

4 What is  $\int e + e^{3x} dx$ ?

A.  $ex + 3e^{3x} + c$

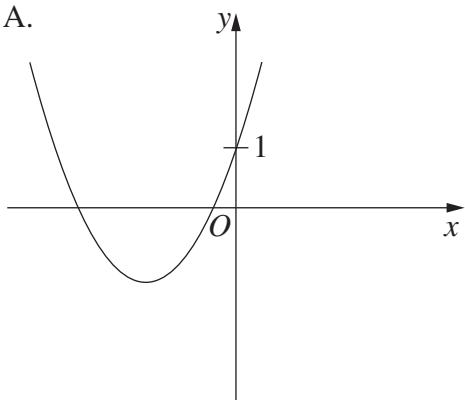
B.  $ex + \frac{1}{3}e^{3x} + c$

C.  $e + 3e^{3x} + c$

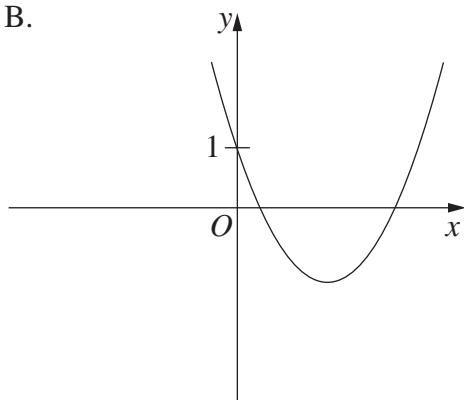
D.  $e + \frac{1}{3}e^{3x} + c$

5 Which of the following could represent the graph of  $y = -x^2 + bx + 1$ , where  $b > 0$ ?

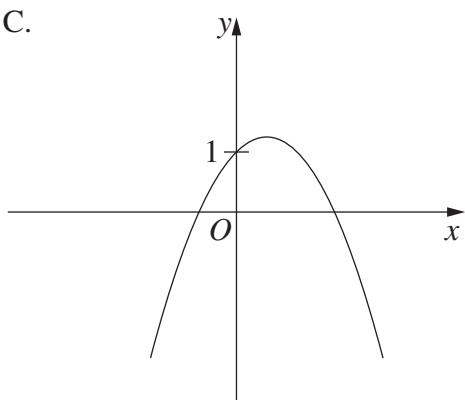
A.



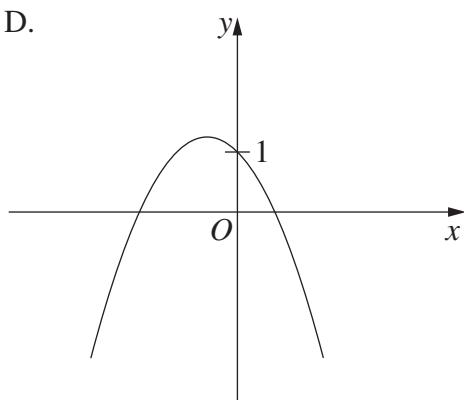
B.



C.



D.



**Question 12 (3 marks)**

Calculate the sum of the arithmetic series  $4 + 10 + 16 + \dots + 1354$ .

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**Question 13 (2 marks)**

$$\text{Evaluate } \int_0^{\frac{\pi}{4}} \sec^2 x \, dx.$$

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Question 17 (2 marks)

Find  $\int \frac{x}{4+x^2} dx$ .

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Question 18 (3 marks)

(a) Differentiate  $e^{2x}(2x + 1)$ .

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(b) Hence, find  $\int (x+1)e^{2x} dx$ .

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**Source: 2022-hsc-mathematics-advanced.pdf**

4 Which of the following is the range of the function  $f(x) = x^2 - 1$ ?

- A.  $[-1, \infty)$
- B.  $(-\infty, 1]$
- C.  $[-1, 1]$
- D.  $(-\infty, \infty)$

5 Let  $h(x) = \frac{f(x)}{g(x)}$ , where

$$\begin{aligned}f(1) &= 2 & f'(1) &= 4 \\g(1) &= 8 & g'(1) &= 12.\end{aligned}$$

What is the gradient of the tangent to the graph of  $y = h(x)$  at  $x = 1$ ?

- A. -8
- B. 8
- C.  $-\frac{1}{8}$
- D.  $\frac{1}{8}$

6 What is  $\int \frac{1}{(2x+1)^2} dx$ ?

- A.  $\frac{-2}{2x+1} + C$
- B.  $\frac{-1}{2(2x+1)} + C$
- C.  $2 \ln(2x+1) + C$
- D.  $\frac{1}{2} \ln(2x+1) + C$

**Question 15 (2 marks)**

$$\text{Evaluate } \int_{-2}^0 \sqrt{2x+4} dx.$$

2

**Question 16** (3 marks)

For what values of  $x$  is  $f(x) = x^2 - 2x^3$  increasing?

3

**Question 17** (2 marks)

$$\text{Find } \int x\sqrt{x^2 + 1} dx .$$

2

**Please turn over**