Contribution of Persistent Na⁺ Current and M-Type K⁺ Current to Somatic Bursting in CA1 Pyramidal Cells: Combined Experimental and Modeling Study

David Golomb, 1 Cuiyong Yue, 2 and Yoel Yaari 2

¹Department of Physiology and Zlotowski Center for Neuroscience, Faculty of Health Sciences, Ben-Gurion University, Be'er-Sheva, Israel; and ²Department of Physiology, Institute of Medical Sciences, Hebrew University-Hadassah Faculty of Medicine, Jerusalem, Israel

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Golomb, David, Cuiyong Yue, and Yoel Yaari. Contribution of persistent Na+ current and M-type K+ current to somatic bursting in CA1 pyramidal cells: combined experimental and modeling Study. J Neurophysiol 96: 1912-1926, 2006. First published June 28, 2006; doi:10.1152/jn.00205.2006. The intrinsic firing modes of adult CA1 pyramidal cells vary along a continuum of "burstiness" from regular firing to rhythmic bursting, depending on the ionic composition of the extracellular milieu. Burstiness is low in neurons exposed to a normal extracellular Ca²⁺ concentration ([Ca²⁺]_o), but is markedly enhanced by lowering [Ca²⁺]_o, although not by blocking Ca²⁺ and Ca²⁺activated K+ currents. We show, using intracellular recordings, that burstiness in low [Ca²⁺]_o persists even after truncating the apical dendrites, suggesting that bursts are generated by an interplay of membrane currents at or near the soma. To study the mechanisms of bursting, we have constructed a conductance-based, one-compartment model of CA1 pyramidal neurons. In this neuron model, reduced [Ca²⁺]_o is simulated by negatively shifting the activation curve of the persistent Na^+ current (I_{NaP}) as indicated by recent experimental results. The neuron model accounts, with different parameter sets, for the diversity of firing patterns observed experimentally in both zero and normal $[Ca^{2+}]_o$. Increasing I_{NaP} in the neuron model induces bursting and increases the number of spikes within a burst but is neither necessary nor sufficient for bursting. We show, using fast-slow analysis and bifurcation theory, that the M-type K^+ current (I_M) allows bursting by shifting neuronal behavior between a silent and a tonically active state provided the kinetics of the spike generating currents are sufficiently, although not extremely, fast. We suggest that bursting in CA1 pyramidal cells can be explained by a single compartment "square bursting" mechanism with one slow variable, the activation of $I_{\mathbf{M}}$.

INTRODUCTION

The intrinsic discharge mode of individual cortical pyramidal cells varies along a spectrum of "burstiness," from regular firing evoked by depolarization of the neuron to spontaneous bursting unprovoked by any extrinsic stimuli (Jensen et al. 1994; Schwartzkroin 1975; for a detailed description of firing and bursting patterns, see Fig. 1 in Su et al. 2001). A large body of evidence now indicates that the propensity of a neuron to burst depends not only on its constitution, i.e., the nature and properties of ionic conductances expressed in its plasma membrane, but also on its environment, i.e., the ionic composition of the milieu in which it is embedded. Thus regular firing pyramidal cells readily convert to a bursting mode when the

extracellular concentrations of Ca²⁺ ([Ca²⁺]_o) or K⁺ ([K⁺]_o) decrease or increase, respectively (Jensen et al. 1994; Su et al. 2001). Such changes in extracellular ion composition accompany neuronal activity (Heinemann et al. 1977), which may explain why the propensity for bursting of pyramidal cells increases with the level of activity in their surrounds (Harris et al. 2001). Interestingly, blocking Ca²⁺ currents or Ca²⁺-activated K⁺ currents (Azouz et al. 1996; Jensen et al. 1994; Su et al. 2001) does not increase the propensity for bursting. Given that the bursting mode plays important roles in electrical signaling, normal and abnormal neuronal synchronization, and induction of long-term synaptic plasticity (Izhikevich et al. 2003; Lisman 1997; Yaari and Beck 2002), it is important to understand how constitution and environment interact in regulating this discharge mode. To date, most theoretical studies of intrinsic bursting have focused on the former factor.

In neocortical, subicular, and CA3 pyramidal cells, intrinsic bursting has been attributed to recruitment of Ca²⁺ currents by the primary Na⁺ spike (Chen et al. 2005; Jung et al. 2001; Larkum et al. 1999; Metz et al. 2005; Wong and Prince 1981). In line with these experimental observations, many models of Ca²⁺ current-dependent bursting suggest a "ping-pong" interplay between fast Na⁺ and K⁺ currents in the soma and slow Ca²⁺ and K⁺ (mostly Ca²⁺-dependent) currents in the apical dendrites (Mainen and Sejnowski 1996; Pinsky and Rinzel 1994; Traub and Miles 1991; Traub et al. 1991, 1994; Warman et al. 1994). In adult CA1 pyramidal cells, however, bursting behavior persists after almost complete truncation of the apical dendrites (Yue et al. 2005). Therefore the mechanism of bursting in the latter neurons may be different from the pingpong mechanism, which depends on the integrity of apical dendrites.

We study the mechanism by which changes in $[Ca^{2+}]_o$ modulate transitions between regular firing and bursting in adult CA1 pyramidal cell by combining electrophysiological, computational, and analysis techniques.

METHODS

Hippocampal slices

All animal experiments were conducted in accordance with the guidelines of the Animal Care Committees of the Hebrew University. Adult male Sabra rats were decapitated under deep isoflurane anes-

Address for reprint requests and other correspondence: D. Golomb, Dept of Physiology, Faculty of Health Sciences, Box 653, Ben-Gurion University, Be'er-Sheva 84105, Israel (E-mail: golomb@bgu.ac.il).

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thesia, and transverse hippocampal slices (400 µm) were prepared with a vibrating microslicer (Leica) and transferred to a storage chamber perfused with oxygenated (95% O₂-5% CO₂) artificial cerebrospinal fluid (ACSF) containing (in mM) 124 NaCl, 3.5 KCl, 2 MgCl₂, 1.6 CaCl₂, 26 NaHCO₃, and 10 D-glucose, pH 7.4, osmolarity 305 mosM, where they were maintained at room temperature. Slices were placed one at a time in an interface chamber (33.5°C) and perfused with oxygenated ACSF. To truncate the apical dendrites of CA1 pyramidal cells, a deep cut was made in stratum radiatum close to and parallel to stratum pyramidale using a broken pipette or a razor blade chip propelled by a micromanipulator (Yue et al. 2005). Truncation was confirmed by recording field potentials in stratum pyramidale (see following text) before and after cutting. Orthodromic field potentials evoked by stimulating in stratum radiatum disappeared after cutting, while antidromic field potentials evoked by stimulating in alveus remained large (Yue et al. 2005). The slices were allowed to recover in the chamber for ≥ 1 h before initiating a recording session.

Electrophysiological recordings

Intracellular recordings were obtained using sharp glass microelectrodes containing 4 M K⁺-acetate (90–110 M Ω). An active bridge circuit in the amplifier (Axoclamp 2B, Axon Instruments, Foster City, CA) allowed simultaneous injection of current and measurement of membrane potential. The bridge balance was carefully monitored and adjusted before each measurement. The intracellular signals were filtered on-line at 10 kHz, digitized at a sampling rate of \geq 10 kHz, and stored by a personal computer using a data-acquisition system (Digidata 1322A) and pCLAMP software (Axon Instruments).

Drugs

Stock solutions of 4β -phorbol 12,13-dibutyrate (PDB; 10 mM), riluzole (10 mM), and phenytoin (100 mM) were prepared in dimethyl sulfoxide (DMSO) and stored at -20° C. They were usually diluted at 1:1,000 when added to the ACSFs. Control ACSFs contained equal amounts of DMSO (0.001%), which by itself had no effects on the measured parameters. All other drugs were added to the ACSFs from aqueous stock solutions. Chemicals and drugs were obtained from Sigma (Petach-Tikva, Israel).

Cell model

The somatic, single-compartment model was represented by coupled differential equations according to the Hodgkin-Huxley-type scheme. We constructed the model in two stages. In the first stage, we introduced only the ionic currents that are involved in firing dynamics in 0 [Ca²⁺]_o, at which it is simpler to analyze. In the second state, we added voltage-gated Ca²⁺ and Ca²⁺-activated K⁺ currents, to explore their influence on bursting behavior.

MODEL FOR 0 [CA²⁺]_o. The model includes the currents that are known to exist in the soma and proximal dendrites: the transient Na⁺ current ($I_{\rm Na}$) and the delayed rectifier K⁺ current ($I_{\rm Kdr}$) that generate spikes, and the muscarinic-sensitive K⁺ current ($I_{\rm M}$) that contributes the slow variable necessary for bursting (Bertram et al. 1995; Yue and Yaari 2004, 2006). A model with these three currents only is the minimal model that allows bursting. We added the persistent sodium current ($I_{\rm NaP}$) because we wanted to focus on its contribution to bursting (Su et al. 2001; Yue et al. 2005). The A-type K⁺ current ($I_{\rm A}$) is included as well even though its density is much higher in the apical dendrites than in the soma (Hoffman et al. 1997). The current balance equation is (Borg-Graham 1999)

$$C\frac{dV}{dt} = -g_{L}(V - V_{L}) - I_{Na} - I_{NaP} - I_{Kdr} - I_{A} - I_{M} + J_{app}$$
 (1)

where $C = 1 \mu F/cm^2$, $g_L = 0.05 \text{ mS/cm}^2$, $V_L = -70 \text{ mV}$, and I_{app} is

the applied current. The ionic currents are: $I_{\rm Na}(V, h) = g_{\rm Na} m_{\rm M}^3(V) h(V - V_{\rm Na}), I_{\rm NaP}(V) = g_{\rm NaP} p_{\rm m}(V) (V - V_{\rm Na}), I_{\rm Kdr}(V, n) = g_{\rm Kdr} n^4 (V - V_{\rm K}), I_{\rm A}(V, b) = g_{\rm A} a_{\rm m}^3(V) b(V - V_{\rm K}), I_{\rm M}(V, z) = g_{\rm M} z(V - V_{\rm K}).$ The conductances and reversal potentials are: $g_{\rm Na} = 35 \, {\rm mS/cm^2}, g_{\rm NaP}$ varies between 0 and 0.41 mS/cm², $g_{\rm Kdr} = 6 \, {\rm mS/cm^2}, g_{\rm A} = 1.4 \, {\rm mS/cm^2}, g_{\rm M} = 1 \, {\rm mS/cm^2}, V_{\rm Na} = 55 \, {\rm mV}, V_{\rm K} = -90 \, {\rm mV}.$ The kinetics equations and parameters are listed in Table 1. The cell model for zero [Ca²⁺]_o has five dynamical variables: $V_{\rm N} = 0.0 \, {\rm m}$ and $V_{\rm N} = 0.0 \, {\rm m$

MODEL FOR NONZERO [CA²+]_O. This second model includes all the currents that belong to the first model, with the same parameters (except for the effect of [Ca²+]_O on θ_p , the half-maximum potential of $I_{\rm NaP}$; see Table 1). In addition, we added three more ionic currents: the high-threshold Ca²+ current ($I_{\rm Ca}$), and two Ca²+-activated K+ currents, namely, the fast Ca²+-activated K+ current ($I_{\rm C}$), which contributes to rapid spike repolarization (Storm 1987), and the slow Ca²+-activated K+ current ($I_{\rm SAHP}$), which mediates a slow afterhyperpolarization (AHP) and spike frequency adaptation (Madison and Nicoll 1984). This model includes, therefore the most important currents known in somata and proximal axons of CA1 cells. The current balance equation in this variation of the model is

$$C\frac{dV}{dt} = -g_{L}(V - V_{L}) - I_{Na} - I_{NaP} - I_{Kdr} - I_{A} - I_{Ca} - I_{C} - I_{SAHP} + I_{app}$$
(2)

The ionic currents are: $I_{\rm Ca}(V,r) = g_{\rm Ca} r^2 (V-V_{\rm Ca}), \ I_{\rm C}(V,c) = g_{\rm C} d_{\infty}([{\rm Ca}^{2+}]_i) c(V-V_{\rm K}), \ I_{\rm sAHP}(V,q) = g_{\rm sAHP} q(V-V_{\rm K}).$ The conductances and reversal potentials are: $g_{\rm Ca}$ is typically between 0 and 0.2 mS/cm², $g_{\rm C}=10$ mS/cm², $g_{\rm sAHP}=5$ mS/cm², $V_{\rm Ca}=120$ mV. The kinetics equations and parameters are listed in Table 2. The dynamics of the calcium concentration inside the cell, $[{\rm Ca}^{2+}]_i$ are

$$\frac{d[Ca^{2+}]_{i}}{dt} = -vI_{Ca} - [Ca^{2+}]_{i}/\tau_{Ca}$$
 (3)

 $v=0.13~{\rm cm^2/(ms}\times\mu{\rm A}),~\tau_{\rm Ca}=13~{\rm ms}.$ The variable $[{\rm Ca^{2+}}]_{\rm i}$ in our model is dimensionless (Traub et al. 1994). It is proportional to the ${\rm Ca^{2+}}$ concentration in a thin internal cylindrical shell adjacent to the membrane.

The low-threshold T-type Ca²⁺ current was not included in the model because it is localized mostly in the distal apical dendrites of adult CA1 pyramidal cells (Karst et al. 1993; Thompson and Wong 1991). The hyperpolarization-activated cationic current (I_b) (Magee 1998; Vasilyev and Barish 2002) was not included in the model because its density in the soma is much lower than in the apical dendrites (Magee 1998) and because the activation kinetics of the largest component of I_h are faster than that of I_M (Maccaferri and McBain 1996; Magee 1998; Spain et al. 1987) and cannot support bursting via a mechanism based on two slow variables (Bertram et al. 1995). The apamin-sensitive, small-conductance (SK) Ca²⁺-activated K^+ current (I_{AHP}) , which can be evoked under voltage-clamp conditions in CA1 pyramidal cells (Gu et al. 2005; Stocker et al. 1999), was not included in the model. The reason for this exclusion is that in current-clamp recordings this current does not contribute appreciably to spike frequency adaptation and the medium AHP (Gu et al. 2005).

NUMERICAL METHODS. Simulations were performed using the fourth-order Runge-Kutta method with a time step of 0.05 ms implemented as a C program or within the software package XPPAUT (Ermentrout 2002), that was used also for computing bifurcation diagrams.

STIMULATION. We analyzed the firing patterns of the neuron model in response to two types of stimuli, namely, brief and prolonged square positive current pulses. In the former case, pulse duration was 3 ms, so it could evoke a spike response without interfering with spike afterpotentials (Su et al. 2001; Yue and Yaari 2004). In the latter case,

TABLE 1. Kinetics equations and parameters for the $0 [Ca^{2+}]_o$ model

Current, Variable	Kinetics/Time Constant, ms Parameters		References/ Comments
I_{Na}, m	$m=m_{\infty}(V)$	$\theta_{m} = -30 \text{mV}, \sigma_{m} = 9.5 \text{mV}.$	1
$I_{\text{Na}}^{\text{Na}}, h$	$dh/dt = \phi[\hat{h}_{\infty}(V) - h]/\tau_h(V)$	$\theta_h^m = -45 \text{mV}, \sigma_h^m = -7 \text{mV},$	1
	$\tau_h(V) = 0.1 + 0.75 \times \{1 + \exp[-(V - \theta_{ht})/\sigma_{ht}]\}^{-1}$	$\theta_{ht} = -40.5 \text{mV}, \sigma_{ht} = -6 \text{mV}, \phi = 1.$	
I_{NaP}, p	$p = p_{\infty}(V)$	$-47 \text{mV} \le \theta_p \le -41 \text{mV}, \sigma_p = 3 \text{mV}.$	2
I_{Kdr}, n	$dn/dt = \phi[n_{\infty}(V) - n]/\tau_n(V)$	$\theta_n = -35 \text{mV}, \sigma_n = 10 \text{mV},$	3
	$\tau_n(V) = 0.1 + 0.5 \times \{1 + \exp[-(V - \theta_{nt})/\sigma_{nt}]\}^{-1}$	$\theta_{nt} = -27 \text{mV}, \sigma_{nt} = -15 \text{mV}, \phi = 1.$	
I_{Kdr}, a	$a = a_{\infty}(V)$	$\theta_{a} = -50 \text{mV}, \sigma_{a} = 20 \text{mV}.$	4
I_{Kdr}, b	$db/dt = [b_{\infty}(V) - b]/\tau_b, \tau_b = 15$	$\theta_{b} = -80 \text{mV}, \sigma_{b} = -6 \text{mV}.$	4
$I_{\mathbf{M}}, z$	$dz/dt = [z_{\infty}(V) - z]/\tau_z, \tau_z = 75$	$\theta_z = -39 \text{mV}, \sigma_z = 5 \text{mV}.$	5

The activation and inactivation curves $x_{\infty}(V)$ are determined by the equation $x_{\infty}(V) = \{1 + \exp[-(V - \theta_x)/\sigma_x]\}^{-1}$ where x = m, h, n, a, b, z. References and comments: I) Fleidervish et al. (1996), Martina and Jonas (1997); Sah et al. (1998b); and Golomb and Amitai (1997). The difference between θ_m and θ_h is smaller than what is usually measured in pyramidal cell somata, partially because the activation curve of axons in pyramidal cells is shifted toward more hyperpolarized values (Colbert and Pan 2002). 2) French et al. (1990). In the cerebellum (Kay et al. 1998) and the entorhinal cortex (Magistretti et al. 2003), these kinetics were found to be as fast as the kinetics of I_{Na} in the submillisecond regime time scale. Therefore we consider the kinetics of I_{Na} to be instantaneous. Recent experiments in CA1 pyramidal cells show that reducing Ca^{2+} concentration leads to a significant negative shift to θ_p [Yue et al. 2005; see also Li and Hatton 1996). Therefore, θ_p is varied throughout the paper (typically between -47 mV at 0 [Ca^{2+}] and -41 mV at physiological [Ca^{2+}] values). 3) Martina et al. (1998); Sah et al. (1998a); 4) Hoffman et al. (1997); Rush and Rinzel (1995); and 5) Halliwell and Adams (1982).

pulse duration was very long, allowing neuronal dynamics to reach steady-state behavior (mathematically, converging to an attractor). There were also conditions in which the neuron model fired spontaneously without application of positive currents.

FIRING PATTERNS. Depending on the model parameters, the neuron model might fire in one of two patterns when stimulated with prolonged positive current pulses. I) Regular, tonic firing, in which neurons fired solitary spikes in a periodic manner. Often, two distinct types of tonic firing were observed: low-frequency tonic firing at frequencies of up to ~ 5 Hz; and high-frequency tonic firing, in which neurons fired continuously at ~ 100 Hz. 2) Rhythmic bursting, in which sequential bursts were separated by periods of neuronal quiescence, typically lasting several hundreds of milliseconds. Rhythmic bursting was either periodic or aperiodic (chaotic) (Terman 1992).

BURSTING. In this study, we defined a burst as a tight cluster (inter-spike interval in the order of 10 ms) of two or more spikes generated alone (as in the case of bursts evoked by brief stimuli) or distinctly separated from the following spikes (as in the cases of spontaneous bursting or bursting evoked by prolonged stimuli). In the cases of prolonged or spontaneous activity, we quantified bursting behavior at long times (after the dynamics has converges to an attractor), namely after transient effects of the initial conditions have decayed. The average number of intraburst spikes (N_s) was computed by averaging the number of spikes per burst during a 1.5-s period 1 s after stimulus onset (i.e., after the dynamics has converged to an attractor) and rounding up this average to the closest integer. Doublet states were particular cases of periodic bursting states in which the

neuron model fired exactly two spikes in a burst, namely, $N_{\rm S}=2$ (Mandelblat et al. 2001). Clearly, in regular spiking cells $N_{\rm S}=1$.

Fast-slow analysis

We used the fast-slow method (Bertram et al. 1995; Hoppensteadt and Izhikevich 1997; Izhikevich 2000, 2006; Rinzel and Ermentrout 1998) to study the bursting mechanism, to determine the role of the currents I_{NaP} and I_{M} in the dynamics, and to determine the necessary conditions for bursting. This method has been applied successfully to analyze periodic bursting of various biophysical models of neurons (e.g., Mandelblat et al. 2001). We applied the method for the case $[\mathrm{Ca}^{2+}]_{\mathrm{o}} = 0$ (and thus $\theta_p = -47$ mV and $g_{\mathrm{Ca}} = 0$) because it has simpler dynamics. The analysis is based on separating the dynamical variables of the system into two subsystems, "fast" and "slow." The model has five dynamic variables: V, h, n, b, and z. The first four variables are considered to be "fast" and belong to the fast subsystem. The variable z is considered to be "slow." The analysis is exact in the limit $\tau_z \to \infty$, where τ_z is the time constant of z. It describes an approximation of the dynamics for large but finite τ_z . In the first stage of the analysis, the bifurcation diagram of the fast subsystem was computed with the slow variable z considered as a parameter. In the second stage, the dynamics of z itself were computed using the time-averaged values of the fast subsystem.

If the dynamics of the fast subsystem converges to a stable rest state (fixed point), V is determined by its value for the fixed point of the fast subsystem for the instantaneous value of z, denoted by $V_{\text{rest,fast}}(z)$, whereas z evolves slowly (Table 1). If $z_{\infty}[V_{\text{rest,fast}}(z)] > z$, z increases

TABLE 2. Kinetics equations and parameters for the non-zero $[Ca^{2+}]_o$ model

Current, Variable	Kinetics/Activation	Time Constant, ms	Parameters	References/ Comment
I_{Ca}, r	$\mathrm{d}r/\mathrm{d}t = [r_{\infty}(V) - r]/\tau_r$	$\tau_r = 1$	$\theta_r = -20 \text{mV},$	1
	$r_{\infty}(V) = \{1 + \exp[-(V - \theta_r)/\sigma_r]\}^{-1}$		$\sigma_r = 10 \text{mV}$	
$I_{\rm C}$, c , d	$dc/dt = [c_{\infty}(V) - c]/\tau_c$	$\tau_c = 2$	$\theta_c = -30 \text{mV},$	2
	$d = d_{\infty}([\operatorname{Ca}^{2+}]_{i})$		$\sigma_c = 7 \text{mV},$	
	$c_{\infty}(V) = \{1 + \exp[-(V - \theta_c)/\sigma_c]\}^{-1}$		$a_c = 6$	
	$d_{\infty}([Ca^{2+}]_i) = (1 + a_c/[Ca^{2+}]_i)^{-1}$			
I_{sAHP}, q	$dq/dt = [q_{\infty}([Ca^{2+}]_i) - q]/\tau_q$	$\tau_q = 450$	$a_q = 2$	2
	$q_{\infty}([Ca^{2+}]_i) = (1 + a_q^4/[Ca^{2+}]_i^4)^{-1}$			

References and comments: 1) Kay and Wong (1987) and 2) Lancaster and Adams (1986). The current I_C is fast and is controlled by both V and $[Ca^{2+}]_i$, whereas I_{SAHP} is slow and is controlled by $[Ca^{2+}]_i$ only.

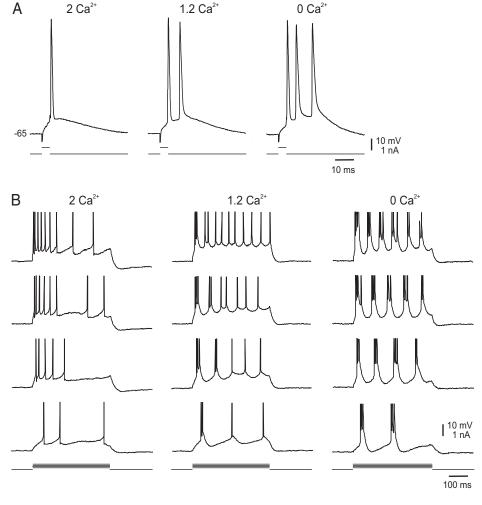


FIG. 1. Effects of lowering [Ca²⁺]_o on the firing mode of a truncated CA1 pyramidal cell. A: in normal artificial cerebrospinal fluid (ACSF; 2 mM Ca²⁺) the neuron fired a solitary spike in response to suprathreshold brief depolarizing current pulses (left). Sequentially lowering $[Ca^{2+}]_0$ to 1.2 mM (*middle*) and to nominally 0 mM (right) caused spike afterdepolarization (ADP) augmentation which converted the single spike response to a burst of 2 and 3 spikes, respectively. B: stimulating with longer (180 ms) depolarizing current pulses of increasing intensity induced repetitive firing. In normal ACSF, the neuron generated an accommodating train of independent spikes (left). Reducing [Ca2+], to 1.2 and to nominally 0 mM converted these responses to repetitive bursting with much less adaptation (middle and right).

slowly, and if $z_{\infty}[V_{\text{rest,fast}}(z)] < z$, z decreases slowly. If, for a certain value of z denoted by z_{FP} , $z_{\infty}[V_{\text{rest,fast}}(z_{\text{FP}})] = z_{\text{FP}}$, namely, the line representing the stable rest state, $V_{\text{rest,fast}}(z)$, intersects with $z_{\infty}(V)$, the activation carve of z (Table 1), the point $[V_{\text{rest,fast}}(z_{\text{FP}}), z_{\text{FP}}]$ represents a fixed point of the full system. It is stable if $dV_{\text{rest,fast}}(z)/dz < [dz_{\infty}(V)/dV]^{-1}$. The dynamics of the fast subsystem may converge also to a stable tonic firing state (limit cycle), where T_z is the time period of the cycle that depends on z. The approximation that τ_z is much larger than the other time scales in the system, and, specifically, $\tau_z > T_z$, means that z does not vary significantly during one cycle of the fast subsystem. Therefore we can average the dynamical equation for dz/dt (Table 1) over one cycle of the fast, tonic firing to obtain (Bertram et al. 1995; Izhikevich 2006; Mandelblat et al. 2001)

$$\left\langle \frac{\mathrm{d}z}{\mathrm{d}t} \right\rangle = \left[z_{\infty}(V_{\mathrm{equiv}}) - z \right] / \tau_{z}$$
 (4)

where $\langle\ldots\rangle$ denotes time average over a period T_z and $V_{\rm equiv}$ is defined implicitly by the equation

$$z_{\infty}(V_{\text{equiv}}) = \frac{1}{T_z} \int_0^{T_z} z_{\infty}(V(t)) dt$$
 (5)

In the slow time scale, we can replace $\langle \mathrm{d}z/\mathrm{d}t \rangle$ by $\mathrm{d}z/\mathrm{d}t$. Therefore the dynamics of the slow variable z is determined, on average, by the right hand side of Eq.~5. If $z_{\infty}[V_{\mathrm{equiv}}(z)] > z$, z increases slowly, and if $z_{\infty}[V_{\mathrm{equiv}}(z)] < z$, z decreases slowly. We consider the case where, for a certain value of z denoted by z_{LC} , the line representing $V_{\mathrm{equiv}}(z)$ intersects with the activation carve of z, $z_{\infty}(V)$, namely $z_{\infty}[V_{\mathrm{equiv}}(z_{\mathrm{LC}})] =$

 $z_{\rm LC}$. In this case, the point $(V_{\rm equiv}(z_{\rm LC}), z_{\rm LC})$ represent a limit cycle of the full system. It is stable if ${\rm d}V_{\rm equiv}(z)/{\rm d}z < [{\rm d}z_{\infty}(V)/{\rm d}V]^{-1}$. In particular, the limit cycle is stable if the slope of $V_{\rm equiv}(z)$ at $z=z_{\rm LC}$ is negative.

RESULTS

Effects of lowering $[Ca^{2+}]_o$ on truncated CA1 pyramidal cells

We have recorded from 24 CA1 pyramidal cells after truncation of their apical dendrites. When activated with brief (3–4) ms) depolarizing current pulses, truncated neurons displayed normal spikes followed by a distinct, albeit variable in size, afterdepolarization (ADP; Fig. 1A, *left*). The mean (\pm SE) resting potential, apparent input resistance, and spike amplitude of these neurons were -67.8 ± 0.5 mV (range, -75 to -61 mV), $40.1 \pm 2.0 \text{ M}\Omega$ (range, 20.5 to 48.7 M Ω), and 92.1 ± 5.7 mV (range, 71.7 to 103.2 mV), respectively. These values are well within the values obtained for intact neurons (Yue and Yaari 2004; Yue et al. 2005) and indicate that despite the damage inflicted by the cut and loss of most apical dendrites, the electrophysiological properties of the axo-soma are well preserved. When activated with prolonged (200 ms) depolarizing current pulses of increasing intensities, the neurons discharged repetitively and displayed spike frequency adaptation (Fig. 1B, left). Like in intact neurons (Su et al. 2001; Yue et al. 2005), approximately half of the neurons were

nonbursters and the other half were mostly high-threshold bursters (bursting only in response to long depolarizing current pulses of 2–3 times threshold intensity) with a small subset of low-threshold bursters (bursting in response to threshold-straddling stimuli).

In all 24 truncated neurons examined, lowering $[Ca^{2+}]_o$ from 2 to nominally 0 mM caused a progressive increase in the spike ADP. In 19 of these neurons (79.2%), the increase in spike ADP culminated in a high-frequency burst of three to six spikes as their minimal response to threshold depolarization (Fig. 1A). Lowering $[Ca^{2+}]_o$ also reduced spike frequency adaptation (Fig. 1B). These effects are similar to those described previously in intact neurons (Azouz et al. 1996; Su et al. 2001). Thus functional apical dendrites are not required for the expression of bursting behavior in low $[Ca^{2+}]_o$.

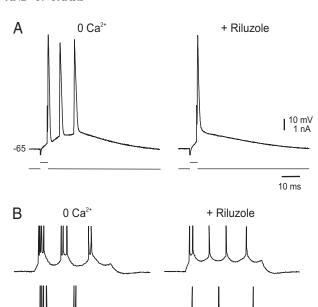
In nominally Ca²⁺-free ACSF, many of the neurons converted to bursting mode manifested rhythmic bursting at their native resting potential (see following text, Fig. 4A) or at more depolarized potentials. Increasing the depolarizing current intensity enhanced the frequency of bursting without strongly affecting the shape of individual bursts. However, at the higher frequencies of bursting, the number of intraburst spikes progressively decreased with time (Fig. 1B, right).

Effects of blocking persistent Na⁺ current

A previous study in intact CA1 pyramidal cells concluded that the augmented spike ADPs and bursting behavior in low [Ca²⁺]_o are driven predominantly by persistent Na⁺ current (I_{NaP}) (Su et al. 2001). To extrapolate this finding to truncated neurons, we tested the effects of the I_{NaP} blocker riluzole (Yue et al. 2005) on bursting induced by low [Ca²⁺]_o in five such neurons. Riluzole (10 μ M) blocks I_{NaP} in CA1 pyramidal cells almost completely while exerting a lesser effect on the transient Na⁺ current (Spadoni et al. 2002; Urbani et al. 2000; Yue et al. 2005). Representative results are shown in Fig. 2. Adding 10 μ M riluzole to the ACSF abolished low Ca²⁺-induced bursting (Fig. 2A) and converted rhythmic bursting during prolonged depolarizations to regular firing (Fig. 2B). Similar results were obtained (data not shown) with 100 μ M phenytoin (n = 3) and 5 μ M PDB (n = 2), which also block I_{NaP} (Cantrell et al. 1996; Chao and Alzheimer 1995; Yue et al. 2005). Together, these data strongly suggest that bursting in low $[Ca^{2+}]_o$ is driven predominantly by I_{NaP} .

Effects of blocking M-type K⁺ current

Because inactivation of $I_{\rm NaP}$ in CA1 pyramidal cells is very slow (in the order of seconds) (French et al. 1990), burst termination likely involves activation of an outward K⁺ current. In nominally Ca²⁺-free ACSF, Ca²⁺-activated K⁺ currents are inoperative. Hence a likely candidate for burst termination in this condition is the M-type K⁺ current ($I_{\rm M}$), previously shown to activate during the spike ADP and repolarize the neuron back to its resting potential (Yue and Yaari 2004). We tested this notion using linopirdine and XE991, selective blockers of $I_{\rm M}$ (Schnee and Brown 1998; Wang et al. 1998). Representative results from one truncated neuron bathed in Ca²⁺-free ACSF are shown in Fig. 3. When activated by brief depolarizing pulses, the neuron generated a burst of three spikes (Fig. 3A, left). Adding 10 μ M linopirdine to the Ca²⁺-free ACSF markedly prolonged the burst and delayed repolar



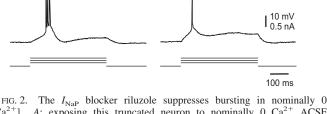
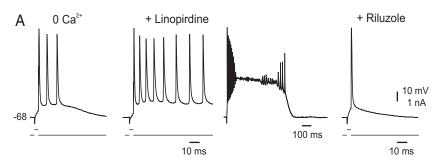


FIG. 2. The $I_{\rm NaP}$ blocker riluzole suppresses bursting in nominally 0 $[{\rm Ca^{2^+}}]_{\rm o}$. A: exposing this truncated neuron to nominally 0 ${\rm Ca^{2^+}}$ ACSF converted it to a low-threshold bursting mode (left). Adding 10 μ M riluzole to the ACSF suppressed bursting within 24 min of exposure (right). B: in the same neuron, repetitive bursting evoked by long depolarizing current pulses (left) was converted to a regular firing mode by riluzole (right).

ization of the neuron for several hundreds of milliseconds (Fig. 3A, middle). Both the primary burst and the underlying plateau potentials were readily suppressed by subsequent addition of 10 μM riluzole to the ACSF (Fig. 3A, right), suggesting that they are driven by I_{NaP} . Similar results were obtained when the neuron was stimulated with prolonged depolarizing current pulses that induced rhythmic bursting (Fig. 3B, left). Under the influence of linopirdine, rhythmic bursting converted to a plateau depolarization that lasted throughout the period of stimulation (Fig. 3B, middle). Again, adding 10 µM riluzole to the ACSF suppressed the initial burst responses and the plateau depolarizations and imposed a regular firing mode (Fig. 3B, right). Similar results were obtained in five truncated neurons treated with 10 µM linopirdine and two truncated neurons treated with 3 µM XE991. Together these data suggest that bursting in truncated neurons bathed in Ca²⁺-free ACSF is due to interplay between I_{NaP} and I_{M} .

Construction of an experimentally based model

We have constructed a model of CA1 pyramidal cells to further understand the mechanisms underlying their somatic bursting. The results of the model are compared with the experimental results from the following aspects. First, can the model account for the variant firing patterns observed experimentally as its parameters are varied? Second, do the propen-



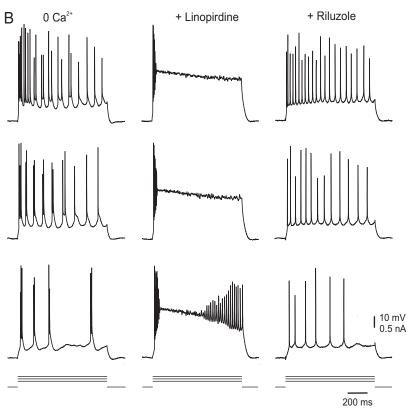


FIG. 3. The $I_{\rm M}$ blocker linopirdine converts repetitive bursting in nominally 0 $[{\rm Ca^{2+}}]_{\rm o}$ to plateau depolarizing potentials. A: exposing this truncated neuron to nominally 0 ${\rm Ca^{2+}}$ ACSF converted it to a low-threshold bursting mode (left). Exposing the neuron to $10~\mu{\rm M}$ linopirdine for 20 min converted the 3-spike burst to a prolonged burst followed by a sustained depolarizing lasting hundreds of milliseconds (middle and inset). The burst and associated plateau depolarization were readily suppressed by subsequent addition of $10~\mu{\rm M}$ riluzole (right). B: in the same neuron, repetitive bursting evoked by long depolarizing current pulses (left) was converted to a sustained plateau potential (middle), which was converted to a regular firing by riluzole (right).

sity for bursting and N_S vary in a similar manner in the model and in the experiments as $I_{\rm app}$, $g_{\rm NaP}$, or $g_{\rm M}$ vary? Finally, are the influences of $g_{\rm Ca}$, $g_{\rm C}$, and $[{\rm Ca^{2+}}]_{\rm o}$ on the propensity for bursting and N_S similar in the model and in the experiments? We have included in the model neuronal dynamics with only two time scales, namely that of spikes (a few milliseconds) and that of bursting (~ 100 ms). Experimentally, we found that many CA1 pyramidal cells also exhibited very slow dynamics (>1 s) that may cause rhythmic bursting to change eventually to repetitive spikes (Figs. 1B, middle, and 3B, left, 2 top traces). The very slow dynamics, however, often reached a steady state. In those cases, the neurons displayed rhythmic bursting continuously, as shown in Fig. 4A. Therefore we omitted the very slow dynamics from the model, allowing it also to manifest rhythmic bursting (Fig. 4B).

Fast-slow analysis of the necessary conditions for bursting and the roles of I_{NaP} and I_{M}

We have shown in the preceding text that two currents, namely $I_{\rm NaP}$ and $I_{\rm M}$, play essential roles in bursting in truncated

CA1 pyramidal cells bathed in 0 [Ca²⁺]_o. The I_{NaP} is considered here to be nonactivating (at the relevant time scales), and its activation variable, p, is considered to be instantaneous and equal to $p_{\infty}(V)$. The activation variable of I_{M} , z, is relatively slow, with time constant $\tau_z = 75$ ms. Therefore we used the fast-slow method in the condition that z is the only slow variable.

To illuminate the contribution of $I_{\rm NaP}$ to bursting, we carried out the analysis for four values of $g_{\rm NaP}$: 0 (Fig. 5A), 0.2 mS/cm² (Fig. 5B), 0.3 mS/cm² (Fig. 5C), and 0.41 mS/cm² (Fig. 5D). In all panels, the bifurcation diagrams of the fast subsystem are computed with z considered as a parameter. The steady state (fixed point; thin black line) is stable for large z. This stable rest state coalesces with an unstable state and ceases to exist in a saddle-node bifurcation. The rest state is stable again for negative values of z (negative z values do not have physiological meaning, but they are important for a complete mathematical analysis). At the z value where the high rest state gains its stability (a Hopf bifurcation that is out of the scale in Fig. 5, A and B), an oscillatory state (limit cycle) emerges, corresponding to tonic, periodic firing. This oscilla-

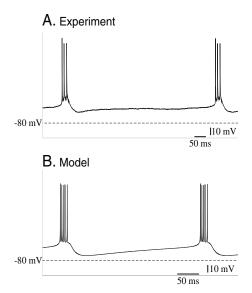


FIG. 4. Comparison of spontaneous rhythmic bursting in a truncated CA1 pyramidal cell and in the neuron model. A: experiment. In this truncated neuron, perfusing the slice with nominally Ca²⁺-free ACSF induced spontaneous rhythmic bursting. B: modeling. An example of spontaneous bursting $(I_{\rm app}=0~\mu{\rm A/cm^2})$ in the neuron model at $[{\rm Ca^{2+}}]_{\rm o}=0$. Other parameters are: $g_{\rm NaP}=0.3~{\rm mS/cm^2},~V_{\rm L}=-62~{\rm mV}.$

tory state extends toward the right. For $g_{NaP} = 0$ (A), the oscillatory state is the only stable state for small (positive) z values, and the rest state is the only stable state for larger z values. There is a tiny regime of bistability where both states are stable, but for our description, it can be ignored. For $g_{\text{NaP}} = 0.2 \text{ mS/cm}^2$ (B), the bistable regime, in which both the rest state and the oscillatory state exist and are stable, is more extended. For $g_{\text{NaP}} = 0.3 \text{ mS/cm}^2$ (C), the oscillatory solution extends toward the right, coalesces with an unstable periodic state, and this unstable state coalesces with another stable oscillatory state with a larger amplitude. For $g_{\text{NaP}} = 0.41 \text{ mS/cm}^2 (D)$, the Hopf bifurcation point is shifted to the right, and there is bistability between a rest state and a depolarized plateau. The stable oscillatory state with large amplitude almost disappears, and the amplitude of the remaining oscillatory state is small.

We then analyzed the behavior of the full system of equations defining the neuronal dynamics. For $g_{\text{NaP}} = 0$ (Fig. 5A), the bistable regime is tiny and cannot generate bursting states with the present kinetics of z; the neuron fires tonically. For $g_{\text{NaP}} = 0.2 \text{ mS/cm}^2$ (Fig. 5B), there is a significant bistable regime. When the neuron fires, z slowly increase until it reaches beyond the bistable regime. The neuron dynamics goes to the rest state, where z decreases. When z reaches the "knee" where the stable rest state disappears, the dynamics goes back to the firing state and a new bursting cycle begins. Similar behavior occurs for $g_{\text{NaP}} = 0.3 \text{ mS/cm}^2$ (Fig. 5C) except that the number of spikes (N_{S}) increases because of the more extended bistable regime. The system does not settle into the fast oscillations with small amplitude for this parameter value. For $g_{\text{NaP}} = 0.41 \text{ mS/cm}^2$ (Fig. 5D), the system first settles into the high plateau, and the amplitude of the oscillations decreases with time. As z increases, the state switches to the fast oscillations with small amplitude, and the amplitude of the oscillations increases with time until the system switches to the

rest state. This scenario leads to bursting state with fast, low-amplitude spikes whose amplitude first decreases and then increases with time (see following text, Fig. 8*B*, III).

From the fast-slow analysis, we derive several conclusions regarding the neuronal firing dynamics.

1. BISTABILITY OF THE FAST SUBSYSTEM. The bursting mechanism in our model depends on the bistability of the fast subsystem. To obtain bistability, there should be strong-enough inward current that is active in steady state at membrane potentials around spike threshold, namely $[g_{\text{Na}}m_{\infty}^{3}(V)h_{\infty}(V) + g_{\text{NaP}}p_{\infty}(V)] \times$ $(V - V_{\rm Na})$ should be large enough for V around spike threshold. In our model, this inward current can be generated by I_{NaP} or the window I_{Na} . In addition, the minimal voltage of the fast subsystem during the tonic state should be depolarized enough (above the thin dotted black line representing the unstable rest state). Therefore the kinetics of the currents underlying spike depolarization and repolarization ($I_{\rm Na}$ and $I_{\rm Kdr}$ in our model) should be fast enough (Bertram et al. 1995). Indeed, a previous model in which h and n were 3.7 times slower than in the present model that did not display bursting behavior (Golomb and Amitai 1997). If the kinetics of these variables are too fast, however, the fast subsystem will exhibit a high plateau depolarization As a result, the neuronal voltage will oscillate between a rest state and a high plateau depolarization instead of exhibiting bursts of spikes.

2. STRENGTH OF $g_{\rm NaP}$. The effect of $I_{\rm NaP}$ on the tonic state is larger than its effect on the rest state because this current is activated at depolarized membrane potentials (Table 1). As $g_{\rm NaP}$ increases, the tonic state is shifted more to the right

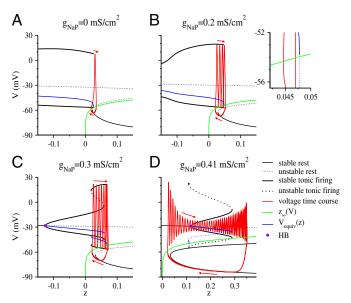


FIG. 5. Theory: fast-slow analysis of the neuronal firing patterns. Bifurcation diagrams of the fast subsystems are plotted with z considered as a parameter for $g_{\rm NaP}=0$ (A), $g_{\rm NaP}=0.2$ mS/cm² (B), $g_{\rm NaP}=0.3$ mS/cm² (C), and $g_{\rm NaP}=0.41$ mS/cm² (D); $I_{\rm app}=1$ μ A/cm². Solid lines denote stable states and dotted lines denote unstable states. Thin black lines denote rest state, and thick black lines denote the minimal and maximal voltages of periodic, tonic firing states (limit cycles). The green curve denotes the curve z = z_∞(V) (Table 1). The blue curve denotes the value of $V_{\rm equiv}$ (Eq. 5) during periodic firing. Violet solid circles denote Hopf bifurcations. The voltage time course of the neuron in the full system (including z as a variable) is denoted by the red curve. Red arrow denotes the direction of that curve in the z–V plane.

(toward larger values of z) than the rest state. Hence the bistable regime expands as $g_{\rm NaP}$ increases. This regime may even be produced by increasing $g_{\rm NaP}$ if it had not existed for $g_{\rm NaP}=0$. This means that elevating $g_{\rm NaP}$ may induce bursting behavior and increase $N_{\rm S}$. Increasing $g_{\rm NaP}$ also shifts the Hopf bifurcation of the depolarized plateau potential to the right (compare Fig. 5, A–D). Therefore when $g_{\rm NaP}$ is very large, the active phase of the burst becomes a high plateau depolarization or a sequence of low-amplitude fast spikes converging to a high plateau depolarization rather than full-blown spikes (Fig. 5D).

3. ACTIVATION CURVE OF $I_{\rm M}$. To allow bursting behavior the activation curve of $I_{\rm M}$, $z_{\infty}(V)$, should be located between the rest state curve and the curve of $V_{\rm equiv}$ (Bertram et al. 1995). If $z_{\infty}(V)$ is shifted toward more depolarized levels, (θ_z) , the half-maximum potential of $I_{\rm M}$, increases), the neuron will fire tonically. If $z_{\infty}(V)$ is shifted toward more hyperpolarized levels (θ_z) decreases, the neuron will be quiescent at rest.

4. STRENGTH OF $g_{\rm M}$. $I_{\rm M}$ is proportional to $g_{\rm M} \times z$. For $g_{\rm M} = 0$ (equivalent to z = 0 in Fig. 5, A–D), the neuron fires tonically or reaches a high plateau depolarization when $g_{\rm NaP}$ is very large. Increasing $g_{\rm M}$ is equivalent to compressing the bifurcation diagram of the fast subsystem along the z axis in Fig. 5, without modifying the kinetics of the slow variable z. Therefore as $g_{\rm M}$ increases, the slow variable z spends less time in the oscillatory state and $N_{\rm S}$ decreases. When $N_{\rm S}$ decreases to 1, the neuron fires in a tonic pattern. For very large $g_{\rm M}$, the rest state of the fast subsystem intersects with the activation curve of z, and the neuron becomes quiescent at rest.

SUMMARY OF NECESSARY CONDITIONS FOR BURSTING. Our analysis reveals four necessary conditions for bursting. All these conditions demand that certain parameters will be in particular ranges. 1) The kinetics of the variables underlying spike generation (inactivation of I_{Na} and activation of I_{Kdr}) should be fast enough (otherwise, there will be no bistability and the neuron will fire continuously) but not be too fast (to prevent a plateau depolarization). 2) The fast subsystem should show bistability, and g_{NaP} supports bistability. Therefore g_{NaP} should be strong enough to generate bistability unless this bistability has already been generated by the window I_{Na} . If g_{NaP} is too strong, however, the neuron model will manifest very fast spiking with small amplitude or a plateau depolarization. 3)The half-maximum potential of $I_{\rm M}$, θ_z , should not be too depolarized (at which condition the neuron will fire tonically) or too hyperpolarized (at which condition the neuron will be at resting potential). 4) $g_{\rm M}$ should be strong enough (otherwise, the neuron will fire in a regular mode or will display a high plateau depolarization) but not too strong (otherwise, the neuron will fire in a regular mode or will not fire at all).

The analysis is carried out in the limit that τ_z is much larger than all the other time constants, even though in reality it is not extremely large ($\tau_z=75$ ms). Therefore it is necessary to examine whether the conditions for bursting obtained using the analysis are still valid for this value of τ_z . In the following subsections, we turn back to the full system and study it using numerical simulations. We also examine whether the model can account for the variant firing patterns of CA1 pyramidal cells.

Effects of varying g_{NaP}

CA1 pyramidal cells perfused with Ca²⁺-free ACSF display a diversity of firing patterns, ranging from regular firing to spontaneous rhythmic bursting (Figs. 1–3 and 4A) (Azouz et al. 1996; Su et al. 2001). We first tested the hypothesis that a variation in the density of persistent Na+ channels may generate such diversity. We assumed that in this condition $\theta_{p}=$ -47 mV and examined the consequences of increasing $g_{\text{NaP.}}$ When g_{NaP} was set to zero, the neuron fired in a regular mode during sustained depolarization (Fig. 6A). As g_{NaP} was raised, the propensity for bursting increased, so that at $g_{\text{NaP}} = 0.08$ mS/cm², the neuron became a periodic burster when strongly depolarized (Fig. 6B) and at $g_{\text{NaP}} = 0.18 \text{ mS/cm}^2$, it burst-fired periodically in response to all suprathreshold stimuli (Fig. 6C). Further increasing g_{NaP} to 0.3 mS/cm² increased the burstiness of the neuron, so it now fired a burst also in response to brief stimuli (Fig. 6D). Changing V_L from -70 to -62 mV destabilized the rest state and caused spontaneous rhythmic bursting when g_{NaP} was high (Fig. 4B). For $g_{\text{NaP}} = 0$, the neuron was quiescent even for $V_{\rm L} = -62$ mV.

In all the cases shown in Figs. 4B and 6, the number of spikes in the first burst was larger than or equal to N_S , the average number of spikes in later bursts. The reason for that is that z, the activation variable of I_M , is nearly zero at the beginning of the stimulus but increases later, so the limiting effect of I_M on the number of spikes is expressed with a delay.

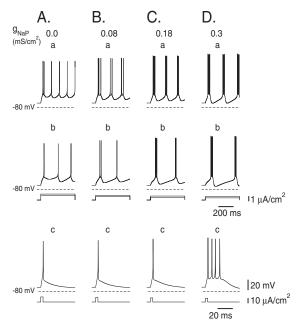


FIG. 6. Modeling: variant firing patterns of the neuron model for $[{\rm Ca^2}^+]_{\rm o}=0$ and various values of $g_{\rm NaP}$. A-D correspond to the following values of $g_{\rm NaP}$ (in mS/cm²): 0 (A), 0.08 (B), 0.18 (C), 0.3 (D). The neuron was at rest without current injection ($V_{\rm L}$ is set to -70 mV and therefore V is about -72 mV). In each part, a and b show responses of the neuron model to strong ($I_{\rm app,th}+0.3\mu{\rm A/cm}^2$; a) and weak ($I_{\rm app,th}+0.05\mu{\rm A/cm}^2$; b) prolonged stimuli, respectively; $I_{\rm app,th}$ is the minimal $I_{\rm app}$ required to attain spike threshold. The values of $I_{\rm app,th}$ (in $\mu{\rm A/cm}^2$) are 0.84, 0.59, 0.46, and 0.36 for $g_{\rm NaP}$ (in mS/cm²) values of 0, 0.08, 0.18, and 0.3 respectively. c presents the membrane potential in response to a brief (3 ms) current pulse with a density of $I_{\rm app,th}+2.5\mu{\rm A/cm}^2$. The values of $I_{\rm app,th}$ in ($\mu{\rm A/cm}^2$) are 7.1, 6.0, 5.3, and 4.7 for $g_{\rm NaP}$ (in mS/cm²) values of 0, 0.08, 0.18, and 0.3 respectively. - - - , -80 mV. The injected current pulses are indicated below the voltage traces. These currents are always 0 at the starting time. It is evident that increasing $g_{\rm NaP}$ enhances burstiness in the neuron model.

To further characterize the neuron model behavior, we have drawn a map of $N_{\rm S}$ in bursts evoked by brief (3 ms; Fig. 7A) and prolonged (Fig. 7B) stimuli in the parameter plane of g_{NaP} and I_{app} . All other parameters were fixed as in the reference parameter set. Brief pulses evoked only a single spike if g_{NaP} was zero or small. As g_{NaP} increased, N_S increased as predicted by the fast-slow analysis. For very large g_{NaP} , the neuron fired many fast and short-amplitude spikes, almost converging to a high plateau, before going back to rest (Fig. 7A, top right). The borders of the regimes of 4, 5, 6, etc. spikes were almost independent of I_{app} when it was not too large. This is consistent with the common experimental observation that when I_{app} is brief, $N_{\rm S}$ is independent of $I_{\rm app}$. The map for bursts evoked by prolonged current pulses also showed that $N_{\rm S}$ increases with g_{NaP} (Fig. 7B). The parameter I_{app} had a larger impact on N_{S} in comparison with the case of brief pulses, so that increasing it could raise $N_{\rm S}$ by one or two spikes.

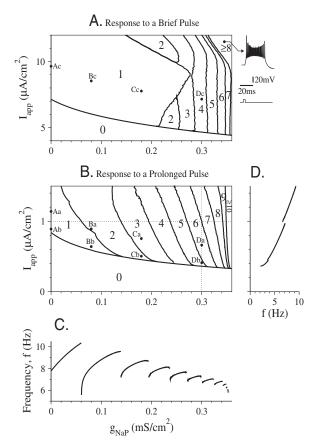


FIG. 7. Modeling: A and B: dependence of $N_{\rm S}$, the number of intraburst spikes, on $g_{\rm NaP}$ and $I_{\rm app}$ for $[{\rm Ca}^{2^+}]_{\rm o}=0$. The number in the bounded regions ("2," "1," etc.) denote $N_{\rm S}$; "0" denotes no firing. The solid circles denoted by letters, such as "Da," indicate the corresponding panel in Fig. 6. A: values of $N_{\rm S}$ in bursts evoked by brief stimuli. There were 2 discontinuous regimes in which 2 spikes were obtained at low and at high values of $I_{\rm app}$, whereas only one spike was elicited at intermediate $I_{\rm app}$ regions. The solid circle on the top-right region of map A denotes the parameter set of a burst of fast low-amplitude spikes, plotted right to the map. The time course of the applied current is plotted below the voltage time course. B: values of $N_{\rm S}$ in bursts evoked by prolonged stimuli. For a given $g_{\rm NaP}$, prolonged pulses evoked more intraburst spikes than brief pulses (at least when $I_{\rm app}$ was not extremely large). The dotted lines correspond to the $I_{\rm app}$ and $g_{\rm NaP}$ values for C and D, respectively. C: dependence of the bursting frequency f on $g_{\rm NaP}$ for $I_{\rm app}=1$ $\mu A/{\rm cm}^2$. D: dependence of the f on $I_{\rm app}$ for $g_{\rm NaP}=0.3$ mS/cm².

We denoted f to be the frequency of periodic bursts evoked by prolonged depolarizations. For a given N_S , f increased as g_{NaP} or I_{app} increased (Fig. 7, C and D) because the neuron was more excitable. At g_{NaP} or I_{app} values at which N_S increased by 1, f decreased abruptly because more prolonged bursts were followed by larger AHPs.

COMPARING EXPERIMENTAL RESULTS, MODELING, AND THEORY. Increasing $g_{\rm NaP}$ increases $N_{\rm S}$ and eventually generates bursts with fast, low-amplitude spiking both in the analysis (Fig. 5) and the simulations (Fig. 7). Similarly, blocking $g_{\rm NaP}$ decreases $N_{\rm S}$ and eventually eliminates bursting in response to prolonged current pulses in the experiments (Fig. 2), the simulations (Figs. 6 and 7) and the mathematical analysis (Fig. 5). The same dependency $N_{\rm S}$ on $g_{\rm NaP}$ is found experimentally and computationally in response to brief pulses. Furthermore, in response to prolonged pulses, the number of spikes in the first burst is larger than the number of spikes in subsequent bursts in both experiments and simulations.

Role of g_M

Our data (Fig. 3), together with previous data about intact neurons (Yue and Yaari 2004, 2006), show that selective block of $I_{\rm M}$ markedly enhances the burstiness of CA1 pyramidal cells. These data suggested that $I_{\rm M}$ normally counteracts the depolarizing drive furnished by $I_{\rm NaP}$. Hence, it is expected that $N_{\rm S}$ will increase with $I_{\rm NaP}$ and decrease with $I_{\rm M}$. The situation, however, is more complicated because other states appear in the model, as we describe in the following text.

We explored the effects of varying $g_{\rm NaP}$ and $g_{\rm M}$ at a given $I_{\rm app}$. In Fig. 8, we present maps of the various states as a function of $g_{\rm M}$ and $g_{\rm NaP}$. For brief pulses (Fig. 8A), bursting states appeared at intermediate $g_{\rm NaP}$ and $g_{\rm M}$ values that were not too small. In this bursting regime, $N_{\rm S}$ increased with $g_{\rm NaP}$ and decreased with $g_{\rm M}$. Three other types of patterns appeared for $g_{\rm NaP}$ values above the regimes of single bursts or spikes, denoted by I–III in Fig. 8A: I, a fast burst of spikes with decaying amplitudes followed by a high plateau; II, sustained, high-frequency firing; III, an irregular burst with many fast, low-amplitude spikes. The patterns in regimes I and II coexisted with the rest states, namely, the system was bistable in these parameter regimes.

The map obtained for neuronal responses to prolonged stimuli (Fig. 8B) was qualitatively similar to the previous map (Fig. 8A), although there were some notable differences. First, there were parameter regimes having $N_S = 1$ (regular spiking behavior) that markedly differed in their firing rates. The firing rate in the regime on the right side of the map, denoted by "1_{slow}," was 5–10 Hz, whereas the firing rate in the regime on the left side of the map, denoted by " $1_{\rm fast}$," was in the order 100 Hz. Second, for $g_{\rm NaP}=0$, it was possible to obtain a burst of two spikes in a restricted $g_{\rm M}$ domain. For larger $g_{\rm NaP}$ values, there were two "fingers" in the map where N_S was 2. The finger that extended to the right showed bursting with frequency in the order of 5 Hz. A second finger extending from $g_{\text{NaP}} = 0$ to higher g_{NaP} values (adjacent to the " 1_{fast} " regime) displayed spiking at a high rate (in the order of 100 Hz) in a doublet manner: the interspike interval alternated between larger and smaller values. Between the two fingers (for $g_{\rm M}$ values larger

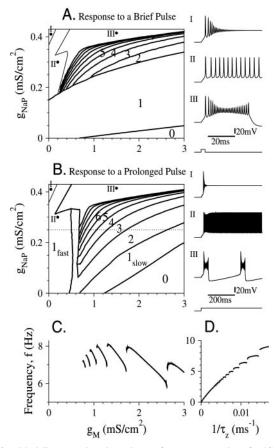


FIG. 8. Modeling. A and B: dependence of $N_{\rm S}$ on $g_{\rm NaP}$ and $g_{\rm M}$ for $[{\rm Ca^{2+}}]_{\rm o}=0$; $\tau_z=75$ ms. Symbols are as in Fig. 7. A: values of $N_{\rm S}$ in bursts evoked by brief stimuli with $I_{\rm app}=7~\mu{\rm A/cm^2}$. Interestingly, $N_{\rm S}$ could switch abruptly from 1 to a value larger than 2 as $g_{\rm NaP}$ increased. For example, for $g_{\rm M}=0.8~{\rm mS/cm^2}$, $N_{\rm S}$ switched from 1 to 3 at $g_{\rm NaP}=0.23~{\rm mS/cm^2}$. B: values of $N_{\rm S}$ in bursts evoked by prolonged stimuli with $I_{\rm app}=1~\mu{\rm A/cm^2}$. The symbols " $1_{\rm fast}$ " and " $1_{\rm slow}$ " denote tonic firing with fast (interspike interval of order 10 ms) and slow (interspike interval of order 100 ms), respectively. The transition from the parameter regime at which $N_{\rm S}=2$ (left "finger," $g_{\rm M}\approx0.6~{\rm mS/cm^2}$) to the regime of normal bursting was very complex and involved chaotic dynamics. The dotted line denotes the $g_{\rm NaP}$ value used for C. The solid circles denoted by I–III in each map represent the parameter sets of the firing patterns shown right to the maps. The time course of the applied current is plotted below the voltage time courses. C: dependence of the bursting frequency f on $g_{\rm M}$. Parameters: $I_{\rm app}=1~\mu{\rm A/cm^2}$, $g_{\rm NaP}=0.25~{\rm mS/cm^2}$, $\tau_z=75~{\rm ms}$. D: dependence of the bursting frequency f on $1/\tau_z$. Parameters: $I_{\rm app}=1~\mu{\rm A/cm^2}$, $g_{\rm NaP}=0.25~{\rm mS/cm^2}$, $g_{\rm MaP}=0.25~{\rm mS/cm^2}$, $g_{\rm MaP}=0.25~{\rm mS/cm^2}$, $g_{\rm MaP}=1~{\rm mS/cm^2}$.

0.6 mS/cm²), the neuron exhibited normal bursting for intermediate g_{NaP} values. Three types of patterns, analogous to the patterns obtained for brief pulses, are denoted by I–III in Fig. 8*B*.

To conclude, for both types of stimuli, regular bursts with large $N_{\rm S}$ appear in a restricted parameter regime with intermediate values of $g_{\rm NaP}$ and $g_{\rm M}$, composed of diagonal bands of constant $N_{\rm S}$. In this regime, $N_{\rm S}$ indeed increases with $g_{\rm NaP}$ and decreases with $g_{\rm M}$. Several irregular patterns appear outside of this regime.

For a given $N_{\rm S}$, f generally decreased as $g_{\rm M}$ increased; At $g_{\rm M}$ values at which $N_{\rm S}$ decreased by 1, f increased abruptly (Fig. 8C). At and above a critical $g_{\rm M}$ value (3.4 mS/cm²), the neuron became quiescent (f=0). As expected from the fast-slow analysis (Table 1, Eqs. 4 and 5, Fig. 5), f depends linearly on $1/\tau_z$ for large τ_z (Fig. 8D). Jumps in f occur at moderate values of τ_z at every τ_z value for which $N_{\rm S}$ increases by 1.

COMPARING EXPERIMENTAL RESULTS, MODELING, AND THEORY. We find that both in the experiment and in the simulations: I) blocking $g_{\rm M}$ increases the $N_{\rm S}$ evoked by brief stimuli (Figs. 3A, middle and left, and 8A) and eventually transfers the neuron to a bistable tonic firing mode (Figs. 3A, third panel from left, and 8A). 2) Blocking $g_{\rm NaP}$ after the $g_{\rm M}$ blockage causes the neuron to fire only one spike in response to a brief pulse (Figs. 3A, right, and 8A). 3) In response to a prolonged pulse, blocking $g_{\rm M}$ can transfer the neuron to a high plateau depolarization state (Figs. 3B, middle and left; and 8B). 4) If $g_{\rm NaP}$ is also blocked, the neuron fires in a regular mode or becomes quiescent (Figs. 3B, right; and 8B). The conclusions of the analysis that are demonstrated in the simulations (Fig. 8) are 1) $g_{\rm M}$ should be strong enough, but not too strong, to obtain bursting, 2) $N_{\rm S}$ decreases with $g_{\rm M}$, and 3) f is proportional to $1/\tau_z$.

Note that the firing frequency of the real neuron under the effects of both linopirdine and riluzole is of order 10 Hz (Fig. 3B), which corresponds to the firing pattern denoted by $1_{\rm slow}$ in Fig. 8B and not to $1_{\rm fast}$. In contrast, in the cases in which the neuron bursts in "intact" cells and blocking $g_{\rm M}$ leads to high plateau, additional blockade of $g_{\rm NaP}$ in the model leads to fast tonic firing. This means that in this respect, the specific example in Fig. 3B is different from what is shown in Fig. 8B. In reality, but not in the model, the high plateau depolarization eventually decreases and the neuron repolarizes (compare Fig. 3B, *middle*, with Fig. 8B, I). This is because the model does not include dynamical processes with very slow time scale, such as slow inactivation of $I_{\rm NaP}$ or of $I_{\rm Na}$ (e.g., Fleidervish et al. 1996; French et al. 1990; Mickus et al. 1999).

Effects of varying $[Ca^{2+}]_o$

The analyses described in the preceding text were done in conditions of 0 [Ca²⁺]_o. Here we use the model to interpret intriguing experimental evidence (Su et al. 2001) that reducing [Ca²⁺]_o, but not blocking Ca²⁺ currents and Ca²⁺-activated K⁺ currents, may transfer a nonbursting cell into a burster. Clearly raising [Ca²⁺]_o will modify the neuronal dynamics by introducing voltage-gated Ca²⁺ currents and Ca²⁺-activated K⁺ currents. In addition, raising [Ca²⁺]_o will shift the voltage dependence of I_{NaP} activation back toward more positive potentials (Li and Hatton 1996; Yue et al. 2005). Figure 9, A—C, illustrates the firing patterns of the neuron model obtained for three sets of parameters (θ_p is the half-maximum potential of the persistent sodium current): $g_{\text{Ca}} = 0.08 \text{ mS/cm}^2$, $\theta_p = -41 \text{ mV (Fig. 9A)}, g_{\text{Ca}} = 0.05 \text{ mS/cm}^2, \theta_p = -44 \text{ mV (Fig. 9B)}, and <math>g_{\text{Ca}} = 0.02 \text{ mS/cm}^2, \theta_p = -46 \text{ mV (Fig. 9C)}.$ The parameter set in Fig. 9A represents parameter values of physiological [Ca²⁺]_o, whereas those in Fig. 9BC represent parameters values of reduced [Ca²⁺]_o. The firing pattern of the neuron model obtained for the set $g_{\text{Ca}} = 0$, $\theta_p = -47 \text{ mV}$, corresponding to $[\text{Ca}^{2+}]_0 = 0$, has already been presented in Fig. 6D. It can be seen that reducing [Ca²⁺]₀ augments burstiness in this model.

REDUCING $[CA^{2+}]_O$ IS NOT EQUIVALENT TO BLOCKING CA^{2+} CURRENTS. Maps showing N_S values in bursts evoked by brief and prolonged current pulses as a function of θ_p and a second parameter related to the Ca^{2+} -gated currents or Ca^{2+} -activated K^+ currents, are shown in Fig. 10. Increasing g_{Ca} with all Ca^{2+} -activated K^+ currents blocked ($g_C = g_{sAHP} = 0$) aug-

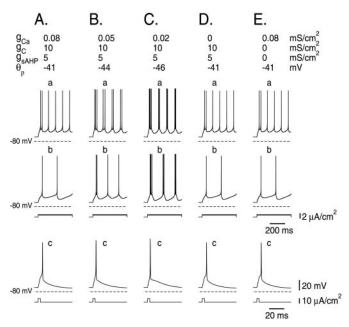


FIG. 9. Modeling: variant firing patterns of the neuron model for different values of $[Ca^{2+}]_o$. The sets of parameters $\{g_{Ca} \text{ (mS/cm}^2), g_{C} \text{ (mS/cm}^2), g_{sAHP}\}$ (mS/cm^2) , θ_p (mV) are A: {0.08, 10, 5, -41}. B: {0.05, 10, 5, -44}. C: {0.02, 10, 5, -46}. D: {0, 10, 5, -46}. E: {0.08, 0, 0, -41}. The parameter sets A-Cmimic gradual reduction of $[Ca^{2+}]_o$ from the physiological level A through B and C; when $[Ca^{2+}]_0$ becomes 0, the parameter set $\{0, 10, 5, -47\}$ is equal to that of Fig. 6D and is not shown here again. The parameter set D mimics blockade of Ca²⁺ conductance. The parameter set E mimics Ca²⁺ buffering, which eliminates Ca²⁺-dependent K⁺ currents. The neuron model is at rest before the current injection. Each column in the figure includes 3 voltage traces. The panels in a and b show the responses of the neuron model to prolonged strong and weak stimuli, respectively. c show the responses of the neuron model to brief (3 ms) stimuli. The horizontal dashed line represents -80 mV. The waveforms of the stimuli are provided below the voltage trace(s). Stimulus intensities are 1 μ A/cm² for a, 0.7 μ A/cm² for b, and 7 μ A/cm² for c. Reducing [Ca²⁺]_o (A-C), but neither blocking g_{Ca} (D) nor blocking g_C and g_{sAHP} (E), induces bursting in a regular firing cell.

mented $N_{\rm S}$ for both brief and prolonged stimuli (Fig. 10, A and B) and weakly reduced f (Fig. 10C). To assess the effects of Ca²⁺-activated K⁺ conductances, we set $g_{\rm Ca}=0.08~{\rm mS/cm^2}$ and computed $N_{\rm S}$ as a function of θ_p and either $g_{\rm C}$ or $g_{\rm sAHP}$. As expected, increasing $g_{\rm C}$ suppressed burstiness and decreased $N_{\rm S}$ for a specific value of θ_p (Fig. 10, D and E); f increased with $g_{\rm C}$ (Fig. 10F). Increasing $g_{\rm sAHP}$ within the range of the parameter we used (from 0 to 20 mS/cm²) did not affect $N_{\rm S}$ substantially (data not shown). This finding is expected because the $I_{\rm sAHP}$ is slow, and the burst is terminated by $I_{\rm M}$ before $I_{\rm sAHP}$ becomes strong enough to have a considerable effect.

When Ca^{2+} -activated K^+ conductances were intact, the effect of varying g_{Ca} on N_S depended on g_C . The value of N_S increased with g_{Ca} for small g_C values and decreased with g_{Ca} for large g_C values. Figure 10, G—I, demonstrates that with our reference parameter set ($g_C = 10 \text{ mS/cm}^2$, $g_{SAHP} = 5 \text{ mS/cm}^2$), the hyperpolarizing effect of g_C dominated, N_S decreased with g_{Ca} for both brief and prolonged stimuli, and f increased with g_{Ca} .

The increase in burstiness on reducing $[Ca^{2+}]_o$ resulted mainly from the decrease in θ_p . However, the decrease of g_{Ca} per se also could affect N_s . Although in most cases blocking g_{Ca} did not change N_s (e.g., Fig. 9D and points 9A and 9D in Fig. 10H), there were also conditions in which blocking g_{Ca}

transferred the system to a higher level of burstiness (for example, when $g_{\text{Ca}} = 0.2 \text{ mS/cm}^2$ and $\theta_p = -45 \text{ mV}$, Fig. 10H). Similarly, although blocking g_{C} did not lead to bursting for our reference parameter set (Fig. 9E), it could increase N_{S} for lower values of θ_p (Fig. 10, D and E). For brief stimuli, bursting was obtained for more hyperpolarized values of θ_p in comparison to the case of prolonged stimuli. Therefore evoking bursts with brief stimuli required lower values of $[\text{Ca}^{2+}]_{\text{O}}$ than evoking bursts with prolonged stimuli.

COMPARING BETWEEN EXPERIMENTAL AND MODELING RESULTS. We observed both in experiments (Fig. 1) and in the simulations (Figs. 6D, 9, A—C, and 10, G and H) that reducing $[\mathrm{Ca}^{2+}]_{\mathrm{o}}$ increases the propensity for bursting in response to brief and prolonged stimuli and augments N_{S} . The neuron model also mimicked two more experimental results obtained in CA1 pyramidal neurons: blocking Ca^{2+} currents pharmacologically, which also blocks Ca^{2+} -activated K^+ currents, or blocking the latter currents only (by injecting a fast Ca^{2+} buffer into the neuron), did not change the regular firing mode

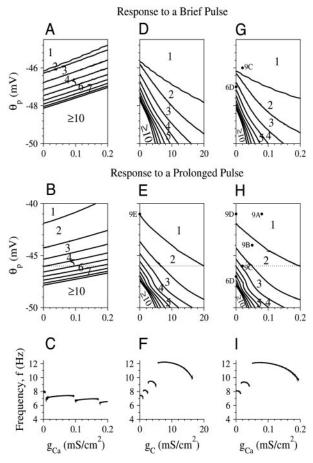


FIG. 10. Modeling. Top and middle: dependence of $N_{\rm S}$ on either $g_{\rm Ca}$ or $g_{\rm C}$ and θ_p . Symbols are as in Fig. 7. Top: response to a brief pulse with $I_{\rm app}=7$ $\mu {\rm A/cm^2}$. Middle: response to a prolonged pulse with $I_{\rm app}=1$ $\mu {\rm A/cm^2}$. Bottom: dependence of the bursting frequency f on either $g_{\rm Ca}$ or $g_{\rm C}$ for $I_{\rm app}=1$ $\mu {\rm A/cm^2}$ and $\theta_p=-46$ mV. A and B, $N_{\rm S}$ vs. $g_{\rm Ca}$ and θ_p for $g_{\rm C}=g_{\rm sAHP}=0$. C: f vs. $g_{\rm Ca}$ for $g_{\rm C}=g_{\rm sAHP}=0$. D and E. $N_{\rm S}$ vs. $g_{\rm Ca}$ and θ_p plane for $g_{\rm Ca}=0.08$ mS/cm², $g_{\rm sAHP}=0$. F: f vs. $g_{\rm C}$ for $g_{\rm Ca}=0.08$ mS/cm², $g_{\rm sAHP}=0$. G and H: $N_{\rm S}$ vs. $g_{\rm Ca}$ and θ_p for for $g_{\rm C}=10$ mS/cm², $g_{\rm sAHP}=5$ mS/cm². I, f vs. $g_{\rm Ca}$ for $g_{\rm C}=10$ mS/cm², $g_{\rm sAHP}=5$ mS/cm². In all the panels, $N_{\rm S}$ increases and $g_{\rm P}$ is hyperpolarized. The solid circles in panels $g_{\rm C}=10$ mS/cm² and letters, such as "9A," indicate the corresponding column in Figs. 9 or 6, respectively.

of these neurons (Su et al. 2001). Examples are shown in Fig. 9D, in which g_{Ca} is set to 0 (other parameters, including θ_p , are as in Fig. 9A), and in Fig. 9E, where both g_{C} and g_{sAHP} are set to 0. It can be seen in these figures that blocking Ca²⁺-activated K⁺ currents in either way does not modify the firing behavior of the neuron model for the chosen parameter set.

DISCUSSION

Major conclusions

Our finding that truncated neurons fire in a similar manner to intact neurons in both normal and low [Ca²⁺]_o allowed us to use a single-compartment model to analyze the underlying mechanism of bursting. Our analysis leads to several conclusions: first, CA1 pyramidal cells can burst via a single-compartment mechanism with one slow variable, namely the activation variable of $I_{\rm M}$ (z), provided two conditions are fulfilled, 1) The kinetics of the spike generating currents (i.e., $I_{\rm Na}$ and I_{Kdr}) are fast, although not too fast and 2) the activation curve of $I_{\rm M}$ is properly tuned. If it is too depolarized, the neuron will fire tonically; if it is too hyperpolarized, the neuron will be quiescent. Accordingly, it was shown experimentally that shifting the activation curve of $I_{\rm M}$ toward more negative potentials with retigabine (Tatulian et al. 2001; Wickenden et al. 2000) suppresses bursting behavior in both normal and 0 [Ca²⁺]_o (Yue and Yaari 2004).

Second, moderate values of $g_{\rm NaP}$ favor burstiness because it enhances bistability of the fast subsystem. Thus $N_{\rm S}$ increases with $g_{\rm NaP}$. Assuming a natural heterogeneity in $g_{\rm NaP}$, the model can replicate the diversity of intrinsic firing patterns found experimentally (Fig. 6), but if $g_{\rm NaP}$ is too large, the neuron will display prolonged bursts with many low-amplitude spikes or a high plateau depolarization (Figs. 7 and 8). Bistability and bursting, however, can be supported also by the window $I_{\rm NaP}$ provided it is sufficiently large (not shown). Therefore the presence of $g_{\rm NaP}$ is not a necessary condition for bursting in our model.

Third, $g_{\rm M}$ is mandatory for bursting in 0 $[{\rm Ca^{2+}}]_{\rm o}$. This feature of the model is consistent with our experimental findings showing that blocking $g_{\rm M}$ with linopirdine converts bursting in 0 $[{\rm Ca^{2+}}]_{\rm o}$ to plateau depolarization (Fig. 3). Conversely, increasing $g_{\rm M}$ decreases $N_{\rm S}$. Ultimately, when $g_{\rm M}$ is large enough, the neuron does not fire spikes. When $[{\rm Ca^{2+}}]_{\rm o}$ is elevated, $I_{\rm sAHP}$ and $I_{\rm M}$ play a similar role in the neuronal dynamics, with $I_{\rm sAHP}$ being slower.

Fourth, our model predicts that shifting the activation curve of $I_{\rm NaP}$ to more negative potentials will increase burstiness (Fig. 10). Given that such a shift is obtained by lowering $[{\rm Ca}^{2^+}]_{\rm o}$ (Li and Hatton 1996; Yue et al. 2005), the model readily accounts for the experimental finding that lowering $[{\rm Ca}^{2^+}]_{\rm o}$, but not blocking ${\rm Ca}^{2^+}$ and ${\rm Ca}^{2^+}$ -activated conductances, induces bursting behavior in regular spiking CA1 pyramidal cells (Su et al. 2001).

Comparison between experimental and modeling results

The dynamics of the neuron model have been compared with the dynamics of native neurons from several aspects.

1. CAN WE OBTAIN IN THE MODEL THE VARIETY OF FIRING PATTERNS RECORDED EXPERIMENTALLY? We have shown in Figs. 6 and 4B that by varying $g_{\rm NaP}$ and $V_{\rm L}$ the model can mimic the

various firing parameters obtained in $[Ca^{2+}]_o = 0$ (see Fig. 1 in Su et al. 2001). In reality, there is biological heterogeneity in other parameters as well that may contribute to the variety of firing patterns. Similarly, the model can mimic the firing patterns obtained experimentally at various levels of $[Ca^{2+}]_o$, g_{Ca} , and g_C (compare Fig. 9 with Fig. 1 here and Fig. 2 in Sue et al. 2001).

2. HOW DOES THE PROPENSITY FOR BURSTING AND $N_{\rm S}$ VARY WITH $I_{\rm app}$, $g_{\rm NaP}$, AND $g_{\rm M}$? In the neuron model (Fig. 7) as well as in native neurons (Fig. 2), $N_{\rm S}$ increases with $g_{\rm NaP}$ and depends only weakly on $I_{\rm app}$. When the neuron bursts, $N_{\rm S}$ decreases with $g_{\rm M}$ (Fig. 8) (see Fig. 1 in Yue and Yaari 2004) and reaches a fast tonic firing state or a high plateau for low levels of $g_{\rm M}$ (Figs. 3 and 8).

3. HOW DOES THE PROPENSITY FOR BURSTING AND $N_{\rm S}$ VARY WITH $g_{\rm Ca}$, $g_{\rm C}$, AND $[{\rm Ca}^{2+}]_{\rm o}$? It has been reported that reducing $[{\rm Ca}^{2+}]_{\rm o}$, but not blocking the ${\rm Ca}^{2+}$ current or ${\rm Ca}^{2+}$ -activated ${\rm K}^+$ currents, increases the propensity for bursting and $N_{\rm S}$ (see Figs. 3, 7, and 8 in Sue et al. 2001). This experimental observation can be replicated in the model (Fig. 10) using certain parameter sets and the assumption that elevating $[{\rm Ca}^{2+}]_{\rm o}$ causes $\theta_{\rm p}$ to shift to more positive voltage. Figure 10 suggests that in principle, however, there may be cases in which $N_{\rm S}$ increases with the blockade of $g_{\rm C}$ (Fig. 10, D and D) or D0 and D1 or D1 or D2 and D3.

DISCREPANCIES BETWEEN MODELING AND EXPERIMENTAL RESULTS. The dynamical equations of the model do not include slow processes (>1 s). Therefore the model cannot explain slow changes observed experimentally, such as the slow repolarization of the membrane potential during a high plateau and the resumption of spiking (Fig. 3, *middle*).

In this paper, we show several diagrams in which N_S varies as a function of two parameters (Figs. 7, 8, and 10). When a third parameter is varied, the relative positions of the areas of particular $N_{\rm S}$ values may shift. The two-dimensional diagrams provide therefore qualitative information about the type of transition that may occur when parameters vary, but one cannot expect that the experimental behavior will always follow the two-dimensional diagrams quantitatively. For example, Fig. 8B shows that in response to a prolonged pulse, reducing $g_{\rm M}$ may transfer a bursting pattern to a high plateau, and further reduction of g_{NaP} may transfer a high plateau neuron to a neuron spiking at high rates. Figure 8B does not overlap the example of Fig. 3, in which $g_{\rm M}$ blockade by linopirdine followed by g_{NaP} blockade by riluzole transfers a bursting pattern to a high plateau and then to a tonic firing pattern (with firing frequency of ~ 10 Hz). It is possible, however, that linopirdine and riluzole, used to blocked $g_{\rm M}$ and $g_{\rm NaP}$, respectively, exert additional effects on neuronal excitability. Note that Fig. 3A is consistent with Fig. 8A regarding the effects of blocking $g_{\rm M}$ and $g_{\rm NaP}$ on the firing patterns in response to a brief current pulse. In both cases, blocking $g_{\rm M}$ in the case of bursting neurons can bring the neuron to a fast spiking state leading to a high plateau, and subsequent blockade of g_{NaP} leads to firing of one spike only.

For the model, we chose a $\theta_{\rm h}$ value that is $\sim\!20$ mV depolarized compared with available voltage-clamp experimental measurements (Colbert and Pan 2002; Gasparini and Magee 2002; Martina and Jonas 1997), to obtain a large enough window $I_{\rm Na}$ to support bistability in the fast subsystem.

Window $I_{\rm Na}$ is needed for bursting and even for spiking in previous models as well and is obtained by assuming a small value of $\theta_{\rm m}-\theta_{\rm h}$ (e.g., 4.2 mV in Pinsky and Rinzel 1994; Traub and Miles 1991; Traub et al. 1991) or by assuming a very large $g_{\rm Na}$ value in the axo-somatic compartment (Mainen and Sejnowski 1996).

Comparison with other models of bursting neurons

A 16-compartmental model of CA1 pyramidal cells, albeit with passive dendrites, was provided by Shuai et al. (2003). This model also displayed rhythmic bursting in zero [Ca²⁺]_o. The reversal potential of the leak current in the soma was -58mV, more depolarized than the value we used (-70 mV). The reversal potential of the leak current in the dendrites, however, was assumed to be 0 mV (Eq. 2 in Shuai et al. 2003), without any apparent biological reason. Simulating their model (using parameters of Table 1, Shuai et al. 2003), we found that after disconnecting the soma from the apical dendrite their respective resting potentials were -63.9 and 0 mV. Bursting in the intact neuron model depended on depolarization of the soma by the dendrite and disappeared after disconnecting the soma from the dendritic compartments. This behavior of the latter neuron model is incongruent with our experimental data showing that bursting behavior persists in truncated neurons (Figs. 1, 2, 3, and 4A).

The kinetics of ionic currents in the model of Shuai et al. (2003) also differed considerably from ours. Most notably, the activation time constant of $I_{\rm NaP}$ in their model was 30 ms even though experimental measurements have shown it to be well below 1 ms (Kay et al. 1998; Magistretti et al. 2003; Vervaeke et al. 2006). In contrast, $I_{\rm NaP}$ activation kinetics in our model is fast, and z is the only slow variable. Consequently, bistability of the fast subsystem of variables is needed to generate bursting behavior.

In other models of hippocampal and neocortical pyramidal neurons, intrinsic bursting in normal [Ca²⁺]_o was attributed to a ping-pong interplay between fast Na⁺ and K⁺ currents in the soma and slow Ca²⁺ and K⁺ (mostly Ca²⁺-dependent) currents in the apical dendrites (Bazhenov et al. 2004; Mainen and Sejnowski 1996; Pinsky and Rinzel 1994; Traub and Miles 1991; Traub et al. 1991). The latter mechanism depends on the coupling between soma and apical dendrites; bursting behavior was not obtained when coupling resistance was too small or too large.

The CA1 pyramidal cell has widely branched basal dendrites, which are electrotonically compact (Zador et al. 1995). In general, the electrotonic separation between the axon, the soma and the basal dendrite may modify the firing patterns of the neuron. The existence of a slow current, such as $I_{\rm M}$, and bistability of the fast subsystem, will be needed for bursting even in models similar to ours where the spatial structure of the truncated dendrite is explicitly considered. Effects of the electrotonic separation between soma and axon can be addressed theoretically as more data about the axon becomes available.

Predictions for future experiments

The major results and predictions of the model, such as the increase of N_S with $g_{\rm NaP}$ and its decrease with $g_{\rm M}$ and the generation of high plateaus, have been confirmed experimen-

tally as reported here and elsewhere (Gilles et al. 1999; Su et al. 2001; Yue and Yaari 2004, 2006). The model yields several more predictions. For example, increasing g_{NaP} ultimately will lead to prolonged bursts with many low-amplitude spikes (Fig. 8) or to high-plateau depolarization. Also, increasing g_{Ca} in normal $[\text{Ca}^{2+}]_{\text{o}}$ will moderately decrease the propensity for bursting when Ca^{2+} -activated K^+ currents are operative and strong enough and will moderately increase this propensity when these currents are blocked (Figs. 9 and 10). It would be interesting to test these predictions by modulating these various currents pharmacologically or by simulating changes in these currents using the dynamic-clamp technique (Sharp et al. 1993; Vervaeke et al. 2006).

Functional implications

Our experimental and computational results suggest that bursting in adult CA1 pyramidal cells in zero and in low [Ca²⁺]_o in vitro is generated by a "square-wave" mechanism, i.e., from interplay between ionic currents located within one compartment, namely, the soma/axon initial segment. Thus separation between fast currents in the soma/axon initial segment and slow currents in the apical dendrites (the ping-pong mechanism) is not obligatory for bursting. However, the latter mechanism may be invoked in adult CA1 pyramidal cells by blocking I_A pharmacologically after which backpropagating spikes evoke dendritic Ca²⁺ spikes that, in turn, trigger somatic bursting (Magee and Carruth 1999). A similar ping-pong mechanism may exist naturally in developing CA1 pyramidal cells (Chen et al. 2005). Thus CA1 pyramidal cells may display both square-wave and ping-pong bursting, depending on their developmental stage and on the composition of the extracellular milieu. Interestingly, although it has been established that pyramidal neurons in cortical layer V can display a ping-pong bursting behavior in some conditions (Larkum et al. 1999), they can also burst after most of their apical dendrites are truncated (A. E. Telfeian and B. W. Connors, personal communication). Thus the square-wave mechanism described here for CA1 pyramidal cells may be relevant for those neurons

Hippocampal pyramidal cells in vivo were shown to alternate between regular firing ("simple" spikes) and burst firing ("complex" spikes), depending on the behavioral state of the animal (Ranck 1973). It is not yet known how intrinsic factors contribute to complex spike bursting in vivo. However, decreases in $[{\rm Ca}^{2+}]_{\rm o}$, which occur during synchronized neuronal activity (Heinemann et al. 1977) and may attain levels of \leq 0.2 mM during epileptic seizures (Pumain et al. 1985), are expected to induce square-wave bursting in CA1 pyramidal cells in vivo. Likewise, factors that upmodulate $g_{\rm NaP}$ (e.g., hypoxia or the accumulation of nitric oxide) (Hammarstrom and Gage 2002), or downmodulate $g_{\rm M}$ (e.g., a variety of neurotransmitters) (Brown and Yu 2000), also are likely to enhance this mode of bursting in these neurons in vivo.

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