## National University of Singapore School of Computing CS1010S: Programming Methodology Semester I, 2018/2019

## Solutions for Recitation 5 Working with Sequences

## **Python**

- 1. Equality Testing
  - == returns True if two objects are equivalent.
  - is returns True if two objects are identical, i.e. they are the same object.
- 2. Membership Testing
  - x in y returns True if x is contained in the sequence type y. There are three basic sequence types in Python: tuples, lists, and range objects. We will discuss lists after the midterm break.
- 3. Range Type
  - The range type represents an immutable sequence of numbers and is commonly used for looping a specific number of times in for loops.
  - range(start, stop[, step]): Creates a sequence starting at start, at intervals of step, up to (but not including stop). If step is zero, ValueError will be raised.
  - range(stop): Creates a sequence starting at 0, at intervals of 1, up to (but not including stop).
  - The advantage of the range type over a regular tuple is that a range object will always take the same (small) amount of memory, no matter the size of the range it represents (as it only stores the start, stop and step values, calculating individual items and subranges as needed), i.e. O(1) space.

## **Problems**

1. Evaluate the following expressions:

```
1 == 1  # True

1 is 1  # True

"foo" == 'foo'  # True

0 == "0"  # False

0 is "0"  # False
```

```
False == False # True
False == 0
          # True
(1, 2) == (1, "2")
                  # False
(1, 2) is (1, 2) # True
(1, 2, 3, 4, 5) == (1, 2, 3, 4, 5) # True
(1, 2, 3, 4, 5) == (1, 2, 3, 5, 4) # False
((1, 2), (2, 3)) == ((1, 2), (3, 2)) # False
x = (1, 2)
y = (1, 2)
z = x
x is y # False
# Note: if you run in IDLE editor, it will be True
       if you run in IDLE shell as 3 separate assignment, it is False
       # True
x == y
x is z # True
3 in (1, 2, 3, 4, 5) # True
(1, 2) in (1, 2, 3, 4, 5) # False
(2) in (1, 2, 3, 4, 5) # True
() == () # True
(1) == 1 # True
(1, ) == 1 # False
a = ((1,2), (3,4))
b = (x, (3,4))
x in a
       # True
x in b
        # True
```

2. The function in will test if an object is inside a tuple by checking for equivalence. Write a function contains that will check if an object is inside a tuple by checking for identity. For example,

```
x = (1, 2)
```

```
a = ((1,2), (3,4))
b = (x, (3,4))

contains(x,a) => False
contains(x,b) => True

Solution:
```

```
def contains(obj, tup):
    for item in tup:
        if item is obj:
            return True
    return False
```

Write a function deep\_contains that will check if an object is nested arbitrarily deep within a tuple. For example,

```
x = (1,2)
a = ((1,2), ((3,4), x), (5,6))

contains(x,a) => False # Note: may return True in Python 3.7
deep_contains(x,a) => True

Solution:

def deep_contains(obj, tup):
    for item in tup:
        if item is obj:
            return True
        elif type(item) == tuple and deep_contains(obj, item):
            return True
    return True
    return False
```

3. The accumulate procedure discussed in lecture is also known as fold\_right, because it combines the first element of the sequence with the result of combining all the elements to the right. There is also a fold\_left, which is similar to fold\_right, except that it combines elements working in the opposite direction:

```
def accumulate(fn, initial, seq):
    if seq == ():
        return initial
    else:
        return fn(seq[0], accumulate(fn, initial, seq[1:]))

def fold_left(fn, initial, seq):
    if seq == ():
        return initial
    else:
        return fn(fold_left(fn, initial, seq[:-1]),seq[-1])
```

(a) Suppose we also define the following functions:

```
def pair(a, b):
    return (a, b)
```

(b) Give a property that fn should satisfy to guarantee that fold\_right (or accumulate) and fold\_left will produce the same values for any sequence.

Where fn is represented with  $\oplus$  which needs to be both:

i. Associative:

$$a \oplus (b \oplus c) = (a \oplus b) \oplus c$$

ii. Commutative:

$$a \oplus b = b \oplus a$$

4. A *queue* is a data structure that stores elements in order. Elements are enqueued onto the tail of the queue. Elements are dequeued from the head of the queue. Thus, the first element enqueued is also the first element dequeued (FIFO, first-infirst-out). The qhead operation is used to get the element at the head of the queue.

```
qhead(enqueue(5, empty_queue()))
# Value: 5

q = enqueue(4, enqueue(5, enqueue(6, empty_queue())))
qhead(q)
# Value: 6

qhead(dequeue(q))
# Value: 5
```

(a) Decide on an implementation for queue.

We will use a tuple q to represent the queue. The head will be q[0]. Note that it is often not sufficient to specify the underlying data structure. We also have to specify certain conditions or constraints, which in this case is the position of the head of the queue.

(b) Implement empty\_queue

```
def empty_queue():
    return ()
```

Order of growth in time? O(1) Space? O(1)

(c) Implement enqueue; a function that returns a new queue with the element x added to the tail of q.

```
def enqueue(x, q):
    return q + (x,)
```

Order of growth in time? O(n) Space? O(n)

Note that the O(n) is due to the fact that the tuple is an immutable data structure and so there is a lot of copying.

(d) Implement dequeue; a function that returns a new queue with the head element removed from q.

```
def dequeue(q):
    return q[1:]
```

Order of growth in time? O(n) Space? O(n)

(e) Implement ghead; a function that returns the value of the head element of q.

```
def qhead(q):
    return q[0]
```

Order of growth in time? O(1) Space? O(1)

5. **Homework:** Suppose x is bound to the tuple (1, 2, 3, 4, 5, 6, 7). Using map, filter, accumulate and/or lambdas (as discussed in Lecture), write an expression involving x that returns:

tuple(filter(lambda i: i%2 == 0, x)) )

You are encouraged to provide multiple solutions for the above questions.

Note that in the above, because map and filter return an iterable instead of tuple, you need to convert iterable into tuple using the function tuple before passing to fold\_left or accumulate.