

# Revisiting Structure from Motion with 3D Reconstruction Priors

Guided Research WS24/25

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Advisor: Prof. Matthias Nießner

30.05.2025

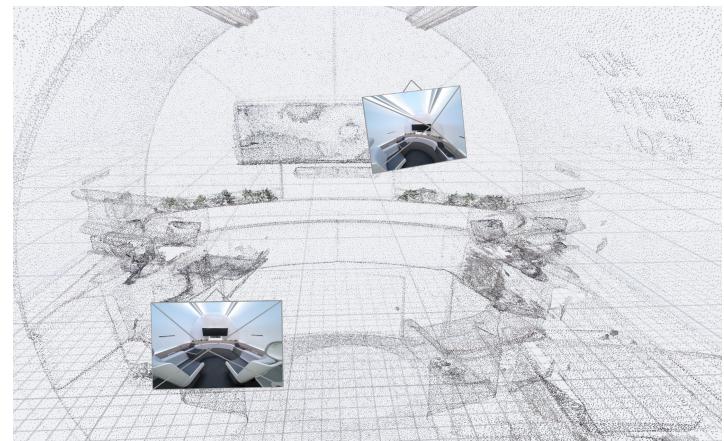
# Introduction

# Structure from Motion

2D Image Collection



3D Reconstruction



Camera Position + 3D Points

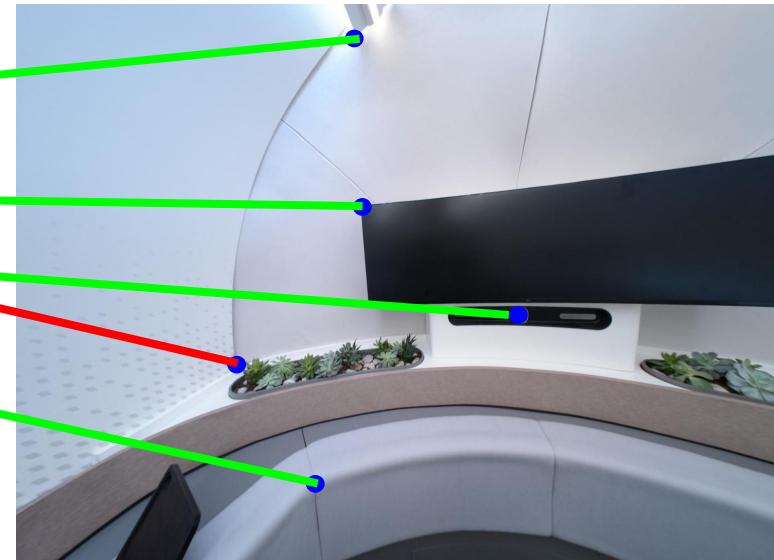
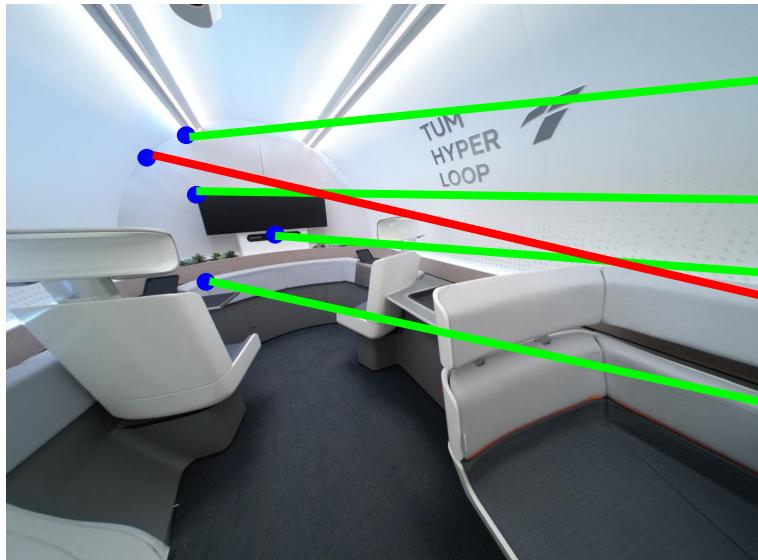
# Detection + Description



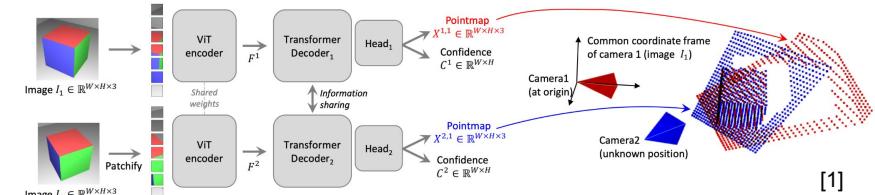
# Descriptor Matching



# Geometric Verification



# 3D Reconstruction Networks



[1]

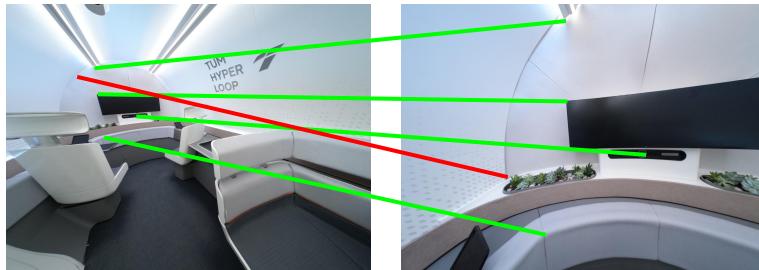
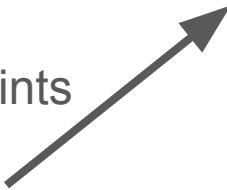


[1] Wang et al., "Dust3r: Geometric 3d vision made easy", CVPR 2024

# SfM Optimization

## Global Optimization

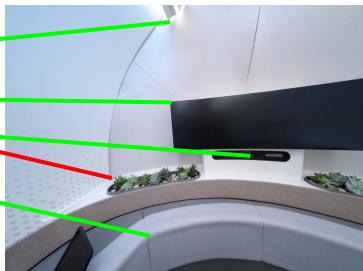
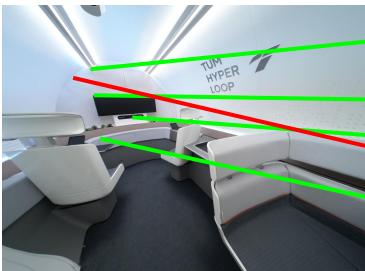
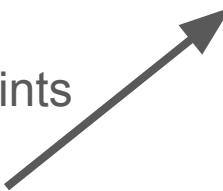
2D Constraints



# SfM Optimization

## Global Optimization

2D Constraints



3D Recon Networks

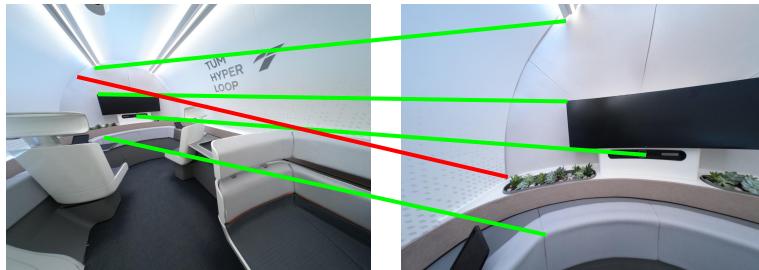
dense 2D-3D mapping



# SfM Optimization

## Global Optimization

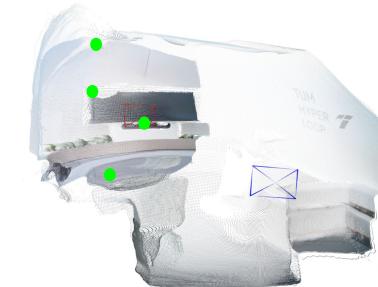
2D Constraints



3D Recon Networks

dense 2D-3D mapping

3D Constraints ?

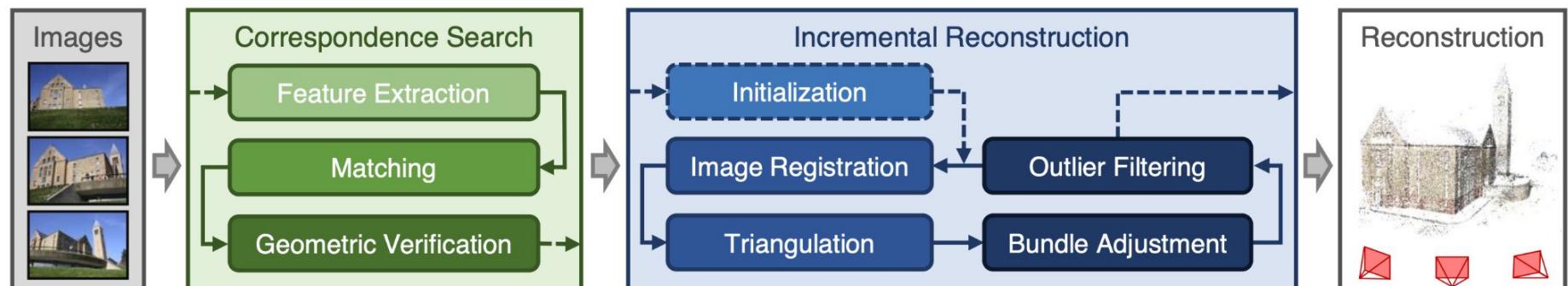


# **Goal**

Add 3D Constraints to SfM Pipeline

# Related Work

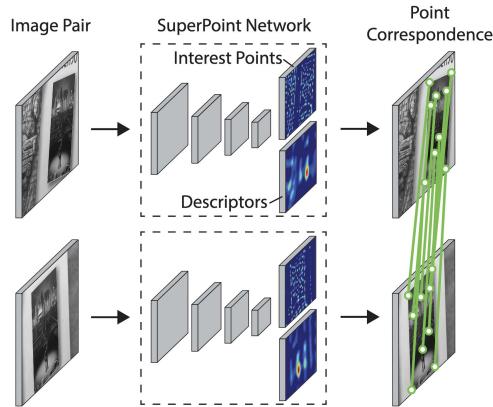
# Incremental SfM Pipeline



[1] Schönberger and Frahm, “Structure-from-motion revisited”, CVPR 2016

# Modern SfM

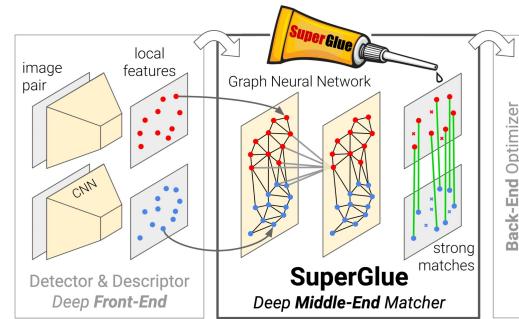
## Detection / Description



SuperPoint [1],  
DeDoDe [2], ...

- [1] DeTone et al., "SuperPoint: Self-supervised interest point detection and description", CVPRW 2018
- [2] Edstedt et al., "DeDoDe: Detect, Don't Describe - Describe, Don't Detect for Local Feature Matching", 3DV 2024c

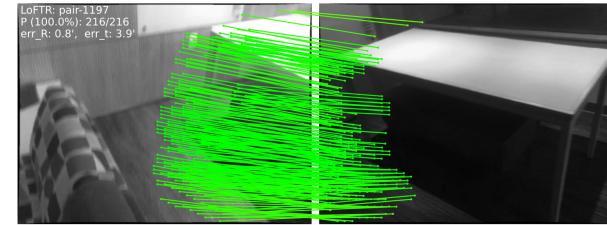
## Descriptor Matching



SuperGlue [3],  
LightGlue [4], ...

- [3] Sarlin et al., "SuperGlue: Learning feature matching with graph neural networks", CVPR 2020
- [4] Lindenberger et al., "LightGlue: Local Feature Matching at Light Speed", ICCV 2023

## Dense Matching

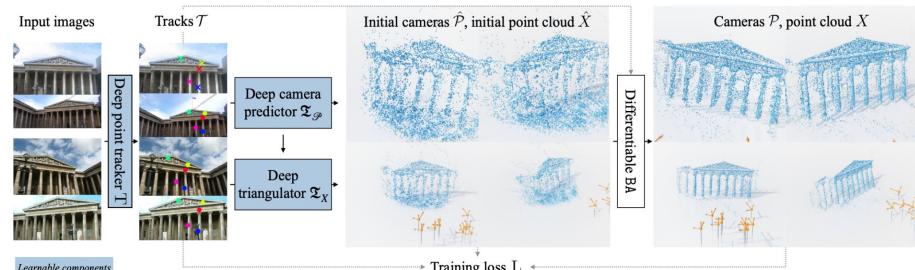


LoFTR [5],  
RoMA [6], ...

- [5] Sun et al., "LoFTR: Detector-free local feature matching with transformers", CVPR 2021
- [6] Edstedt et al., "RoMA: Robust Dense Feature Matching", CVPR 2024

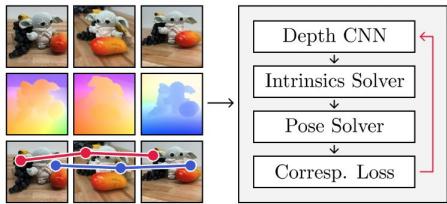
# End-to-End differentiable SfM

VGGsFm [1]



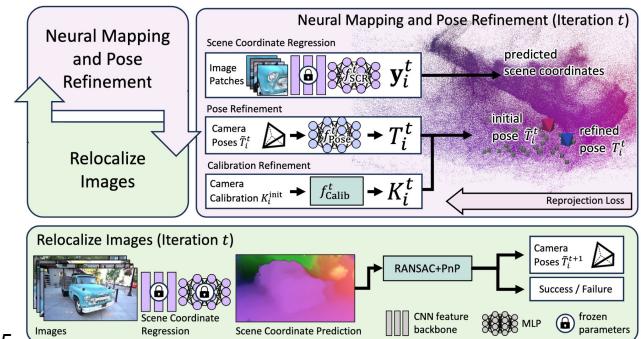
FlowMap [2]

Video and Off-the-Shelf Correspondences  
FlowMap Optimization via **Gradient Descent**



Downstream Task:  
Gaussian Splatting

ACE0 [3]



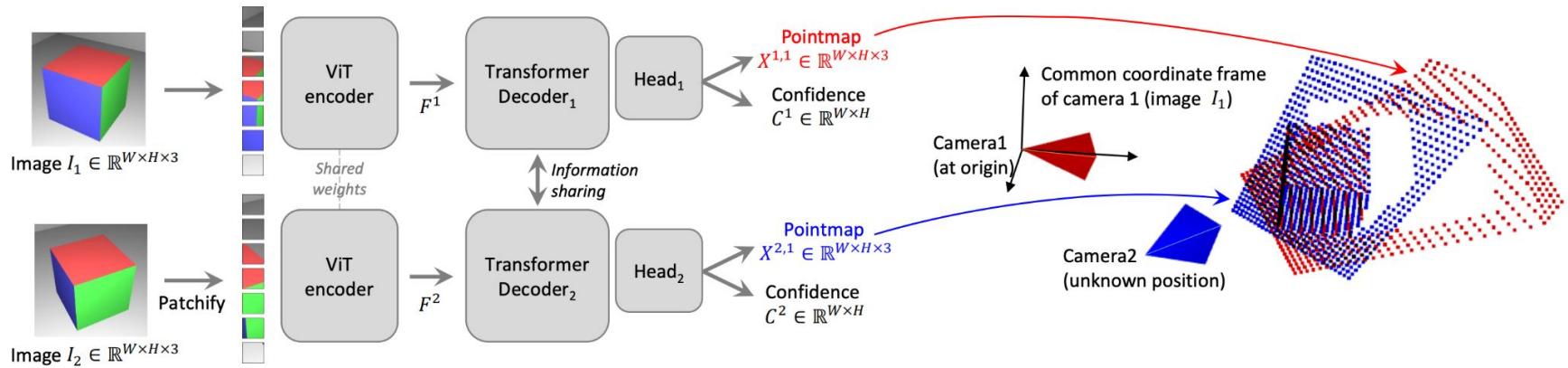
[1] Wang et al., “VGGsFm: Visual geometry grounded deep structure from motion”, CVPR 2024

[2] Smith & Charatan et al., “Flowmap: High-quality camera poses, intrinsics, and depth via gradient descent”, 3DV 2025

[3] Brachmann et al., “Scene Coordinate Reconstruction: Posing of image collections via incremental learning of a relocalizer”, ECCV 2024

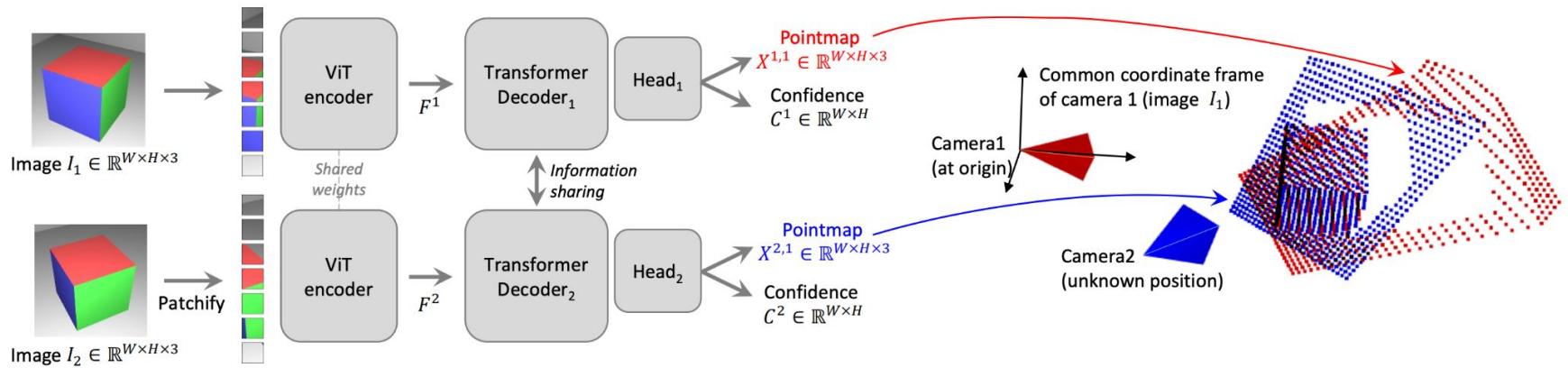
# 3D Reconstruction Networks - DUST3R [1]

[1] Wang et al., "Dust3r: Geometric 3d vision made easy", CVPR 2024



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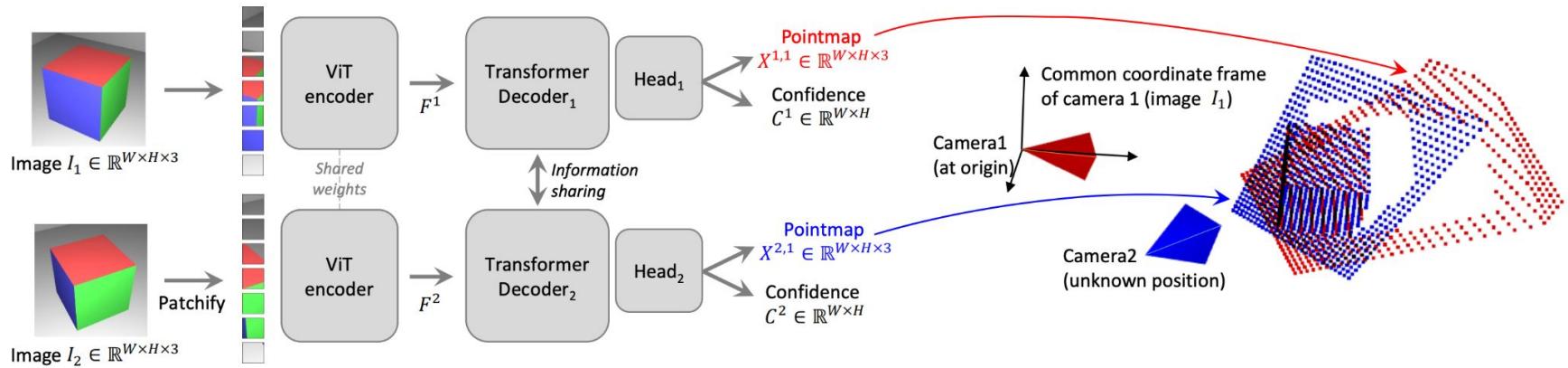
**Follow-up:**  
MASt3R [2],  
MASt3R-SfM [3]

[2] Leroy et al., "Grounding image matching in 3d with mast3r", arXiv 2024

[3] Duisterhof et al., "MASt3R-SfM: a fully-integrated solution for unconstrained structure-from-motion", 3DV 2025

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[1] Wang et al., "Dust3r: Geometric 3d vision made easy", CVPR 2024



**Follow-up:**  
MASt3R [2],  
MASt3R-SfM [3]

**Multiple Views:**  
MV-DUST3R+ [4],  
VGGT [5]

[2] Leroy et al., "Grounding image matching in 3d with mast3r", arXiv 2024

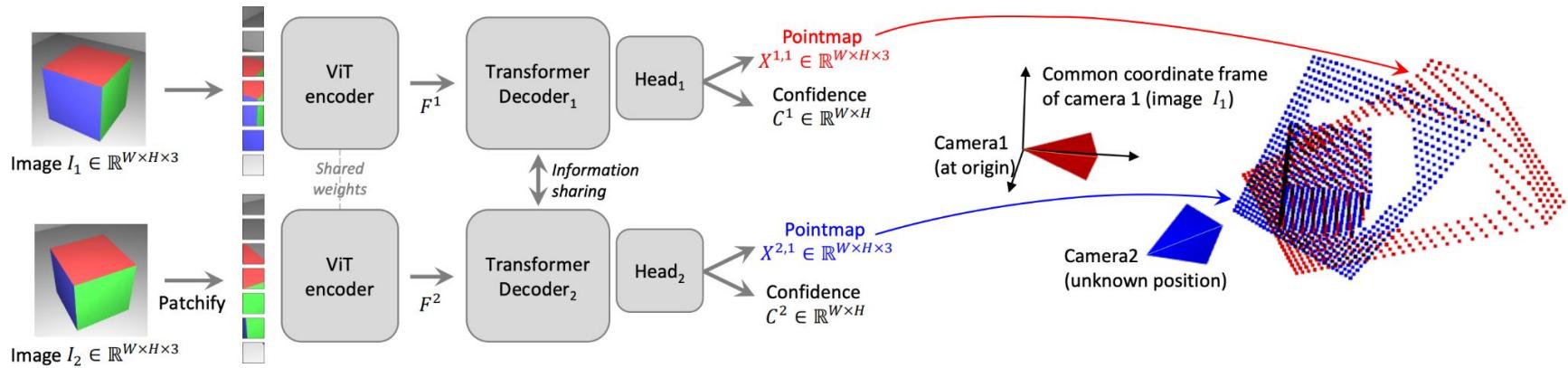
[3] Duisterhof et al., "MASt3R-SfM: a fully-integrated solution for unconstrained structure-from-motion", 3DV 2025

[4] Tang et al., "MV-DUST3R+: Single-stage scene reconstruction from sparse views in 2 seconds", CVPR 2025

[5] Wang et al., "VGGT: Visual geometry grounded transformer", CVPR 2025

# 3D Reconstruction Networks - DUST3R [1]

[1] Wang et al., "Dust3r: Geometric 3d vision made easy", CVPR 2024



**Follow-up:**  
MASt3R [2],  
MASt3R-SfM [3]

**Multiple Views:**  
MV-DUST3R+ [4],  
VGGT [5]

**Adapt to downstream:**  
MASt3R-SLAM [6],  
InstantSplat [7],

[2] Leroy et al., "Grounding image matching in 3d with mast3r", arXiv 2024

[3] Duisterhof et al., "MASt3R-SfM: a fully-integrated solution for unconstrained structure-from-motion", 3DV 2025

[4] Tang et al., "MV-DUST3R+: Single-stage scene reconstruction from sparse views in 2 seconds", CVPR 2025

[5] Wang et al., "VGGT: Visual geometry grounded transformer", CVPR 2025

[6] Murai et al., "MASt3R-SLAM: Real-time dense SLAM with 3D reconstruction priors", CVPR 2025

[7] Fan et al., "InstantSplat: Sparse-View Gaussian Splatting in Seconds", arXiv 2024

# Reconstruction Evolution

## Incremental SfM



# Reconstruction Evolution

## Incremental SfM

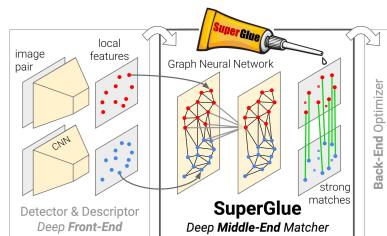
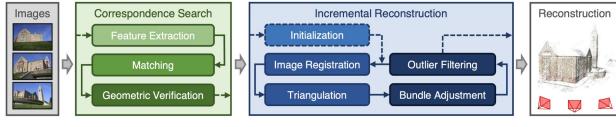
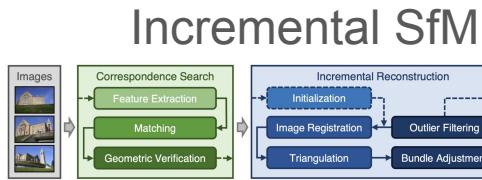
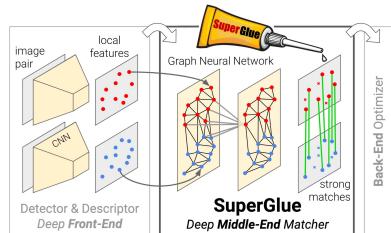
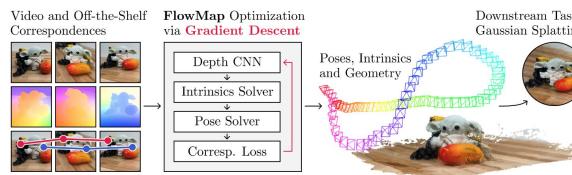


Image Matching

# Reconstruction Evolution



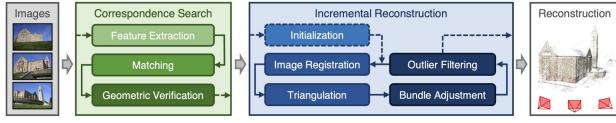
## End-to-End SfM



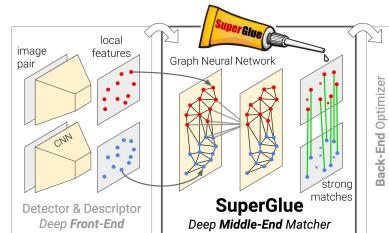
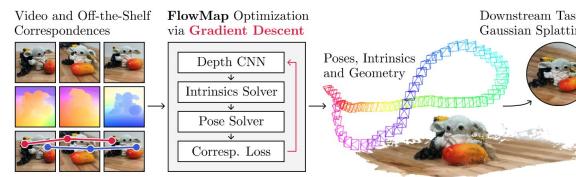
## Image Matching

# Reconstruction Evolution

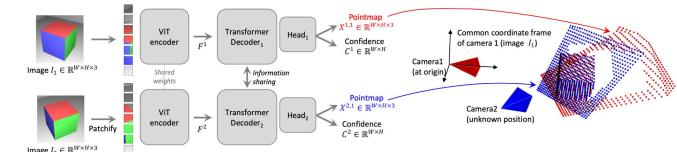
## Incremental SfM



## End-to-End SfM

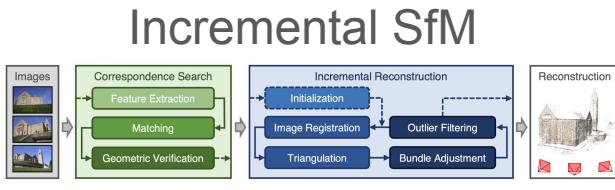


## Image Matching

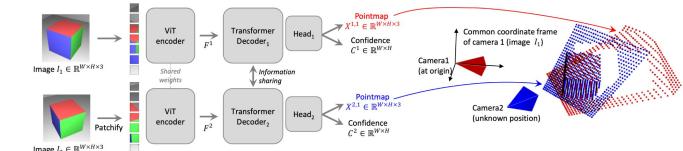
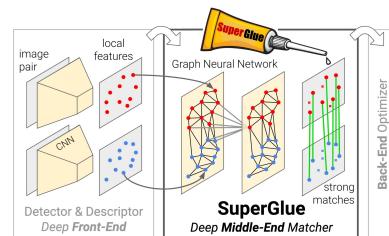
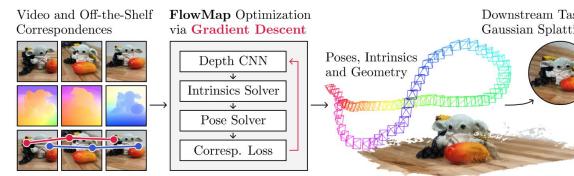


## 3D Reconstruction Networks

# Reconstruction Evolution

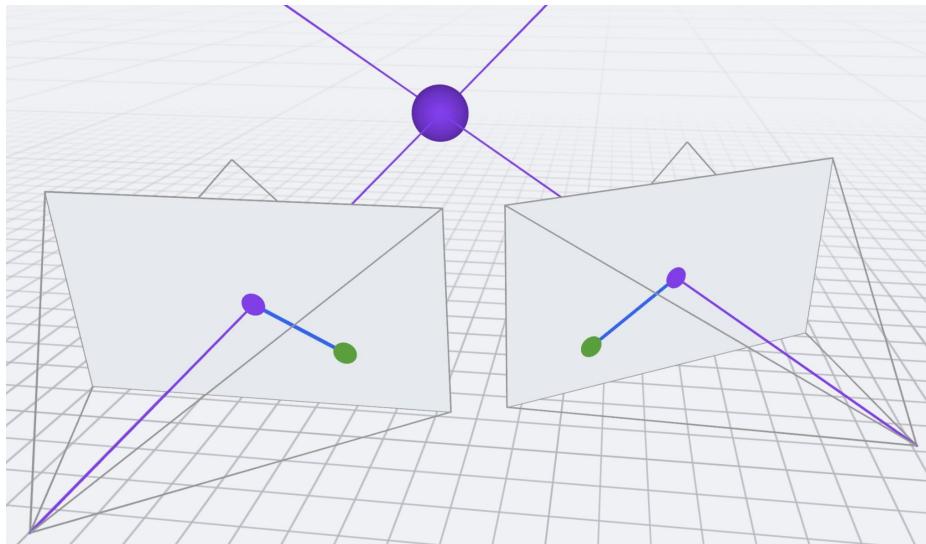


## End-to-End SfM



# Preliminaries

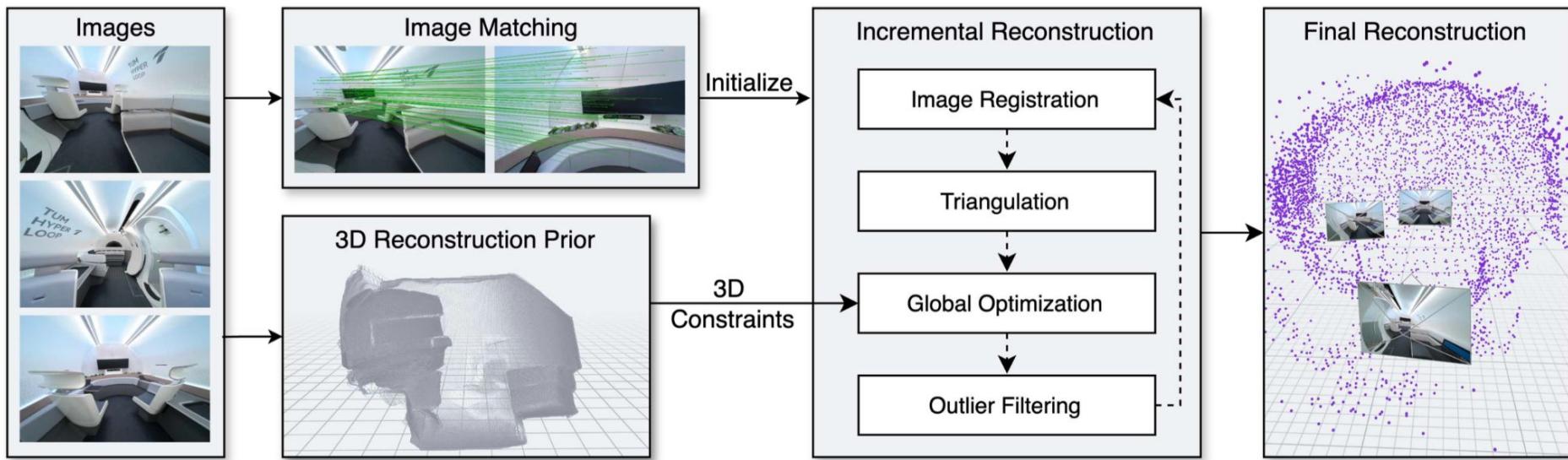
# Bundle Adjustment



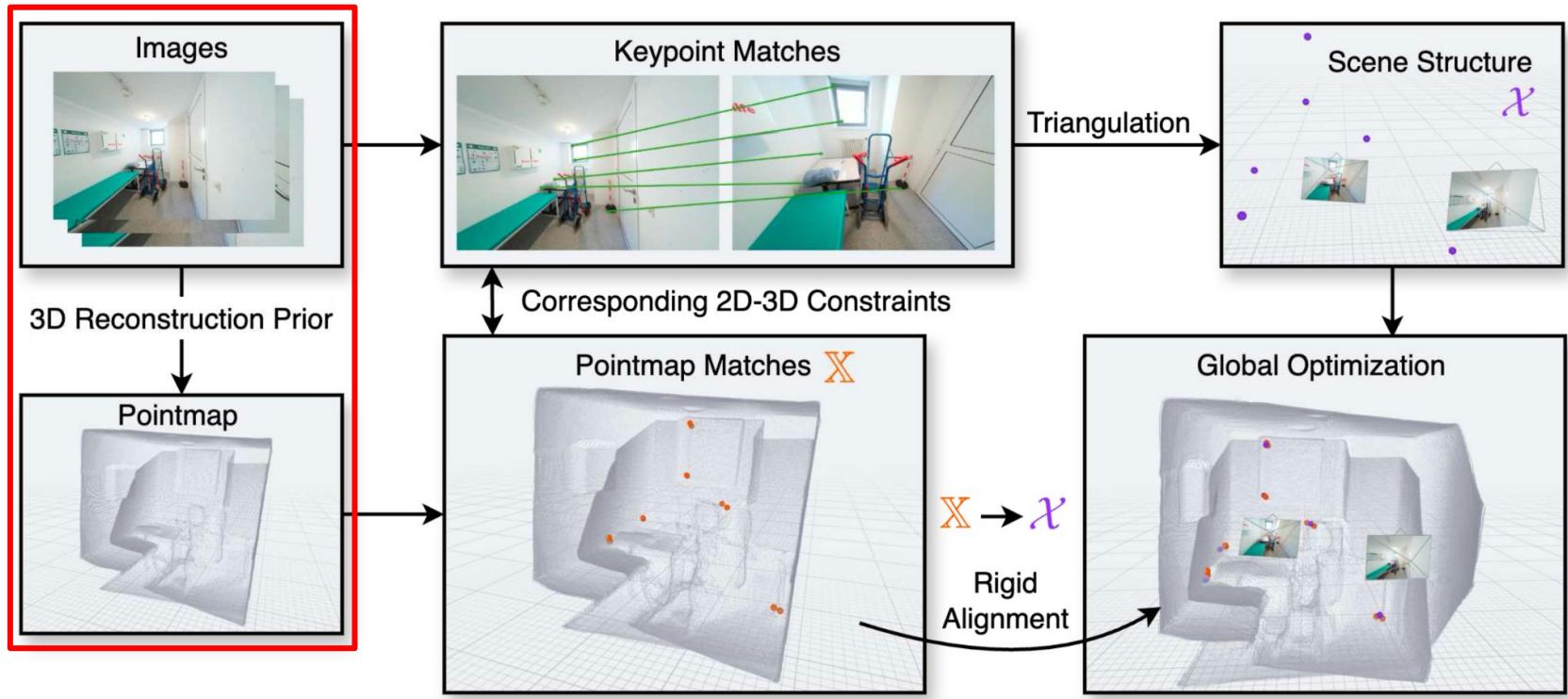
$$E_{\text{BA}} = \sum_{i=1}^N \sum_{k=1}^M \| \boxed{y_{i,k}} - \pi(K_i, T_i, \boxed{x_k}) \|^2$$

# Method

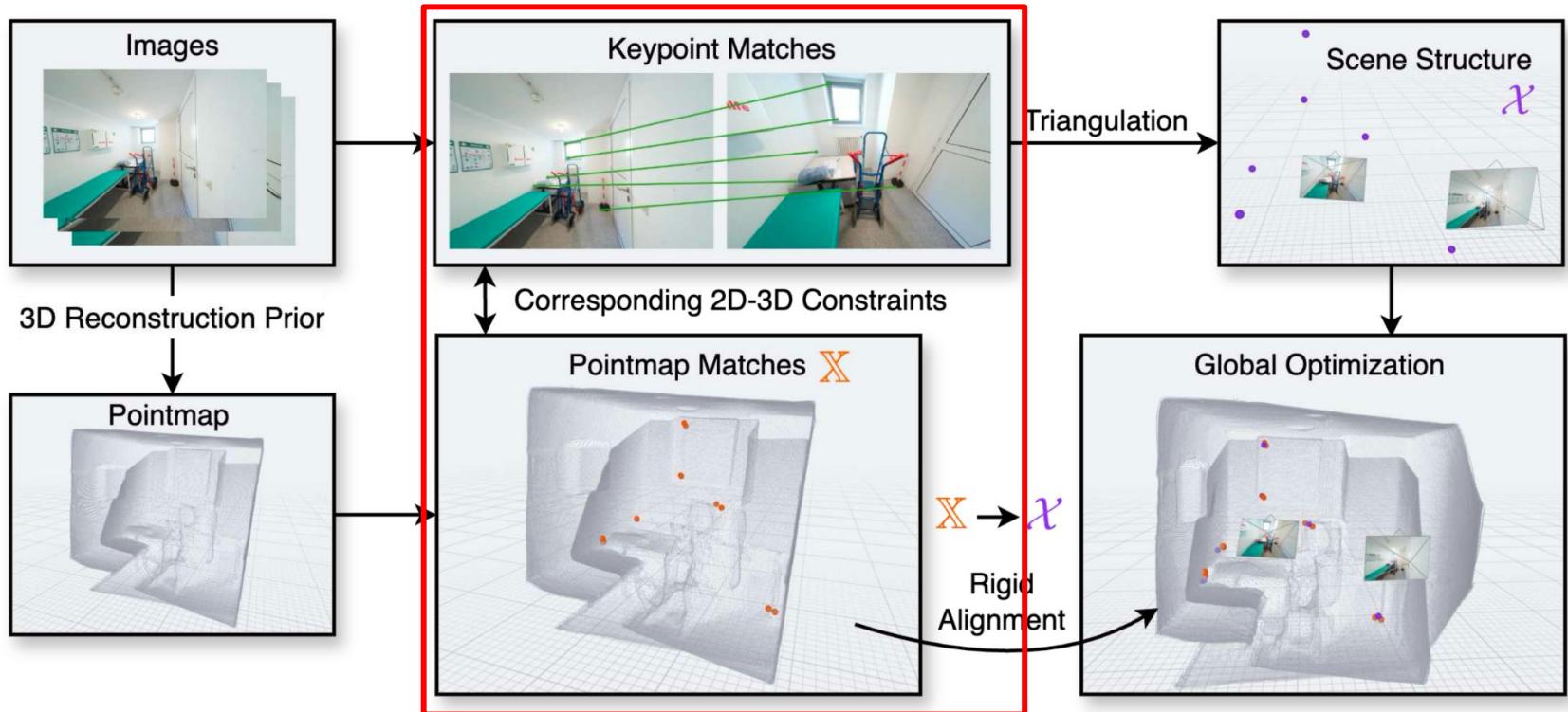
# Pipeline



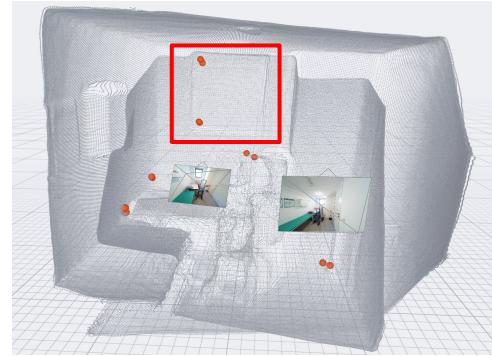
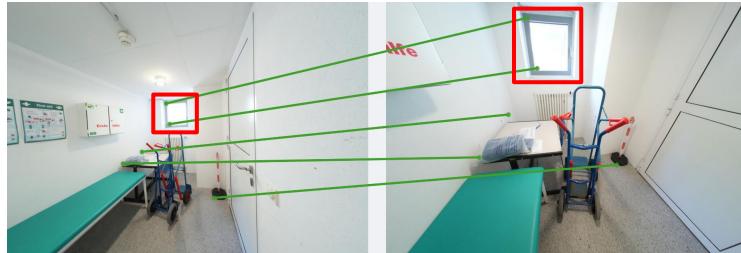
# Method Overview



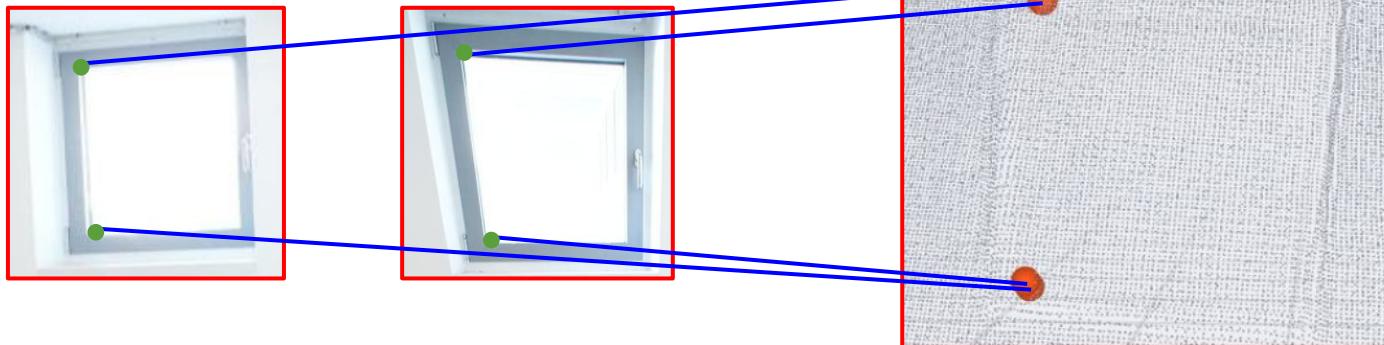
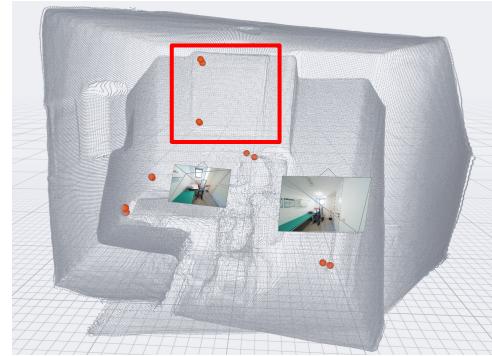
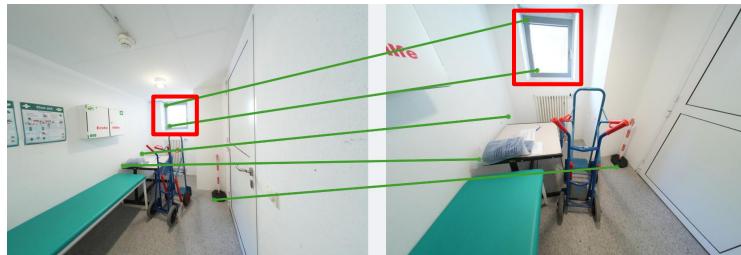
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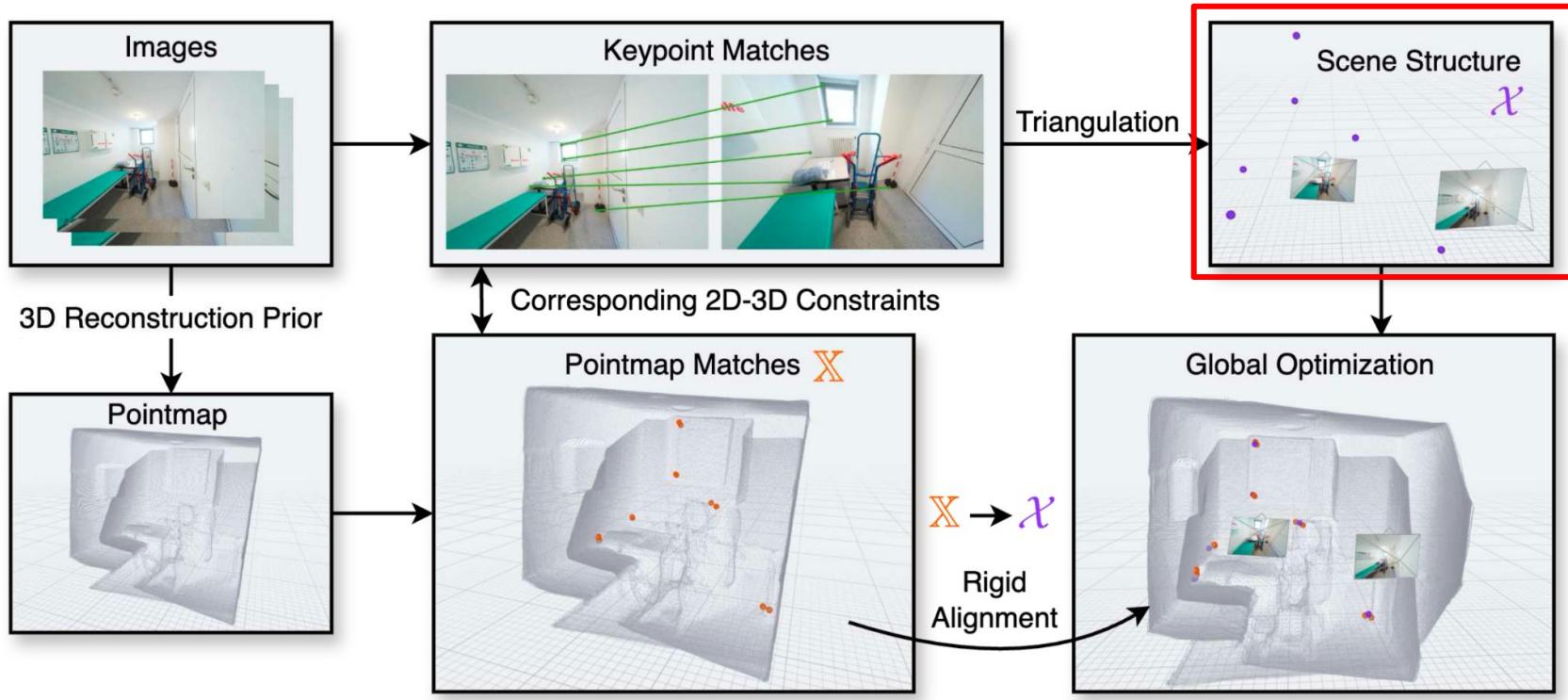
# 2D-3D Matches



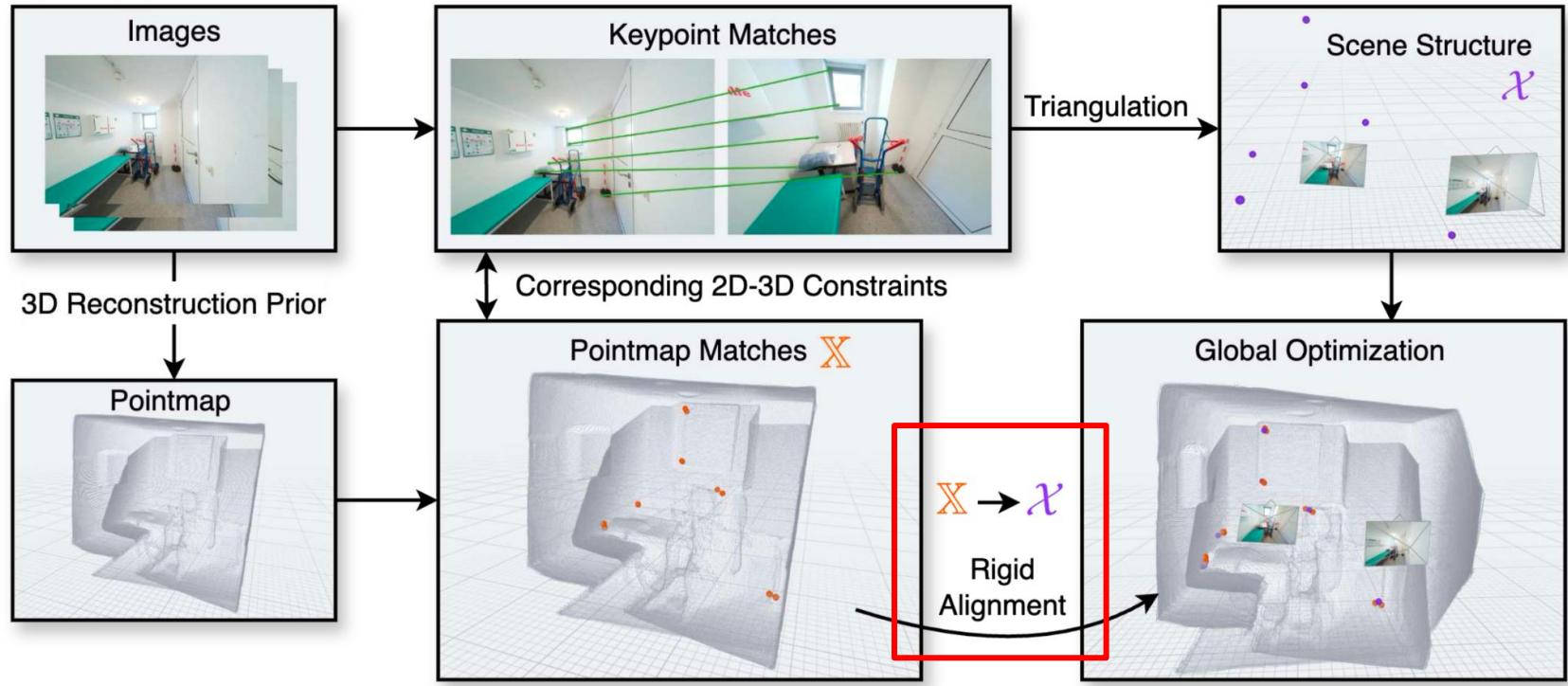
# 2D-3D Matches



# Method Overview

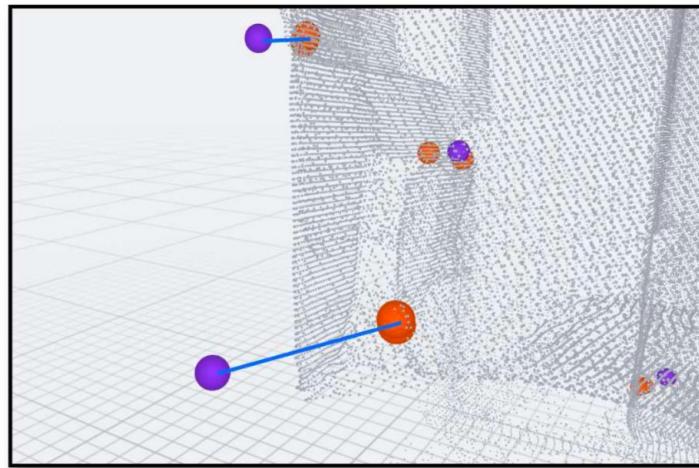


# Method Overview



# Global Optimization

Point-to-Point Error



$$\min_{\mathcal{X}, T} \| \mathcal{X} - T(\mathbb{X}) \|$$

Intuitively: Make Scene Structure “agree” with 3D Reconstruction Networks

## More Formally

$$E_{\text{P2P}} = \sum_{e \in \mathcal{E}} \sum_{l \in \{i, j\}} \sum_{k=1}^{M_e} \|x_k - s_e T_e(x_k^{l,e})\|^2$$

## More Formally

$$E_{\text{P2P}} = \sum_{e \in \mathcal{E}} \sum_{l \in \{i, j\}} \sum_{k=1}^{M_e} \| \boxed{x_k} - s_e T_e(x_k^{l,e}) \|_2^2$$

## More Formally

$$E_{\text{P2P}} = \sum_{e \in \mathcal{E}} \sum_{l \in \{i, j\}} \sum_{k=1}^{M_e} \| \boxed{x_k} - \boxed{s_e T_e(x_k^{l,e})} \|^2$$

scene point      pointmap point  
rigid transformation  
(+ scale)

## More Formally

$$E_{\text{P2P}} = \sum_{e \in \mathcal{E}} \sum_{l \in \{i, j\}} \sum_{k=1}^{M_e} \| x_k - s_e T_e(x_k^{l,e}) \|^2$$

scene point      pointmap point  
rigid transformation  
(+ scale)

for all pairwise  
 pointmaps

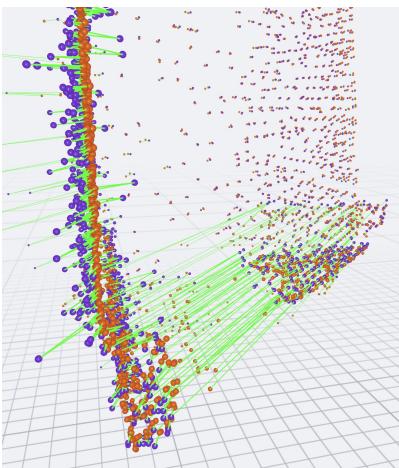
## More Formally

$$E_{\text{P2P}} = \sum_{e \in \mathcal{E}} \sum_{l \in \{i, j\}} \left| \sum_{k=1}^{M_e} \| x_k - s_e T_e(x_k^{l,e}) \|^2 \right|$$

for all pairwise pointmaps      for all matches

# More Formally

$$E_{\text{P2P}} = \sum_{e \in \mathcal{E}} \sum_{l \in \{i, j\}} \sum_{k=1}^{M_e^*} \|x_k - s_e T_e(x_k^{l,e})\|^2$$



**-> Rigid Alignment (RANSAC) + only minimize for inliers**

## More Formally

$$E_{\text{P2P}} = \sum_{e \in \mathcal{E}} \sum_{l \in \{i, j\}} \sum_{k=1}^{M_e^*} \boxed{c_k^{l,e}} \|x_k - s_e T_e(x_k^{l,e})\|^2$$

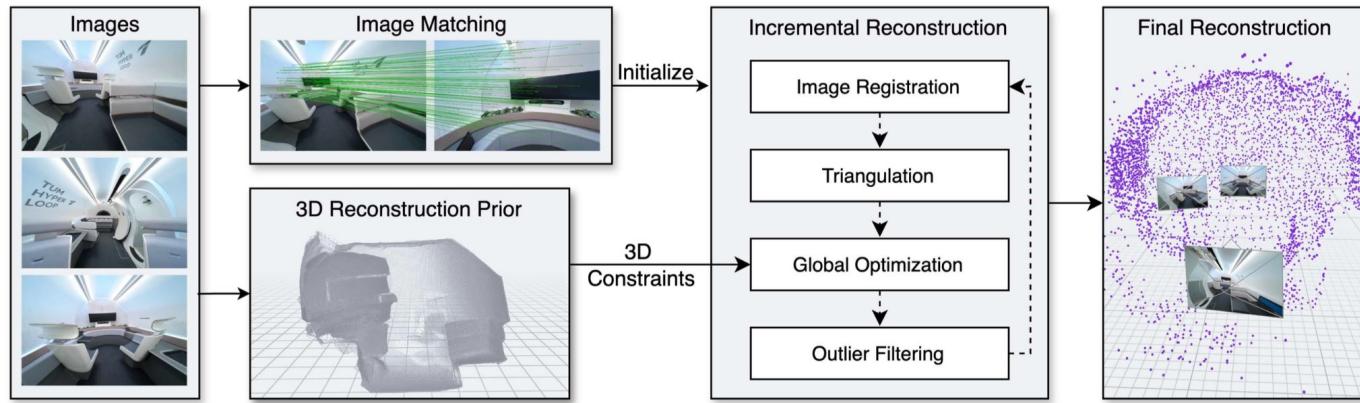
**pointmap confidence -> downweight impact of inaccurate pointmaps**

# Global Optimization

$$\mathcal{X}^*, \mathcal{H}^* = \arg \min_{\mathcal{X}, \mathcal{H}, \mathcal{T}} (E_{BA} + \beta E_{P2P})$$

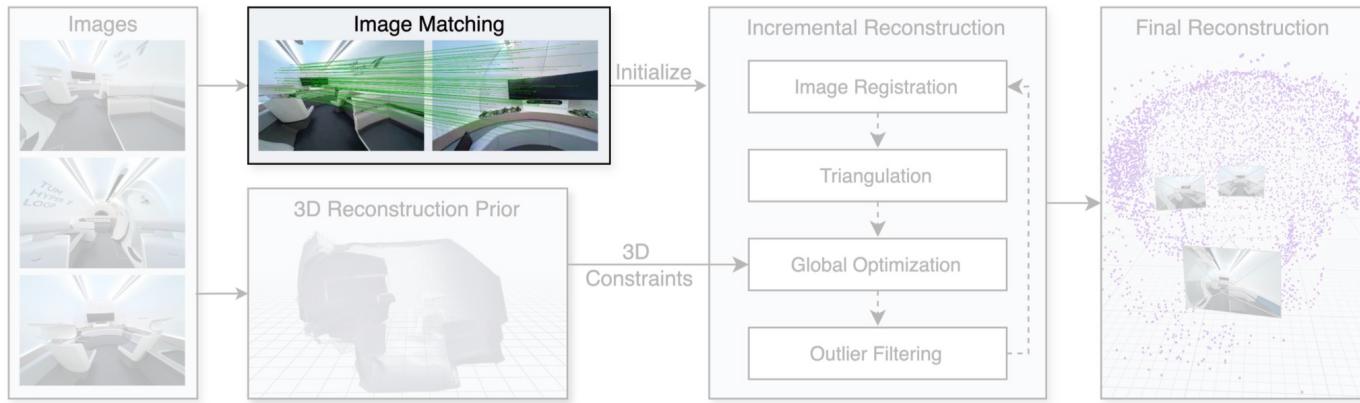
The diagram illustrates the inputs to the optimization equation. It features three labels at the bottom: "Scene Cloud" in purple, "Camera Params" in yellow, and "Rigid Transformations" in cyan. Arrows point from each label to the corresponding term in the equation above. A purple arrow points from "Scene Cloud" to the first term  $\mathcal{X}^*$ . A yellow arrow points from "Camera Params" to the second term  $\mathcal{H}^*$ . A cyan arrow points from "Rigid Transformations" to the third term  $\mathcal{T}$ .

# Implementation Details



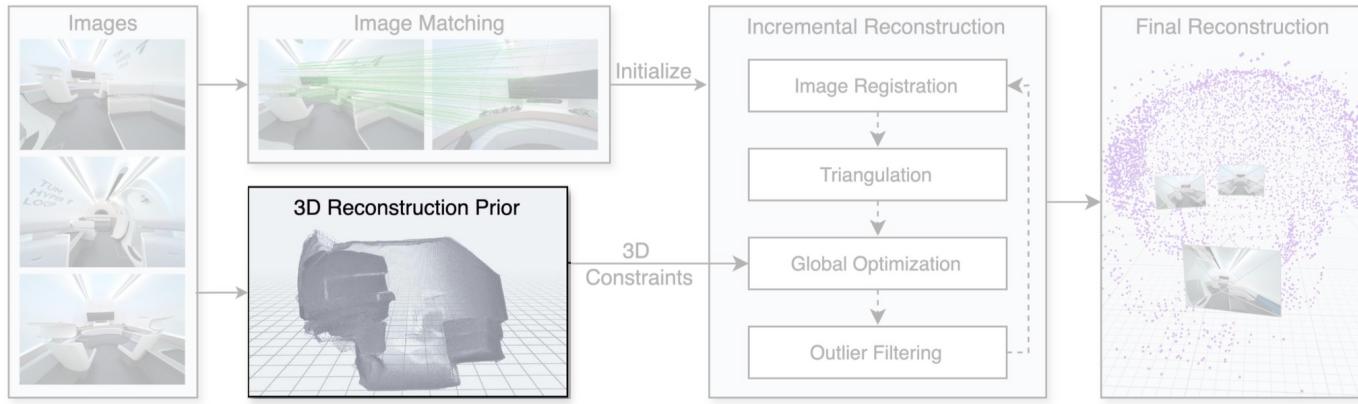
- implemented with opencv & torch

# Implementation Details - Image Matching

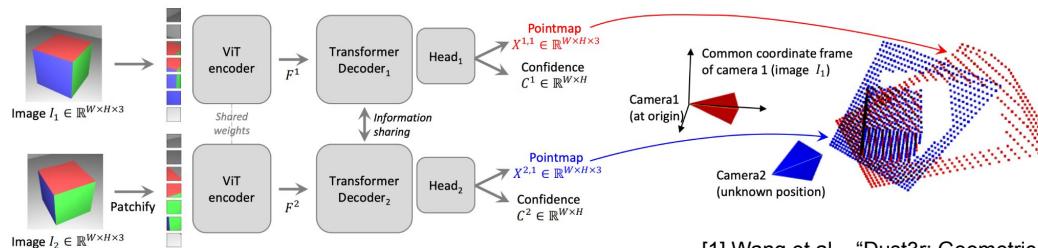


- Feature Extraction + Matching: MASt3R (limit to 256 matches)
- Geometric Verification: Essential Matrix + RANSAC

# Implementation Details - 3D Reconstruction Prior

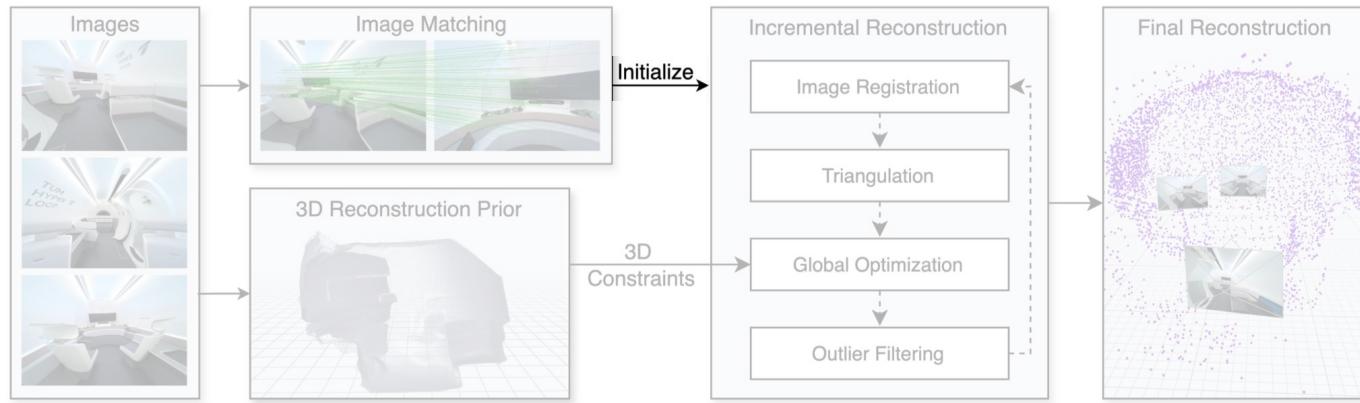


- DUStr3R 512x512 input res + DPT [1]



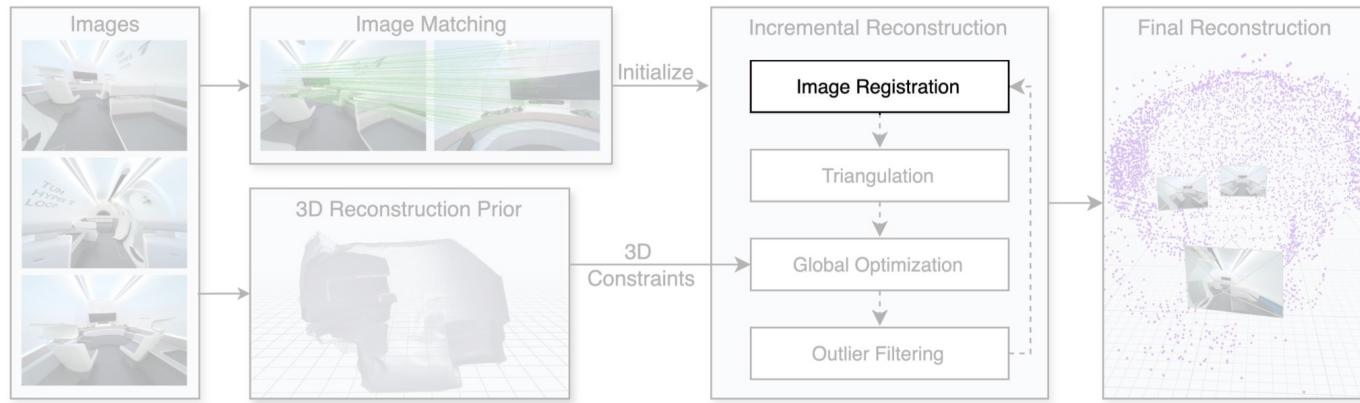
[1] Wang et al., "Dust3r: Geometric 3d vision made easy", CVPR 2024

# Implementation Details - Initialization



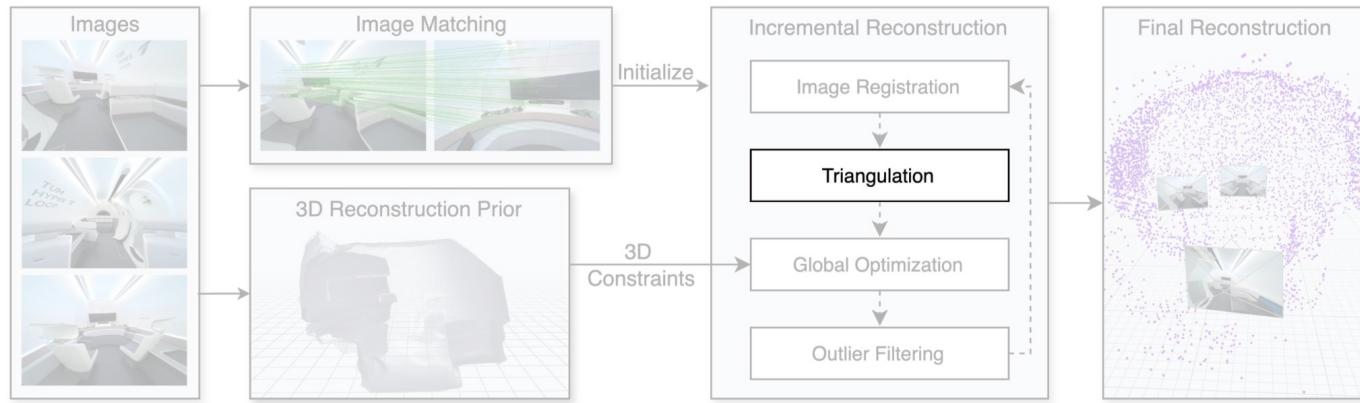
- Select initial pair based on #Matches and median triangulation angle

# Implementation Details - Image Registration



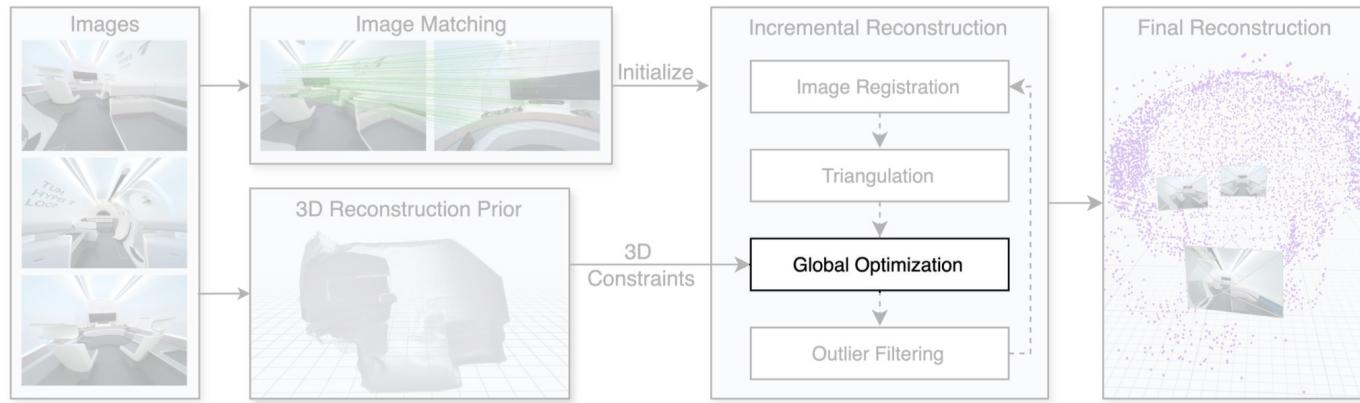
- Next Best View: #Visible Points
- Registration: PnP + RANSAC

# Implementation Details - Triangulation



- Multi-View Triangulation (using DLT Method)
- Reject points with high reprojection error or low triangulation angle

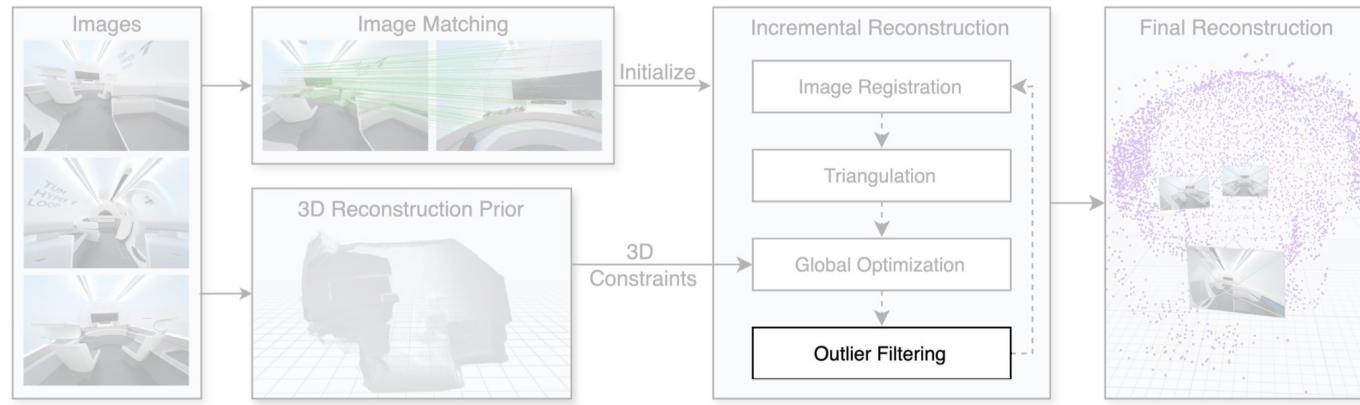
# Implementation Details - Global Optimization



1. Pairwise RANSAC Alignment to Global Scene (use as initial parameters)
2. Remove outliers from energy
3. Minimize (GD + Linesearch)

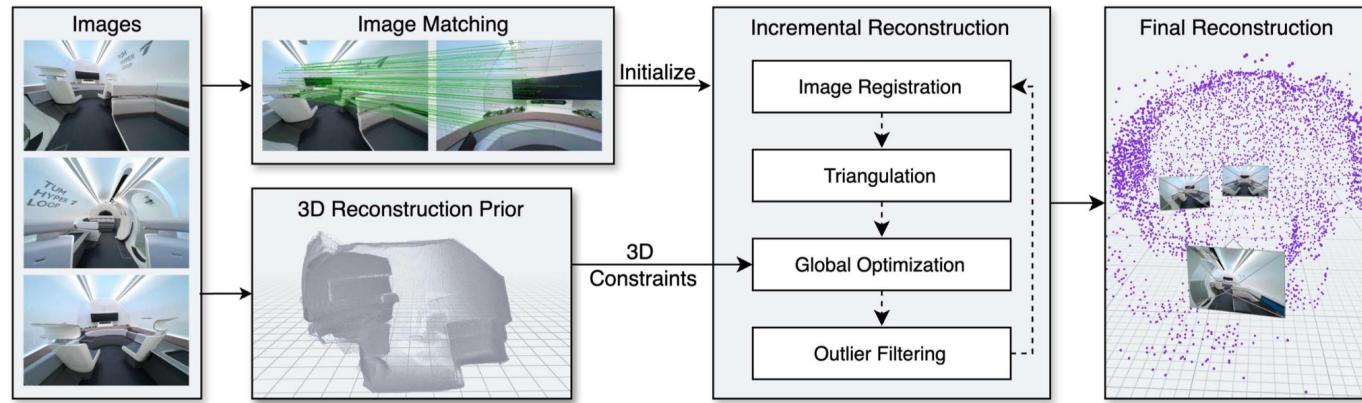
$$\mathcal{X}^*, \mathcal{H}^* = \arg \min_{\mathcal{X}, \mathcal{H}, \mathcal{T}} (E_{BA} + \beta E_{P2P})$$

# Implementation Details - Outlier Filtering

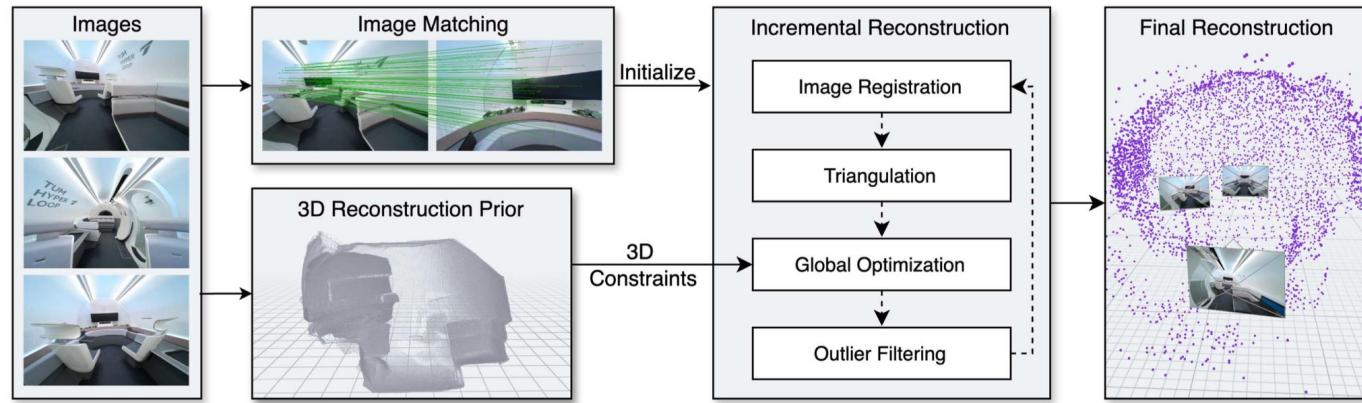


- High Reprojection Error
- Low Triangulation Angle

# Implementation Details



# Implementation Details - TEMPLATE SLIDE



- TEMPLATE SLIDE

# Experiments

# Experimental Setup - Metrics

## Methods:

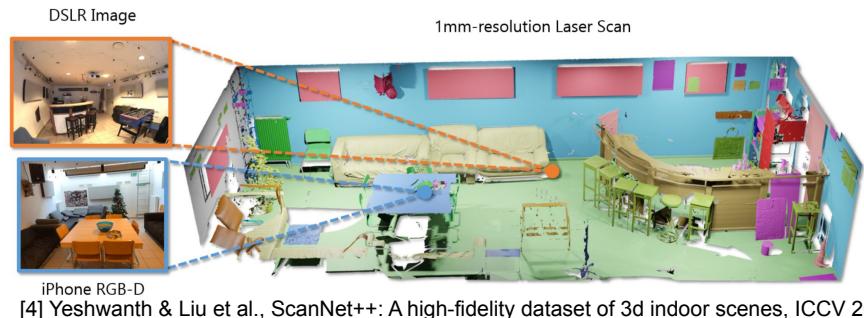
- Baseline
- Baseline+Ours
- 
- DUSt3R + GO [1]
- VGGT [2]
- MAST3R-SfM [3]

## Metrics:

- Average Translation Error (ATE)
- AUC@30
- Registration Rate

## Data:

- ScanNet++ [4] **v2** scenes
- pseudo-GT through COLMAP

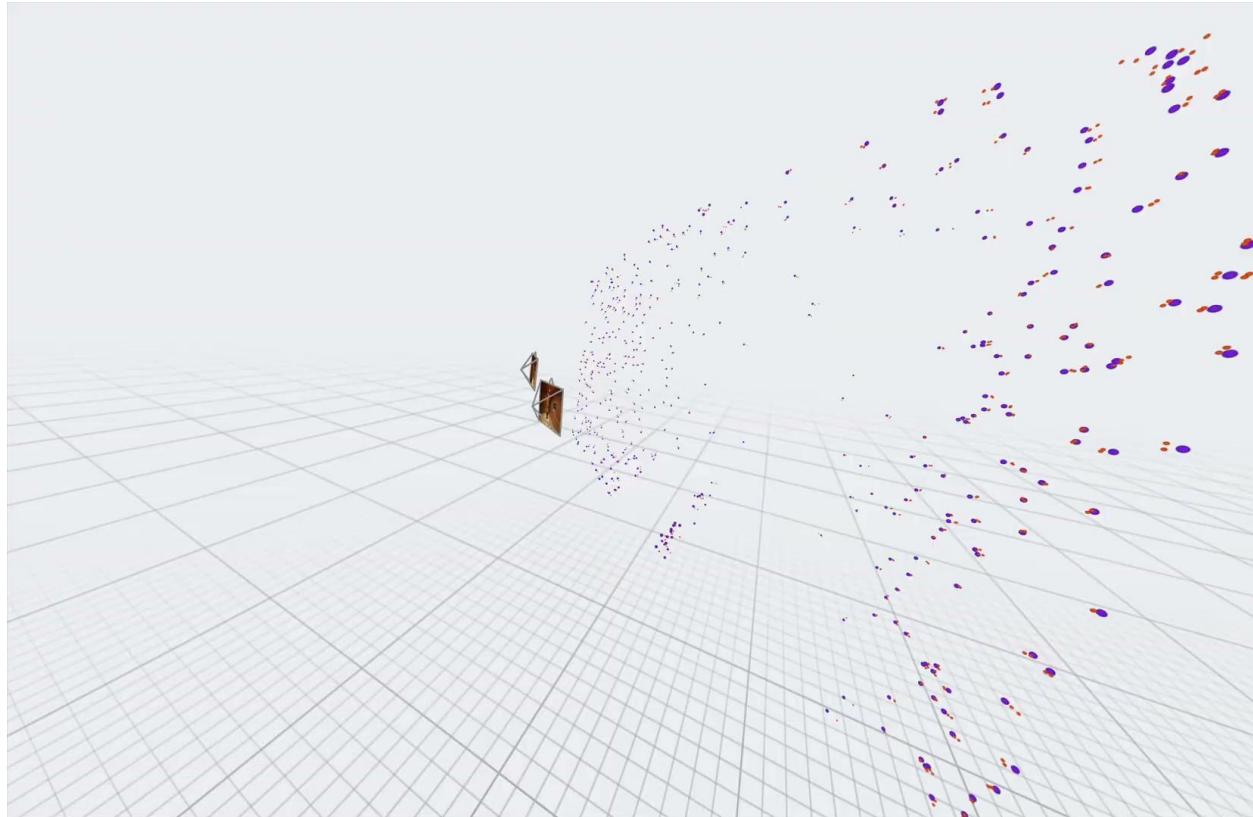


[1] Wang et al., "Dust3r: Geometric 3d vision made easy", CVPR 2024

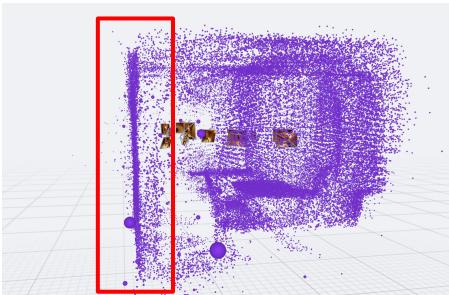
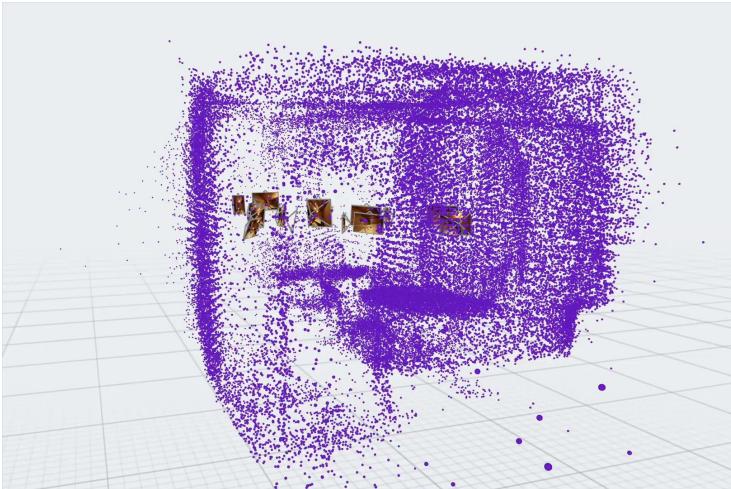
[2] Wang et al., "VGGT: Visual geometry grounded transformer", CVPR 2025

[3] Duisterhof et al., "MASt3R-SfM: a fully-integrated solution for unconstrained structure-from-motion", 3DV 2025

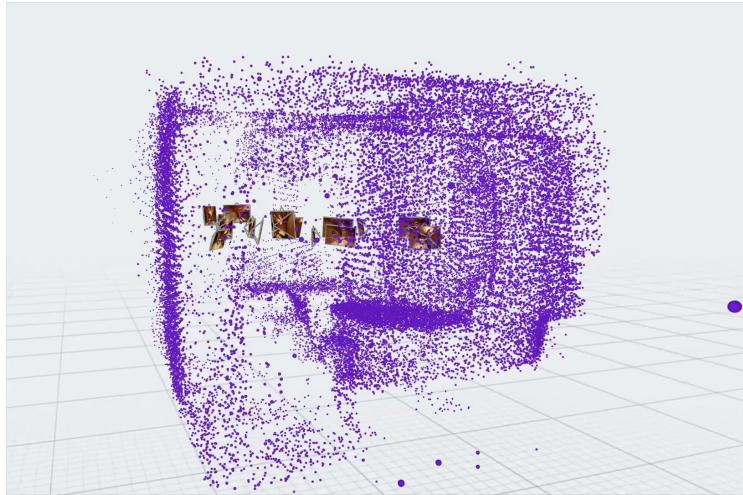
# Visualization of Reconstruction Process



# Visual Comparison



Baseline



Ours



\*baseline has more scene points in general

# Main Results

Method	15 Images			20 Images			25 Images		
	ATE ↓	AUC@30 ↑	Reg. ↑	ATE ↓	AUC@30 ↑	Reg. ↑	ATE ↓	AUC@30 ↑	Reg. ↑
Baseline	<b>0.0181</b>	82.4	97.1	0.0117	86.6	98.0	0.0107	86.7	99.3
Baseline+Ours	0.0190	<b>83.5</b>	96.9	<b>0.0090</b>	<b>88.3</b>	98.7	<b>0.0074</b>	<b>90.8</b>	98.6

**Table 1.** Camera pose estimation on ScanNet++ [31] with varying view counts (15, 20, 25). ATE (↓), AUC@30 (↑), and registration rate (↑). Metrics averaged over 30 scenes. \*Feed-forward pose regression without further optimization.

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DUSt3R+GO	0.0234	80.8	<b>100</b>	0.0147	84.7	<b>100</b>	0.0134	85.2	<b>100</b>
VGGT*	0.0240	69.9	<b>100</b>	0.0192	71.4	<b>100</b>	0.0179	71.5	<b>100</b>
MASt3R-SfM	0.0211	76.3	<b>100</b>	0.0133	78.8	<b>100</b>	0.0118	78.8	<b>100</b>

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# Ablations

# Energy Design Choices

<b>Method</b>	<b>ATE ↓</b>	<b>AUC@30 ↑</b>	<b>Reg. ↑</b>	<b>#Pts ↑</b>
Baseline	0.0159	80.6	95.3	1204
+P2P	0.0736	54.0	74.0	795

**Table 2.** Ablation study on design choices for our energy formulation. Metrics are averaged over 15 images from 10 different scenes in ScanNet++ [31].

# Energy Design Choices

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<i>+Inliers only</i>	0.0166	82.6	94.0	1224

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+ <i>Inliers only</i>	0.0166	82.6	94.0	1224
+ <i>Conf. Weight</i>	<b>0.0138</b>	<b>84.9</b>	<b>98.0</b>	<b>1260</b>

**Table 2.** Ablation study on design choices for our energy formulation. Metrics are averaged over 15 images from 10 different scenes in ScanNet++ [31].

# Image Matching (2D Constraints)

Matches	Method	ATE ↓	AUC@30 ↑	Reg. ↑
SIFT+NN	Baseline	0.0243	73.3	<b>64.0</b>
	+Ours	<b>0.0228</b>	<b>73.8</b>	<b>64.0</b>
MASt3R	Baseline	0.0159	80.6	95.3
	+Ours	<b>0.0138</b>	<b>84.9</b>	<b>98.0</b>



**Table 3.** Ablation study on different image matching methods (2D constraints). NN stands for nearest neighbor, MASt3R matches are computed using fast reciprocal matching [14]. Metrics are averaged over 10 ScanNet++ [31] scenes, each with 15 images.

# 3D Reconstruction Prior (3D Constraints)

<b>3D Reconstruction Prior</b>	<b>ATE ↓</b>	<b>AUC@30 ↑</b>	<b>Reg. ↑</b>
Baseline (No Prior)	0.0159	80.6	95.3
DUSt3R	0.0138	<b>84.9</b>	<b>98.0</b>
VGGT	0.0137	82.61	96.7
VGGT-MV	<b>0.0110</b>	84.06	97.3

**Table 4.** Ablation study on different 3D reconstruction priors. VGGT-MV extracts multi-view pointmaps instead of pairwise ones. Metrics are averaged over 10 ScanNet++ [31] scenes, each with 15 images.

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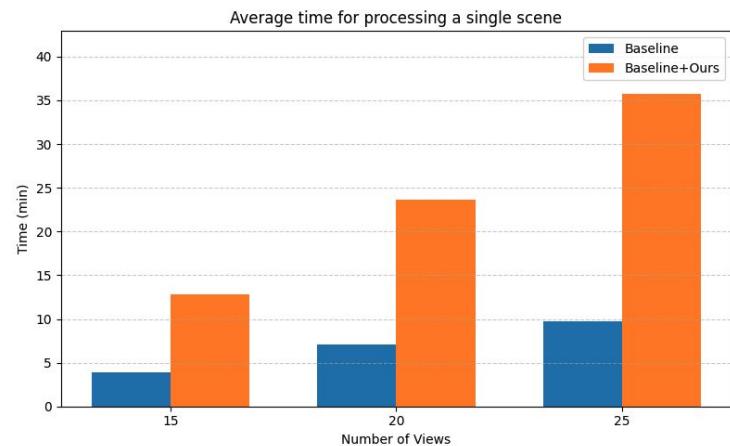
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# Limitations & Future Work

# Scalability

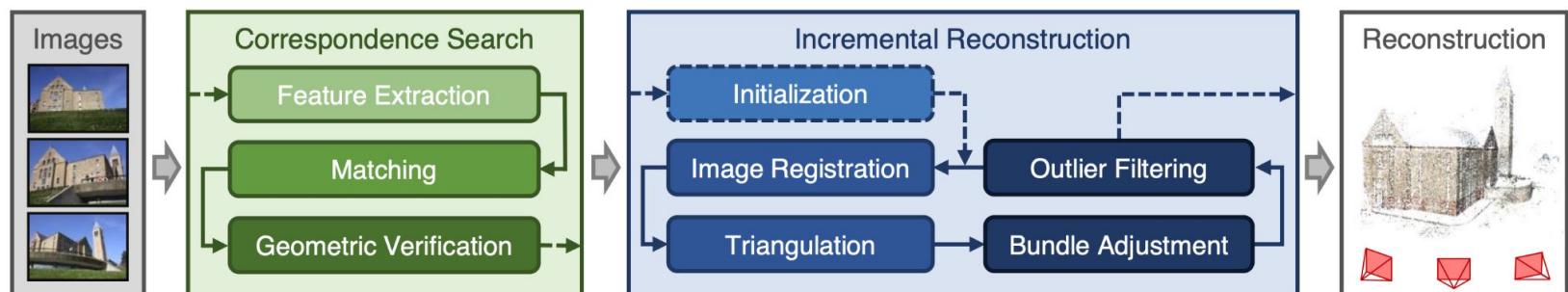
$N$  Images  $\rightarrow$  up to  $[N \text{ choose } 2] \binom{N}{2}$  pairwise pointmaps

- > Multi-View Methods
- > Merging pairwise pointmaps during scene alignment



# Integrate into other parts of the pipeline

3D constraints **only** valid in Global Optimization, rest of pipeline relies **solely** on 2D keypoint matches



[1] Schönberger and Frahm, "Structure-from-motion revisited", CVPR 2016

# Conclusion

# Revisiting Structure from Motion with 3D Reconstruction Priors

Guided Research WS24/25  
Daniel Korth  
Advisor: Prof. Matthias Nießner

30.05.2025