

11. $m = 10 \text{ kg}$ $R = 0.3 \text{ m}$.

(a)

$$F - f = ma \quad \text{又} \because f = 10 - 10 \times 0.6 = 4 \text{ N}.$$

(b)

$$\tau = I \cdot \alpha = f \cdot R$$

$$\text{又} \because \alpha = \frac{a}{R} \quad \text{又} \because I = \frac{f R^2}{a} = \frac{4 \times 0.09}{0.6} = 0.6 \text{ kg} \cdot \text{m}^2.$$

12. (a). 能量守恒.

$$mg(h-2R) = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$$

$$\text{又} \because mg(h-2R) = \frac{1}{2}mgR.$$

$$\therefore h = \frac{5}{2}R = \frac{5}{2} \times 0.12 = 30 \text{ cm}.$$

$$\text{又} \because mg = m \frac{v^2}{R}.$$

$$\text{又} \because h = 0.324 \text{ m}$$

(b). $h = 6R$ Q 点有速度

$$\therefore \frac{v^2}{R} = 10gR.$$

$$\frac{1}{2}I\omega^2 = \frac{1}{2}mv^2 - 0 = mg(h-R) = 5mgR.$$

$$\frac{1}{2}mv^2 = \frac{1}{2}m \frac{v^2}{R} = \frac{10 \times 9.8 \times 0.12 \times \frac{1}{2}}{0.12} = 3.2 \times 10^{-2} \text{ J}.$$

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$$\approx 1.346 \times 10^{-2} \text{ N}.$$

(a) $v_1 = -0.11 \text{ m/s}$.

(b) 滑动时 $ma = f_k = \mu mg$. $a = -2.058 \text{ m/s}^2$

(c) $\tau = I \cdot \alpha$. $I = \frac{2}{5}mR^2$

$$\tau = f \cdot R \quad \text{又} \because \alpha = -46.8 \text{ rad/s}^2$$

(d) 有 $v_0 + at = \omega R$

$$\text{又} \because t = 1.18 \text{ s}$$

(e). $d = v_0 t + \frac{1}{2}at^2$ $d = 8.6 \text{ m}$.

(f). 开始时 $v = v_0 + at = 6.07 \text{ m/s}$.



23.

$$\vec{\tau} = \vec{r} \times \vec{F}$$

$$(a) \quad \vec{\tau} = \vec{r} \times \vec{F} = (-k - 1.5\hat{i} - 4\hat{j}) \text{ N}\cdot\text{m}.$$

$$2(2\hat{i} - 3\hat{k}) \times (0.5\hat{j} - 2\hat{k})$$

$$= 1 - 4 - 1.5 = -4.5 \text{ kg}\cdot\text{m}^2\cdot\text{s}^{-2}$$

$$(b) \quad \vec{r} = (0.5\hat{j} - 2\hat{k}) - (2\hat{i} - 3\hat{k}) = -2\hat{i} + 0.5\hat{j} + \hat{k}$$

$$\vec{\tau} = \vec{r} \times \vec{F} = (-1.5\hat{i} - 4\hat{j} - \hat{k}) \text{ N}\cdot\text{m}$$

31.

$$(a) \quad \text{at } t = 2 \text{ s} \quad h = \frac{v^2}{2g} = \frac{1600}{2 \times 9.8} = \frac{800}{9.8} \text{ m} \approx 81.63 \text{ m}$$



$$\vec{\tau} = \vec{r} \times \vec{p} = 81.63 \times 0 \times \sin \theta = 0$$

$$(b) \quad \vec{\tau} = \vec{r} \times \vec{p} = m(\vec{r} \times \vec{v}) = 0.4 \times \left(\frac{81.63}{2} \hat{j} + 4 \times \sqrt{800} \times \sin \theta \right)$$

$$= 16\sqrt{2} \approx 22.6 \text{ kg}\cdot\text{m}^2\cdot\text{s}^{-1}$$

$$(c) \quad \vec{\tau} = \vec{r} \times \vec{F} = \sqrt{4 + (81.63)^2} \times mg \times \sin \theta = 2mg = 7.84 \text{ kg}\cdot\text{m}^2\cdot\text{s}^{-2}$$

$$(d) \quad \vec{\tau} = \vec{r} \times \vec{F} = 2mg = 7.84 \text{ kg}\cdot\text{m}^2\cdot\text{s}^{-2}$$

39.

$$(a) \quad \vec{\tau} = I \alpha = \vec{r} \times \vec{F}$$

$$\vec{\tau} = \vec{r} \times \vec{p} = m(\vec{r} \times \vec{v}) \quad T_{\text{ave}} = \frac{\Delta b}{\Delta t} = 1.4 \text{ N}\cdot\text{m}$$

$$(b) \quad \vec{\tau} \propto \alpha \quad I \cdot \omega_0 = L_1 \quad \vec{\tau} = I \cdot \alpha$$

$$\Delta \theta = \omega_0 t + \frac{\alpha}{2} t^2 \quad \Delta \theta = 20.4 \text{ rad}$$

$$(c) \quad |\omega| = \frac{1}{2} I (\omega_1^2 + \omega_2^2) \quad \omega_1 = \frac{L_1}{I} \quad \omega_2 = \frac{L_2}{I}$$

$$\Delta \theta = \omega = -29.86 \text{ J}$$

(d)

$$P = \frac{|\omega|}{T} = 19.9 \text{ W}$$



18. 能量守恒. 有 $I_1 = 590 \text{ kg} \cdot \text{m}^2$ $I_2 = 165 \text{ kg} \cdot \text{m}^2$

$$\frac{1}{2} m \cdot (\omega \cdot R)^2 + \frac{1}{2} I \omega^2 = \frac{1}{2} m (\omega' \cdot 0.5)^2 + \frac{1}{2} I_2 \omega'^2$$

$$2 \times 30 \times 9 + \frac{1}{2} \times 590 \times 2.5^2 = \frac{1}{2} \times 30 \times \omega'^2 \times 0.25 + \frac{1}{2} \times 165 \times \omega'^2$$

$$\omega' = 2.21 \text{ rad} \cdot \text{s}^{-1}$$

角动量守恒

$$I \omega_f = I \omega_i \quad \text{At } a \cdot \omega' = 2.4 \text{ rad} \cdot \text{s}^{-1}$$

61. $I' = I + m l^2 = 0.12 + 0.2 \times 0.36 = 0.192 \text{ kg} \cdot \text{m}^2$

$$I' \omega' = I \omega = 0.288 \text{ kg} \cdot \text{m}^2 \cdot \text{s}^{-1}$$

$$\omega' = 1.5 \text{ rad} \cdot \text{s}^{-1}$$

