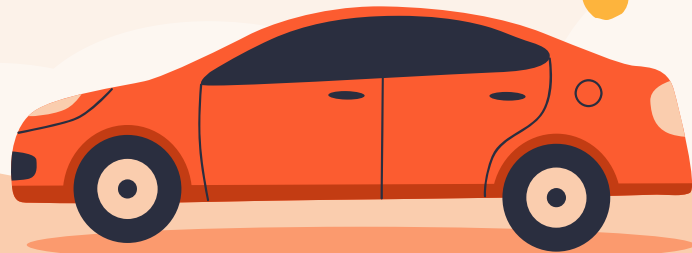


**JUDY's Carbon Crusaders:**

# **CO<sub>2</sub> Emission by Vehicles**

Jonathan Serrano, Umar Ali-Salaam, Daniel Li, Yaseen Mohammed



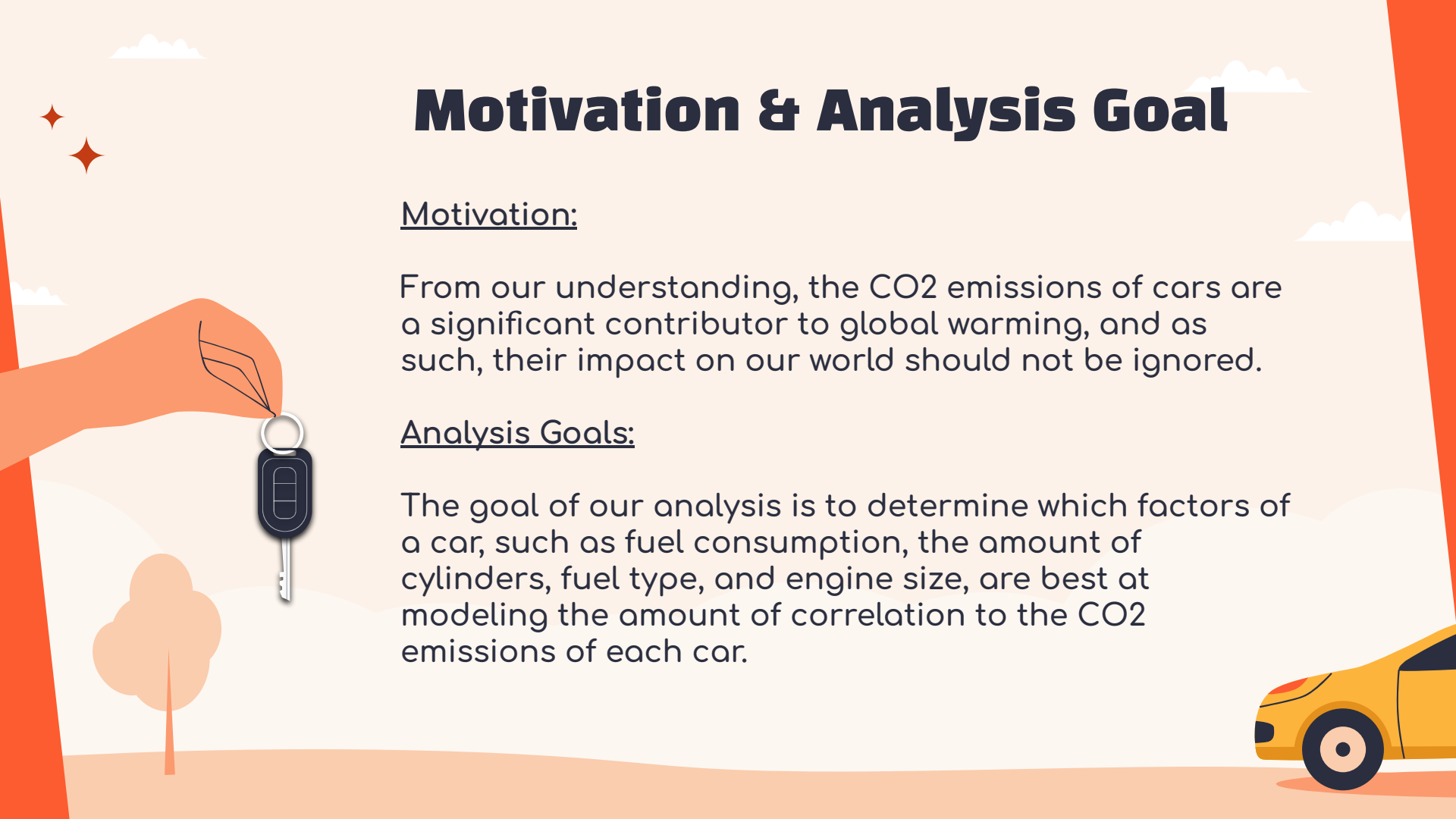
# Motivation & Analysis Goal

## Motivation:

From our understanding, the CO<sub>2</sub> emissions of cars are a significant contributor to global warming, and as such, their impact on our world should not be ignored.

## Analysis Goals:

The goal of our analysis is to determine which factors of a car, such as fuel consumption, the amount of cylinders, fuel type, and engine size, are best at modeling the amount of correlation to the CO<sub>2</sub> emissions of each car.



# Describing Our Dataset

- We found our dataset on Kaggle, however the origin of the data is from the Canadian Government official open data website.
- Since the data originates from a government institution, we believe that the data is reliable.
- The data contains 7385 observations of vehicles from a period of 7 years, 6282 of them being unique.
- There are 12 columns that describe certain features of the car, statistics of the fuel, and CO2 emissions.



# Data Variables

## Regressor Variables

0582

**Vehicle Class**

(Discrete)



**Engine Size**

(Ranges from 0.9 to 8.4)



**Transmission Type**

(Discrete)



**Fuel Type**

(Discrete)



**Fuel Consumption Hwy**

(Ranges : 4-20.6)  
(L/100 km)



**Fuel Consumption Comb**

(Ranges : 4.1 - 26.1)(L/100 km)



**Car Model**

(Discrete)



**Car Make**

(Discrete)



**Cylinders**

(Discrete)



**Fuel Consumption City**

(Ranges : 4.2 -  
30.6)(L/100 km)

## Predictor Variable



**CO2 Emissions (g/km)**

(Ranges from 96 to 522)



# Data Cleaning

- There was no NA values
- Removed unnecessary column (Fuel Consumption Comb (mpg))
- Added Dummy variable columns for discrete variables



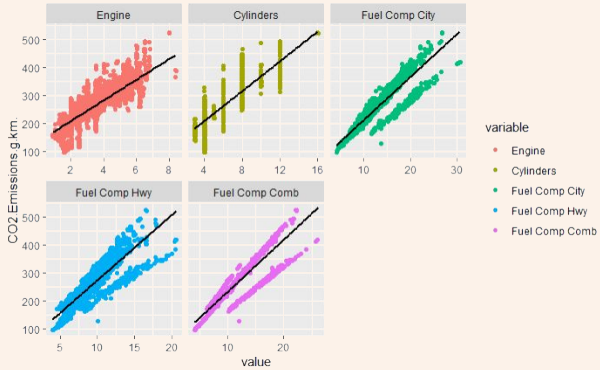


01

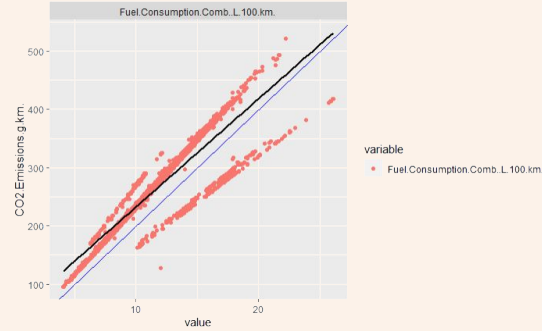
# Data Exploration

# Simplifying Data

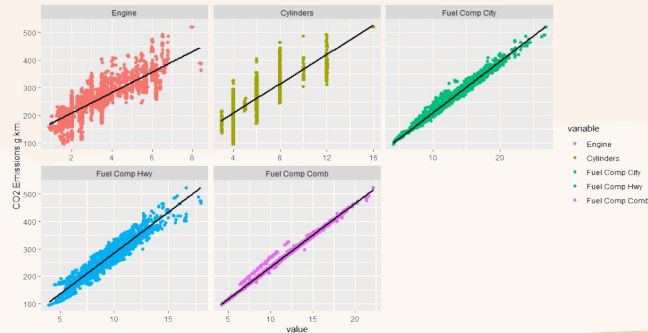
## 1. Original Correlation Plots



## 2. Separated Distributions

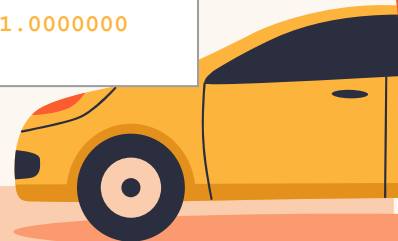


## 3. End Result



# Correlation Matrix

	Engine	Cylinders	Fuel Comp City	Fuel Comp Hwy	Fuel Comp Comb	CO2 Emissions
Engine	1.0000000	0.9259199	0.8616495	0.7956075	0.8518779	0.8514051
Cylinders	0.9259199	1.0000000	0.8468025	0.7641587	0.8310884	0.8321540
Fuel Comp City	0.8616495	0.8468025	1.0000000	0.9353228	0.9926066	0.9882668
Fuel Comp Hwy	0.7956075	0.7641587	0.9353228	1.0000000	0.9709317	0.9662925
Fuel Comp Comb	0.8518779	0.8310884	0.9926066	0.9709317	1.0000000	0.9953828
CO2 Emissions	0.8514051	0.8321540	0.9882668	0.9662925	0.9953828	1.0000000



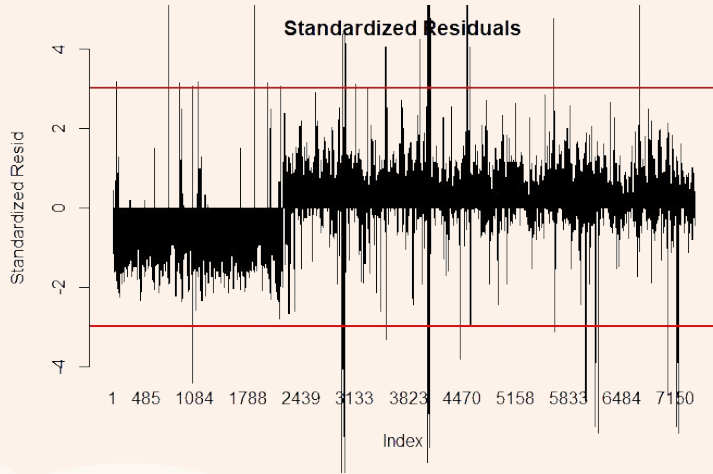


The background is a light beige color with a subtle orange border on the left and right sides. It features several white, fluffy clouds scattered across the top. Small, four-pointed orange stars are placed at various intervals. At the bottom, there are two stylized orange trees with rounded canopies and thin trunks, standing on a light orange ground line. In the center, there is a white square with an orange border, containing the number '02' in a bold, orange, sans-serif font.

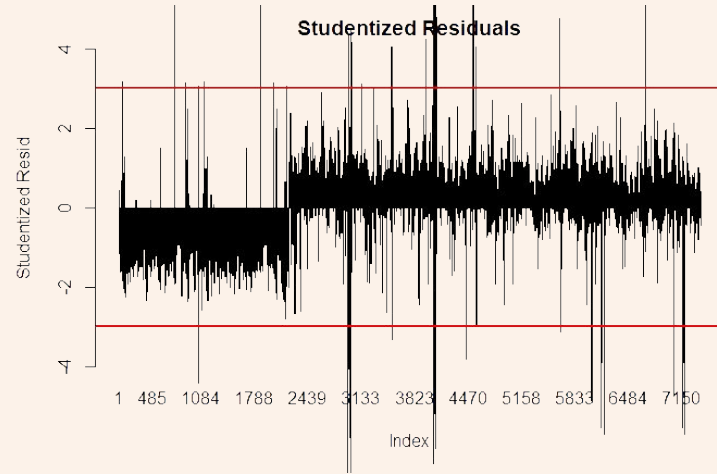
02

# **Residual Analysis**

# Residuals

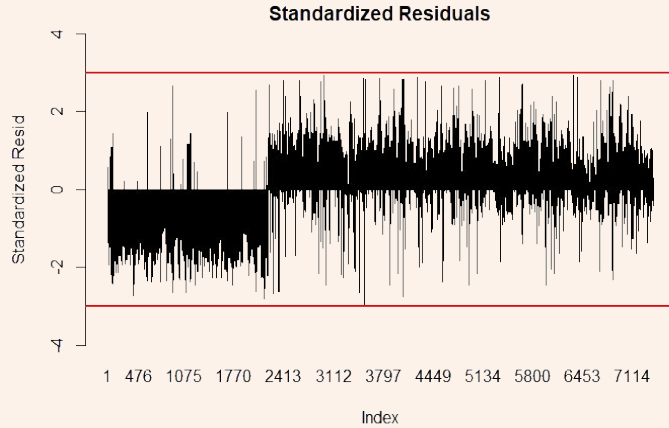


**Standardized  
Residual**

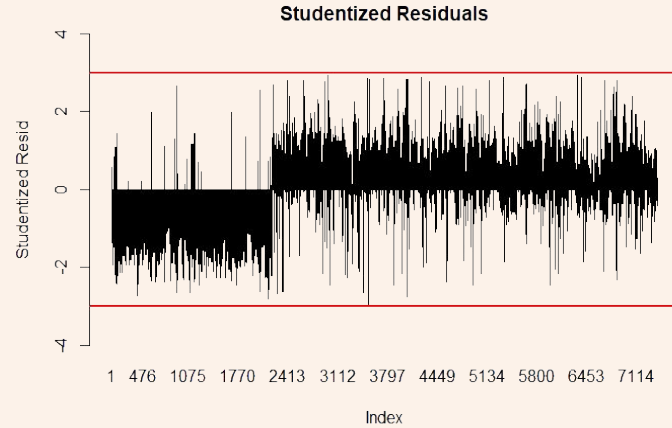


**Studentized  
Residual**

# Residuals

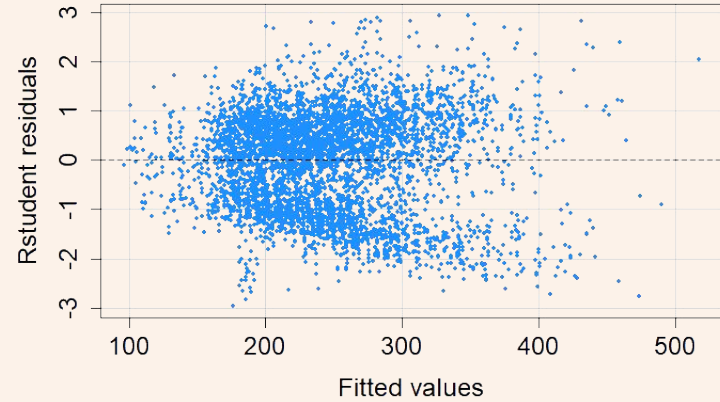
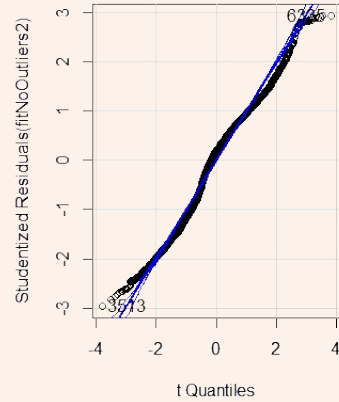
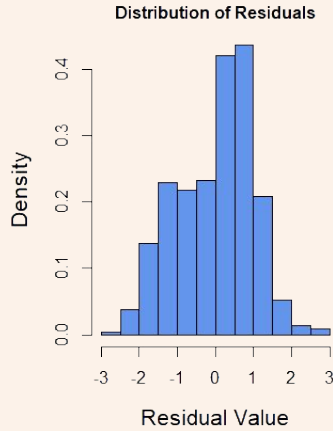


**Standardized  
Residual**



**Studentized  
Residual**

# Residuals



**Distribution of  
Residuals**

**Residual  
Plot**



03

# VIF Analysis

# VIF Test

	GVIF
Engine.Size.L.	10.516585
Cylinders	9.638679
Fuel.Consumption.City..L.100.km.	1703.791684
Fuel.Consumption.Hwy..L.100.km.	438.338248
Fuel.Consumption.Comb..L.100.km.	3682.298415
Fuel.Type	2.620058
Transmission	13.712245
Vehicle.Class	17.165901

**Fuel Consumption Per Road Type**



# VIF Test



	GVIF		GVIF
Engine.Size.L.	4.312856	Engine.Size.L.	4.300666
Fuel.Consumption.Comb..L.100.km.	5.188675	Fuel.Consumption.Comb..L.100.km.	4.541783
Fuel.Type	1.717297	Fuel.Type	1.887630
vehicle.class	2.705236	Transmission	2.725601

**Vehicle Class**

**Vs.**

**Transmission**

# VIF Test



	GVIF		GVIF
Cylinders	4.753246	Engine.Size.L.	5.116296
Fuel.Consumption.Comb..L.100.km.	6.156082	Fuel.Consumption.Comb..L.100.km.	6.289634
Fuel.Type	2.551260	Fuel.Type	2.529080
Vehicle.Class	10.768431	Vehicle.Class	10.026738
Transmission	9.694901	Transmission	10.102218

**Engine Size**

**Vs**

**Cylinders**





04

# **Multilinear Regression Models**

# Akaike Information Criterion (AIC)

```
Call:  
lm(formula = CO2.Emissions.g.km. ~ Fuel.Consumption.Comb..L.100.km. +  
  Fuel.Type + Transmission + Vehicle.Class + Fuel.Consumption.Hwy..L.100.km. +  
  Fuel.Consumption.City..L.100.km. + Cylinders + Engine.Size.L.,  
  data = noOutliersDF2)
```

**Backward Elimination**

**Forward Selection**

**Stepwise Selection**

```
Call:  
lm(formula = CO2.Emissions.g.km. ~ Fuel.Consumption.Comb..L.100.km. +  
  Fuel.Type + Transmission + Vehicle.Class + Fuel.Consumption.Hwy..L.100.km. +  
  Fuel.Consumption.City..L.100.km. + Cylinders + Engine.Size.L.,  
  data = noOutliersDF2)
```





05

# Anova Analysis

# Anova

## Fit 1: with Engine Size

Analysis of Variance Table

Response: CO2.Emissions.g.km.

	Df	Sum Sq	Mean Sq	F value	Pr(>F)	
Engine.Size.L.	1	17088330	17088330	4.8900e+05	< 2.2e-16	***
Fuel.Consumption.City..L.100.km.	1	5929123	5929123	1.6967e+05	< 2.2e-16	***
D	1	111939	111939	3.2033e+03	< 2.2e-16	***
X	1	12776	12776	3.6560e+02	< 2.2e-16	***
COMPACT	1	10954	10954	3.1347e+02	< 2.2e-16	***
SUV...SMALL	1	6986	6986	1.9991e+02	< 2.2e-16	***
MID.SIZE	1	23969	23969	6.8589e+02	< 2.2e-16	***
TWO.SEATER	1	2608	2608	7.4644e+01	< 2.2e-16	***
MINICOMPACT	1	554	554	1.5849e+01	6.930e-05	***
SUBCOMPACT	1	19139	19139	5.4768e+02	< 2.2e-16	***
FULL.SIZE	1	53292	53292	1.5250e+03	< 2.2e-16	***
STATION.WAGON...SMALL	1	15669	15669	4.4839e+02	< 2.2e-16	***
SUV...STANDARD	1	1222	1222	3.4975e+01	3.499e-09	***
VAN...CARGO	1	694	694	1.9862e+01	8.455e-06	***
VAN...PASSENGER	1	956	956	2.7366e+01	1.733e-07	***
PICKUP.TRUCK...STANDARD	1	5370	5370	1.5366e+02	< 2.2e-16	***
MINIVAN	1	2000	2000	5.7238e+01	4.361e-14	***
SPECIAL.PURPOSE.VEHICLE	1	279	279	7.9761e+00	0.004753	**
STATION.WAGON...MID.SIZE	1	4332	4332	1.2396e+02	< 2.2e-16	***
Residuals	6920	241822	35			

## Fit 2: with Cylinder

Analysis of Variance Table

Response: CO2.Emissions.g.km.

	Df	Sum Sq	Mean Sq	F value	Pr(>F)	
Cylinders	1	16296093	16296093	4.6783e+05	< 2.2e-16	***
Fuel.Consumption.City..L.100.km.	1	6722893	6722893	1.9300e+05	< 2.2e-16	***
D	1	114523	114523	3.2877e+03	< 2.2e-16	***
X	1	10721	10721	3.0779e+02	< 2.2e-16	***
COMPACT	1	10508	10508	3.0166e+02	< 2.2e-16	***
SUV...SMALL	1	6282	6282	1.8035e+02	< 2.2e-16	***
MID.SIZE	1	23654	23654	6.7905e+02	< 2.2e-16	***
TWO.SEATER	1	2545	2545	7.3062e+01	< 2.2e-16	***
MINICOMPACT	1	488	488	1.4000e+01	0.0001843	***
SUBCOMPACT	1	19098	19098	5.4826e+02	< 2.2e-16	***
FULL.SIZE	1	53082	53082	1.5239e+03	< 2.2e-16	***
STATION.WAGON...SMALL	1	15809	15809	4.5385e+02	< 2.2e-16	***
SUV...STANDARD	1	1306	1306	3.7483e+01	9.726e-10	***
VAN...CARGO	1	723	723	2.0768e+01	5.274e-06	***
VAN...PASSENGER	1	1200	1200	3.4448e+01	4.580e-09	***
PICKUP.TRUCK...STANDARD	1	4835	4835	1.3879e+02	< 2.2e-16	***
MINIVAN	1	2138	2138	6.1369e+01	5.441e-15	***
SPECIAL.PURPOSE.VEHICLE	1	257	257	7.3907e+00	0.0065725	**
STATION.WAGON...MID.SIZE	1	4813	4813	1.3817e+02	< 2.2e-16	***
Residuals	6920	241048	35			

```
> qf(p=.05, df1=1, df2=6909, lower.tail=FALSE)
[1] 3.842805
> qf(p=.05, df1=1, df2=6920, lower.tail=FALSE)
[1] 3.842803
```



# Anova Reduced

## Anova Without Vehicle Class

**Fit 1 :**

```
> abs(qt(0.05/2, 6920, lower.tail=TRUE))  
[1] 1.960307
```

**Fit 2:**

### Analysis of Variance Table

Model 1: CO2.Emissions.g.km. ~ Engine.Size.L. + Fuel.Consumption.City..L.100.km. + D + X

Model 2: CO2.Emissions.g.km. ~ Engine.Size.L. + Fuel.Consumption.City..L.100.km. + D + X + COMPACT + SUV...SMALL + MID.SIZE + TWO.SEATER + MINICOMPACT + SUBCOMPACT + FULL.SIZE + STATION.WAGON...SMALL + SUV...STANDARD + VAN...CARGO + VAN...PASSENGER + PICKUP.TRUCK...STANDARD + MINIVAN + SPECIAL.PURPOSE.VEHICLE + STATION.WAGON...MID.SIZE

	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	6935	389846				
2	6920	241822	15	148024	282.39	< 2.2e-16 ***

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

### Analysis of Variance Table

Model 1: CO2.Emissions.g.km. ~ cylinders + Fuel.Consumption.City..L.100.km. + D + X

Model 2: CO2.Emissions.g.km. ~ cylinders + Fuel.Consumption.City..L.100.km. + D + X + COMPACT + SUV...SMALL + MID.SIZE + TWO.SEATER + MINICOMPACT + SUBCOMPACT + FULL.SIZE + STATION.WAGON...SMALL + SUV...STANDARD + VAN...CARGO + VAN...PASSENGER + PICKUP.TRUCK...STANDARD + MINIVAN + SPECIAL.PURPOSE.VEHICLE + STATION.WAGON...MID.SIZE

	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	6935	387785				
2	6920	241048	15	146737	280.84	< 2.2e-16 ***

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1



06

# Conclusion

# Final Linear Model

```
Call:
lm(formula = CO2.Emissions.g.km. ~ Cylinders + Fuel.Consumption.City..L.100.km. +
  D + X + COMPACT + SUV...SMALL + MID.SIZE + TWO.SEATER + MINICOMPACT +
  SUBCOMPACT + FULL.SIZE + STATION.WAGON...SMALL + SUV...STANDARD +
  VAN...CARGO + VAN...PASSENGER + PICKUP.TRUCK...STANDARD +
  MINIVAN + SPECIAL.PURPOSE.VEHICLE + STATION.WAGON...MID.SIZE,
  data = noOutliersDF2)
```

Residuals:

Min	1Q	Median	3Q	Max
-22.583	-3.926	-0.314	3.544	44.158

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	40.75706	0.70798	57.568	< 2e-16	***
Cylinders	0.37907	0.08004	4.736	2.22e-06	***
Fuel.Consumption.City..L.100.km.	17.88895	0.05062	353.417	< 2e-16	***
D	21.09429	0.53653	39.316	< 2e-16	***
X	-1.96512	0.18059	-10.881	< 2e-16	***
COMPACT	-15.89446	0.54449	-29.192	< 2e-16	***
SUV...SMALL	-7.89868	0.51896	-15.220	< 2e-16	***
MID.SIZE	-16.25583	0.53818	-30.205	< 2e-16	***
TWO.SEATER	-13.38506	0.58945	-22.708	< 2e-16	***
MINICOMPACT	-12.94830	0.62155	-20.832	< 2e-16	***
SUBCOMPACT	-15.35453	0.56699	-27.081	< 2e-16	***
FULL.SIZE	-15.82483	0.56195	-28.160	< 2e-16	***
STATION.WAGON...SMALL	-12.13207	0.62808	-19.316	< 2e-16	***
SUV...STANDARD	-3.52665	0.54636	-6.455	1.16e-10	***
VAN...CARGO	6.83230	1.77621	3.847	0.000121	***
VAN...PASSENGER	4.07212	1.00935	4.034	5.53e-05	***
PICKUP.TRUCK...STANDARD	0.38479	0.56858	0.677	0.498589	
MINIVAN	-9.78644	0.86223	-11.350	< 2e-16	***
SPECIAL.PURPOSE.VEHICLE	-5.23061	0.87420	-5.983	2.30e-09	***
STATION.WAGON...MID.SIZE	-11.27962	0.95958	-11.755	< 2e-16	***

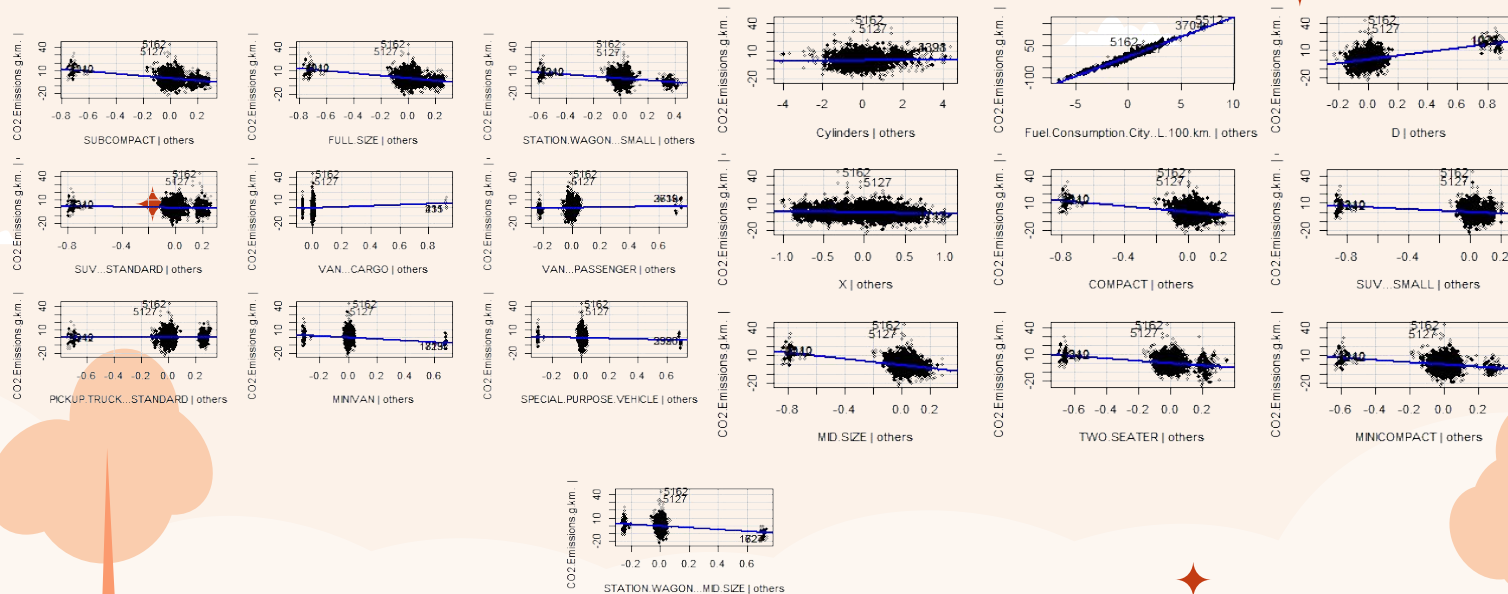
---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.902 on 6920 degrees of freedom

Multiple R-squared: 0.9898, Adjusted R-squared: 0.9897

F-statistic: 3.519e+04 on 19 and 6920 DF, p-value: < 2.2e-16

# Multilinear Regression Plots







07

# Future Direction

# Future Direction

- Look at the secondary Distribution
- Consider looking at bigger datasets/other datasets with other car brands and more counts of other discrete variables
- Consider impact of Influential points





**Thank You**