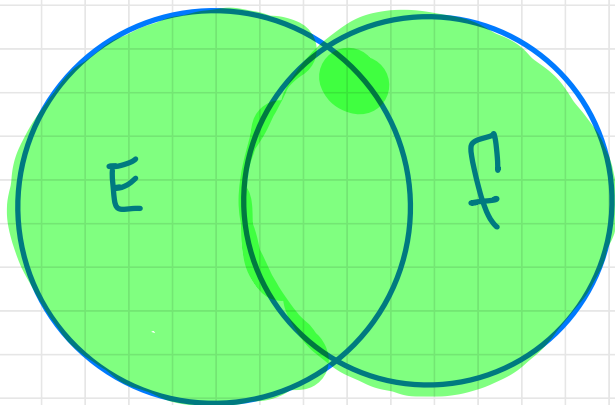


①

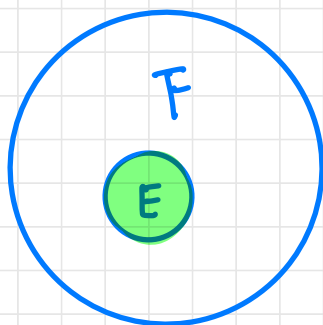
Daniel
Chong



a)

$$P(E \cup F) = \frac{1}{2} + \frac{1}{3} = \frac{3+2}{6} = \boxed{\frac{5}{6}}$$

b)



Smallest will be

$$e = \boxed{\frac{1}{2}}$$

$$c) P(E \cup F) = P(E) + P(F) - P(E \cap F)$$

$$\frac{1}{2} + \frac{1}{3} - \frac{1}{12} = \frac{6+4-1}{12}$$

$$= \frac{9}{12}$$

$$= \boxed{\frac{3}{4}}$$

2) a) (a, b, c) (a, c, b)
 (b, a, c) (b, c, a)
 (c, a, b) (c, b, a)

b) $\frac{1}{6}$ because there are 6 possible schedules, so you have 1 probability to have one of each.

c) $\frac{4}{6}$

3) A = Allison B = Betty C = Chelsea.

(A, B, C) (A, C, B)

(B, C, A) (B, A, C)

(C, A, B) (C, B, A)

4) $\frac{1}{8} + \frac{2}{8} + \frac{5}{8} = \frac{8}{8}$ of winning

So 0% chance of not winning.

$$5) a) P(A) = \left\{ \begin{matrix} (1,4) & (2,6) \\ (3,5) & (6,2) \\ (5,3) & (4,4) \end{matrix} \right\} \quad 6/36 = \boxed{1/6}$$

$$P(B) = \left\{ \begin{matrix} (3,1) & (3,4) \\ (3,2) & (3,5) \\ (3,3) & (3,6) \end{matrix} \right\}$$

$$b) P(A \cap B) = (3,5) = \boxed{1/36}$$

$$c) P(B|A) = \frac{1/36}{1/6} =$$

$$\frac{1}{36} \cdot \frac{6}{1} = \boxed{\frac{1}{6}}$$

$$6) \left. \begin{array}{l} 2 = G \\ 2 = F \\ 1 = C \end{array} \right\} \text{Team} \quad \left. \begin{array}{l} 5 = G \\ 3 = F \\ 4 = C \end{array} \right\} \text{available}$$

$$\binom{5}{2} \cdot \binom{3}{2} \cdot \binom{4}{1} + \binom{5}{1} \cdot \binom{3}{2} \cdot \binom{4}{1} + \binom{5}{2} \cdot \binom{3}{1} \cdot \binom{4}{1}$$

$$\frac{5!}{2!(5-2)!} = \frac{5 \cdot \cancel{4}^2 \cdot \cancel{3}}{\cancel{2} \cdot \cancel{3}} = 10 \quad \textcircled{1} \quad 10 \cdot 3 \cdot 4 = 120$$

$$5 \cdot 3 \cdot 4 = 60$$

$$\frac{3!}{2!(3-2)!} = \frac{3 \cdot \cancel{2}}{\cancel{2} \cdot 1!} = 3 \quad 10 \cdot 3 \cdot 4 = 120$$

$$\frac{4!}{1!(4-1)!} = \frac{4 \cdot \cancel{3}}{1! \cdot \cancel{3}} = 4$$

$$120 + 60 + 120 = \underline{\underline{300}}$$

$$\frac{5!}{1!(5-1)!} = \frac{5 \cdot \cancel{4}}{1! \cdot \cancel{4}} = 5$$

$$\frac{3!}{1!(3-1)!} = \frac{3 \cdot \cancel{2}}{1! \cdot \cancel{2}} = 3$$

$$b) \left. \begin{array}{l} 2 = G \\ 2 = F \\ 1 = C \end{array} \right\} \text{A Team} \quad \left. \begin{array}{l} 3 = G \\ 5 = F \\ 3 = C \\ 2 = X \end{array} \right\} \text{Roster}$$

$$\frac{13!}{5!(13-5)!}$$

$$\frac{13 \cdot \overset{6}{\cancel{12}} \cdot \overset{2}{\cancel{11}} \cdot \overset{3}{\cancel{10}} \cdot \overset{2}{\cancel{9}} \cdot \overset{3}{\cancel{8}}}{\underset{2}{5} \cdot \cancel{4} \cdot \cancel{3} \cdot \cancel{2} \cdot 1 \cdot \cancel{8}}$$

$$\frac{13 \cdot \underset{2}{3} \cdot 11 \cdot 2 \cdot 3}{2} = 1287$$

$$\begin{aligned} & \binom{3}{2} \cdot \binom{10}{2} \cdot \binom{3}{1} + \binom{3}{0} \cdot \binom{10}{2} \cdot \binom{3}{1} + \binom{3}{2} \cdot \binom{5}{0} \cdot \binom{3}{1} + \\ & \binom{3}{1} \cdot \binom{5}{1} \cdot \binom{3}{1} + \binom{3}{2} \cdot \binom{5}{1} \cdot \binom{3}{1} + \binom{3}{1} \cdot \binom{5}{2} \cdot \binom{3}{1} + \end{aligned}$$

$$\checkmark \quad \frac{3!}{2!(3-2)!} = \frac{3 \cdot \cancel{2}!}{\cancel{2}! 1!} = 3 \quad \frac{3!}{1!(3-1)!} = \frac{3 \cdot \cancel{2}!}{\cancel{2}!} = 3$$

$$\frac{5!}{2!(5-2)!}$$

$$\frac{5 \cdot \overset{2}{\cancel{4}} \cdot \cancel{3}!}{\cancel{2} \cdot \cancel{1} \cdot \cancel{3}!} = 10$$

$$\frac{3!}{0!(3-0)!}$$

$$\frac{\cancel{3}!}{0! \cdot \cancel{3}!} = \frac{1}{1} = 1$$

$$90 + 30 + 9 + 45 + 45$$

$$90 + 45 + 90$$

0.345

$$\frac{3!}{1!(3-1)!}$$

$$\frac{3 \cdot \cancel{2}!}{\cancel{2}!} = 3$$

$$\frac{5!}{2!(5-2)!}$$

$$\frac{5 \cdot \overset{2}{\cancel{4}} \cdot \cancel{3}!}{\cancel{2}! \cdot \cancel{3}!} = 10$$