multipset5

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```
college <- read.csv("~/Downloads/Universities.csv")
college</pre>
```

```
##
           University
                          SAT Top10 Accept SFRatio Expenses Grad
##
              Harvard 14.00
                                         14
                                                   11
                                                        39.525
## 2
                                                        30.220
            Princeton 13.75
                                 91
                                         14
                                                    8
                                                                  95
## 3
                  Yale 13.75
                                 95
                                         19
                                                   11
                                                        43.514
                                                                  96
                                         20
                                                        36.450
## 4
             Stanford 13.60
                                 90
                                                   12
                                                                  93
##
   5
                   MIT 13.80
                                 94
                                         30
                                                   10
                                                        34.870
                                                                  91
##
  6
                                         30
                                                   12
                                                        31.585
                  Duke 13.15
                                 90
                                                                  95
##
  7
              CalTech 14.15
                                         25
                                                    6
                                                        63.575
                                 100
                                                                  81
## 8
                                         23
            Dartmouth 13.40
                                 89
                                                   10
                                                        32.162
                                                                  95
## 9
                 Brown 13.10
                                 89
                                         22
                                                   13
                                                        22.704
                                                                  94
## 10
         JohnsHopkins 13.05
                                 75
                                         44
                                                    7
                                                        58.691
                                                                  87
             UChicago 12.90
                                                        38.380
## 11
                                 75
                                         50
                                                   13
                                                                  87
                                         36
                                                        27.553
## 12
                 UPenn 12.85
                                 80
                                                   11
                                                                  90
## 13
              Cornell 12.80
                                 83
                                         33
                                                   13
                                                        21.864
                                                                  90
##
   14
         Northwestern 12.60
                                 85
                                         39
                                                   11
                                                        28.052
                                                                   89
##
  15
             Columbia 13.10
                                 76
                                         24
                                                   12
                                                        31.510
                                                                  88
##
   16
            NotreDame 12.55
                                 81
                                         42
                                                   13
                                                        15.122
                                                                  94
##
   17
                  UVir 12.25
                                 77
                                         44
                                                   14
                                                        13.349
                                                                  92
## 18
           Georgetown 12.55
                                 74
                                         24
                                                   12
                                                        20.126
                                                                  92
                                                    9
                                                        25.026
                                                                  72
## 19
      CarnegieMellon 12.60
                                 62
                                         59
## 20
            UMichigan 11.80
                                 65
                                         68
                                                   16
                                                        15.470
                                                                  85
##
   21
                                 95
                                         40
                                                                  78
           UCBerkeley 12.40
                                                   17
                                                        15.140
##
   22
                                                   15
                                                        11.857
           UWisconsin 10.85
                                 40
                                         69
                                                                  71
##
  23
            PennState 10.81
                                 38
                                         54
                                                   18
                                                        10.185
                                                                  80
## 24
               Purdue 10.05
                                 28
                                         90
                                                   19
                                                         9.066
                                                                  69
## 25
             TexasA&M 10.75
                                 49
                                         67
                                                   25
                                                         8.704
                                                                  67
```

1) The variables seem to be mainly continuous variable so I think Euclidean distance as a metric would work in order to measure distance between points. The standard deviations of the variables seem to vary so I will scale/standardize my data in part 2.

```
var(college[,c(2, 3, 4, 5, 6, 7)])
```

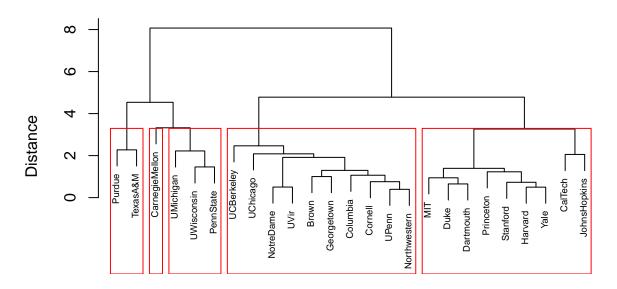
```
##
                    SAT
                                                                               Grad
                             Top10
                                        Accept
                                                   SFRatio
                                                              Expenses
## SAT
               1.174184
                          19.42697
                                     -18.93633
                                                 -3.581217
                                                              12.17599
                                                                           7.338783
## Top10
              19.426967
                         377.67667 -329.39167 -50.860000
                                                             171.41354
                                                                         131.306667
## Accept
            -18.936333
                        -329.39167
                                     389.16667
                                                 50.683333
                                                            -158.91183
                                                                       -146.441667
             -3.581217
## SFRatio
                         -50.86000
                                                 16.543333
                                                             -45.87133
                                                                         -20.665000
                                      50.68333
## Expenses
             12.175995
                         171.41354 -158.91183 -45.871333
                                                             208.07725
                                                                         51.425625
                                                              51.42562
## Grad
               7.338783
                         131.30667 -146.44167 -20.665000
                                                                         82.043333
```

```
collegenorm <- college[,c("SAT","Top10","Accept","SFRatio","Expenses","Grad")]
rownames(collegenorm) <- college[,1]
collegenorm <- scale(na.omit(collegenorm)) # scaling my variables

#get the distance matrix
dist1 <- dist(collegenorm, method="euclidean")

clust1 <- hclust(dist1)

#draw the dendrogram
plot(clust1,labels= rownames(collegenorm), cex=0.6, xlab="",ylab="Distance",main="Clustering of Univers rect.hclust(clust1, k =5)</pre>
```

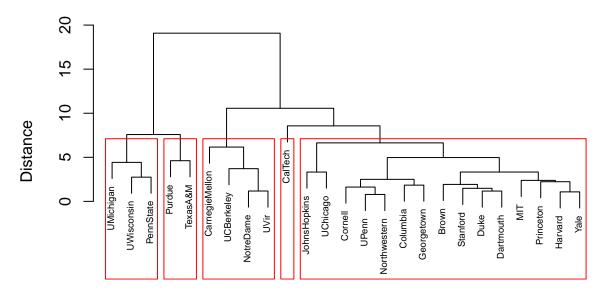


hclust (*, "complete")

Using eu-

clidean distance metrics and complete linkage method, there appears to be perhaps 5 main groups associated with the clustering of universities.

```
dist2 <- dist(collegenorm, method="manhattan")
clust2 <- hclust(dist2)
plot(clust2,labels= rownames(collegenorm), cex=0.6, xlab="",ylab="Distance",main="Clustering of Univers
rect.hclust(clust2, k = 5)</pre>
```

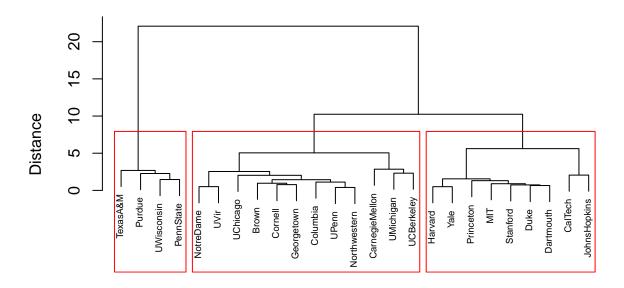


hclust (*, "complete")

Using

manhattan distance metrics and complete linkage method, there seems to be a bunch larger abudnace of smaller subgroups, mot likely attributted to the non-euclidean distance metric

```
dist3 <- dist(collegenorm, method="euclidean")
clust3 <- hclust(dist3, method = "ward.D")
plot(clust3,labels= rownames(collegenorm), cex=0.6, xlab="",ylab="Distance",main="Clustering of Univers
rect.hclust(clust3, k = 3)</pre>
```

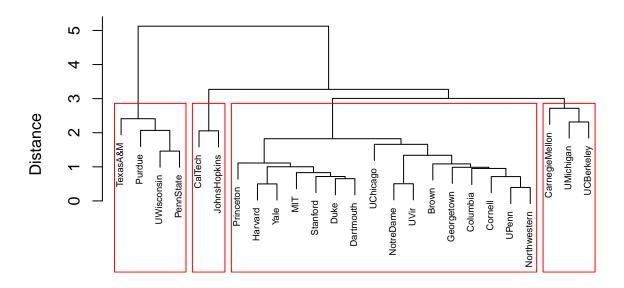


hclust (*, "ward.D")

Using eu-

clidean distance metrics and ward linkage method, you could argue for maybe 3 main groups, attributted to the ward method of minimizing sum of squares.

```
dist4 <- dist(collegenorm, method="euclidean")
clust4 <- hclust(dist4, method = "average")
plot(clust4,labels= rownames(collegenorm), cex=0.6, xlab="",ylab="Distance",main="Clustering of Univers
rect.hclust(clust4, k = 4)</pre>
```



hclust (*, "average")

Using eu-

clidean distance metrics and average linkage method, you could argue for around 4 cluster groups. This method is a space conserving method which could be the reason why.

```
3)
```

```
source("http://reuningscherer.net/stat660/R/HClusEval.R.txt")
hclus_eval(collegenorm, dist_m = 'euclidean', clus_m = 'ward', plot_op = T)

## [1] "Creating Distance Matrix using euclidean"
## [1] "Clustering using ward"

## The "ward" method has been renamed to "ward.D"; note new "ward.D2"

## [1] "Clustering Complete. Access the Cluster object in first element of output"

## [1] "Calculating RMSSTD"

## [1] "RMSSTD Done. Access in Element 2"

## [1] "Calculating RSQ"

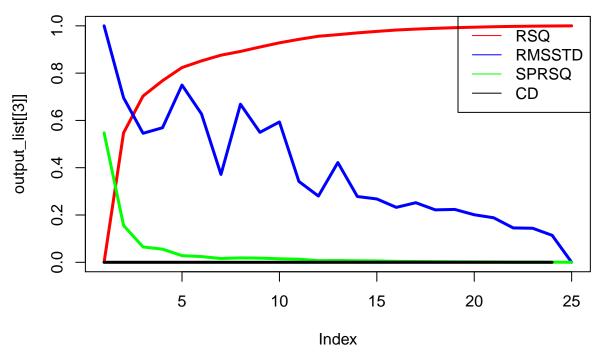
## [1] "RSQ Done. Access in Element 3"

## [1] "Calculating SPRSQ"

## [1] "Calculating Cluster Dist. "

## [1] "Calculating Cluster Dist. "

## [1] "CD Done. Access in Element 5"
```



```
## [[1]]
##
## Call:
## hclust(d = dist1, method = clus_m)
##
## Cluster method
                   : ward.D
## Distance
                   : euclidean
## Number of objects: 25
##
##
## [[2]]
   [1] 1.0000000 0.6957217 0.5455504 0.5690948 0.7494865 0.6275674 0.3716089
   [8] 0.6684786 0.5496442 0.5934966 0.3418013 0.2801410 0.4217875 0.2781637
## [15] 0.2678412 0.2322383 0.2519726 0.2217753 0.2235236 0.2010975 0.1882320
##
  [22] 0.1453734 0.1439020 0.1139935 0.0000000
##
## [[3]]
   [1] 0.0000000 0.5474127 0.7031216 0.7680337 0.8236317 0.8518232 0.8758776
##
   [8] 0.8918210 0.9104404 0.9282034 0.9428800 0.9559672 0.9627676 0.9701803
## [15] 0.9765147 0.9823232 0.9862763 0.9894854 0.9922634 0.9943452 0.9962389
  [22] 0.9977152 0.9985957 0.9994586 1.0000000
##
## [[4]]
   [1] 0.5474127146 0.1557088738 0.0649120744 0.0555979982 0.0281915177
   [6] 0.0240543736 0.0159434824 0.0186193184 0.0177630311 0.0146765903
## [11] 0.0130872221 0.0068004396 0.0074126959 0.0063344024 0.0058084457
## [16] 0.0039531123 0.0032090666 0.0027780177 0.0020817835 0.0018937129
## [21] 0.0014763040 0.0008805596 0.0008628244 0.0005414387 0.0000000000
##
## [[5]]
```

It looks like there are around 5 cluster groups. While the RMSSTD and CD lines offer little information, the

points where the RSQ and SPRSQ curves start to level out is around 5 cluster groups.

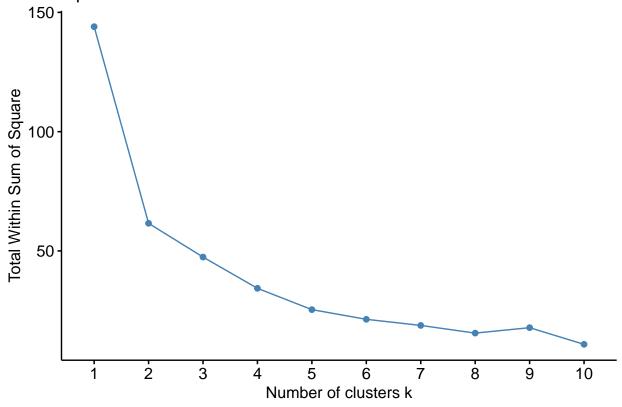
4) km1 <- kmeans(collegenorm,centers=5)</pre> ## K-means clustering with 5 clusters of sizes 4, 2, 7, 9, 3 ## Cluster means: ## SAT Top10 Accept SFRatio Expenses ## 1 -1.89129229 -1.9414523 1.5612876 1.60546806 -1.2086753 -1.6527233 0.86342006 0.5670502 -0.2382484 -1.52925136 2.3393604 -0.3002944 ## 3 0.89637905 0.7692006 -0.9008542 -0.52824852 0.5606384 0.8668162 ## 4 0.07386915 0.1811267 -0.2185352 -0.06774818 -0.2143826 0.4357213 ## 5 -0.36704889 -0.1276120 0.8347143 0.31470124 -0.6130148 -0.9259078 ## Clustering vector: ## Harvard Princeton Yale Stanford MIT ## 3 3 3 3 3 ## Duke CalTech Dartmouth Brown JohnsHopkins ## 2 3 2 3 4 ## UChicago **UPenn** Cornell Northwestern Columbia ## 4 ## NotreDame UVir Georgetown CarnegieMellon UMichigan ## 4 4 5 5 UCBerkeley ## UWisconsin PennState Purdue TexasA&M ## 5 1 1 1 1 ## ## Within cluster sum of squares by cluster: ## [1] 7.089134 2.113429 2.825243 6.628474 6.740760 (between_SS / total_SS = 82.4 %) ## ## Available components: ## ## [1] "cluster" "centers" "totss" "withinss" "tot.withinss" ## [6] "betweenss" "size" "iter" "ifault" for (i in 1:5){ print(paste("Universities in Cluster ",i)) print(college\$University[km1\$cluster==i]) print (" ") } ## [1] "Universities in Cluster 1" ## [1] UWisconsin PennState Purdue TexasA&M ## 25 Levels: Brown CalTech CarnegieMellon Columbia Cornell Dartmouth ... Yale ## [1] " " ## [1] "Universities in Cluster 2" JohnsHopkins ## [1] CalTech ## 25 Levels: Brown CalTech CarnegieMellon Columbia Cornell Dartmouth ... Yale ## [1] " " ## [1] "Universities in Cluster 3" ## [1] Harvard Princeton Yale Stanford MIT Duke Dartmouth

25 Levels: Brown CalTech CarnegieMellon Columbia Cornell Dartmouth ... Yale

[1] " "

```
## [1] "Universities in Cluster
                             UPenn
## [1] Brown
                 UChicago
                                        Cornell
                                                   Northwestern
## [6] Columbia
                 NotreDame
                             UVir
                                        Georgetown
## [1] " "
## [1] "Universities in Cluster 5"
## [1] CarnegieMellon UMichigan
                                UCBerkeley
## 25 Levels: Brown CalTech CarnegieMellon Columbia Cornell Dartmouth ... Yale
## [1] " "
set.seed(123)
library(factoextra)
## Loading required package: ggplot2
## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
fviz_nbclust(collegenorm, kmeans, method = "wss")
```

Optimal number of clusters



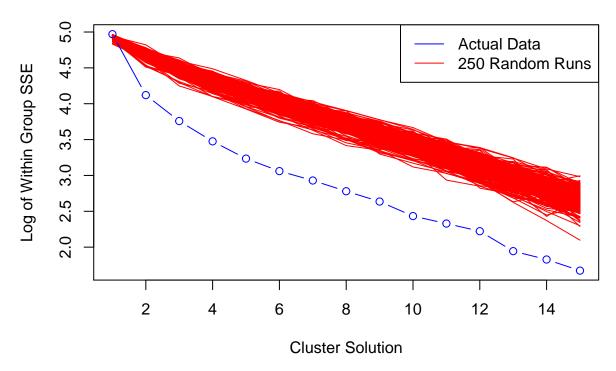
```
kdata <- collegenorm
n.lev <- 15  #set max value for number of clusters k

# Calculate the within groups sum of squared error (SSE) for the number of cluster solutions selected b
wss <- rnorm(10)
while (prod(wss==sort(wss,decreasing=T))==0) {
   wss <- (nrow(kdata)-1)*sum(apply(kdata,2,var))
   for (i in 2:n.lev) wss[i] <- sum(kmeans(kdata, centers=i)$withinss)}

# Calculate the within groups SSE for 250 randomized data sets (based on the original input data)</pre>
```

```
k.rand <- function(x){</pre>
  km.rand \leftarrow matrix(sample(x), dim(x)[1], dim(x)[2])
  rand.wss <- as.matrix(dim(x)[1]-1)*sum(apply(km.rand,2,var))</pre>
  for (i in 2:n.lev) rand.wss[i] <- sum(kmeans(km.rand, centers=i)$withinss)</pre>
  rand.wss <- as.matrix(rand.wss)</pre>
  return(rand.wss)
rand.mat <- matrix(0,n.lev,250)
k.1 <- function(x) {
  for (i in 1:250) {
    r.mat <- as.matrix(suppressWarnings(k.rand(kdata)))</pre>
    rand.mat[,i] <- r.mat}</pre>
  return(rand.mat)
}
# Same function as above for data with < 3 column variables
k.2.rand <- function(x){</pre>
  rand.mat <- matrix(0,n.lev,250)</pre>
  km.rand <- matrix(sample(x),dim(x)[1],dim(x)[2])</pre>
  rand.wss <- as.matrix(dim(x)[1]-1)*sum(apply(km.rand,2,var))</pre>
  for (i in 2:n.lev) rand.wss[i] <- sum(kmeans(km.rand, centers=i)$withinss)
  rand.wss <- as.matrix(rand.wss)</pre>
  return(rand.wss)
}
k.2 <- function(x){</pre>
  for (i in 1:250) {
    r.1 <- k.2.rand(kdata)
    rand.mat[,i] <- r.1}</pre>
  return(rand.mat)
# Determine if the data data table has > or < 3 variables and call appropriate function above
if (\dim(kdata)[2] == 2) { rand.mat <- k.2(kdata) } else { rand.mat <- k.1(kdata) }
# Plot within groups SSE against all tested cluster solutions for actual and randomized data - 1st: Log
xrange <- range(1:n.lev)</pre>
yrange <- range(log(rand.mat),log(wss))</pre>
plot(xrange, yrange, type='n', xlab='Cluster Solution', ylab='Log of Within Group SSE', main='Cluster So
for (i in 1:250) lines(log(rand.mat[,i]),type='l',col='red')
lines(log(wss), type="b", col='blue')
legend('topright',c('Actual Data', '250 Random Runs'), col=c('blue', 'red'), lty=1)
```

Cluster Solutions against Log of SSE



There seems to be around 5 groups when looking at the k-means result. Looking at the SSE plotted against the cluster groups for the actual data against 250 random runs, the point where the distance between the two stops cannging is around 5 groups.

5)

Based on the variety of dendrograms, we would reason that there should be somewhere around 4-6 groups among our data when clustering. The R square and semi-partial R squared graphs seem to place the number of groups around 5 and this is supplanted by the k-means data where we can graph the sum of squares within groups against cluster groups to see that the number of groups present seems to be around 5.