

# Spatial Reading Group

## Optional Subtitle

February 9, 2017

# Outline

## First Main Section

First Subsection

Second Subsection

## Extension - Preferential Sampling

# Outline

## First Main Section

### First Subsection

### Second Subsection

## Extension - Preferential Sampling

# First Slide Title

Optional Subtitle

- ▶ My first point.
- ▶ My second point.

# Outline

## First Main Section

First Subsection

Second Subsection

Extension - Preferential Sampling

## Second Slide Title

- ▶ First item.

## Second Slide Title

- ▶ First item.
- ▶ Second item.

## Second Slide Title

- ▶ First item.
- ▶ Second item.
- ▶ Third item.



## Second Slide Title

- ▶ First item.
- ▶ Second item.
- ▶ Third item.
- ▶ Fourth item.

## Second Slide Title

- ▶ First item.
- ▶ Second item.
- ▶ Third item.
- ▶ Fourth item.
- ▶ Fifth item.

## Second Slide Title

- ▶ First item.
- ▶ Second item.
- ▶ Third item.
- ▶ Fourth item.
- ▶ Fifth item. Extra text in the fifth item.

# Preferential Sampling

## The Problem

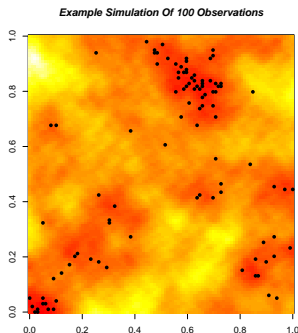
- ▶ So far we have assumed the sampling locations  $X$  are fixed, or assumed known.
- ▶ What if the sampling locations depend on the underlying field  $S$ ?

## Example

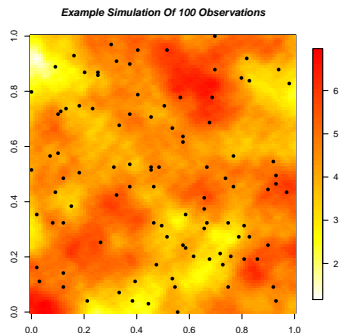
- ▶ Pollution data from measuring stations
- ▶ Ocean temperature data from marine mammals
- ▶ Lead concentration in Galicia (to be shown)

# Preferential Sampling

**Figure:** Example of a single realisation of  $S$  and corresponding 100 sampling locations selected using a spatial Poisson Process with intensity  $\lambda(x) = \exp(\beta S(x))$ .



(a) Example of 100 preferentially sampled locations ( $\beta = 2$ )



(b) Example of 100 non-preferentially sampled locations ( $\beta = 0$ )

# Preferential Sampling

## Solution

- ▶ We must account for the dependence between  $X$  and  $S$ .

$$L(\boldsymbol{\theta}) = \int [X, Y, S] \mathrm{d}S. \quad (1)$$

- ▶ Diggle et al. 2010 - Monte Carlo
- ▶ Integrated Nested Laplace Approximation (INLA) - Joe
- ▶ Template Model Builder - Danny

# Preferential Sampling

## Results

Model	Parameter	Standard MLE	<i>TMB</i>
Preferential	Bias	(0.77, 1.36)	(0.41, 0.94)
Preferential	Root-mean-square error	(0.86, 1.40)	(0.60, 1.05)

**Table:** Comparison of approximate 95% confidence intervals for the root-mean-square errors and bias between standard MLE and *TMB* over 50 independent simulations for preferential ( $\beta = 2$ ) at location  $x_0 = (0.49, 0.49)$ .

# Summary

- ▶ The **first main message** of your talk in one or two lines.
- ▶ The **second main message** of your talk in one or two lines.
- ▶ Perhaps a **third message**, but not more than that.
- ▶ Outlook
  - ▶ Something you haven't solved.
  - ▶ Something else you haven't solved.



# For Further Reading I



A. Author.

*Handbook of Everything.*

Some Press, 1990.



S. Someone.

On this and that.

*Journal of This and That*, 2(1):50–100, 2000.