

CS1010

Programming Methodology

<http://www.comp.nus.edu.sg/~cs1010/>

UNIT 3

Algorithmic Problem Solving



Leading The World With Asia's Best

Unit 2: Algorithmic Problem Solving

1. Plinko by Pseudocode
2. Algorithm
3. Control Structures
4. Examples of Pseudocodes
5. Euclid's Algorithm

IS PROGRAMING SCARY?

An example of a “program” by pseudocode

What is programming?

Programmer



What my friends think I do



What my mom thinks I do



What society thinks I do



What my boss thinks I do



What I think I do



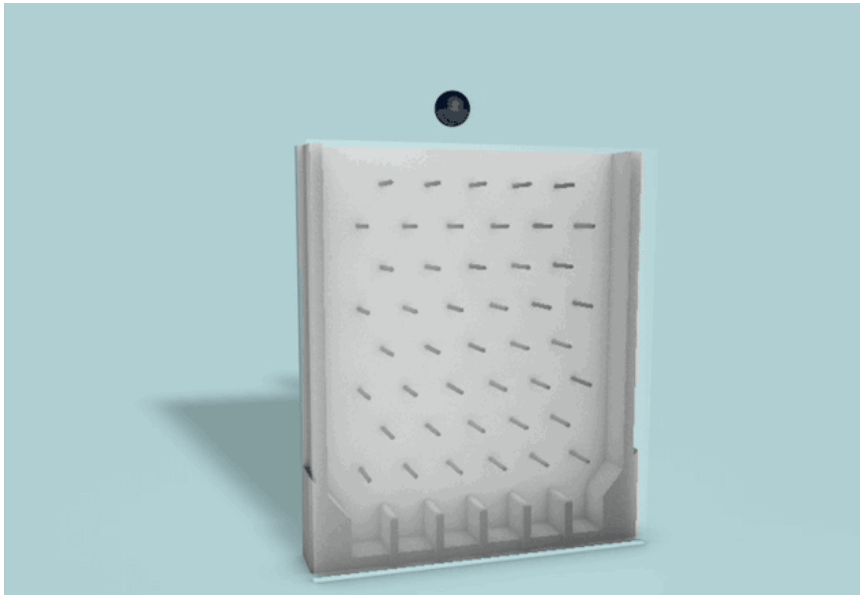
What I actually do

Imagine



Running a Booth

- Dropping a ball from the top and you will get
 - 3: Big prize
 - 2: Medium prize
 - 1: Small prize



Let's see what we have for prizes

- Giant Teddy Bears
 - X 10



- Water guns
 - X 50



- Candy
 - X 200



Your Job is

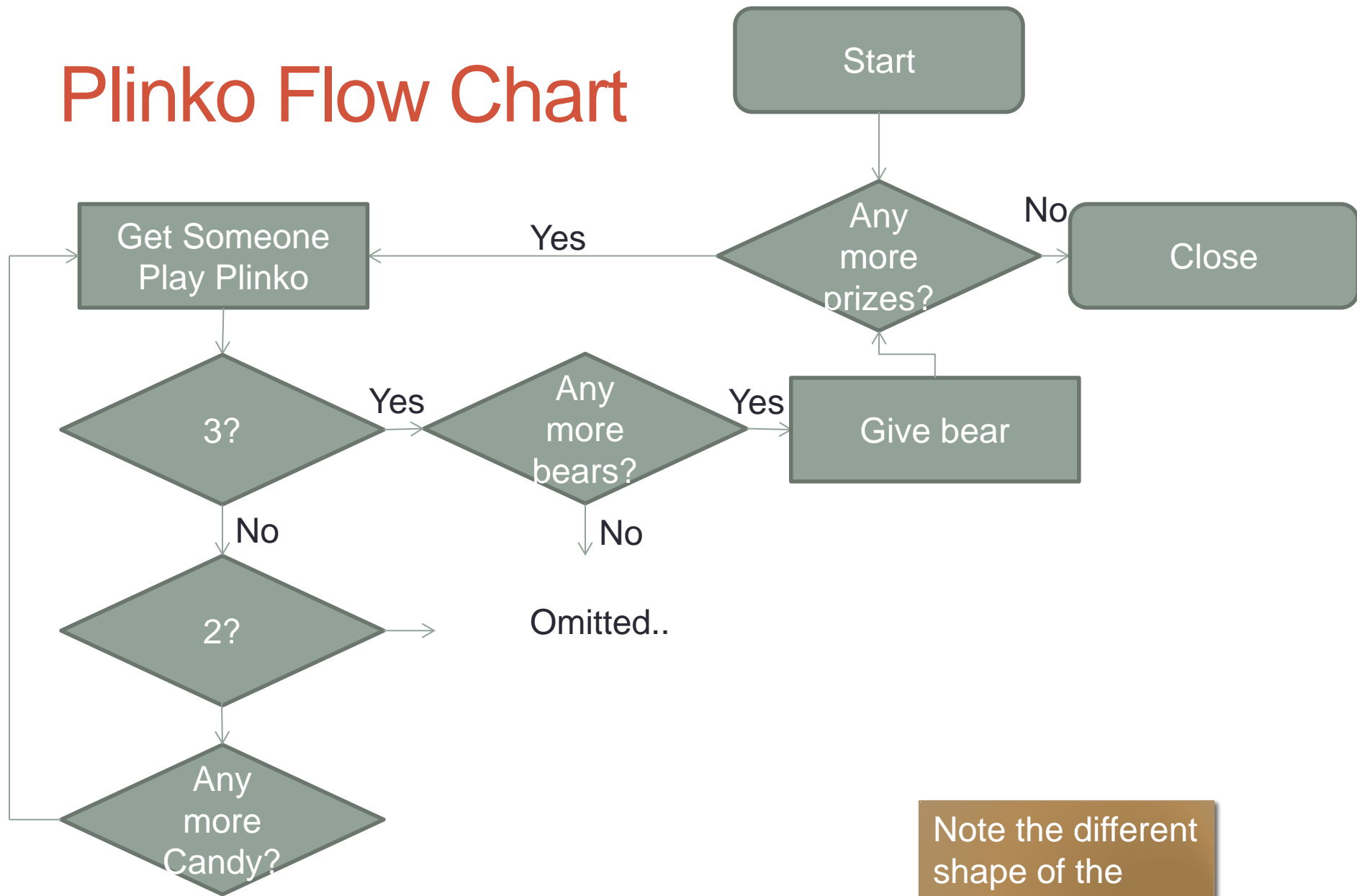
- Run the booth until the end of the day or all prizes given out
 - 3: Giant Teddy Bear
 - 2: Water Gun
 - 1: Candy
- What is the potential problem?
- You may run out of Teddy Bears!
 - Or Water guns or candies
- Any suggestion?



Before Real Coding

- A Program can be expressed by
 - **Pseudocode**
 - An artificial and informal language that helps programmers develop algorithms.
 - "text-based"
 - Or A **Flow Chart**

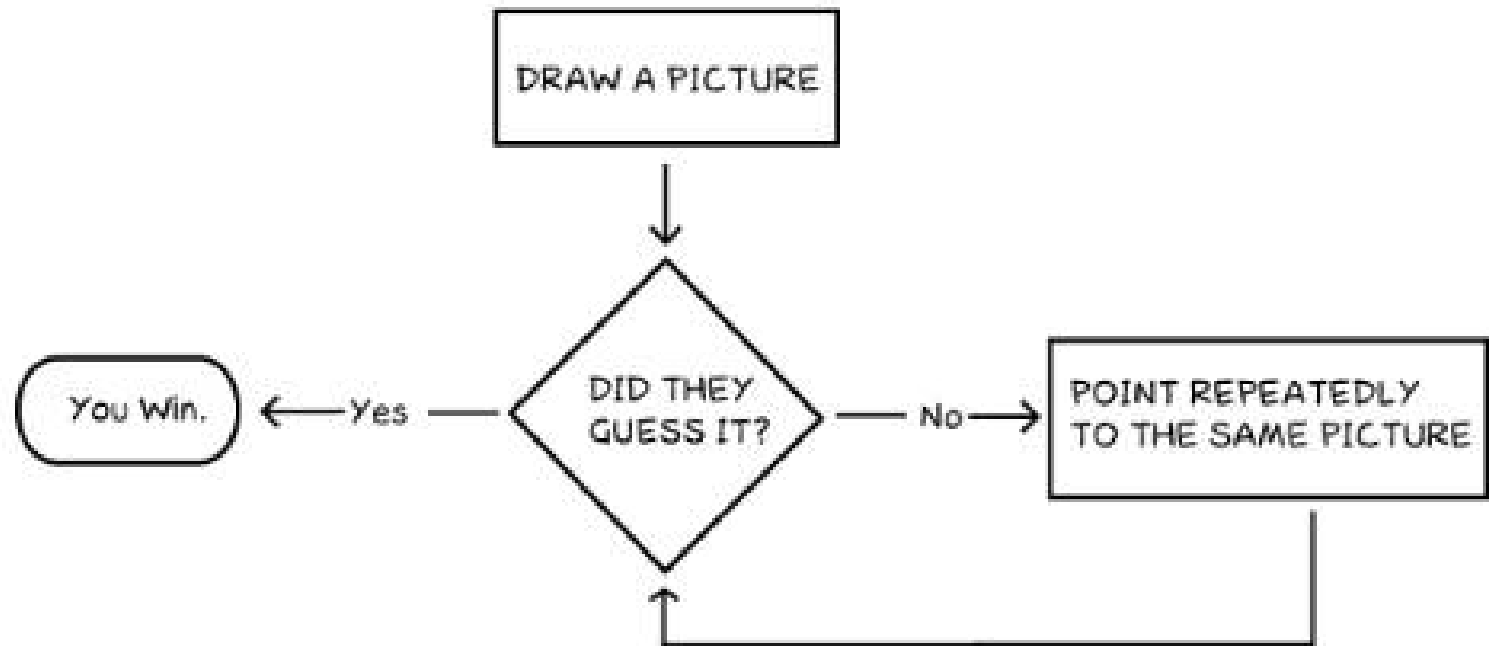
Plinko Flow Chart



Note the different shape of the bubbles

Control Structures on Pictionary

How To Play Pictionary



Choose Your Own Adventure

From Wikipedia, the free encyclopedia

This article is about the trademarked book series. For the genre, see [Gamebook](#). For the TV series, see [Lawrence Leung's Choose Your Own Adventure](#).

Choose Your Own Adventure is a series of children's [gamebooks](#) where each story is written from a [second-person](#) point of view, with the reader assuming the role of the protagonist and making choices that determine the main character's actions and the plot's outcome. The series was based upon a concept created by [Edward Packard](#) and originally published by Constance Cappel's and [R. A. Montgomery](#)'s Vermont Crossroads Press as the "Adventures of You" series, starting with Packard's *Sugarcane Island* in 1976.^[1]

Choose Your Own Adventure, as published by [Bantam Books](#), was one of the most popular children's series during the 1980s and 1990s, selling more than 250 million copies between 1979 and 1998.^[2] When Bantam, now owned by [Random House](#), allowed the *Choose Your Own Adventure* trademark to lapse, the series was relaunched by [Chooseco](#), which now owns the trademark. Chooseco does not reissue titles by Packard, who has started his own imprint, U-Ventures.^[3]

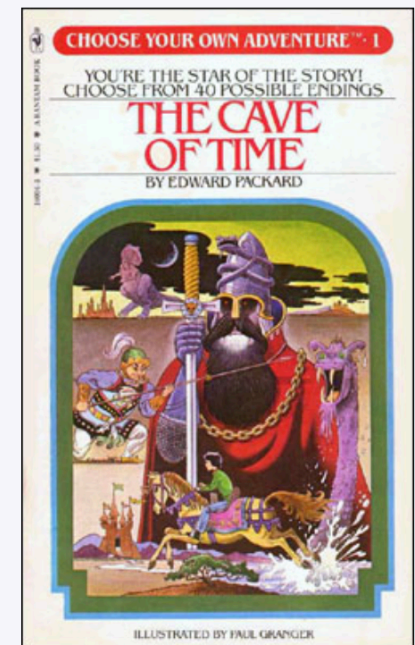
Contents [\[hide\]](#)

- [Format](#)
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- [See also](#)
- [References](#)
- [External links](#)

Format [\[edit\]](#)

Originally created for 7- to 14-year-olds, the books are written in the second person. The protagonist—that is, the reader—takes on a role relevant to the adventure; for example, private investigator, mountain climber, race car driver, doctor, or spy. Stories are generally gender and race neutral, though in some cases, particularly in illustrations, presumption of a male

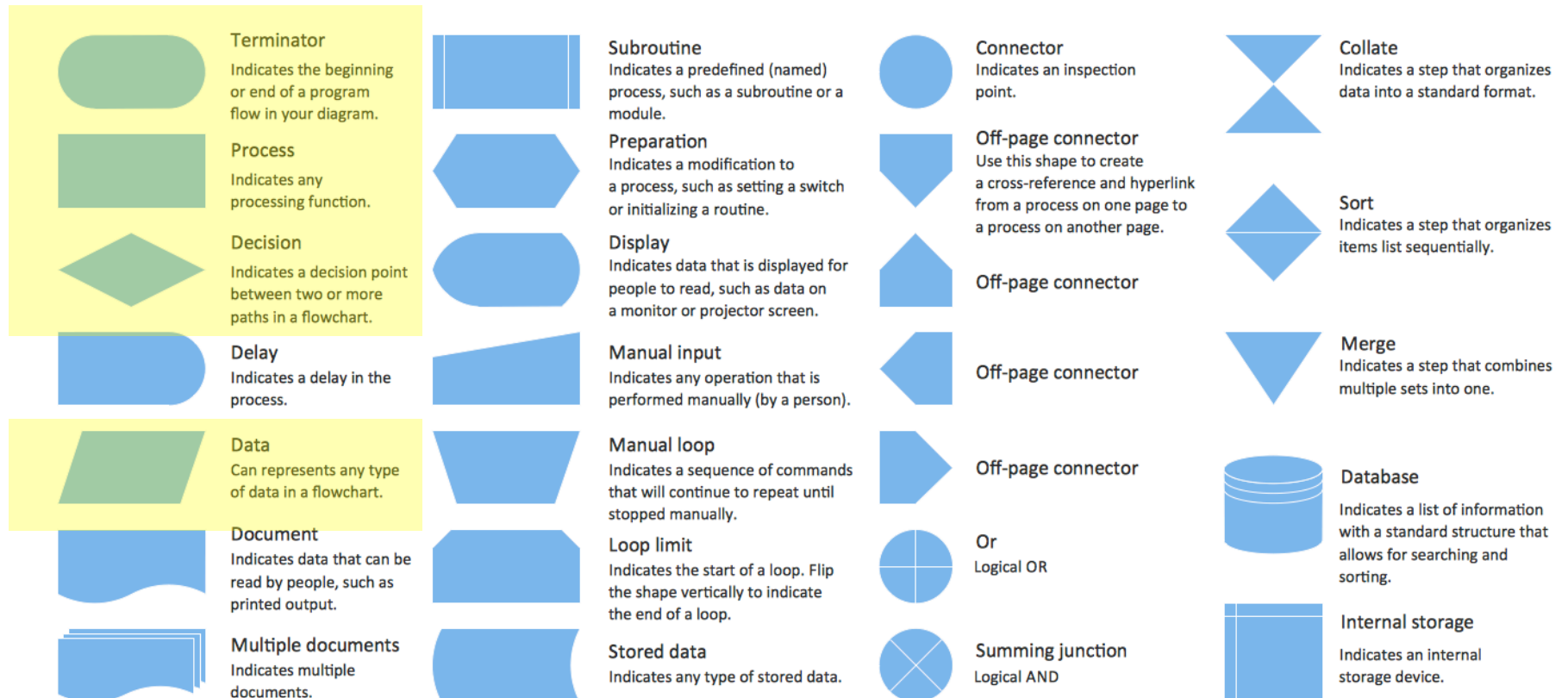
Choose Your Own Adventure



The Cave of Time by [Edward Packard](#), the first book in the series

Cover artist [Paul Granger](#)
Language [English](#)

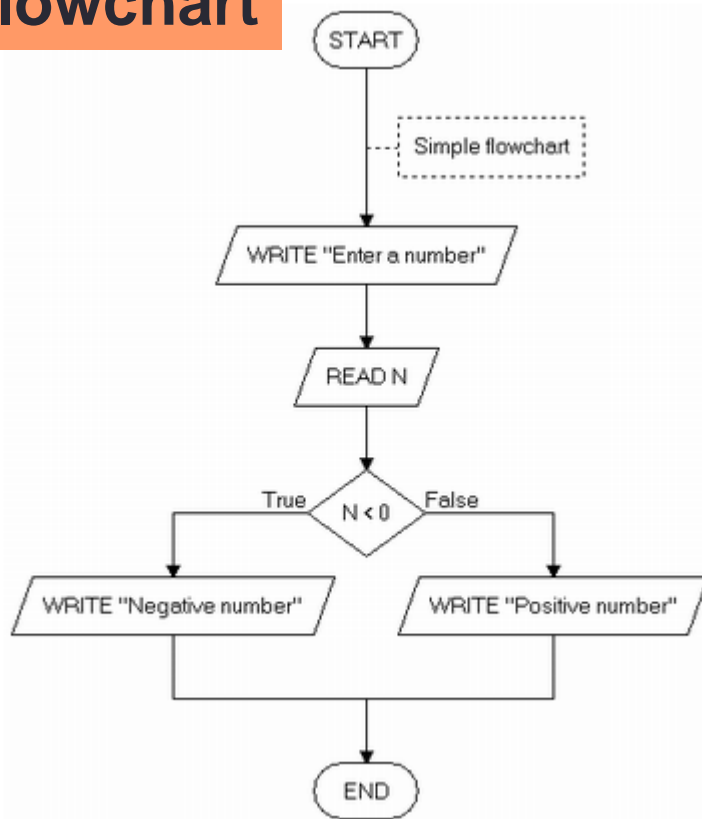
Flow Chart Bubble Types



Algorithm

- Ways of representing an algorithm:

Flowchart



Pseudocode

PSEUDOCODE

set total to zero

get list of numbers

loop through each number in the list
 add each number to total
end loop

if number more than zero
 print "it's positive" message
else
 print "it's zero or less" message
end if

lynda. com

Algorithms

- Named for al-Khwārizmī (780-850)
 - Persian mathematician
- Many ancient algorithms
 - Multiplication: Rhind Papyrus
 - Babylon and Egypt: ~1800BC
 - Euclidean Algorithm: Elements
 - Greece: ~300BC
 - Sieve of Eratosthenes
 - Greece: ~200BC



What is an
Algorithm?



Algorithm (noun.)

Word used by programmers when...
they do not want to explain what they did.

Algorithm (1/3)

- An **algorithm** is a well-defined computational procedure consisting of *a set of instructions*, that takes some value or set of values as *input*, and produces some value or set of values as *output*.



‘Algorithm’ stems from ‘Algoritmi’, the Latin form of al-Khwārizmī, a Persian mathematician, astronomer and geographer.

Source: <http://en.wikipedia.org/wiki/Algorithm>

Control Structures

- An algorithm is a set of instructions, which are followed sequentially by default.
- However, sometimes we need to change the default sequential flow.
- We study 3 control structures.

CONTROL STRUCTURES

Control Structures

Sequence

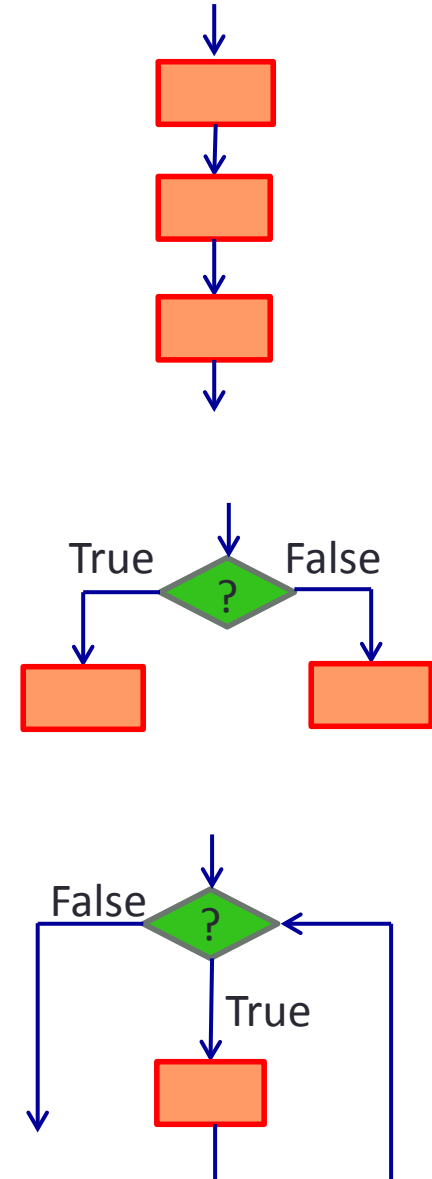
- Default

Selection

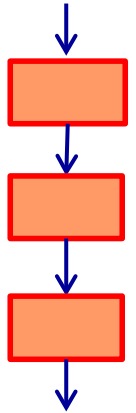
- Also called branching

Repetition

- Also called loop



Control Structure: Sequence



Method 1 Making Vanilla Pound Cake

1. Gather your ingredients. Pound cake is one of the simplest cakes to bake. ...
2. Preheat the oven to 325 degrees.
3. Grease a cake pan. ...
4. Cream the butter and sugar. ...
5. Add the eggs and vanilla. ...
6. Stir in the cake flour. ...
7. Pour the batter into the pan. ...
8. Bake the cake for an hour and 15 minutes.



4 Ways to Bake a Cake - wikiHow

www.wikihow.com/Bake-a-Cake

Control Structure: Sequence

A Block

```
#include <stdio.h>
```

```
int main(void) {
```

```
    int a,b,c;
```

```
    a = 2001;
```

```
    b = 4002;
```

```
    c = a + b;
```

```
    printf(" The value of %d + %d = %d\n",a,b,c);
```

```
    return 0;
```

```
}
```

Sequentially run
this line by line

Tips: How to read a C
program?

You look for the
“main()” and start
reading it’s “block”

Don’t worry about the C syntax; we will
discuss it next week. For now, just to show
you how the algorithm is translated into the
code. **The logic remains the same**, but you
need to write the code according to the
rules of the programming language.

Control Structures: Sequence

- Task: Compute the average of three integers
- How the program might look like

Unit3_prog1.c

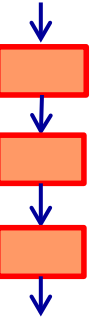
```
// This program computes the average of 3 integers
#include <stdio.h>

int main(void) {
    int num1, num2, num3;
    float ave;

    printf("Enter 3 integers: ");
    scanf("%d %d %d", &num1, &num2, &num3);

    ave = (num1 + num2 + num3) / 3.0;
    printf("Average = %.2f\n", ave);

    return 0;
}
```



Control Structures

Sequence

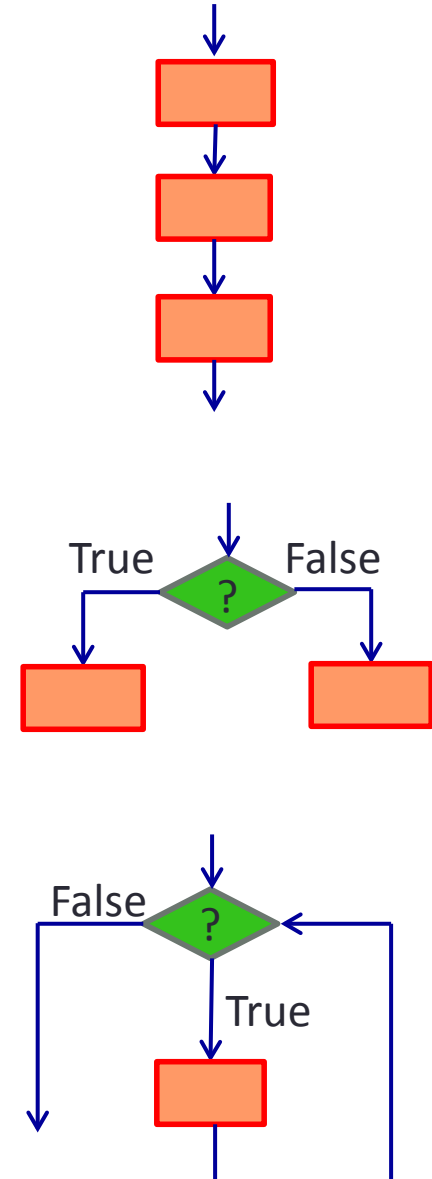
- Default

Selection

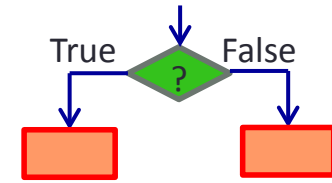
- Also called branching

Repetition

- Also called loop



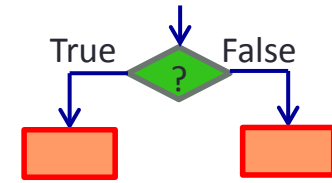
Control Structure: Selection



- **If** the player strikes a “3”
 - Give him a bear
- **Else**
 - Let him choose a water gun or a candy



Control Structure: Selection



If (a condition is true)

Do A

Else

Do B

Can be **MORE THAN** one
single instruction

- For example:

If (I have \$10000000000000000000)

Buy a car

Eat a lot of buffets

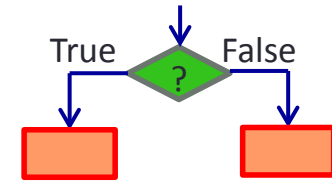
Go travel

Quit NUS!

Else

Be good and study

Control Structure: Selection



If (a condition is true)

Do A

Else

Do B

Can be **MORE THAN** one single instruction

- For example:

If (I have \$10000000000000000000)

If (I am heartless)

 Buy a car

 Eat a lot of buffets

 Go travel

 Quit NUS!

Else

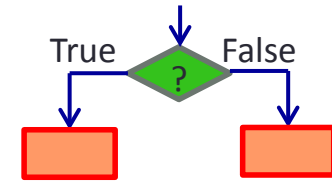
 donate all the money to charity

} Nested "if"

Else

 Be good and study

Control Structure: Selection



If (a condition is true)

Do A

~~Else~~

~~Do B~~

→ Can be **WITHOUT** “else”

- For example:

If (I have \$10000000000000000000)

Buy a car

Eat a lot of buffets

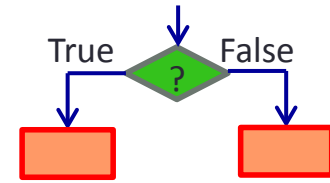
Go travel

Quit NUS!

~~Else~~

~~Be good and study~~

Control Structures: Selection (1/3)



- Task: Arrange two integers in ascending order (sort)

Algorithm A:

enter values for *num1*, *num2*

// Assign smaller number into *final1*,

// and larger number into *final2*

if (*num1* < *num2*)

 then *final1* ← *num1*

final2 ← *num2*

 else *final1* ← *num2*

final2 ← *num1*

// Transfer values in *final1*, *final2* back to *num1*, *num2*

num1 ← *final1*

num2 ← *final2*

// Display sorted integers

print *num1*, *num2*

**Variables
used:**

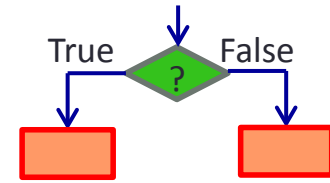
num1

num2

final1

final2

Control Structures: Selection (2/3)



- Task: Arrange two integers in ascending order (sort)

Algorithm B:

enter values for *num1*, *num2*

// Swap the values in the variables if necessary

if (*num2* < *num1*)

 then *temp* ← *num1*

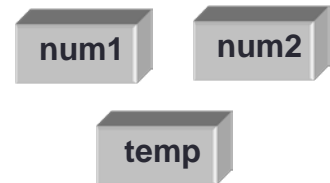
num1 ← *num2*

num2 ← *temp*

// Display sorted integers

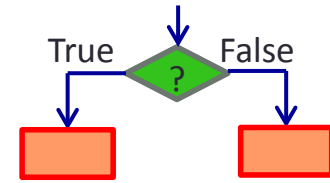
print *num1*, *num2*

**Variables
used:**



Compare Algorithm A with Algorithm B.

Control Structures: Selection (3/3)



- How the program might look like for Algorithm B

```
// This program arranges 2 integers in ascending order
#include <stdio.h>

int main(void) {
    int num1, num2, temp;

    printf("Enter 2 integers: ");
    scanf("%d %d", &num1, &num2);

    if (num2 < num1) {
        temp = num1;
        num1 = num2;
        num2 = temp;
    }
    printf("Sorted: num1 = %d, num2 = %d\n", num1, num2);
    return 0;
}
```

Unit3_prog2.c

Control Structures

Sequence

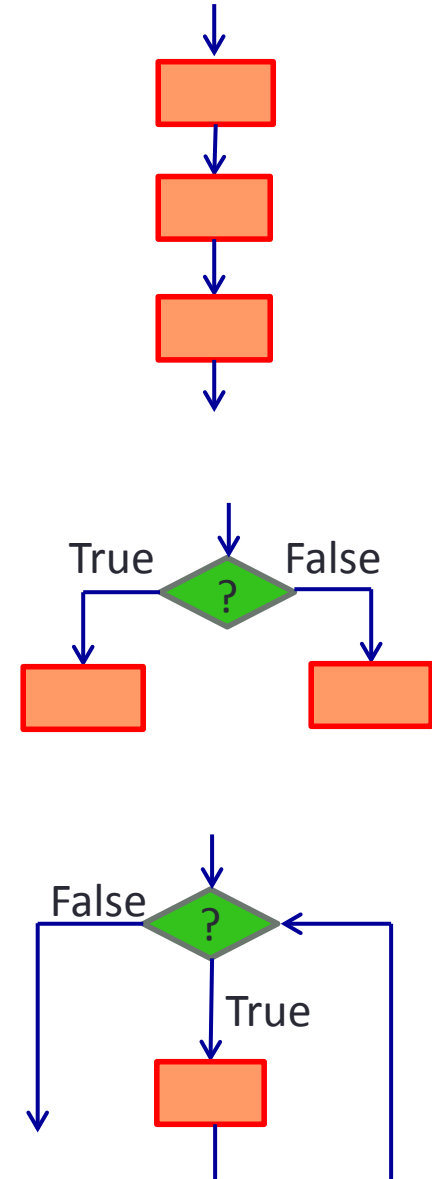
- Default

Selection

- Also called branching

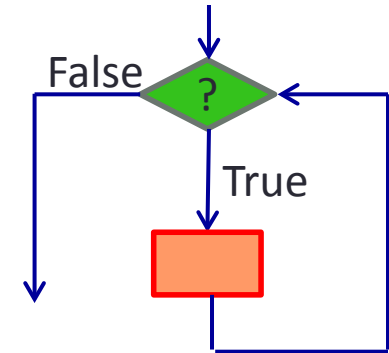
Repetition

- Also called loop



Control Structure: Repetition

- While there are prizes left
 - Play Plinko and give prizes



Control Structure: Repetition

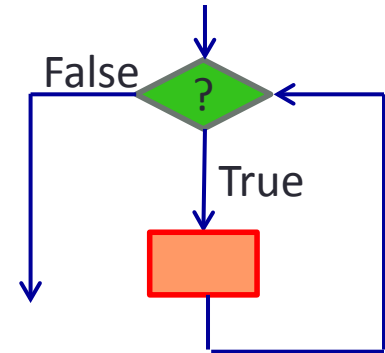
- While (a condition)
 - Do something

- For example

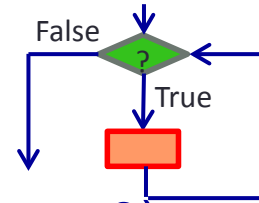
```
While (I am hungry)  
    Eat a bun
```

- Again, can be more than one single instruction

```
While(I have money in bank)  
    Take some money out from bank  
    Eat an expensive meal  
While(I have money in my wallet)  
    Go Shopping
```



Control Structures: Repetition (1/3)



- Task: Find sum of positive integers up to n (assume $n > 0$)

Algorithm:

enter value for n

// Initialise a counter $count$ to 1, and ans to 0

$count \leftarrow 1$

$ans \leftarrow 0$

while ($count \leq n$) do

$ans \leftarrow ans + count$ **// add $count$ to ans**

$count \leftarrow count + 1$ **// increase $count$ by 1**

// Display answer

print ans

Variables
used:

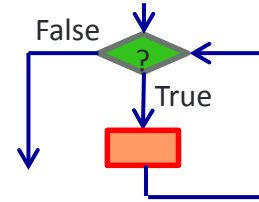
n

$count$

ans

Initialisation is
very important!

Control Structures: Repetition (2/3)



- Important to **trace** pseudocode to check its correctness

Algorithm:

```

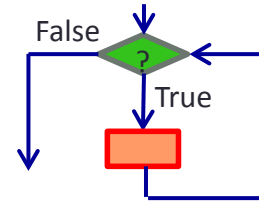
→ enter value for  $n$ 
→  $count \leftarrow 1$ 
→  $ans \leftarrow 0$ 
→ while ( $count \leq n$ ) do
  →  $ans \leftarrow ans + count$ 
  →  $count \leftarrow count + 1$ 
  // Display answer
→ print  $ans$ 
  
```

Assume user enters 3 for n .

$(count \leq n)?$	$count$	ans
	1	0
true	2	1
true	3	3
true	4	6
false		

Output: **6**

Control Structures: Repetition (3/3)



- How the program might look like

Unit3_prog3.c

```
// Computes sum of positive integers up to n
#include <stdio.h>

int main(void) {
    int n; // upper limit
    int count = 1, ans = 0; // initialisation

    printf("Enter n: ");
    scanf("%d", &n);

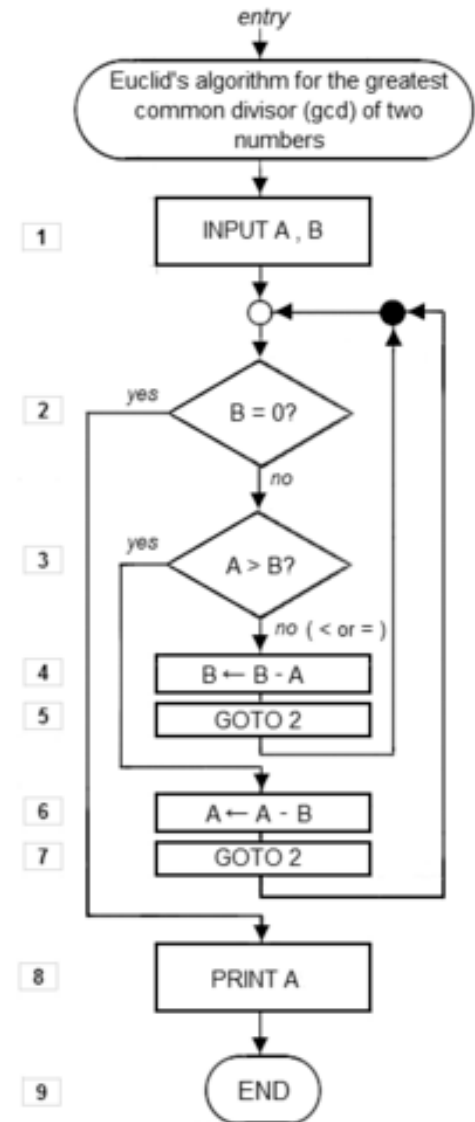
    while (count <= n) {
        ans += count;
        count++;
    }
    printf("Sum = %d\n", ans);

    return 0;
}
```

Euclid's Algorithm (1/3)

- To compute the **greatest common divisor (GCD)** of two integers
 - First documented algorithm by Greek mathematician Euclid in 300 B.C.
 - Also known as Euclidean Algorithm

1. Let A and B be integers with $A > B \geq 0$.
2. If $B = 0$, then the GCD is A and algorithm ends.
3. Otherwise, find q and r such that
$$A = q \times B + r \quad \text{where } 0 \leq r < B$$
4. Replace A by B , and B by r . Go to step 2.



Euclid's Algorithm (2/3)

1. Let A and B be integers with $A > B \geq 0$.
2. If $B = 0$, then the GCD is A and algorithm ends.
3. Otherwise, find q and r such that
$$A = q \times B + r \quad \text{where } 0 \leq r < B$$
4. Replace A by B , and B by r . Go to step 2.

- q is not important; r is the one that matters.
- r could be obtained by A modulo B (i.e. remainder of A / B)
- Assumption on $A > B$ unnecessary
- We will rewrite the algorithm

Euclid's Algorithm (3/3)

- Euclid's algorithm rewritten in modern form

```
// Assume A and B are non-negative
// integers, but not both zeroes.
```

```
Algorithm GCD(A, B) {
```

```
→ while (B > 0) {
```

```
→ r ← A modulo B
```

```
→ A ← B
```

```
→ B ← r
```

```
}
```

```
→ result is A
```

```
}
```

Let's trace GCD(12, 42)

$(B > 0)?$	r	A	B
		12	42
true	12	42	12
true	6	12	6
true	0	6	0
false			

Result: **6**

What is the difference between

Algorithm vs Program

- Algorithm
 - Ideas
 - Machine independent
- Program
 - The final code on a machine
 - Machine dependent

Research Idea vs Thesis

- Research Idea
 - Can be drawings, sketches, concepts, in any languages
- Thesis
 - Well-written documents in any languages, English, German, Chinese, etc...

Algorithm (1/3)

- An **algorithm** is a well-defined computational procedure consisting of *a set of instructions*, that takes some value or set of values as *input*, and produces some value or set of values as *output*.



‘Algorithm’ stems from ‘Algoritmi’, the Latin form of al-Khwārizmī, a Persian mathematician, astronomer and geographer.

Source: <http://en.wikipedia.org/wiki/Algorithm>

And computer will follow exactly

- “I asked my husband to peel half of the potatoes and put them on to boil...”
- And finally....



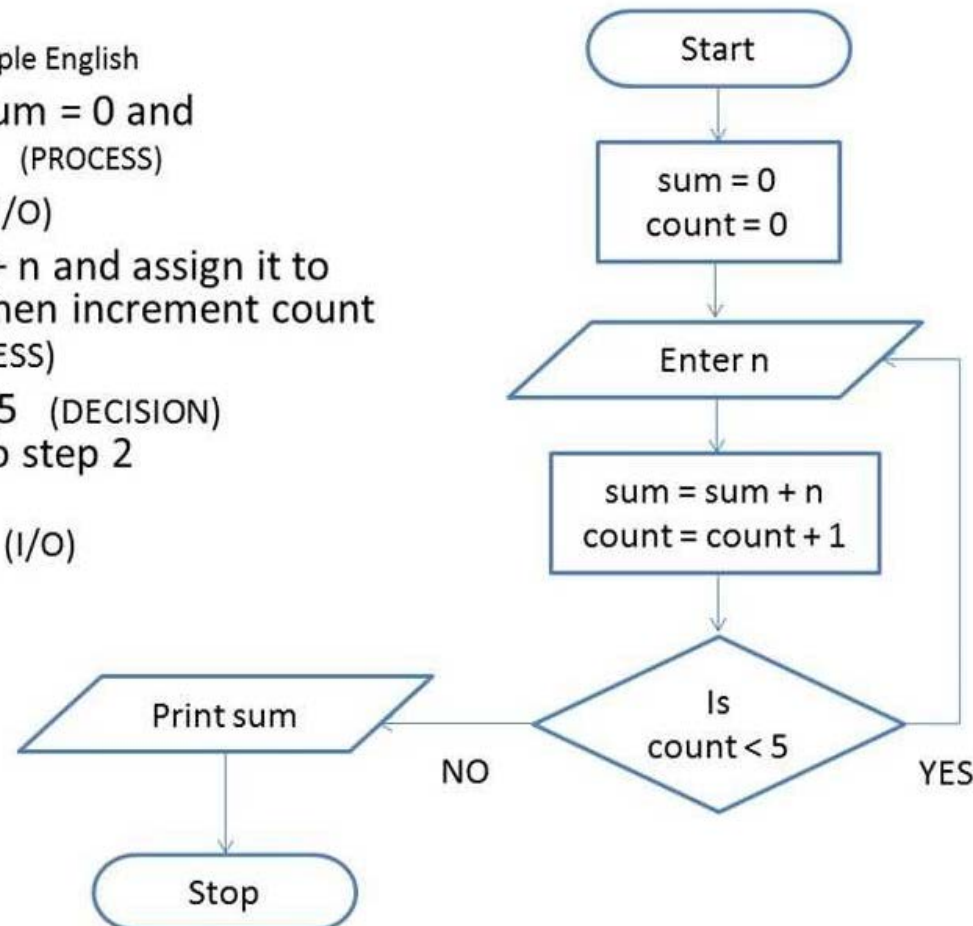
Algorithm: Example #1

Find the sum of 5 numbers

Flowchart

Algorithm in simple English

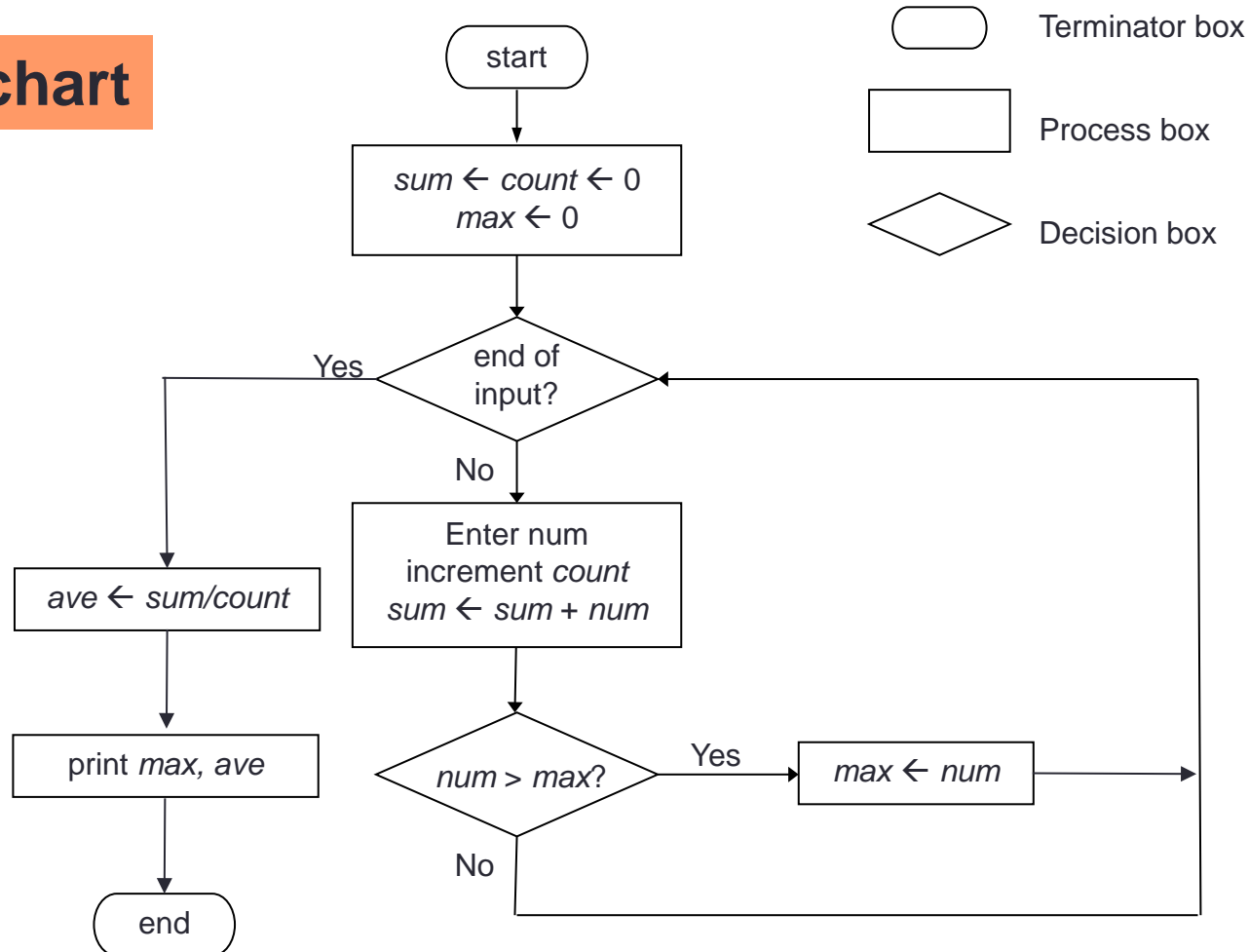
1. Initialize $\text{sum} = 0$ and $\text{count} = 0$ (PROCESS)
2. Enter n (I/O)
3. Find $\text{sum} + n$ and assign it to sum and then increment count by 1 (PROCESS)
4. Is $\text{count} < 5$ (DECISION)
if YES go to step 2
else
Print sum (I/O)



Algorithm: Example #2 (1/2)

- Find maximum and average of a list of numbers:

Flowchart



Algorithm: Example #2 (2/2)

- Find maximum and average of a list of numbers:

Pseudocode

The need to initialise variables.

```
sum ← count ← 0 // sum = sum of numbers
                  // count = how many numbers are entered?
max ← 0           // max to hold the largest value eventually
```

for each *num* entered,

```
    count ← count + 1
```

```
    sum ← sum + num
```

```
    if num > max
```

```
        then max ← num
```

The need to indent.

```
ave ← sum / count
```

```
print max, ave
```

Are there any errors in this algorithm?

Algorithm: Pseudocode

- We will write algorithms in pseudocode instead of flowchart as the former is more succinct
- However, there are no standard rules on how pseudocodes should look like
- General guidelines:
 - Every step must be unambiguous, so that anybody is able to hand trace the pseudocode and follow the logic flow
 - Use a combination of English (keep it succinct) and commonly understood notations (such as \leftarrow for assignment in our previous example)

Summary

- In this unit, you have learned about
 - The process of algorithmic problem solving
 - The properties of an algorithm
 - The three control structures
 - How to write algorithms in pseudocode
 - Tracing algorithms to verify their correctness