

Database assignment 2

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1 Relational Algebra

Exercise 1 -

1.

$\pi_{\text{mid}} \sigma_{\text{title} = \text{"Not clickbait"} \wedge \text{likecount} > 9000} \text{messages}$

2.

$\rho(\text{invited}, \pi_{\text{id}}((\pi_{\text{eid}} \sigma_{\text{name} = \text{"Cheap sunglasses check description"}} \text{event}) \bowtie_{\text{eid}} \text{invitedToEvent})) \bowtie_{\text{id}} \text{user})$

$\rho(\text{users}, \pi_{\text{id}} \text{user})$

$\pi_{\text{id}}(\text{invited} \bowtie_{\text{invited.id} \neq \text{user.id}} \text{users})$

3.

$\rho(\text{mes1}, \text{message})$

$\rho(\text{mes2}, \text{message})$

$\rho(\text{res}, \pi_{\text{mes1.mid}}((\text{message} \times \text{message}) - \sigma_{\text{mes1.likecount} < \text{mes2.likecount}}(\text{mes1} \times \text{mes2})))$

$\pi_{\text{id}}(\pi_{\text{mid}}(\text{res}) \bowtie_{\text{mid}} \text{messageLikes}) \bowtie_{\text{id}} \text{user}$

4.

$\rho(\text{invited}, \pi_{\text{id}}(\sigma_{\text{accepted} = \text{"true"}}(\pi_{\text{eid}} \sigma_{\text{name} = \text{"Nude painting"}} \text{event}) \bowtie_{\text{eid}} \text{invitedToEvent})) \bowtie_{\text{id}} \text{user})$

$\rho(\text{users}, \pi_{\text{id}} \text{user})$

$\rho(\text{friends}, \pi_{\text{id}}(\pi_{\text{fid}} \text{friend}) \bowtie_{\text{id}} \text{user})$

$\pi_{\text{name}}(\text{invited} \bowtie_{\text{invited.id} = \text{user.id}} \text{users} \cup \text{friends})$

5.

$\rho(\text{friends}, \pi_{\text{id}}(\pi_{\text{fid}} \text{friend}) \bowtie_{\text{id}} \text{user})$

$\rho(\text{othergender}, \pi_{\text{id}} \text{friends} - \pi_{\text{id}}(\pi_{\text{id}} \text{friends}) \bowtie_{\text{gender}} \text{user})$

$\rho(\text{otherage}, \pi_{\text{id}}(\pi_{\text{id}} \text{friends}) \bowtie_{\text{friends.age} < \text{user.age}} \text{user})$

$\pi_{\text{name}}(\text{friends} / (\text{othergender} \cap \text{otherage})) \text{user}$

6.

$\rho(\text{one}, \pi_{\text{id}} \sigma_{\text{name} = \text{"Crazy Cosplay Caroline"}} \text{user})$

$\rho(\text{onemessages}, \pi_{\text{mid}} \rho_{\text{creator} = \text{one}} \text{message})$

$\rho(\text{messageliked}, \pi_{\text{id}} \sigma_{\text{mid} = \text{onemessages}} \text{messageLikes})$

$\pi_{\text{name}}((\text{messageliked}) / (\pi_{\text{id}, \text{name}} \text{user}))$

7.

$\rho(\text{mes1}, \sigma_{\text{likecount} > 999} \text{message})$

$\rho(\text{mes2}, \sigma_{\text{likecount} > 999} \text{message})$

$\rho(\text{mes3}, \sigma_{\text{likecount} > 999} \text{message})$

$\rho(\text{res1}, \pi_{\text{mes1.creator}}(\sigma_{\text{mes1.mid} \neq \text{mes2.mid} \wedge \text{mes2.mid} \neq \text{mes3.mid} \wedge \text{mes1.mid} \neq \text{mes3.mid}}(\text{mes1} \times \text{mes2} \times \text{mes3})))$

$\rho(\text{res2}, \pi_{\text{mes2.creator}}(\sigma_{\text{mes1.mid} \neq \text{mes2.mid} \wedge \text{mes2.mid} \neq \text{mes3.mid} \wedge \text{mes1.mid} \neq \text{mes3.mid}}(\text{mes1} \times \text{mes2} \times \text{mes3})))$

$\rho(\text{res3}, \pi_{\text{mes3.creator}}(\sigma_{\text{mes1.mid} \neq \text{mes2.mid} \wedge \text{mes2.mid} \neq \text{mes3.mid} \wedge \text{mes1.mid} \neq \text{mes3.mid}}(\text{mes1} \times \text{mes2} \times \text{mes3})))$

$\pi_{\text{id}}(\sigma_{\text{res1.creator} = \text{res2.creator} \wedge \text{res2.creator} = \text{res3.creator} \wedge \text{res1.creator} = \text{res3.creator}}(\text{res1} \times \text{res2} \times \text{res3})) \bowtie_{\text{res.creator} = \text{user.id}} \text{user}$

2 Shema Normalization

Exercise 2 -

1.

Determine all the functional dependencies (F) that are derivable from the points mentioned above.

$V \rightarrow TUCSD$ (A video ID implies all video attributes)

$UT \rightarrow V$ (Since an uploader cannot upload more than one video with the same title, these attributes imply the video ID)

$S \rightarrow C$ (Since subcategories are unique per category, there are no subcategories placed in more than one

category)

$N \rightarrow BA$ (Since a comment number is unique, it implies all comment attributes)

$N \rightarrow U$ (Since a comment number is unique and used by the same account used for uploading, it implies the uploader)

$N \rightarrow V$ (Since every comment is linked via its number to a single video ID, the comment number implies the video ID)

2. Determine the key(s) in this table

$N \rightarrow V, V \rightarrow TUCSD$

implies $N \rightarrow TUCSD$ (Transitivity)

$N \rightarrow BA, N \rightarrow U, N \rightarrow V, N \rightarrow TUCSD$

implies $N \rightarrow BAUVTUCSD$ (Union)

Since N is never on the right side,

N is certainly part of all existing keys and since N is a key of itself,

N must be the only existing key.

3. Derive a minimal cover (G) for R

First, we listed all FD's:

$V \rightarrow T$

$V \rightarrow U$

$V \rightarrow C$

$V \rightarrow S$

$V \rightarrow D$

$UT \rightarrow V$

$S \rightarrow C$

$N \rightarrow A$

$N \rightarrow B$

$N \rightarrow U$

$N \rightarrow V$

Then we try to derive existing FD's from others:

$N \rightarrow V, V \rightarrow U$ implies $N \rightarrow U$ (Transitivity)

So, we delete $N \rightarrow U$ from the list

Finally, we write down the minimal cover: $V \rightarrow TUCSDUT \rightarrow VS \rightarrow CN \rightarrow ABV$

4.

Using your minimal cover, derive a lossless join decomposition in BCNF and indicate a primary key for each table in the decomposition.

VTUCSDNBA

$\Downarrow \Rightarrow NVBA$

VTUCSD

The resulting lossless join decomposition in BCNF is: VTUCSD, NVBA

5.

Is your decomposition also dependency preserving? Why is or isn't it? If it is not, derive a dependency preserving decomposition in 3NF.

The decomposition is not dependency preserving, because not all FD's in the minimal cover have their own table

To make it dependency preserving, we add a table for all other FD's, the resulting decomposition is:

VTUCSD, NVBA, UTV, SC

6.

Prove, if $XY \rightarrow B$ and $X \rightarrow Y$ then $X \rightarrow B$

$XY \rightarrow B$

$X \rightarrow Y$

$XX \rightarrow XY$ (Augmentation X)

$XX \rightarrow B$ (Transitivity XYB)

$X \rightarrow B$ (Union)

Exercise 3 -

1.

<https://preview.ibb.co/gm0R67/graph.jpg>

2.

The graph is not conflict serializable because there exists a cycle in between T1 and T2.

3.

T1:	S(C)R(C)		S(B)R(B)	X(C)W(C)	X(A)W(A)
T2:		S(B)R(B)	X(B)W(B)		
T3:	S(A)R(A)		X(A)W(A)		S(A)R(A)
T4:					S(C)R(C)