DIGITAL LOGIC

Chapter 6 : Registers & Counters

2023 Fall

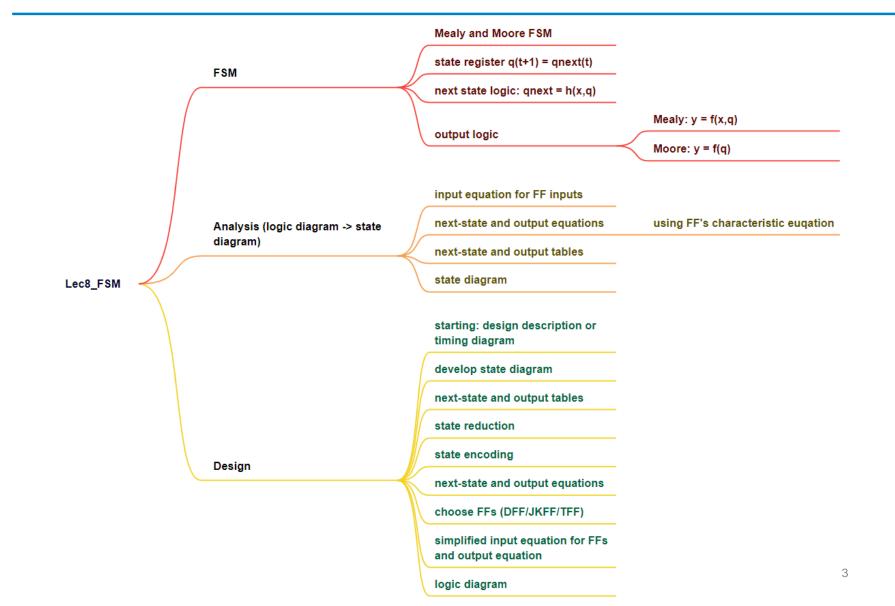


Today's Agenda

- Recap
- Context
 - Registers
 - Design a sequence generator
 - Counters
 - Design a counter
- Reading: Textbook, Chapter 6.1-6.9



Recap





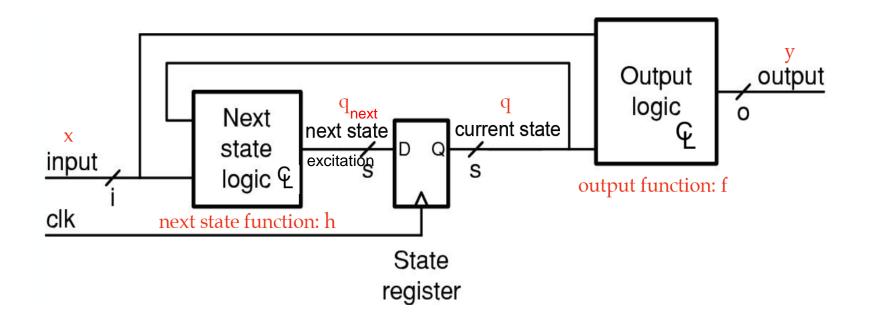
Outline

- Various types of registers
- Sequence generator with shift register
- Asynchronous counter
- Synchronous counter
- Design a synchronous counter



Clocked Sequential Circuits

- Clocked sequential circuits have flip-flops and combinational gates.
- FFs are essential, otherwise reduce to combinational.
- Circuits that include flip-flops are usually classified by the function they perform rather than by the name of the sequential circuit.
- Two such circuits are registers and counters.





Registers and Counters

Register

- A group of binary cells (FFs) suitable for holding binary data information
- In addition to the FFs, a register may have combinational gates to control when and how the new information is transferred into the register (MUXes, ...)

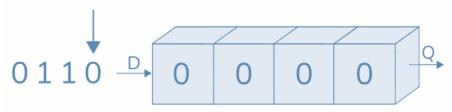
Counter

- A register that goes through a predetermined sequence of states upon the application of input pulses
- The gates in a counter are connected in such a way as to produce a pre-described sequence of binary states in the register (arithmetic circuits)



Shift Register

- Register: bitwise extension of a FF.
 - The shift register permits the stored data to move from a particular location to some other location within the register.
 - All the n FFs are driven by the common clock signal
 - sometimes with load control
- Type: Based on input & output
 - Serial-in to Serial-out (SISO)
 - Serial-in to Parallel-out (SIPO)
 - Parallel-in to Serial-out (PISO)
 - Parallel-in to Parallel-out (PIPO)
- Direction
 - Left shift
 - Right shift
 - Rotate (right or left)
 - Bidirectional



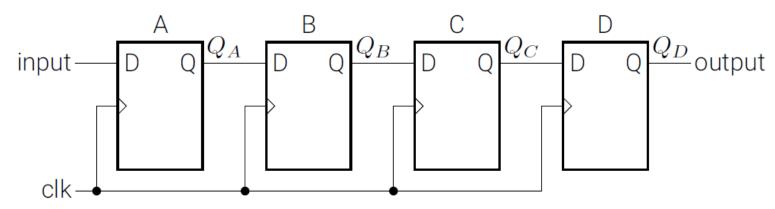
Bits moving through a SISO shift register

Universal shift register



4-bit Serial-in to Serial-out

 SISO: the data is shifted serially "IN" and "OUT" of the register, one bit at a time in either a left or right direction under clock control.



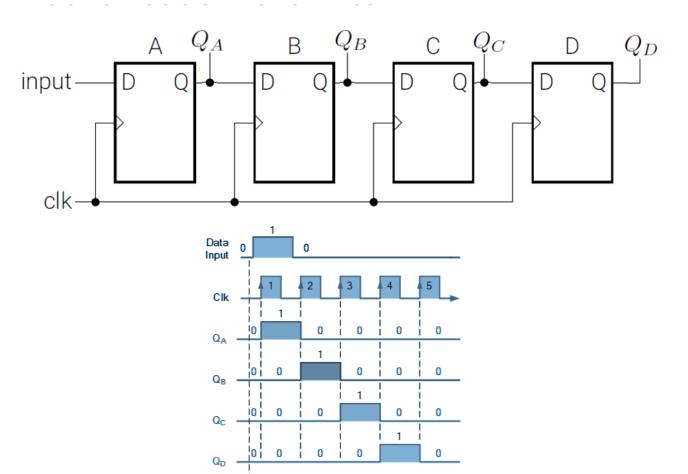
• An example of 1011 into the register. (Input from LSB to MSB, Right shift)

CLK	In	Q_A	Q_B	Q_{C}	Q_D	Out
initial		0	0	0	0	0
↑	1 -	→ 1 <u></u>	0	0	0 —	• 0
1	1 -	1	1	0	0	• 0
↑	0 —	O (1	1	0 —	• 0
\uparrow	1 -	→ 1	0	1	1 —	1



4-bit Serial-in to Parallel-out

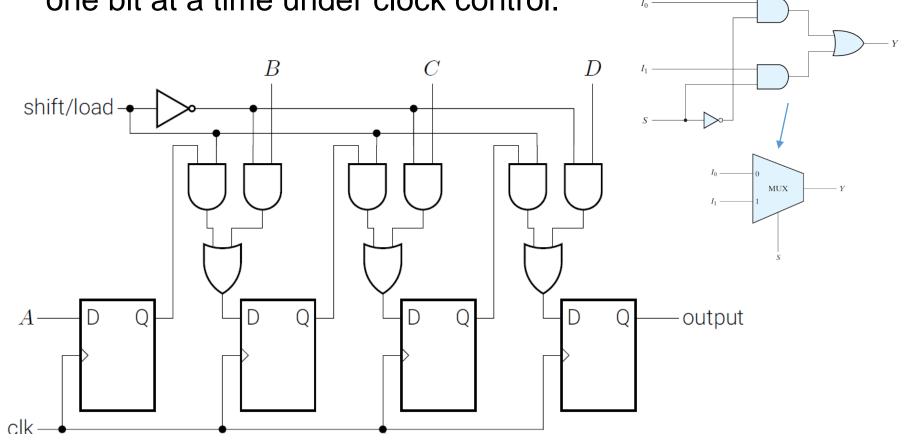
• SIPO: the register is loaded with serial data, one bit at a time, with the stored data being available at the output in parallel form.





4-bit Parallel-in to Serial-out

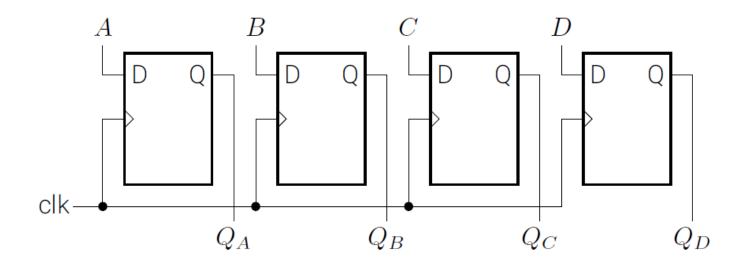
• PISO: the parallel data is loaded into the register simultaneously and is shifted out of the register serially one bit at a time under clock control.





4-bit Parallel-in to Parallel-out

• PIPO: the parallel data is loaded simultaneously into the register, and transferred together to their respective outputs by the same clock pulse.



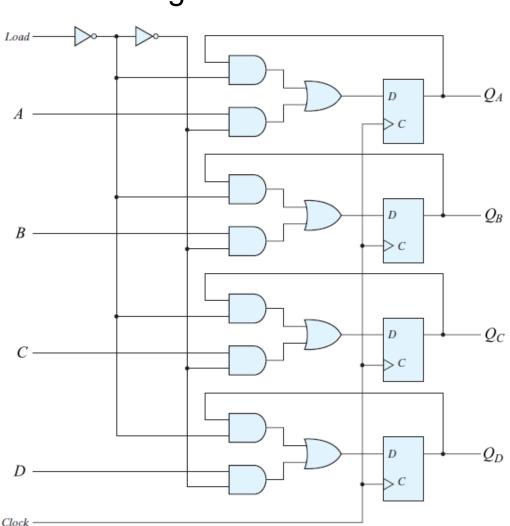


PIPO with Parallel Load

 4-bit Parallel-in to Parallel-out Register with Parallel Load Logic diagram

function table

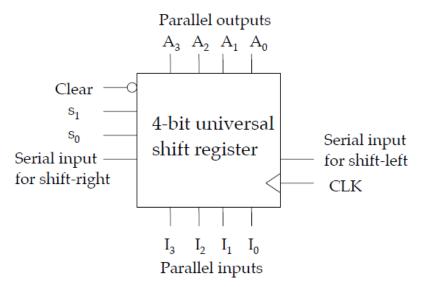
Present	Next state
state	
Load	$Q_A Q_B Q_C Q_D$
0	No change
1	ABCD





Universal Shift Register

- Universal shift register
 - Capable of both-direction shifting and parallel load/out functional table

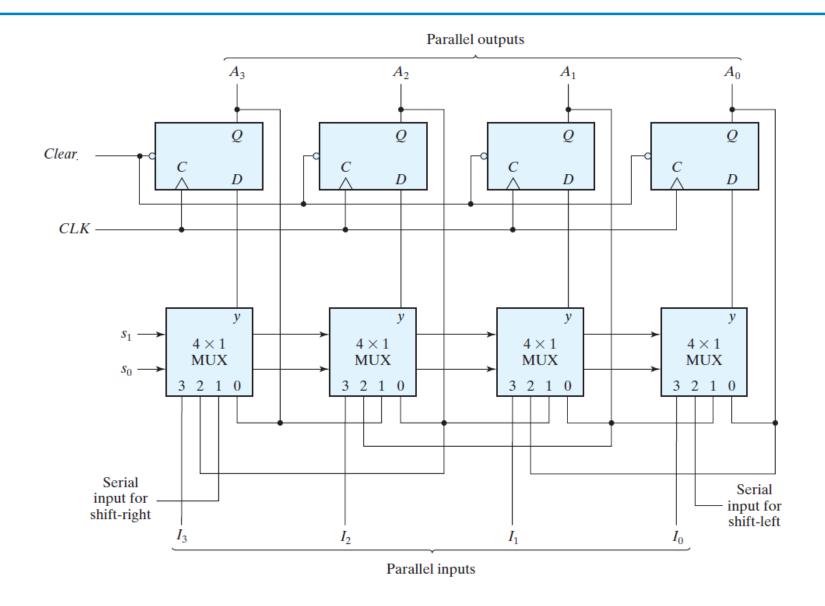


Clear	S ₁	S ₀	A ₃ +	A ₂ +	A ₁ +	A ₀ +	Operation
0	Х	х	0	0	0	0	Clear
1	0	0	A ₃	A ₂	A ₁	A ₀	No change
1	0	1	sri	A ₃	A ₂	A ₁	Shift right
1	1	0	A ₂	A ₁	A ₀	sli	Shift left
1	1	1	l ₃	l ₂	I ₁	I ₀	Parallel load

graphic symbol



Universal Shift Register

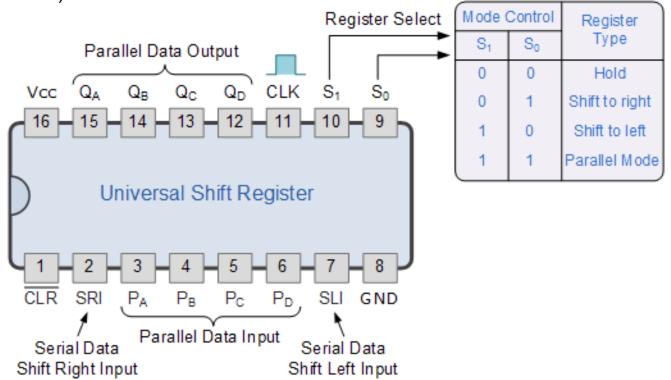




74 Series Shift Register

- Some of the IC's available for shift registers
 - 74164 8-bit SIPO shift register
 - 74165 8-bit PISO shift register
 - 74194 4-bit PIPO shift register

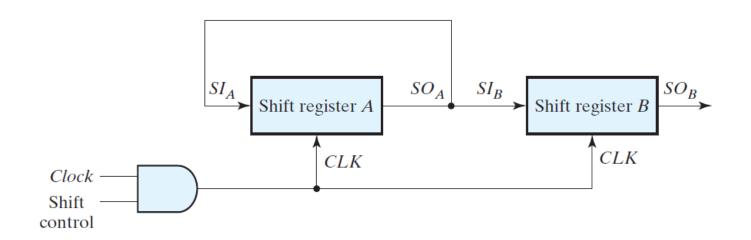
74195 – 4-bit Universal shift register (can be used for SISO, SIPO, and PIPO operations)





Serial Transfer

Serial Transfer from Reg A to Reg B



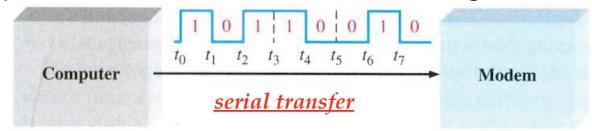
Clock		
		1
Shift control		
CLK —	T_1 T_2 T_3 T_4	

Timing Pulse	Shift	t Re	gist	er A	Shif	t Re	gist	er B
Initial value	1	0	1	1	0	0	1	0
After T_1	1	1	0	1	1	0	0	1
After T_2	1	1	1	0	1	1	0	0
After T_3	0	1	1	1	0	1	1	0
After T_4	1	0	1	1	1	0	1	1

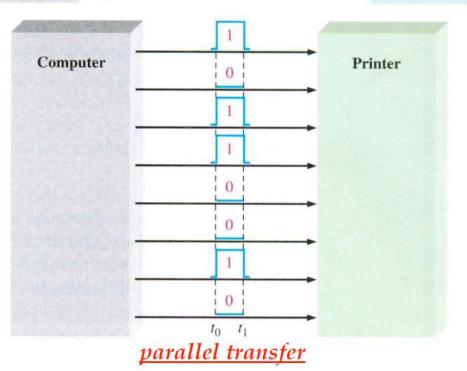


Serial/Parallel Transfer

 Shifters are useful in serializers and deserialisers that convert data from parallel to serial form and back again



- Serial
 - One bit a time
 - Need more time, low complexity
- Parallel
 - All bits at the sane time
 - Transfer faster, higher complexity





SIPO

PIPO

Serial to Parallel Converter

out[3] ____

out[1] _____

out[2] _____

out[0]

serial input clk for SIPO is faster clk1 (4f) clk2 (f) out[3] out[2] out[1] out[0] parallel output a[3] a[2] _____ a[0] clk2



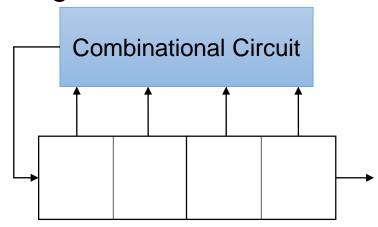
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Sequence Generator

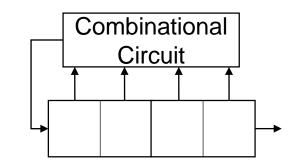
- A sequence generator is a circuit that generates a desired sequence of bits in synchronization with a clock.
- Can be used as a random bit generator, code generator, and prescribed period generator.
- The output of the combinational circuit is a function of the shift register state and is connected to the serial input of the shift register

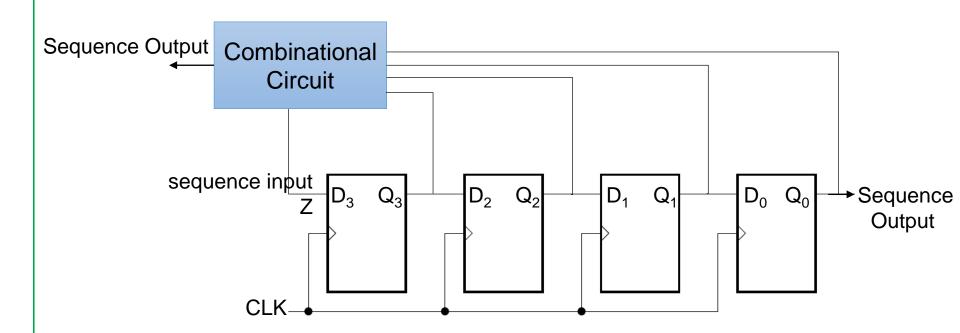




Sequence Generator

- n FFs can generate a sequence with the maximum length of $N = 2^n 1$
- The required sequence can be obtained from the output of any FF, or the output of the combinational circuit

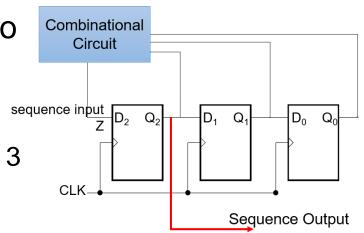


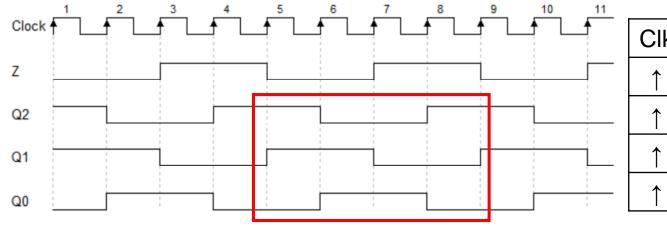


Example: Design a 4-bit Sequence Generator

• Design of a sequence generator to generate a sequence of **1001**.

The minimum number of flip-flops required to generate a sequence of length N is given by N ≤ 2ⁿ - 1 → n = 3 (3 FFs)





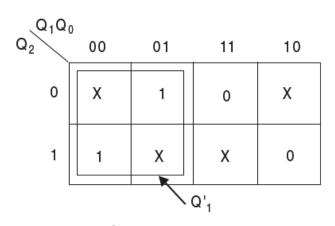
Clk	Z	Q_2	Q_1	Q_0
↑		1	1	0
↑		0	1	1
↑		0	0	1
1		1	0	0

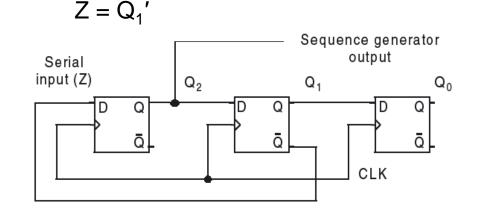
Example: Design a 4-bit Sequence Generator

- Design of a sequence generator to generate a sequence of 1001.
 - The minimum number of flip-flops required to generate a sequence of length N is given by $N \le 2^n 1 \rightarrow n = 3$ (3 FFs)

CLK	Z	Q_2	Q_1	Q_0
↑		1	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	Q
↑		0	1	1
↑		0	0	1
1		1	0	0

CLK	Z	Q_2	Q_1	Q_0
↑	0	1	1	0
↑	0	0	1	1
↑	1	0	0	1
↑	1	1	0	0

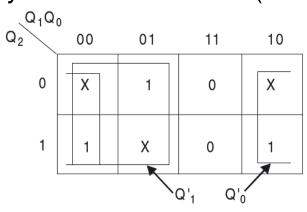




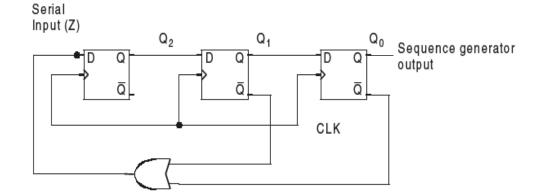
Example: Design a 5-bit Sequence Generator

- Design of a sequence generator to generate a sequence of 10011.
 - The minimum number of flip-flops required to generate a sequence of length N is given by $N \le 2^n 1 \rightarrow n = 3$ (3 FFs)

CLK	Z	Q_2	Q_1	Q_0
↑	0	\bigwedge	1	1
1	0	0	1	1
1	1	0	0	1
1	1 _	1	0	0
1	1 🗸	1	1	0



$$Z = Q_1' + Q_0'$$



Example: Design a 6-bit Sequence Generator

有方針技义等 SOUTHERN UNIVERSITY OF SCIENCE AND TECHNOLOGY

- Design of a sequence generator to generate a sequence of 110101
 - The minimum number of flip-flops required to generate a sequence of length N is given by $N \le 2^n 1$
 - The minimum value of *n* to satisfy the above condition is 3.

CLK	Z	Q_2	Q_1	Q_0
↑		1	1	0
↑		1	1	1
1		0	1	1
↑		1	0	1
1		0	1	0
<u></u>		1	0	1

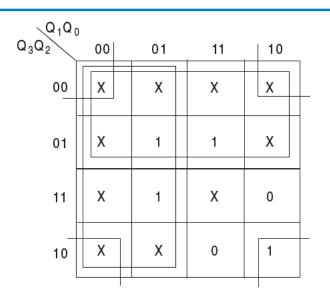
State 101 occurs twice!

3 flip-flops are not sufficient to generate the given sequence.

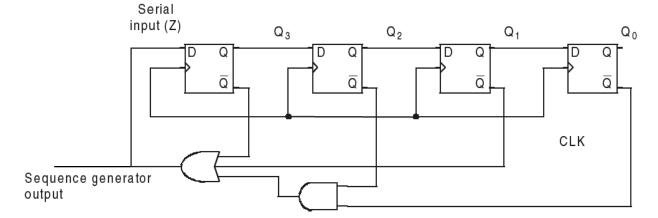
Example: Design a 6-bit Sequence Generator

Needs 4 FFs to generate 110101

clk	Z	Q_3	Q_2	Q_1	Q_0
↑	1	₹	1	0	0
1	0	1	1	1	0
↑	1_	0	1	1	1
1	0	1	0	1	1
1	1	0	1	0	1
1	1	1	0	1	0



$$Z = Q_3' + Q_1' + Q_2'Q_0'$$





Outline

- Various types of registers
- Sequence generator with shift register
- Asynchronous counter
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- Design a synchronous counter



Counters

- A counter is a special type of register that counts upward, downward, or in any prespecified sequence
 - Ripple counters (asynchronous counter)
 - The output transition of flip-flop serves as a source for triggering other flip-flops
 - Synchronous counters
 - The clock inputs of all flip-flops receive a common clock



Asynchronous Counters

- aka. Serial or ripple counters
- All the flip-flops are not driven by the same clock pulse.
 - The successive flip-flop is triggered by the output of the previous flip-flop.
 - Hence the counter has cumulative settling time, which limits its speed of operation

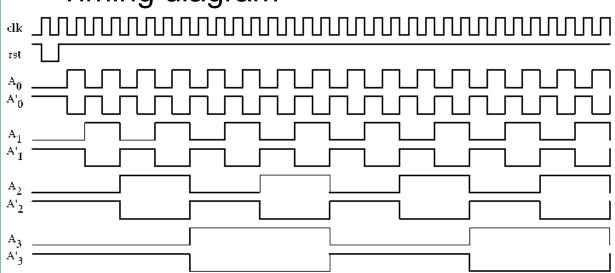


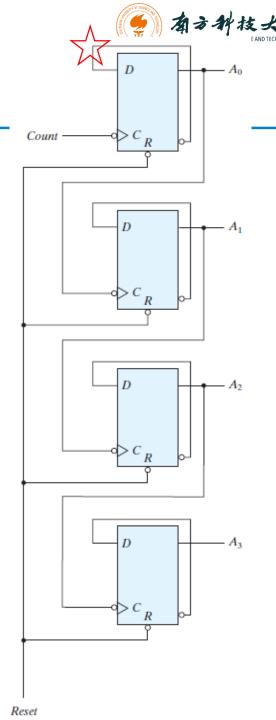
4-bit Binary Ripple Counter

Binary Up count sequence

A ₃	A ₂	A ₁	A 0
0	0	0	0
0	0	0	1
0	0	1	0
0	0	1	1
0	1	0	0
0	1	0	1
0	1	1	0
0	1	1	1
1	0	0	0

Timing diagram

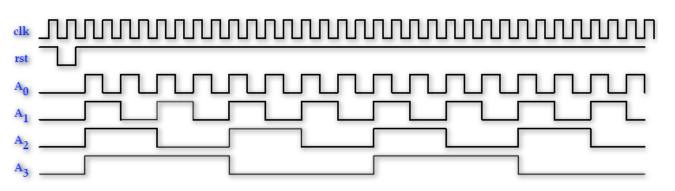


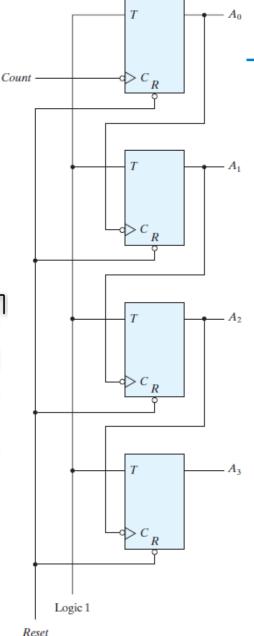




4-bit Binary Ripple Counter

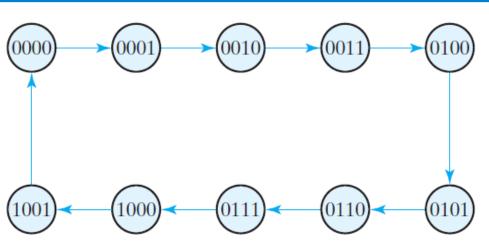
- For Down counter with TFF
 - Replace negative-edge triggered clock with positive-edge triggered clock







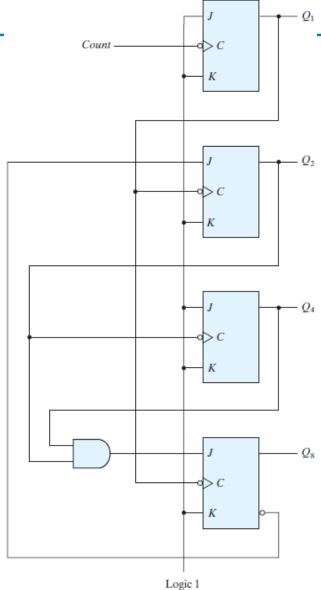
BCD Ripple Counter



Next State

Q8	Q4	Q2	2 Q1	Q8	3 Q4	1 Q2	2 Q1
0	0	0	0	0	0	0	1
0	0	0	1	0	0	1	0
0	0	1	0	0	0	1	1
0	0	1	1	0	1	0	0
0	1	0	0	0	1	0	1
0	1	0	1	0	1	1	0
0	1	1	0	0	1	1	1
0	1	1	1	1	0	0	0
1	0	0	0	1	0	0	1
1	0	0	1	0	0	0	0

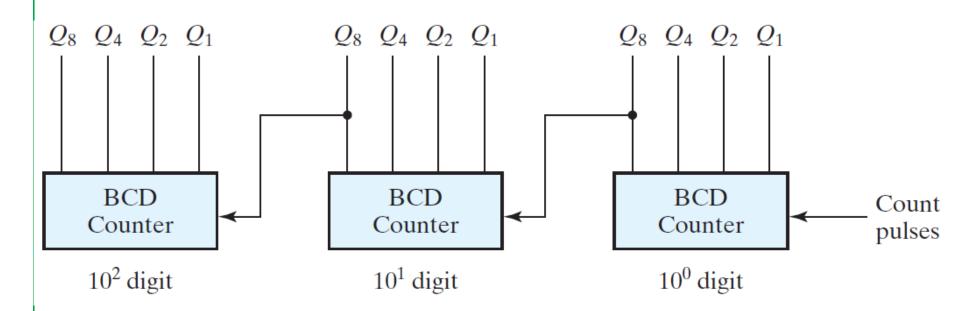
Present State





Three-decade BCD Ripple Counter

 When Q8 in one decade goes from 1 to 0, it triggers the count for the next higher decade while it's own decade goes from 9 to 0.





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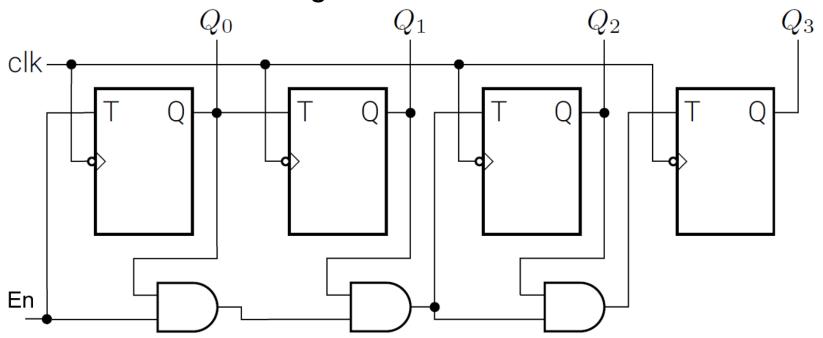
Synchronous counters

- The ripple or asynchronous counter is the simplest to build, but its highest operating frequency is limited because of ripple action.
 - delay time
 - glitches
- Both of these problems can be overcome, if all the flipflops are clocked synchronously.
- The resulting circuit is known as a synchronous counter.



4-bit Synchronous Binary Counters

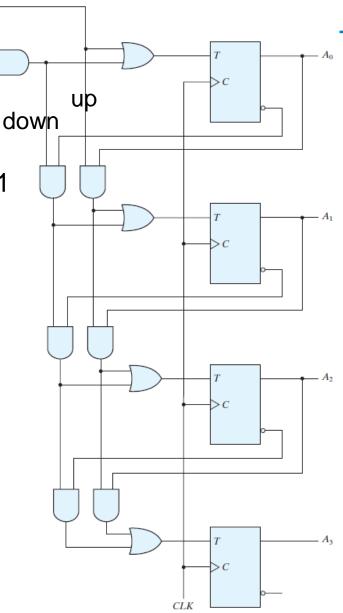
- Count up
- As the number of stages increases, the number of AND gates also increases, along with the number of inputs for each of those AND gates.





4-bit Up/Down Binary Counter

- Up=1, Down=0 =>
- counting up
 - $A_3A_2A_1A_0$
 - $0000 \rightarrow 0001 \rightarrow 0010 \rightarrow 0011 \rightarrow 0100 \rightarrow 0101$
- Up=0, Down=1 =>
- counting down
 - $A_3A_2A_1A_0$
 - $1111 \rightarrow 1110 \rightarrow 1101 \rightarrow 1100 \rightarrow 1011 \rightarrow 1010$





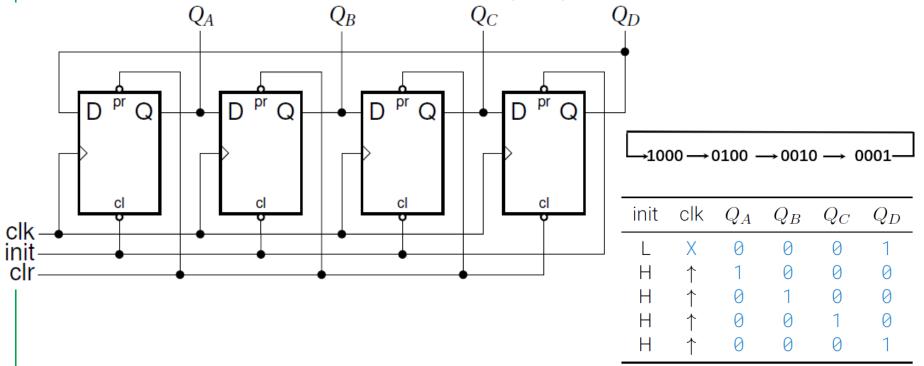
Shift Register Counters

- Shift registers may be arranged to form different types of counters.
- These shift registers use feedback, where the output of the last flip-flop in the shift register is fed back to the first flip-flop.
- Based on the type of this feedback connection, the shift register counters are classified as
 - ring counter
 - switch-tail ring counter or Johnson counter



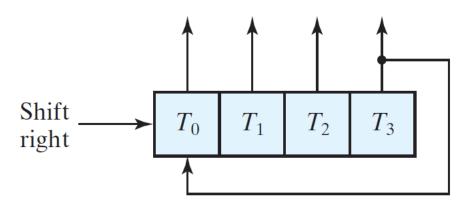
Ring Counter

- A circular shift register with only one flip-flop being set at any particular time, all others are cleared. (initial value 0001 as in example)
- The single bit is shifted from one flip-flop to the next to produce the sequence of timing signals

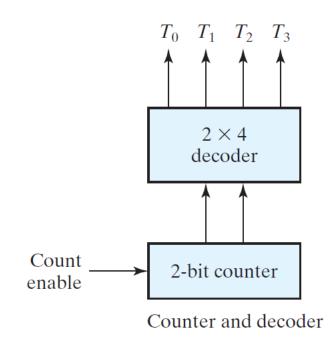


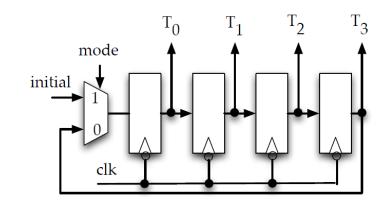


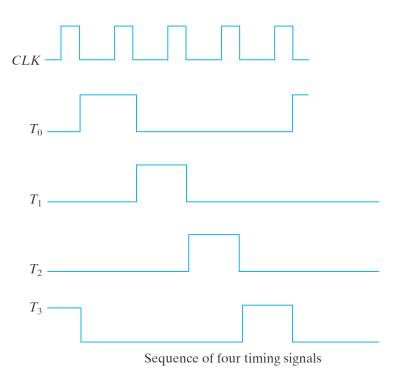
Ring Counter for Decoder



Ring-counter (initial value = 1000)



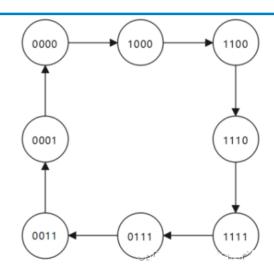


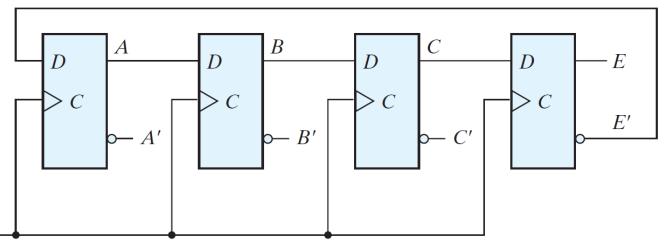




Johnson counter

- Switch-tail ring counter: a circular shift register with its complement output of the last flip-flop connected to the input of the first flip-flop
- Johnson counter is a k-bit switch-tail ring counter will go through a sequence of 2k distinguishable states (initial value 0000 as in example)

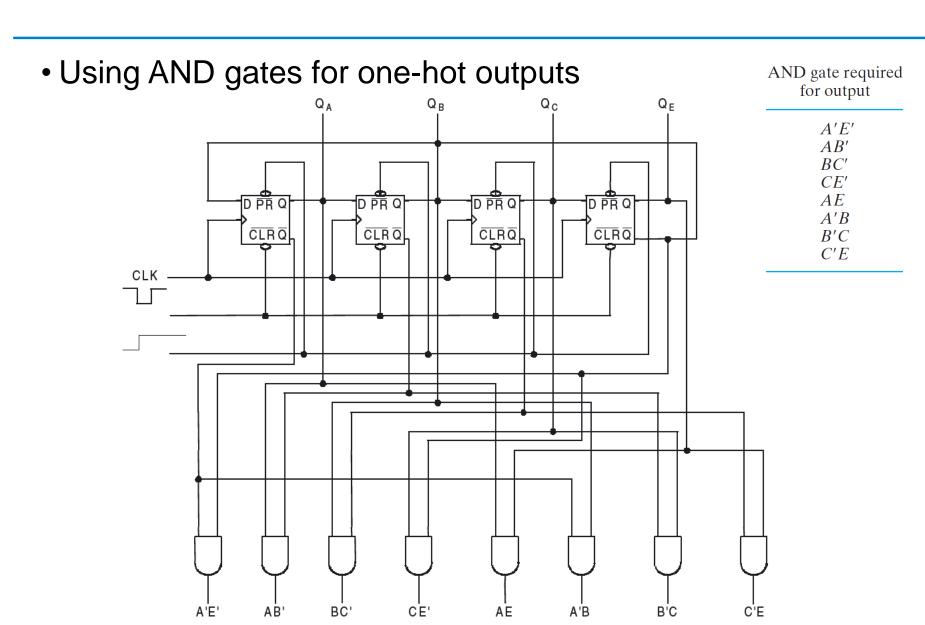




Saguanca	Fli	Flip-flop outputs							
Sequence number	\overline{A}	В	C	E					
1	0	0	0	0					
2	1	0	0	0					
3	1	1	0	0					
4	1	1	1	0					
5	1	1	1	1					
6	0	1	1	1					
7	0	0	1	1					
8	0	0	0	1					



Johnson counter for decoder





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Design a Synchronous Counter

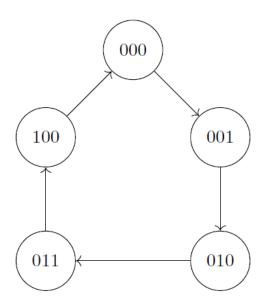
Recall: Design Procedure of Sequential Circuits

- 1. Specification: design description or timing diagram
- 2. Formulation: develop state diagram
- 3. Generate next-state table in form of count sequence
- 4. Choose type of Flip-Flop
- 5. Derive simplified excitation equations of FFs
- 6. Draw logic diagram



Modulo-N Counter

- Counters can be designed to generate any desired sequence of states. A divide-by-N counter (also known as a modulo- N counter)
- e.g. mod-5 counter
 - A counter that goes through the following binary repeated sequence: 0, 1, 2, 3, 4, 0, 1, 2, ...





Counters with Unused States

- n flops => 2ⁿ states
- Unused states
 - States that are not used in specifying the FSM, may be treated as don't-care conditions or may be assigned specific next states
- Self-correcting counters
 - Ensure that when a circuit enter one of its unused states, it eventually goes into one of the valid states after one or more clock pulses so that it can resume normal operation
 - Analyze the circuit to determine the next state from an unused state after it is designed

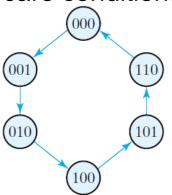


Example: Counters with Unused States

 Design a counter that goes through the following binary repeated sequence: 0, 1, 2, 4, 5, 6

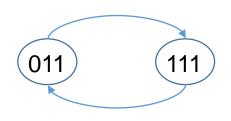
• The unused state is 011 & 111, they are considered as don't

care conditions.



Pre	sent S	State	ate	Flip-Flop Inputs							
Α	В	C	A	В	С	J _A	K _A	J _B	K _B	Jc	Kc
0	0	0	0	0	1	0	X	0	X	1	X
0	0	1	0	1	0	0	X	1	X	X	1
0	1	0	1	0	0	1	X	X	1	0	X
0	1	1	X	X	X	X	X	X	X	X	X
1	0	0	1	0	1	X	0	0	X	1	X
1	0	1	1	1	0	\mathbf{X}	0	1	X	X	1
1	1	0	0	0	0	X	1	X	1	0	X
1	1	1	X	X	X	X	X	X	X	X	X

- Lock out problem
 - It may be possible that the counter might go from one unused state to another and never arrive at a used state.



Pre	sent	Stat	Ne	xt Sta	ate	Flip-Flop Inputs					
Α	В	C	Α	В	С	J _A	K _A	J _B	K _B	J _C	K _C
0	1	1	1	1	1	1	1	0	0	0	0
1	1	1	0	1	1	1	1	0	0	0	0

since J and K are don't care condition



Counters with Unused States

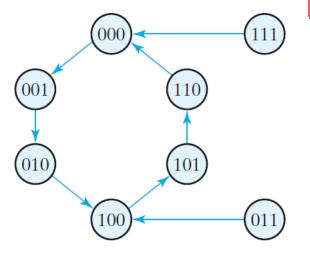
- To ensure that lock out does not occur, assuming 111→000, 011→100.
- Input equations:

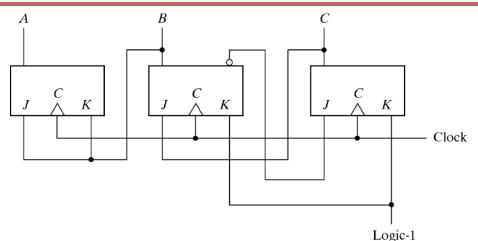
•
$$J_A = B$$
, $K_A = B$

•
$$J_B = C, K_B = 1$$

•
$$J_C = B', K_C = 1$$

Pre	sent S	State	Ne	xt Sta	ate	Flip-Flop Inputs					
A	В	С	A	В	C	J _A	K _A	J _B	K _B	Jc	Kc
0	0	0	0	0	1	0	X	0	X	1	X
0	0	1	0	1	0	0	X	1	X	X	1
0	1	0	1	0	0	1	X	X	1	0	X
0	1	1	1	0	0	1	X	X	1	X	1
1	0	0	1	0	1	X	0	0	X	1	X
1	0	1	1	1	0	X	0	1	X	X	1
1	1	0	0	0	0	X	1	X	1	0	X
1	1	1	0	0	0	X	1	X	1	X	1





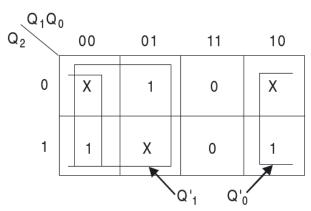
有方种技义等 SOUTHERN UNIVERSITY OF SCIENCE AND TECHNOLOGY

Exercise: Design a 5-bit Sequence Generator

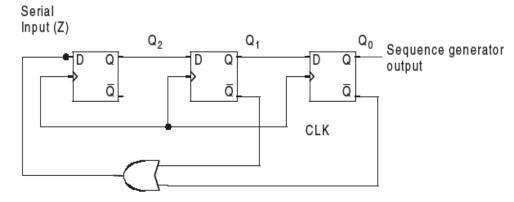
• Design of a sequence generator to generate a sequence of **10011**.

 $N \le 2^n - 1 \rightarrow n = 3 (3 \text{ FFs})$

CLK	Z	Q_2	Q_1	Q_0
↑	0	\bigwedge 1	1	1
↑	0	0	1	1
↑	1	0	0	1
↑	1	1	0	0
1	1	1	1	0



$$Z = Q_1' + Q_0'$$





Exercise: Design a mod-5 Counter

- mod-5 counter
 - A counter that goes through the following binary repeated sequence: 0, 1, 2, 3, 4, 0, 1, 2, ...

