
legend('m','h')
```

and print your answer.

# ANS:



## **END ANS**

This verifies that m(t) and h(t) tend to "cancel each other out" through most of the process (except during a spike!).

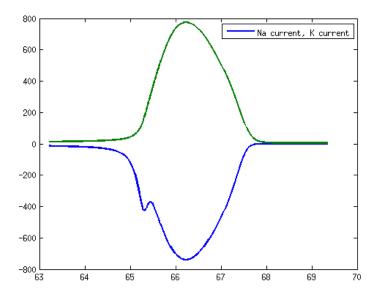
d) Now add this code, which generates plots for the sodium and potassium currents (I used the range 3800:4200 to focus on the part of the plot where the action potential happened):

```
figure(3)
I_Na = g_N_bar*(s(:,1)-E_N).*s(:,2).^3.*s(:,3);
I_K = g_K_bar*(s(:,1)-E_K).*s(:,4).^4;
figure(3)
set(gca,'fontsize',14)
plot(t(3800:4200),I_Na(3800:4200),t(3800:4200),I_K(3800:4200),'Linewidth',2)
legend('Na current, K current')
```

## Plot and print.

Observe that the action potential begins with a sodium influx, followed by the flow of potassium out of the cell. (This is seen in the delay in changes between the blue and green lines.)

### ANS:



END ANS