

# CSSS 510: Lab 6

## Multinomial Logit

2017-11-10

## 0. Agenda

1. Deriving a likelihood function for the multinomial model
2. Fitting a multinomial logit model using `optim()` and `glm()`
3. Simulating predicted values and confidence intervals
4. Evaluating goodness of fit

# 1. Deriving a likelihood function for multinomial logit

Recall from lecture the multinomial logit model:

$$\Pr(y_i = j | \mathbf{x}_i) = \frac{\exp(\mathbf{x}_i \beta_j)}{\sum_{l=1}^M \exp(\mathbf{x}_i \beta_l)}$$

If we make the identifying assumption that  $\beta_1 = 0$ , then we have

For  $j = 1$

$$\Pr(y_i = 1 | \mathbf{x}_i) = \frac{1}{1 + \sum_{l=2}^M \exp(\mathbf{x}_i \beta_l)}$$

For  $j > 2$

$$\Pr(y_i = j | \mathbf{x}_i) = \frac{\exp(\mathbf{x}_i \beta_j)}{1 + \sum_{l=2}^M \exp(\mathbf{x}_i \beta_l)}$$

# 1. Deriving a likelihood function for multinomial logit

In many ways, this is the most tractable model we've seen so far.

1. We assume that  $\Pr(y_i = j|x)$  is a function of the linear combination  $\mathbf{x}_i\beta_j$ . One key difference between this and previous models is that  $\beta_j$  differs for *each outcome*. We therefore have a set of  $\beta$  for each outcome category.

We then take two simple steps.

2. We take the exponential of  $\mathbf{x}_i\beta_j$  to ensure that the probabilities are nonnegative. (Why?)
3. We then divide each  $\exp(\mathbf{x}_i\beta_j)$  and divide it by  $\sum_{l=2}^M \exp(\mathbf{x}_i\beta_l)$  to make the probabilities sum to 1. (Why?)

## 1. Deriving a likelihood function for multinomial logit

Our model looks very similar to logit but with more than 2 categories. Indeed, multinomial logit can be thought of as a way to estimate separate logits for all categories all at once.

Like ordered probit, the likelihood function for multinomial logit finds the  $\beta_j$  that make the observed data most likely. That is, it maximizes the likelihood that  $y_{ij}$  falls into category  $j$ . All other categories  $\neq j$  are irrelevant.

$$\mathcal{L}(\beta_2, \dots, \beta_m | \mathbf{y}, \mathbf{X}) = \prod_{i=1}^N \prod_{j=1}^M p_{ij}^{y_{ij}}$$

$$\mathcal{L}(\beta_2, \dots, \beta_m | \mathbf{y}, \mathbf{X}) = \prod_{i=1}^N \prod_{j=1}^M \left[ \frac{\exp(\mathbf{x}_i \beta_j)}{1 + \sum_{l=2}^M \exp(\mathbf{x}_i \beta_l)} \right]^{y_{ij}}$$

$$\mathcal{L}(\beta_2, \dots, \beta_m | \mathbf{y}, \mathbf{X}) = \sum_{i=1}^N \sum_{j=1}^M y_{ij} \log \frac{\exp(\mathbf{x}_i \beta_j)}{1 + \sum_{l=2}^M \exp(\mathbf{x}_i \beta_l)}$$

# 1. Deriving a likelihood function for multinomial logit

Our coefficients can be interpreted in a similar way as logit coefficients:  $\beta$  is the change in the log of the odds ratio of one outcome versus another outcome.

Suppose that we have outcome  $m$  and outcome  $n$ . We will then have a  $\beta$  that corresponds to the change in the log of the odds of outcome  $m$  versus outcome  $n$ .

$$\log \frac{\Pr(y = m | \mathbf{x}_c, \beta_2, \dots, \beta_M)}{\Pr(y = n | \mathbf{x}_c, \beta_2, \dots, \beta_M)} = \mathbf{x}_c(\beta_m - \beta_n)$$

If the  $k$ th covariate increases by 1, then the log of the odds of category  $m$  versus category  $n$  increases by the *difference* of their coefficients.

## 2. Fitting a multinomial logit model

```
rm(list=ls())

# Load data and libraries
library(simcf)           # for mlogit simulators
library(tile)            # for graphics

## Loading required package: grid

library(RColorBrewer)    # for colors
library(MASS)            # for mvrnorm()
library(nnet)            # for multinom()

# homemade extractor function for multinom() coef's
coef.multinom <- function(x) {
  nlevel <- length(mlogit.result$lev)
  ncoef <- length(mlogit.result$coefnames)
  coef <- x$wts[(ncoef+2):length(x$wts)]
  coef[-((0:(nlevel-2))*(ncoef+1) + 1)]
}

# Load data (in simcf library)
data(gator)
gator <- as.data.frame(cbind(food, size, female))
```

## 2. Fitting a multinomial logit model

```
# Estimate MNL using the nnet library
```

```
model <- food ~ size + female  
mlogit.result <- multinom(model, Hess=TRUE)
```

```
## # weights: 12 (6 variable)  
## initial value 64.818125  
## iter 10 value 48.292498  
## final value 48.291021  
## converged
```

```
pe <- coef(mlogit.result)  
vc <- solve(mlogit.result$Hess) # var-cov matrix  
se <- sqrt(diag(vc))  
pe
```

```
## [1] 4.8969032 -2.5259623 -0.7899437 -1.9471694 0.1337791 0.3817674
```

```
se
```

```
## 2:(Intercept)      2:size      2:female 3:(Intercept)      3:size  
##      1.7063258      0.8475594      0.7122227      1.5305908      0.5181170  
##      3:female  
##      0.9083499
```



## 2. Fitting a multinomial logit model

```
gator$foodnm[gator$food==1]<-"Invertebrates"  
gator$foodnm[gator$food==2]<-"Fish"  
gator$foodnm[gator$food==3]<-"Other"  
  
model <- foodnm ~ size + female  
mlogit.result <- multinom(model, data=gator,Hess=TRUE)
```

```
## # weights: 12 (6 variable)  
## initial value 64.818125  
## iter 10 value 48.291150  
## final value 48.291021  
## converged
```

```
mlogit.result
```

```
## Call:  
## multinom(formula = model, data = gator, Hess = TRUE)  
##  
## Coefficients:  
##              (Intercept)          size          female  
## Invertebrates  -4.896281  2.525668  0.7897795  
## Other          -6.843614  2.659585  1.1714407  
##  
## Residual Deviance: 96.58204  
## AIC: 108.582
```

## 2. Simulating predicted values and confidence intervals

```
# Simulate parameters from predictive distributions
sims <- 10000
simbetas <- mvrnorm(sims,pe,vc)           # draw parameters, using MASS::mvrnorm
simB <- array(NA, dim = c(sims,3,2))     # re-arrange simulates to array format
simB[, ,1] <- simbetas[,1:3]             # for MNL simulation
simB[, ,2] <- simbetas[,4:6]

#####
# Create full factorial set of counterfactuals
sizerange <- seq(1,4,by=0.1)              # range of counterfactual sizes
femalerange <- c(0,1)                    # range of counterfactual sexes
xhyp1 <- cfFactorial(size = sizerange, female = femalerange)

# Simulate expected probabilities with 68% CI
mlogit.ev1 <- mlogitsimev(xhyp1, simB, ci=0.68)
```

## 2. Simulating predicted values and confidence intervals

```
#####  
# Plot expected values for all combinations of size and sex in 2 plots  
  
# Get 3 colors  
cols <- brewer.pal(3,"Set1")  
  
# Create one trace for each predicted category of the response, and each sex  
trace1a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==0],  
  y=mlogit.ev1$pe[xhyp1$x$female==0,1],  
  lower=mlogit.ev1$lower[xhyp1$x$female==0,1],  
  upper=mlogit.ev1$upper[xhyp1$x$female==0,1],  
  ci=list(mark="shaded"),  
  extrapolate=list(data=cbind(size,female),  
    cfact=xhyp1$x[xhyp1$x$female==0,],  
    omit.extrapolated=FALSE),  
  col=cols[1],  
  plot=1  
)  
  
trace2a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==0],  
  y=mlogit.ev1$pe[xhyp1$x$female==0,2],  
  lower=mlogit.ev1$lower[xhyp1$x$female==0,2],  
  upper=mlogit.ev1$upper[xhyp1$x$female==0,2],  
  ci=list(mark="shaded"),  
  extrapolate=list(data=cbind(size,female),  
    cfact=xhyp1$x[xhyp1$x$female==0,],  
    omit.extrapolated=FALSE),  
  col=cols[3],  
  plot=1  
)
```

## 2. Simulating predicted values and confidence intervals

```
trace3a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==0],
  y=mlogit.ev1$pe[xhyp1$x$female==0,3],
  lower=mlogit.ev1$lower[xhyp1$x$female==0,3,],
  upper=mlogit.ev1$upper[xhyp1$x$female==0,3,],
  ci=list(mark="shaded"),
  extrapolate=list(data=cbind(size,female),
    cfact=xhyp1$x[xhyp1$x$female==0,],
    omit.extrapolated=FALSE),
  col=cols[2],
  plot=1
)

trace4a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==1],
  y=mlogit.ev1$pe[xhyp1$x$female==1,1],
  lower=mlogit.ev1$lower[xhyp1$x$female==1,1,],
  upper=mlogit.ev1$upper[xhyp1$x$female==1,1,],
  ci=list(mark="shaded"),
  extrapolate=list(data=cbind(size,female),
    cfact=xhyp1$x[xhyp1$x$female==1,],
    omit.extrapolated=FALSE),
  col=cols[1],
  plot=2
)
```

## 2. Simulating predicted values and confidence intervals

```
trace5a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==1],
  y=mlogit.ev1$pe[xhyp1$x$female==1,2],
  lower=mlogit.ev1$lower[xhyp1$x$female==1,2,],
  upper=mlogit.ev1$upper[xhyp1$x$female==1,2,],
  ci=list(mark="shaded"),
  extrapolate=list(data=cbind(size,female),
    cfact=xhyp1$x[xhyp1$x$female==1,],
    omit.extrapolated=FALSE),
  col=cols[3],
  plot=2
)

trace6a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==1],
  y=mlogit.ev1$pe[xhyp1$x$female==1,3],
  lower=mlogit.ev1$lower[xhyp1$x$female==1,3,],
  upper=mlogit.ev1$upper[xhyp1$x$female==1,3,],
  ci=list(mark="shaded"),
  extrapolate=list(data=cbind(size,female),
    cfact=xhyp1$x[xhyp1$x$female==1,],
    omit.extrapolated=FALSE),
  col=cols[2],
  plot=2
)
```

## 2. Simulating predicted values and confidence intervals

```
linelabels <- textTile(labels=c("Invertebrates",  
                                "Fish",  
                                "Other"),  
                      x= c(1.75, 3, 3),  
                      y= c(0.95, 0.95, 0.375),  
                      col=c(cols[1], cols[2], cols[3]),  
                      cex = 0.75,  
                      plot=c(1,2)  
)  
  
at.x <- c(1,2,3,4)  
at.y <- c(0,0.2,0.4,0.6,0.8,1)  
  
# Plot traces using tile  
file <- "gatorsEV"  
tile(trace1a,  
      trace2a,  
      trace3a,  
      trace4a,  
      trace5a,  
      trace6a,  
      linelabels,  
      RxC = c(1,2),  
      limits = c(1,4,0,1),  
      output = list(outfile=file, width=7),  
      xaxis = list(at=at.x),  
      yaxis = list(at=at.y, major=FALSE),  
      xaxistitle = list(labels="Size of alligator (meters)",  
                        yaxistitle = list(type="first", labels="Probability primary diet is...", x=0.1),  
      plottitle = list(labels=c("Male alligators", "Female alligators"), y=1),  
      gridlines = list(type="xy")  
)
```

## Loading required package: WhatIf

## 2. Simulating predicted values and confidence intervals

```
#####  
## Alternate version with 95% CIs and one plot per trace (6 plots)  
  
# Simulate expected probabilities with 95% CI  
mlogit.ev1 <- mlogitsimev(xhyp1, simB, ci=0.95)  
  
# Create one trace for each predicted category of the response, and each sex  
trace1a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==0],  
  y=mlogit.ev1$pe[xhyp1$x$female==0,1],  
  lower=mlogit.ev1$lower[xhyp1$x$female==0,1],  
  upper=mlogit.ev1$upper[xhyp1$x$female==0,1],  
  ci=list(mark=c("shaded", "dashed")),  
  extrapolate=list(data=cbind(size,female),  
    cfact=xhyp1$x[xhyp1$x$female==0,],  
    omit.extrapolated=TRUE),  
  plot=1  
)  
  
trace2a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==0],  
  y=mlogit.ev1$pe[xhyp1$x$female==0,2],  
  lower=mlogit.ev1$lower[xhyp1$x$female==0,2],  
  upper=mlogit.ev1$upper[xhyp1$x$female==0,2],  
  ci=list(mark="shaded", "dashed"),  
  extrapolate=list(data=cbind(size,female),  
    cfact=xhyp1$x[xhyp1$x$female==0,],  
    omit.extrapolated=TRUE),  
  plot=3  
)
```

## 2. Simulating predicted values and confidence intervals

```
trace3a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==0],
  y=mlogit.ev1$pe[xhyp1$x$female==0,3],
  lower=mlogit.ev1$lower[xhyp1$x$female==0,3],
  upper=mlogit.ev1$upper[xhyp1$x$female==0,3],
  ci=list(mark="shaded", "dashed"),
  extrapolate=list(data=cbind(size,female),
    cfact=xhyp1$x[xhyp1$x$female==0,],
    omit.extrapolated=TRUE),
  plot=2
)

trace4a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==1],
  y=mlogit.ev1$pe[xhyp1$x$female==1,1],
  lower=mlogit.ev1$lower[xhyp1$x$female==1,1],
  upper=mlogit.ev1$upper[xhyp1$x$female==1,1],
  ci=list(mark="shaded", "dashed"),
  extrapolate=list(data=cbind(size,female),
    cfact=xhyp1$x[xhyp1$x$female==1,],
    omit.extrapolated=TRUE),
  plot=4
)
```



## 2. Simulating predicted values and confidence intervals

```
trace5a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==1],
  y=mlogit.ev1$pe[xhyp1$x$female==1,2],
  lower=mlogit.ev1$lower[xhyp1$x$female==1,2],
  upper=mlogit.ev1$upper[xhyp1$x$female==1,2],
  ci=list(mark="shaded", "dashed"),
  extrapolate=list(data=cbind(size,female),
    cfact=xhyp1$x[xhyp1$x$female==1,],
    omit.extrapolated=TRUE),
  plot=6
)

trace6a <- lineplot(x=xhyp1$x$size[xhyp1$x$female==1],
  y=mlogit.ev1$pe[xhyp1$x$female==1,3],
  lower=mlogit.ev1$lower[xhyp1$x$female==1,3],
  upper=mlogit.ev1$upper[xhyp1$x$female==1,3],
  ci=list(mark="shaded", "dashed"),
  extrapolate=list(data=cbind(size,female),
    cfact=xhyp1$x[xhyp1$x$female==1,],
    omit.extrapolated=TRUE),
  plot=5
)
```

## 2. Simulating predicted values and confidence intervals

```
# Plot traces using tile
file <- "gatorsEVsep95"
tile(trace1a,
      trace2a,
      trace3a,
      trace4a,
      trace5a,
      trace6a,
      RxC = c(2,3),
      limits = c(1,4,0,1),
      output = list(file=file, width=10),
      xaxis = list(at=at.x),
      yaxis = list(at=at.y, major=FALSE),
      xaxistitle = list(labels="Size of alligator (meters)"),
      maintitle = list(labels="Probability primary diet is..."),
      rowtitle = list(labels=c("Male\n alligators", "Female\n alligators"), cex=1.25),
      columntitle = list(labels=c("Invertebrates", "Fish", "Other"), cex=1.25),
      height=list(columntitle=5),
      width=list(rowtitle=1.5),
      gridlines = list(type="xy")
)
```

```
## [1] "Running whatif"
## [1] "Preprocessing data ..."
## [1] "Performing convex hull test ..."
## [1] "Calculating distances ...."
## [1] "Calculating the geometric variance..."
## [1] "Calculating cumulative frequencies ..."
## [1] "Finishing up ..."
## [1] "Whatif finished; returning to tile"
## [1] "Running whatif"
## [1] "Preprocessing data ..."
## [1] "Performing convex hull test ..."
## [1] "Calculating distances ...."
## [1] "Calculating the geometric variance..."
```

## 2. Simulating predicted values and confidence intervals

```
#####  
# Create a specific comparison for first diffs and relative risks  
# Load data (in simcf library)  
data(gator)  
gator <- as.data.frame(cbind(food, size, female))  
model <- food ~ size + female  
  
xhyp2 <- cfMake(model, gator, nscen=1)  
# Scenario 1: Large vs small (male mu + 1sd vs male mu - 1sd), holding male fixed  
xhyp2 <- cfName(xhyp2, "Large vs Small Males", scen=1)  
xhyp2 <- cfChange(xhyp2, "size",  
  x=mean(gator$size[gator$female==0]) + sd(gator$size[gator$female==0]),  
  xpre=mean(gator$size[gator$female==0]) - sd(gator$size[gator$female==0]),  
  scen=1)  
xhyp2 <- cfChange(xhyp2, "female", x=0, xpre=0, scen=1)  
  
# Simulate first differences with 95% CI  
mlogit.fdl <- mlogitsimfd(xhyp2, simB, ci=0.95)  
  
# Simulate relative risks with 95% CI  
mlogit.rr1 <- mlogitsimrr(xhyp2, simB, ci=0.95)
```

## 2. Simulating predicted values and confidence intervals

```
#####  
# Make ropeladder plot of First Differences  
  
# Make trace of FDs, large vs small males, all categories  
traceFD <- ropeladder(x=mlogit.fdi$pe,  
  lower=mlogit.fdi$lower,  
  upper=mlogit.fdi$upper,  
  labels=c("Invertebrates",  
    "Fish",  
    "\"0ther food\""),  
  size=0.65,  
  lex=1.75,  
  lineend="square",  
  plot=1  
)  
  
# Make reference line trace for first diffs (at 0)  
vertmarkFD <- linesTile(x=c(0,0), y=c(0,1), plot=1)  
  
# Set tick marks for x axis  
xat <- c(-0.5,-0.25,0, 0.25, 0.5)  
xlab <- c("-50%", "-25%", "0%", "+25%", "+50%")  
  
# Make plot with tile  
file <- "gatorsFD"  
tile(traceFD, vertmarkFD,  
  xaxis=list(at=xat, labels=xlab),  
  topaxis=list(add=TRUE, at=xat, labels=xlab),  
  plottitle=list(labels="Large male gators (+1sd) compared to small (-1sd)",  
    xaxis=list(labels="difference in probability this is gator's primary diet"),  
    width=list(null=4),  
    height=list(xaxis=3, plottitle=4),  
    gridlines=list(type="xt"),  
    output=list(file=file, width=7)  
)
```

## 2. Simulating predicted values and confidence intervals

```
#####  
# Make ropeladder plot of Relative Risks  
  
# Make trace of RRs, large vs small males, all categories  
traceRR <- ropeladder(x=mlogit.rr1$pe,  
                      lower=mlogit.rr1$lower,  
                      upper=mlogit.rr1$upper,  
                      labels=c("Invertebrates",  
                              "Fish",  
                              "\"Other food\""),  
                      size=0.65,  
                      lex=1.75,  
                      lineend="square",  
                      plot=1  
)  
  
# Make reference line trace for relative risks (at 1)  
vertmarkRR <- linesTile(x=c(1,1), y=c(0,1), plot=1)  
  
# Set tick marks for x axis  
xat <- c(0.01, 0.1, 0.5, 1, 2, 5, 10 )  
  
# Make plot with tile  
file <- "gatorsRR"  
tile(traceRR, vertmarkRR,  
      xaxis=list(log=TRUE, at=xat, labels=paste0(xat,"x")),  
      topaxis=list(add=TRUE, log=TRUE, at=xat, labels=paste0(xat,"x")),  
      plottitle=list(labels="Large male gators (+1sd) compared to small (-1sd)",  
                    xaxistitle=list(labels="relative likelihood this is gator's primary diet"),  
      width=list(null=4),  
      height=list(xaxistitle=3, plottitle=4),  
      gridlines=list(type="xt"),  
      output=list(file=file, width=7)  
)
```

## 2. Simulating predicted values and confidence intervals

```
#####  
# Create several comparisons for first diffs and relative risks  
xhyp3 <- cfMake(model, gator, nscen=5)  
  
# Scenario 1: Large vs small (male mu + 1sd vs male mu - 1sd), holding male fixed  
xhyp3 <- cfName(xhyp3, "Large Male (Small Male)", scen=1)  
xhyp3 <- cfChange(xhyp3, "size",  
                  x=mean(gator$size[gator$female==0]) + sd(gator$size[gator$female==0]),  
                  xpre=mean(gator$size[gator$female==0]) - sd(gator$size[gator$female==0]),  
                  scen=1)  
xhyp3 <- cfChange(xhyp3, "female", x=0, xpre=0, scen=1)  
  
# Scenario 2: Large vs small (female mu + 1sd vs female mu - 1sd), holding female fixed  
xhyp3 <- cfName(xhyp3, "Large Female (Small Female)", scen=2)  
xhyp3 <- cfChange(xhyp3, "size",  
                  x=mean(gator$size[gator$female==1]) + sd(gator$size[gator$female==1]),  
                  xpre=mean(gator$size[gator$female==1]) - sd(gator$size[gator$female==1]),  
                  scen=2)  
xhyp3 <- cfChange(xhyp3, "female", x=1, xpre=1, scen=2)  
  
# Scenario 3: Female vs male holding size fixed at mean of all gators  
xhyp3 <- cfName(xhyp3, "Average Female (Average Male)", scen=3)  
xhyp3 <- cfChange(xhyp3, "size",  
                  x=mean(gator$size),  
                  xpre=mean(gator$size),  
                  scen=3)  
xhyp3 <- cfChange(xhyp3, "female", x=1, xpre=0, scen=3)
```

## 2. Simulating predicted values and confidence intervals

```
# Scenario 4: Female vs male holding size fixed at high of all gators
```

```
xhyp3 <- cfName(xhyp3, "Large Female (Large Male)", scen=4)
```

```
xhyp3 <- cfChange(xhyp3, "size",  
                  x=mean(gator$size) + sd(gator$size),  
                  xpre=mean(gator$size) + sd(gator$size),  
                  scen=4)
```

```
xhyp3 <- cfChange(xhyp3, "female", x=1, xpre=0, scen=4)
```

```
# Scenario 5: Female vs male holding size fixed at low of all gators
```

```
xhyp3 <- cfName(xhyp3, "Small Female (Small Male)", scen=5)
```

```
xhyp3 <- cfChange(xhyp3, "size",  
                  x=mean(gator$size) - sd(gator$size),  
                  xpre=mean(gator$size) - sd(gator$size),  
                  scen=5)
```

```
xhyp3 <- cfChange(xhyp3, "female", x=1, xpre=0, scen=5)
```

```
# Simulate first differences with 95% CI
```

```
mlogit.fd2 <- mlogitsimfd(xhyp3, simB, ci=0.95)
```

```
# Simulate relative risks with 95% CI
```

```
mlogit.rr2 <- mlogitsimrr(xhyp3, simB, ci=0.95)
```

```
sorted <- rev(order(mlogit.rr2$pe[,3]))
```

```
# Make trace of RRs, large vs small males, all categories
```

```
traceRR2 <- ropeladder(x=mlogit.rr2$pe[sorted,3],  
                      lower=mlogit.rr2$lower[sorted,3,1],  
                      upper=mlogit.rr2$upper[sorted,3,1],  
                      labels=rownames(xhyp3$x)[sorted],  
                      size=0.65,  
                      lex=1.75,  
                      lineend="square",  
                      plot=1
```

```
)
```

## 2. Simulating predicted values and confidence intervals

```
# Make reference line trace for relative risks (at 1)
vertmarkRR2 <- linesTile(x=c(1,1), y=c(0,1), plot=1)

# Set tick marks for x axis
xat <- c(0.5, 1, 2, 5, 10 )

# Make plot with tile
file <- "gatorsRRmultiscen"
tile(traceRR2, vertmarkRR2,
      xaxis=list(log=TRUE, at=xat, labels=paste0(xat,"x")),
      topaxis=list(add=TRUE, log=TRUE, at=xat, labels=paste0(xat,"x")),
      plottitle=list(labels="Gator 1 compared to (Gator 2)"),
      xaxistitle=list(labels="relative likelihood of mostly eating \"other\" food"),
      width=list(null=4),
      height=list(xaxistitle=3, plottitle=4),
      gridlines=list(type="xt"),
      output=list(file=file, width=7)
)
```



## 2. Simulating predicted values and confidence intervals

```
#####  
## A cross-validated goodness of fit test  
  
## A simple leave-one-out cross-validation function for multinom; returns predicted probs  
loocv <- function(obj, model, data) {  
  ncat <- length(obj$lev)  
  m <- nrow(data)  
  form <- model  
  loo <- matrix(NA, nrow=m, ncol=ncat)  
  for (i in 1:m) {  
    i.mlogit <- multinom(model, data=data[-i,])  
    loo[i,] <- predict(i.mlogit, newdata = data[i,], type="probs")  
  }  
  loo  
}  
  
predIS <- predict(mlogit.result, type="probs")  
predCV <- loocv(mlogit.result, model, gator)
```

```
## # weights: 12 (6 variable)  
## initial value 63.719513  
## iter 10 value 47.889490  
## final value 47.888873  
## converged  
## # weights: 12 (6 variable)  
## initial value 63.719513  
## iter 10 value 47.680671  
## final value 47.680063  
## converged  
## # weights: 12 (6 variable)  
## initial value 63.719513  
## iter 10 value 47.444174  
## final value 47.443479  
## converged  
## # weights: 12 (6 variable)
```

## 2. Simulating predicted values and confidence intervals

```
pcpIS
```

```
## [1] 0.2372881
```

```
pcpCV
```

```
## [1] 0.559322
```