

Lsg Vorschlag A+N Ü011 Maximilian Maag

Aufgabe A

$$f_x(x, y) = (y - 1) + 3x^2$$

$$f_y(x, y) = x$$

$$0 = y - 1 + x^3$$

$$0 = x$$

$$x = 0; y = 1$$

$$f_{xx} = 6x^2$$

$$f_{yy} = 0$$

$$f_{xy} = 1$$

Das entsprechende Delta ist gleich 0 daher Sattelpunkt.

Aufgabe B

a)

$$f(x) = x^5 - 4x^4 + 2x^2 + 4x + 1$$

$$f'(x) = 5x^4 - 16x^3 + 4x + 4$$

$$x_{n+1} = x_n - 0,01 * (5x_n^4 - 16x_n^3 + 4x_n + 4)$$

- $x_0 = 2$
- $x_1 = 2,36$
- $x_2 = 2,778$
- $x_3 = 3,079$
- $x_4 = 3,092$
- $x_4 = 3,088$
- $x_6 = 3,089$
- $x_7 = 3,089$

b)

3,089019349

Aufgabe C

a)

$$F(x) = \frac{1}{4}x^4$$

$$\int_0^1 f(x)dx = F(1) - F(0)$$

$$\int_0^1 f(x)dx = \frac{1}{4}$$

b)

$$F(x) = \sin(x)$$

$$\int_0^{\frac{\pi}{2}} f(x)dx = \sin(\frac{\pi}{2}) - \sin(0)$$

$$\int_0^{\frac{\pi}{2}} f(x)dx = 1$$

c)

$$F(x) = \frac{1}{4}x^{-4}$$

$$\int_1^2 f(x)dx = \frac{15}{64}$$

Aufgabe 1

$$f(x, y) = 3xy - x^3 - y^3$$

$$f_x = 3y - 3x^2$$

$$f_y = 3x - 3y^2$$

Bilde LGS:

$$A1: 3y - 3x^2 = 0$$

$$B1: 3x - 3y^2 = 0$$

$$A2: y = x^2$$

$$B2: 3x - 3(x^2)^2 = 0$$

$$B3: 3x - 3x^4 = 0$$

$$B4: 3x(1 - x^3) = 0$$

$$x_0 = 0; x_1 = 1 \quad y_0 = 0; y_1 = 1$$

$$E1(0, 0, 0); E2(1, 1, 1)$$

$$f_{xx} = -6x; f_{yy} = -6y; f_{xy} = 3; f_{yx} = 3$$

$$\det = -6x * -6y - 3^2$$

$$\det = 36xy - 9$$

$$\det(0, 0) < 0 \text{ E1 ist Sattelpunkt.}$$

$$\det(1, 1) > 0 \quad f_{1,1} < 0 \text{ E2 ist ein isoliertes Minimum.}$$

Aufgabe 2

$$\int_0^{\frac{\pi}{2}} \int_0^2 \int_0^1 3x^2 y * \cos(z) dx dy dz$$

$$\int_0^1 3x^2 y * \cos(z) dx$$

$$F(x) = x^3 y * \cos(z)$$

$$\int_0^1 f(x) dx = F(1) - F(0)$$

$$F(1) = 1^3 * y * \cos(z) = y * \cos(z); F(0) = 0^3 * y * \cos(z) = 0$$

$$\int_0^1 f(x) dx = y * \cos(z) - 0$$

$$\int_0^1 f(x) dx = y * \cos(z)$$

$$\int_0^2 y * \cos(z) dy$$

$$F(y) = \frac{1}{2} * y^2 * \cos(z)$$

$$F(2) = 2 * \cos(z); F(0) = 0 \quad F(0) \text{ ist hier } 0 \text{ da ein Produkt } 0 \text{ wird einer der Faktoren } 0 \text{ ist.}$$

$$\int_0^2 f(y) dy = 2 * \cos(z)$$

$$\int_0^{\frac{\pi}{2}} 2 * \cos(z) dz$$

$$F(z) = 2 * \sin(z)$$

$$\int_0^{\frac{\pi}{2}} 2 * \cos(z) dz = F\left(\frac{\pi}{2}\right) - F(0)$$

$$F\left(\frac{\pi}{2}\right) = 2; F(0) = 0$$

$$\int_0^{\frac{\pi}{2}} \cos(z) dz = 2$$

$$\int_0^{\frac{\pi}{2}} \int_0^2 \int_0^1 3x^2 y * \cos(z) dx dy dz = 2$$

Aufgabe 3

a)

Mit $[0,80]$ und $n = 8$ Streifen.

$$\int_a^b f(x) dx \approx \frac{1}{2} \frac{b-a}{n} * (y_0 + 2y_1 + 2y_2 + 2y_3 + 2y_4 + 2y_5 + 2y_6 + 2y_7 + y_8)$$

$$\bullet y_1 = f\left(0 + 1 * \frac{80-0}{8}\right) = f(10) = 5$$

$$\bullet y_2 = 15$$

$$\bullet y_3 = 37$$

$$\bullet y_4 = 50$$

$$\bullet y_5 = 60$$

$$\bullet y_6 = 55$$

$$\bullet y_7 = 35$$

- $y_8 = 0$

$$\begin{aligned}\int_a^b f(x)dx &\approx \frac{1}{2} \frac{b-a}{n} * (y_0 + 2y_1 + 2y_2 + 2y_3 + 2y_4 + 2y_5 + 2y_6 + 2y_7 + y_8) \\ \int_0^{80} f(x)dx &\approx \frac{1}{2} \frac{80}{8} * (2 + 2 * 5 + 2 * 15 + 2 * 37 + 2 * 50 + 2 * 60 + 2 * 55 + 2 * 35 + 0) \\ \int_0^{80} &\approx 2580\end{aligned}$$

b)

Mit $n = 4$ Streifen und $[0,80]$

$$\begin{aligned}\int_a^b f(x)dx &\approx \frac{b-a}{6n} * (y_0 + 2y_1 + 4y_2 + 2y_3 + 4y_4 + 2y_5 + 4y_6 + 2y_7 + y_8) \\ \int_0^{80} f(x)dx &\approx \frac{80}{24} * (2 + 2 * 5 + 4 * 15 + 2 * 37 + 4 * 50 + 2 * 60 + 4 * 55 + 2 * 35 + 0) \\ \int_0^{80} f(x)dx &\approx \frac{80}{24} * (2 + 4 * 5 + 2 * 15 + 4 * 37 + 2 * 50 + 4 * 60 + 2 * 55 + 4 * 35 + 0) \\ \int_0^{80} f(x)dx &\approx 2633,333...\end{aligned}$$