

Group Theory Assignment 1

1. Determine whether or not the given \star is a binary operation on the given set S.

(a)
$$S = \mathbb{R}$$
, $a \star b = \frac{a}{a^2 + b^2}$

(b)
$$S = \mathbb{R}, a \star b = a$$

(c)
$$S = \{1, 6, 3, 2, 18\}, a \star b = ab$$

(d)
$$S = \{1, -2, 3, 2, -4\}, a \star b = |b|$$