$$O(\beta^{-6})$$