## Master's degree in Computer Science - A.A. 21/22

## OPTIMIZATION FOR MACHINE LEARNING - 6 CFU

## Project N. 4

Given the dataset **dataset4.mat**, where X is the matrix whose rows contain the points to be classified and y is the array of the corresponding class labels, perform a **spherical separation**, aimed at separating the set  $\mathcal{A}$  from the set  $\mathcal{B}$ , on the basis of the following guidelines:

- 1. Use the Gaussian kernel with  $\sigma = 1$ .
- 2. Choose the sets  $\mathcal{A}$  and  $\mathcal{B}$  at your convenience, between the two sets of points (positive with label +1 and negative with label -1).
- 3. Perform a bilevel 10-fold cross validation, using, for the model selection, a 5-fold cross validation. In fixing the grid of C, consider only the cases such that

$$C \ge \frac{1}{2r}$$
,

with  $r = \min\{m, k\}$ , where  $m = |\mathcal{A}|$  and  $k = |\mathcal{B}|$ .

4. Each time, fix the center  $x_0$  of the separating sphere

$$S(x_0, R) \stackrel{\triangle}{=} \{x \in R^n \mid ||x - x_0||^2 = R^2\}$$

as the bariycenter of the set A.

- 5. Compute the following performance indexes:
  - the average training correctness;
  - the average training sensitivity;
  - the average training specificity;
  - the average training F-score;
  - the average testing correctness (accuracy);
  - the average testing sensitivity;
  - the average testing specificity;
  - the average testing F-score.