Transcript

 $\underline{\text{Version v1.0}}$

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Myth Busting

Myth: I prefer programming language X because it makes it more convinient to implement my application.

Answer: Wrong!

The fundamental problem of programming is to establish functional <u>correctness</u> and adequate <u>performance</u>. Different languages provide different tools of automating the process of <u>establishing</u> correctness and performance. The language should be chosen based on that insight.

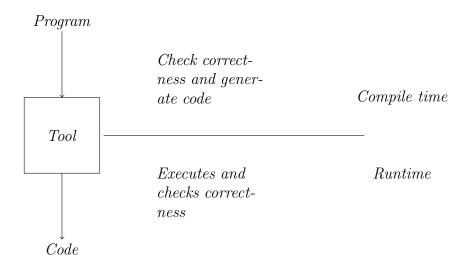


Figure 1: Process of establishing correctness.

Ultimate goal:

A Compiler checking correctness in such a sense that no exception is thrown while executing in any case. But this is infeasible (mathematical proof possible).

Hardware Exception: Interrupts, a mechanism to stop memory accesses in hardware.

Myth: I like garbage-collected languages like Java because they free me from memory management.

Answer: Wrong!

A garbage collector (GC) provides safe deallocation of unneeded memory but the programmer still needs to say what is unneeded, otherwise the system will run out of memory (memory leak).

General runtime complexity of a garbage collector: the size of the heap.



Figure 2: Unreachable, reachable and needed set of a program.

Multicore

Amdahl's Law: P represents program parallelism on N cores

• S(N) = N if P = 100%. This is ideal multicore scalability.

• In general: $S(N) = \frac{1}{(1-P) \cdot \frac{P}{N}}$

Sequential vs. Parallelized Code

The bottleneck of parallelized is the memory bus. It is limiting execution even if a problem can be perfectly parallelized without any side effects. Thus a parallelization factor of 100% is infeasible. Any shared resource at any level of an architecture creates a limitation.



Figure 3: Amdahl's law plot.



Figure 4: Bottleneck of parallelized code.

Architecture

Von Neumann Architecture

Introduced in 1945. This is a stored program computer: data = program. The Fetch-Decode-Execute cycle (see Figure 7) modifies the state of the machine.

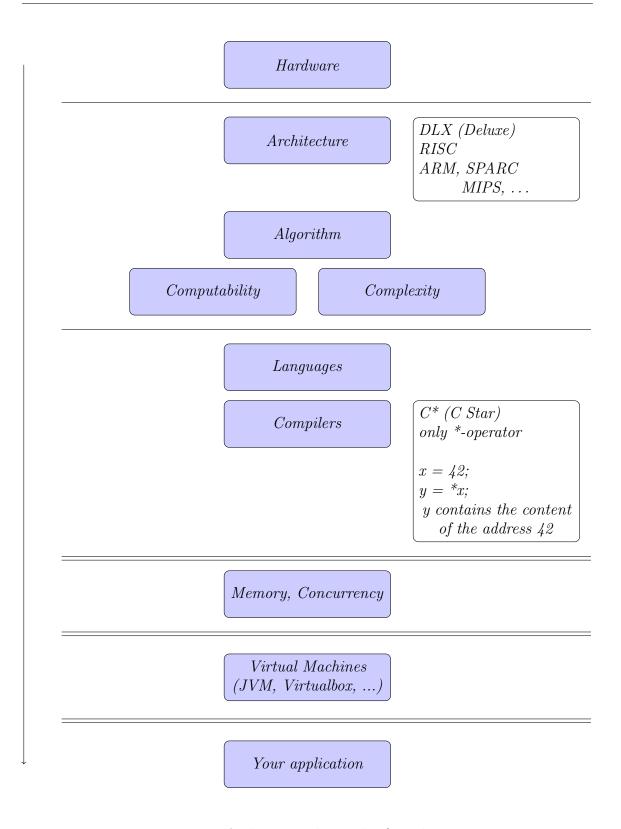


Figure 5: Architecture hierarchy (top-down.

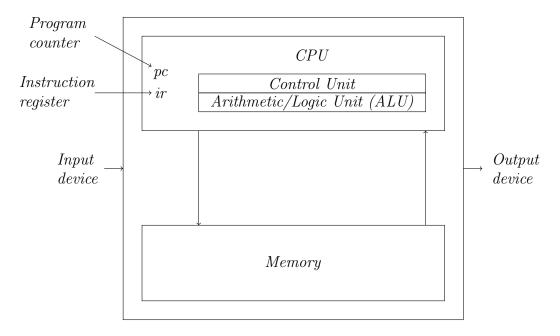


Figure 6: Von Neumann Architecture.

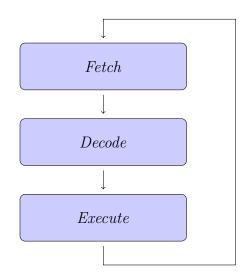


Figure 7: Fetch-Decode-Execute cycle.

DLX Machine

• Control unit: Instruction register (ir) and program counter (pc).

• Arithmetic unit:

32x 32-bit registers; reg[0], reg[1], ..., reg[31]. reg[0] always contains the value 0 and reg[31] is the link register. Both are reserved by convention and must not be used for any other purpose.

• Memory:

n 32-bit words, byte-addressed (see Figure 8), word-aligned; $mem[0], \ldots, mem[n-1]$.

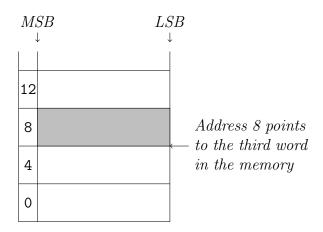


Figure 8: Visualization of a byte-addressed memory of 32-bit words.

Syntax Formats

General syntax of an instruction: op a, b, c.

$\mathbf{F1}$

The length of a and b allow to address all 32 registers. The two's complement is used here because the implementation of arithmetics is easier (in contrast to the one's complement).

op	$0 \le a \le 31$	$0 \le b \le 31$	$-2^{15} \le c \le 2^{15} - 1$
$\begin{array}{c} 6 \ bits \\ 2^6 \ ops \end{array}$	$5 bits 2^5 - 1$	$5 \ bits \ 2^5 - 1$	16 bits sign-extended to 32 bits

$\mathbf{F2}$

E.g.
$$R1 = R2 + R3$$

op	$0 \le a \le 31$	$0 \le b \le 31$	unused	$0 \le c \le 31$
$\begin{array}{c} 6 \ bits \\ 2^6 \ ops \end{array}$	$5 \ bits \ 2^5 - 1$	$5 \ bits \ 2^5 - 1$	11 bits	$5 \ bits \ 2^5 - 1$

F3

Absolute addressing in memory.

op	$0 \le c \le 2^{26} - 1$
${6 \atop 2^6} {bits} \ {2^6 \atop ops}$	$26 \ bits$ $2^{26} - 1$

<u>Von Neumann Bottleneck:</u> Memory read/write operations limit the performance.

Register Instructions

Arithmetic Instructions

$\mathbf{F}\mathbf{1}$

Instruction	Semantics	Additional information
ADDI a, b, c	reg[a]:=reg[b]+c;	Add immediate
	pc:=pc+4;	c is data (a constant)
SUBI a, b, c	reg[a]:=reg[b]-c;	Substract immediate
	pc:=pc+4;	c is data (a constant)
MULI a, b, c	reg[a]:=reg[b]*c;	Multiply immediate
	pc:=pc+4;	c is data (a constant)
DIVI a, b, c	reg[a]:=reg[b]/c;	Divide immediate
	pc:=pc+4;	c is data (a constant)
MODI a, b, c	reg[a]:=reg[b]%c;	Modulo immediate
	pc:=pc+4;	c is data (a constant)
CMPI a, b, c	reg[a]:=reg[b]-c;	Compare immediate
	pc:=pc+4;	c is data (a constant)
		reg[a] == 0 if reg[b] == c
		reg[a] >= 0 if reg[b] >= c
		reg[a]>0 if reg[b]>c
		reg[a] = <0 if reg[b] = <c< td=""></c<>
		reg[a]<0 if reg[b] <c< td=""></c<>
		reg[a]!=0 if reg[b]!=c

F2

Instruction	Semantics	Additional information
ADD a, b, c	reg[a]:=reg[b]+reg[c];	Add
	pc:=pc+4;	Register addressing reg[c]
SUB a, b, c	reg[a]:=reg[b]-reg[c];	Substract
	pc:=pc+4;	Register addressing reg[c]
MUL a, b, c	reg[a]:=reg[b]*reg[c];	Multiply
	pc:=pc+4;	Register addressing reg[c]
DIV a, b, c	reg[a]:=reg[b]/reg[c];	Divide
	pc:=pc+4;	Register addressing reg[c]
MOD a, b, c	reg[a]:=reg[b]%reg[c];	Modulo
	pc:=pc+4;	Register addressing reg[c]
CMP a, b, c	reg[a]:=reg[b]-reg[c];	Compare
	pc:=pc+4;	Register addressing reg[c]
		reg[a]==0 if reg[b]==reg[c]
		reg[a]>=0 if reg[b]>=reg[c]
		reg[a]>0 if reg[b]>reg[c]
		reg[a]=<0 if reg[b]= <reg[c]< td=""></reg[c]<>
		reg[a]<0 if reg[b] <reg[c]< td=""></reg[c]<>
		reg[a]!=0 if reg[b]!=reg[c]

Register Allocation Problem

Registers have to be used in order to execute an instruction. There are 29 registers (in theory) to use. In practice, at least in this course, less registers can be used because some registers are reserved for special purposes (stack pointer, heap pointer, globals pointer, frame pointer, ...). It must be guaranteed that these will not be used and furthermore already allocated registers must not be used for an instruction.

Examples:

C Code	Instructions	Additional information
1 + 2;	ADDI 1, 0, 1 ADDI 2, 0, 2 ADD 1, 1, 2	First, naive solution
1 + 2;	ADDI 1, 0, 1 ADDI 1, 1, 2	Second, better solution
1 + 2;	ADDI 1, 0, 3	Third, best solution Constant folding
if(1 < 2)	ADDI 1, 0, 1 ADDI 2, 0, 2 CMP 1, 0, 2	
	BGE 1, 0, <loc></loc>	<pre><loc> represents the line of code in the assembly code the CPU continues with</loc></pre>

Memory Instructions

 $\mathbf{F1}$

Instruction	Semantics	Additional information
LDW a, b, c	reg[a]:=mem[(reg[b]+c)/4];	Load word (from memory)
	pc:=pc+4;	Register-relative addressing
STW a, b, c	mem[(reg[b]+c)/4]:=reg[a];	Store word (into memory)
	pc:=pc+4;	Register-relative addressing
POP a, b, c	reg[a]:=mem[reg[b]/4];	Pop (from stack)
	reg[b]:=reg[b]+c;	c: size of the popped chunk
	pc:=pc+4;	reg[b]: contains stack pointer
PSH a, b, c	reg[b]:=reg[b]-c;	Push (onto stack)
	mem[reg[b]/4]:=reg[a];	c: size of the popped chunk
	pc:=pc+4;	reg[b]: contains stack pointer

The stack grows from high to low addresses (top-down). In the POP and PSH instructions, reg[b]:=reg[b]+c and reg[b]:=reg[b]-c represent the actual removal of the element from the stack, respectively. In case of the C* language c will always be 4 because only a single type (int) exists in this particular language. In general c is the amount of data you want to remove from the stack.

Without register-relative addressing, which is a concrete form of indirect addressing, you could only talk about as many memory cells as your program uses. The only way to get the same expressivity as with register-relative addressing is to write self-modifying code.

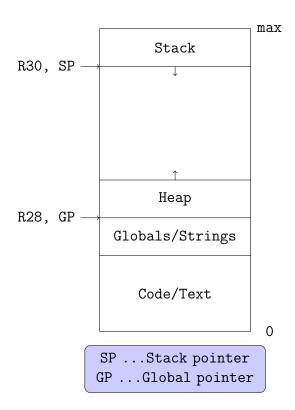


Figure 9: Memory layout when executing a program

Examples:

C Code	Instructions	Additional information
int x;	LDW 1, 28, -4	R1 := x
x = x + 1;	ADDI 2, 0, 1	R2 := 1
	ADD 1, 1, 2	R1 := R1 + R2
	STW 1, 28, -4	mem[x] = R1
*x + 1;	LDW 1, 28, -4	R1 := x
	LDW 1, 1, 0	R1 := mem[R1 + 0]
	ADDI 2, 0, 1	R2 := 1
	ADD 1, 1, 2	R1 := R1 + R2
*(x + 1);	LDW 1, 28, -4	R1 := x
	ADDI 2, 0, 4	R2 := 0 + 4, (4 because it's an address)
	ADD 1, 1, 2	R1 := R1 + R2
	LDW 1, 1, 0	R1 := mem[R1 + 0]
		*(x + i) is equivalent to $x[i]$

When dealing with *(x + 1), the type of x has to be known as well as its size in the memory. The size of x in the memory determines the offset which is added to the address of x. In case of the C* language this value is always 4 because there is only one type and no support for composed types (struct). Nevertheless, the size of the type needs to be added in general.

Formula to compute *(x + i) = x[i]: x + sizeof(x) * i.

Control Instructions

$\mathbf{F1}$

Instruction	Semantics	Additional information
BEQ a, c	if(reg[a]==0) pc:=pc+c*4;	Branch on equal to zero
	else pc:=pc+4;	Conditional branch, pc-relative
BGE a, c	if(reg[a]>=0) pc:=pc+c*4;	Branch on greater than or equal to zero
	else pc:=pc+4;	Conditional branch, pc-relative
BGT a, c	if(reg[a]>0) pc:=pc+c*4;	Branch on greater than to zero
	else pc:=pc+4;	Conditional branch, pc-relative
BLE a, c	if(reg[a]<=0) pc:=pc+c*4;	Branch on less than or equal to zero
	else pc:=pc+4;	Conditional branch, pc-relative
BLT a, c	if(reg[a]<0) pc:=pc+c*4;	Branch on less than to zero
	else pc:=pc+4;	Conditional branch, pc-relative
BNE a, c	if(reg[a]!=0) pc:=pc+c*4;	Branch on not equal to zero
	else pc:=pc+4;	Conditional branch, pc-relative
BR c	pc:=pc+c*4;	Branch (unconditional)
BSR c	reg[31]:=pc+4;	Branch to subroutine (unconditional)
	pc:=pc+c*4;	Tthe link register $(R31)$ is saved to be
		able to return to the correct instruction

$\mathbf{F2}$

Instruction	Semantics	Additional information
RET c	<pre>pc:=reg[c];</pre>	c = R31

$\mathbf{F3}$

Instruction	Semantics	Additional information
JSR c	reg[31]:=pc+4;	c = R31
	pc:=c;	absolute addressing

All branches (conditional as well as unconditional) are pc-relative. The multiplication of c by 4 is because the words in the memory are byte-addressed. Branches are useful (especially because they operate pc-relative) because you generate so-called relocatable code. Relocatable code can be moved in memory anywhere and will not change its behavior because every address is computed relative to the program counter. The drawback of branches is the restriction of the addressable space: there may be more memory than you can use with branches. The solution is absolute addressing used by the F3 format. The F3 format allows you to address a range of 2^{26} .

Example:

C Code	Instructions	Additional information
while(x<1) $\{$	LDW 1, 28, -4	R1 := x
<body></body>	ADDI 2, 0, 1	R2 := 1
}	CMP 1, 1, 2	R1 := R1 - R2
	BGE 1, 0, 0	c is set to zero, because at this point of time
		we don't know where to jump to (in general).
		A FixUp will later update this address.
	<body></body>	The body of the function
	BR 0, 0, <top></top>	<top> is the address offset to branch BEFORE</top>
		the first generated instruction (LDW 1, 28, -4).

C* is a Turing-complete language:

- arithmetics or integer
- dereferencing operator
- assignment
- while loops

Functions are not needed to satisfy Turing-completeness but reduces the size of code by preventing code duplication.

In general, every if-else-construct can be replaced by while loops, but not the other way round. However, a while loop can be replaced by a combination of functions and if-else-constructs for Turing-completeness.

Functions

Why do we use a stack and no other data structure? Because a stack guarantees proper nesting of functions, constant time access and has no spatial drawback. These facts are a result of the LIFO (Last In First Out) property of a stack.

Example:

C Code	Instructions	Additional information
f(x);	LDW 1, 28, -4	R1 := x
	PSH 1, 30, 4	Push argument on stack
	<body f="" of=""></body>	
	BSR 0, 0, <faddr></faddr>	Branch to subroutine at address offset <faddr></faddr>
	ADD 1, 0, 27	R27 is the return register (by convention)

<faddr> is often resolved by a part of the compiler called Linker. There may be two
kinds of references: symbolic references (e.g. f, the name of the function) and direct
references (e.g. addr(f), the absolute address of the function in memory).

Examples:

C Code	Instructions	Additional information
<pre>int f(int x) {</pre>	PSH 31, 30, 4	Save link register (push R31 onto stack)
<body f="" of=""></body>	PSH 29, 30, 4	Save frame pointer (push R29 onto stack)
}	ADD 29, 0, 30	Set new frame pointer to current stack pointer
		See Figure 10
return x;	LDW 1, 29, 12	Load argument \mathbf{x} from memory. The offset is
		12 here because \mathbf{x} is pushed onto the stack
		before link and frame register.
	ADD 27, 0, 1	Save x into return register
	POP 29, 30, 4	Restore caller's frame (register)
	POP 31, 30, 8	Pop link register from stack as well as x.
		This could also be done by two POP instructions
		each popping 4 bytes. In general the size to pop
		is $4 + \#args * sizeof(arg_i)$.
	RET 0, 0, 31	Return to where function was invoked

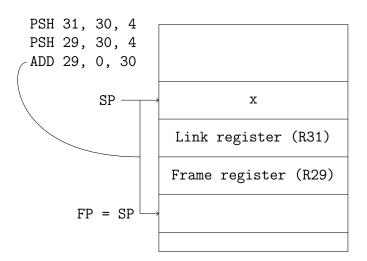


Figure 10: Stack snapshot of a function with one argument x.

Caller vs. Callee:

```
The caller of a function f invokes the function, e.g. f(x);. The callee is the function itself, e.g. int f(int x) { ... }. The callee can again be a caller if it invokes another function in its body, e.g. int f(int x) { ... g(x); ... }.
```

Declaration vs. Definition:

A declaration is inserted into the symbol table of a compiler, e.g. int x;. The declaration tells the compiler that a variable or function exists.

A definition is the actual value assignment, e.g. x = 2;. A definition can be done multiple times in a source code.

Example:

C Code	Instructions	Additional information
y = x + f(x);	LDW 1, 28, -4	Load x
	PSH 1, 30, 4	Save context of f
	LDW 1, 28, -4	Load x
	PSH 1, 30, 4	Push actual argument(s) for f onto stack
	BSR 0, 0, <faddr></faddr>	Branch to f
		Execute function f
	POP 1, 30, 4	Restore context of f
	ADD 2, 0, 27	Store return value into R2
	ADD 1, 1, 2	Actual addition of x and $f(x)$
	STW 1, 28, -8	Store result.
		-8 because it's the second global variable

Heap

Dynamically allocated memory is located on the heap. In C there is the malloc/free combination to accomplish this, in Java there is the new keyword to allocate memory dynamically but no explicit mechanism to deallocate it. Java has a garbage collector which safely deallocates unneeded memory. However, Java provides implicit deallocation mechanisms. The first is to set a reference explicitly to null:

```
x = new A(); // dynamic allocation
...
x = null;
// if no other reference to x exists here
// x will be deallocated by the garbage collector
```

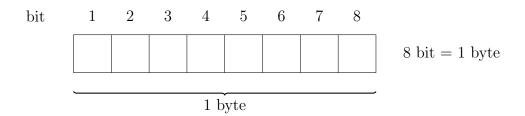
The second approach uses namespaces. When jumping out from a namespace, every namespace-local variables are unneeded if and only if there are no references from outside. If there are no such references the garbage collector will deallocate these variables:

```
{
    x = new A();
    ...
    ...
}
```

The simplest (but most unintelligent) implementation of a dynamic heap allocator is a so-called *bump pointer allocator*. A bump pointer is a pointer which only counts upwards, never downwards. In this case, there is no free to deallocate because it only grows upwards. However, the implementation of malloc is pretty simple and straigh-forward:

```
void* malloc(int s) {
    LDW 1, 29, 12
    ADD 27, 0, 26
    ADD 26, 26, 1 // R26 = Heap pointer
}
```

So every time malloc is invoked, these three DLX instructions are executed.



Byte-addressing and word-alignment:



Wie funktioniert der Zugriff auf den Stack? Wieso wird R1, R28, -4 gemacht? Latency.

Implementation von void* malloc(int s):

LDW 1, 29, 12 ADD 27, 0, 26 ADD 26, 26, 1

s: R1 = sum[R29 + 12]

Da man in C* keinen Zugriff auf Register hat, muss obiges Verhalten per Assembler implementiert werden.

malloc ist in der (g)libc enthalten und ist heutzutage de facto ein Betriebssystemfeature.

Implementation von int getchar():

RDC 0, 0, 27

Implementation von void putchar(int c):

LDW 1, 29, 12 WRC 0, 0, 1

Liest den nächsten Character aus einem Stream.

R27 = getchar();

Streams: stdin, stdout, stderr

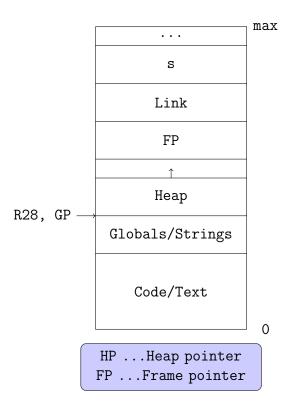


Figure 11: Memory layout revisited

$\mathbf{F2}$

Instruction	Semantics	Additional information
RDC c	reg[c] = getchar();	
WRC c	<pre>pc:=pc+4; putchar(reg[c]);</pre>	
	pc:=pc+4;	

Why is it so hard to implement \mathtt{RDC} and \mathtt{WRC} on application level? Because operating systems stuff is self-referential!



Figure 12: Application and processor

How does I/O work on a processor?

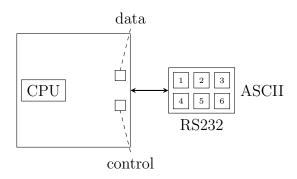


Figure 13: I/O on a processor

Computability & Complexity of algorithms

What is the minimal machine that is still universal?

- RISC: Reduced Instruction Set Computer Has separate instructions to load/store & compute. E.g. ARM, MIPS, SPARC, . . .
- CISC: Complex Instruction Set Computer More complex instructions which load, compute & store in a single instruction. E.g. x86

RISC vs. CISC \leftrightarrow Compiler vs. processor.

OISC/URISC: One/Ultimate Reduced Instruction Set Computer

```
SUBLEQ a, b, c: Subtraction less or equal
  mem[b] := mem[b] - mem[a];
  if mem[b] \leq 0 goto c;
  else pc := pc + 4;
```

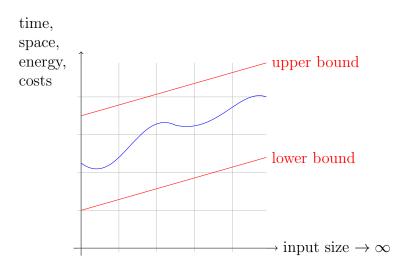


Figure 14: Asymptotic computational complexity [1]

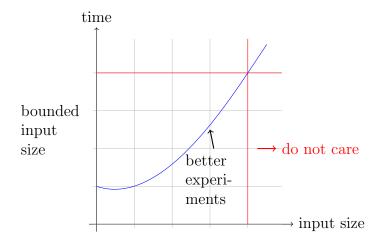


Figure 15: Asymptotic computational complexity [2] (for operating systems)

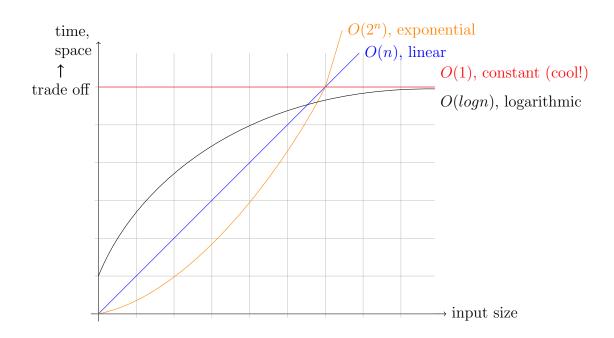


Figure 16: Big O notation (upper bound)

Big O notation (upper bound): O(#bits)

$$O(\#bits) = O(\#bytes) = O(\#char) = O(\#instructions) = O(\#objects)$$

Numeric representation

```
unary: \underbrace{||||||||||||0}_{16}, binary: \underbrace{10000}_{16}, octal: \underbrace{20}_{16}, decimal: \underbrace{16}_{16}, hexadecimal: \underbrace{10}_{16}
```

Exponential reduction from unary to binary representation: $1 + n = \lfloor log_2 n \rfloor + 1$ The main difference ist the denseness of the representations.

```
 \begin{array}{ll} \mbox{fib(n)} \ \{ \\ & \mbox{if} \ n \leq 2 \\ & \mbox{return n;} \\ & \mbox{else} \\ & \mbox{return (fib($n-1$) + fib($n-2$));} \end{array}
```

This implementation has a worst-case time complexity of $O(2^n)$. Thus, fib(7) will terminate correctly but something like fib(1024) will not terminate correctly on most systems.

There exists another implementation of the Fibonacci numbers using dynamic programming. This implementation has a logarithmic worst-case time complexity.

$$log(n) \cdot log_d(2) = log_d(n)$$

From Turing to digital:

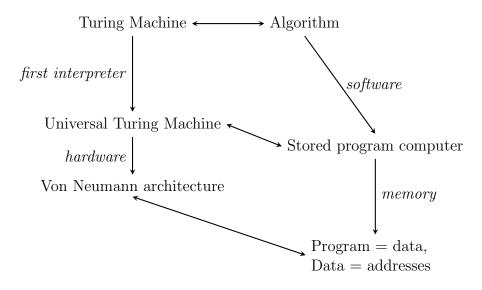


Figure 17: From Turing to digital

<u>TM:</u>

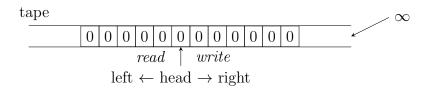


Figure 18: TM read/write

Program:

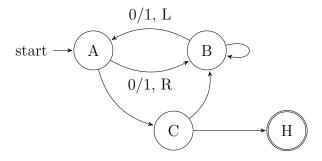


Figure 19: Busy beaver (3 states)

$$n! = \text{factorial(n)} = \begin{cases} 1 & \text{if n} = 0 \\ \text{factorial}(n-1) \cdot n & \text{otherwise} \end{cases} \Rightarrow O(n)$$

$$\underbrace{1024!}_{\text{just 4 digits but 1024 iterations/calls}} = O(2^d), d \dots \text{number of digits}$$

n! is pseudo-polynomial!

1 0000 + 0 0001 = 1 0001
$$\Rightarrow O(d)$$

Addition is much better because it has linear time complexity in the number of digits. If the computation is done numerically (the numbers are represented numerically), the time complexity is logarithmic in the size of digits: O(log(d)).

If we represent the number binary, the time complexity is doubly-exponential: $O\left(2^{2^d}\right)$.

Considering the above recursion: There are at most O(n) elements on the stack at any point of time (also in the worst case). Thus, this recursion has linear space complexity.

For some algorithm, e.g. sorting algorithms, the representation of the numbers has no effect because the numbers are only used in the comparison.

Computability:

Alan Turing:

There is no algorithm to decide whether an arbitrary program halts on a given input (1936). Halting problem.

Rice:

Generalization to any non-trivial property of partial functions (programs that may or may not terminate) computed by arbitrary programs. A compiler can not analyze a program for an arbitrary property.

Church:

1 month earlier than Turing using λ -calculus.

Proof sketch:

total function: defined on our inputs

partial function: will not terminate for inputs for which it is not defined

1.
$$h(i, x) = \begin{cases} 1 & \text{program } i \text{ halts on } x \\ 0 & \text{otherwise} \end{cases}$$
 $h(i, x)$ is a total, computable function.

2. Let f be any total, computable function with two arguments (in fact it may even be h(i, x).

```
3. g(i) = \begin{cases} 0 & \text{if } f(i,i) = 0\\ \text{undefined} & \text{otherwise} \end{cases}
```

Equivalent program code:
if(f(i, i) == 0) return 0;
else while(true) {};

g(i) is a partial, computable function.

- 4. g(i) may be partial but is computable by a program e (as described in the step before).
- 5. If f(e,e) = 0: g(e) = 0 by definition $\Rightarrow h(e,e) = 1$. If $f(e,e) \neq 0$: g(e) = undefined (does not terminate) $\Rightarrow h(e,e) = 0$. $\Rightarrow f$ is always different from $h \Rightarrow h$ can not be programmed.

This proof technique is called *Diagonalization* and was introduced by Cantor in 1891.

Given 2 infinite sets: which one is bigger (cardinality)? E.g. \mathbb{N} vs. $P(\mathbb{N})$: $\mathbb{N} < P(\mathbb{N})$ (strictly bigger!)

N: There are enough natural numbers to encode any program you can ever think of.

Another view on the halting problem:

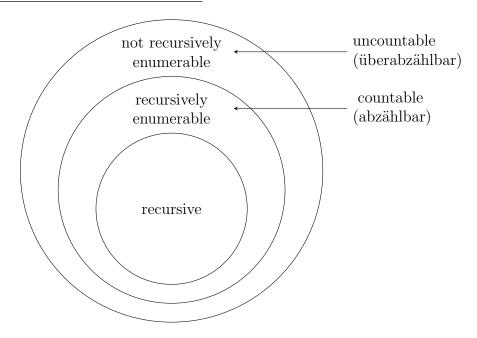


Figure 20: The halting problem in terms of languages.

• Recursive:

A language (a set of strings) is recursive if it is accepted by a Turing machine which always terminates/halts.

- Recursively enumerable (r. e.): A language is recursively enumerable if it is accepted by a Turing machine which may terminate/halt on a string not in the language. $\{(i, x) | \text{program } i \text{ halts on } x\}$
- Not recursively enumerable (n. r. e.): Is actually <u>not</u> a superset of the r. e. set but n. r. e. \cup r. e. results in the set of all reachable programs. This set is uncountable. $\{(i,x)|\text{program }i\text{ does not halt on }x\}$

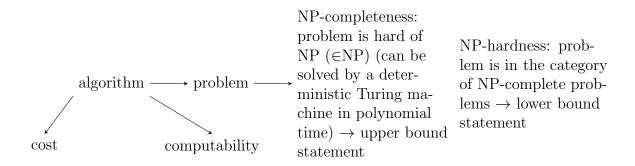


Figure 21: NP-completeness & NP-hardness

In full generality, a compiler cannot choose whether a code is dead or not \Rightarrow NP-hard.

In some trivial cases, the compiler can actually recognize dead code.

Syntex & Semantics:

Syntax: Parser, Syntax analysis, ...

Semantics: Code generator, semantics definition, ...

In combination: compiler

Syntax:

- 1. What is correct syntax? Specification
- 2. Parser

```
Example: 1 + (2 + y) * z
```

Grammar:

Symbol	Description
<pre><string> (e.g. expression)</string></pre>	non-terminal
" <string>" (e.g. "a")</string>	terminal
[<symbol>] (e.g. ["-"])</symbol>	optionality
{ <symbol>} (e.g. {digit})</symbol>	repetition
	OR

Parser: context-free \rightarrow counts symbols (e.g. matching parentheses); Recursive-decent parser

```
 \begin{array}{l} \text{expression} := \ ["-"] \ \text{term} \ \big\{ ("+" \mid "-") \ \text{term} \big\}. \\ \\ \text{term} := \ \text{factor} \ \big\{ ("*" \mid "/") \ \text{factor} \big\}. \\ \\ \text{factor} := \ \text{identifier} \ | \ \text{integer} \ | \ "(" \ \text{expression} \ ")". \\ \\ \end{array}
```

Scanner (FSM): reads character-wise and decides; regular \rightarrow if you can transform this into a single equation

```
identifier := letter {letter | digit}.
letter := "a" | "b" | ...| "z" | "A" | "B" | ...| "Z".
digit := "0" | "1" | ...| "9".
integer := digit {digit}.
```

Implementation of expression():

```
expression() {
  if(symbol == MINUS)
    getSymbol(); // next symbol
  term();
  while((symbol == PLUS) || (symbol == MINUS)) {
    getSymbol();
    term();
  }
}
```

So far no semantics!

See

- \bullet CS4NonCSs Introduction.pdf
- \bullet CS4NonCSs Architecture.pdf

What we want:

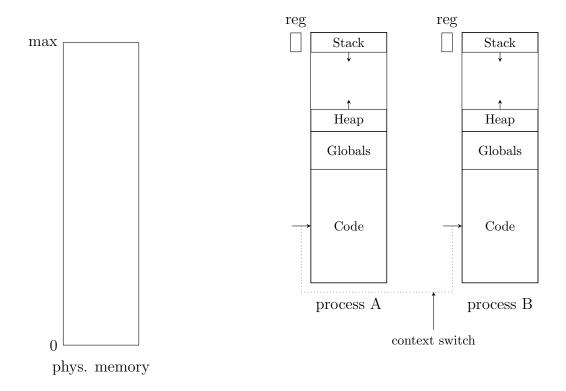


Figure 22: Each process thinks it owns the whole memory.

Each process has its own virtual memory which is loaded whenever a context switch is performed. Concurrency (competing for resources, time sharing) \neq Parallelism (truely parallel, multiple processors). Spatial isolation is necessary to enable concurrency.

<u>Data structures:</u>

2 Goals:

- 1. Abstraction: table, list, tree, graph, ...
- 2. Safety: only accessing memory we have declared, memory access as specified.
- 2 levels where we can have safety:

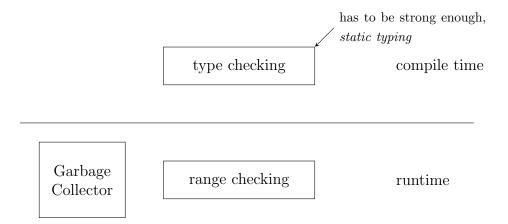


Figure 23: safety levels

Unless all accesses use constants as indices, in general no compiler can perform a range check at compile time. At some point there is a limit. E.g. i = 10; a[i]; is recognized by some compilers.

If you do not allow dynamic allocation, your language does not allow to write a program which accesses memory outside (type and range checks required of course!). Suppose a free mechanism: you could free something and access it afterwards, or you could do free(obj); which creates a dangling pointer, and do obj.field = 1; afterwards.

Arrays:

```
int a[3];
```

The advantage of the contiguous layout in memory: constant time access. The big drawback of the contiguous layout in memory: fragmentation.

3 ingredients of fragmentation:

- 1. contiguously allocated memory gives us constant time access (could be splitted as well)
- 2. blocks of different size
- 3. the order of deallocation is not equal to the order of allocation

In the worst case, there is a 50/50 allocation present. If we then want to allocate a big chunk of memory, it is not possible without some reordering.

Records:

```
struct rec {
  int i;
  struct rec *r;
};
```

The advantages of the contiguous layout in memory:

- constant time access (even faster than the array access because the offsets can be computed at compile time)
- no fragmentation (if the implementer knows what s/he is doing)

The disadvantage is the fact that the access complexity is not constant but linear in the size of the list.

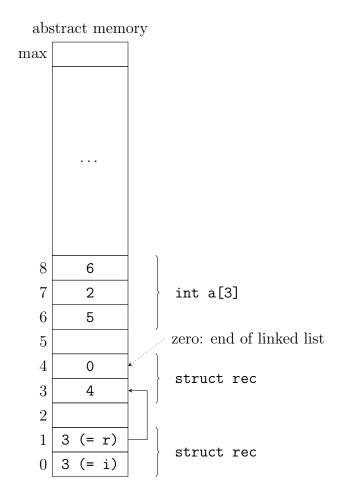


Figure 24: Arrays and records in the memory

The only other option (to use contiguous allocation):

Construct data structures out of pointers.

If we just allocate a billion of struct rec (which actually all have the same size), there is no fragmentation.

Memory Hierarchy:

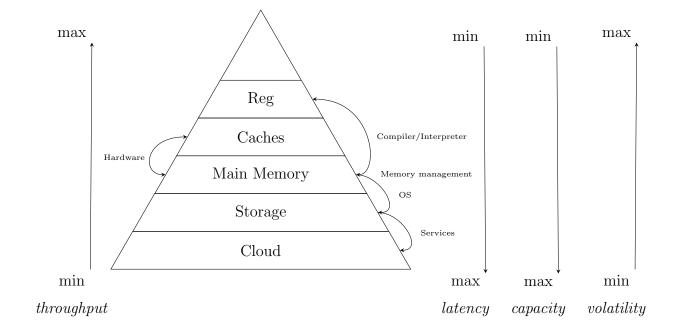


Figure 25: Memory hierarchy

Services: Dropbox, Google Cloud, ...