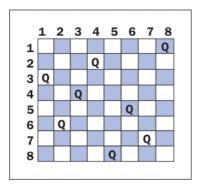
## The N Queens problem

(a variation of the Eight Queens problem)

acknowledgements to Robert Glen Martin for this assignment

Perhaps you are familiar with the Eight Queens problem, which consists of trying to place eight queens on a chessboard (which is 8 by 8 squares) in such a manner that none of the queens can attack each other. According to the rules of chess, a queen can attack any other piece in the same row, column, or diagonal, so there can be at most one queen in each row, column, or diagonal of the board. It is not obvious that there is a solution, but the diagram at the right shows one of them.

In this assignment you will implement the N Queens problem, which seeks to place n queens on an n by n board in such a way that no queen can attack another queen. Theoretically we could solve for any number of queens on a chessboard of the same size.



To get started, click on the link and then download, extract, and save the following N Queens project files.

- a. ChessBoard the class that implements the solution to the N Queens problem and displays it (this is the only class you will modify).
- b. Main contains the main method.
- c. ImageTool used to display each queen.
- 1. Compile and run the program as is. You should see a square board with no queens. Look over the code in the ChessBoard class. Pay particular attention to the instance variables and methods. Make sure you understand the method headings so you know what the methods need to do.
- 2. Many times recursive methods need a starter method to get the recursion started. In this case, the method that starts the recursion is the solve method. Complete the solve method by calling placeQueen to place a queen in the first row (which row is that?). Recall that the *q*th queen is placed in the row *q*, so what will be the simple one line command to place a queen in row 0?
  - Then, to test your work so far, temporarily modify the placeQueen method to add a queen (using the addQueen method) to the first column of the correct row for that queen, and then remove the queen (using the removeQueen method). Note that addQueen and removeQueen require a row number and a column number.

(In this first test case, the location row and column numbers will both be zero.)

Compile and Run the program and then click on the Run button at the bottom of the screen. The size of the board does not matter, so simply type in 0 and press enter. Try "step" mode to make sure your program is adding and removing the queen correctly and then choose the default speed by typing -1. You should see one queen appear and then disappear from the upper left corner of the board.

Make sure this is working correctly before proceeding any further.

3. This next step is challenging, so let's start by reviewing the overall concept. The idea is to write a recursive method that continues to place all of the queens until all of them are placed. Every recursive method needs a **base case** (how to know when you're done) and a **recursive step** (where the method calls itself again). We are going to start with placing the first queen in the first (top) row, and then place the next queen in the next row and so on. In this case, the method is going to continue to recursively call itself to place the next queen (q + 1), until we run out of rows to place them in. In other words, if the current row is less than the total number of rows, then the recursive step takes place, otherwise we are done. Therefore, what will be the test for the base case? For an idea, think about how you might test to see if you are still in the middle of an array. Now apply that concept to check if a given row is within the board or not. It is helpful to know that the number of rows that the board has in defined by the variable size.

Now it's time to start writing the recursive method.

- ✓ First, delete all of the code in the body of the placeQueen method.
- ✓ In its place write an if statement that tests if we are *not* done yet.
- ✓ If that test is true (i.e. not done yet) then make the one line recursive call as follows: if (.....) return true;
  - The recursive call will attempt to place the next queen. This way if the recursive call successfully places a queen then it will signify it by returning true.
- ✓ Place a return false statement at the very end of the placeQueen method (meaning we are all done placing queens). *Make sure your code compiles before proceeding any further.*

Now, we want to use our recursive method to place a queen (using the addQueen method) in column 0 of each row, one-at-a-time. Again, recall that the qth queen is placed in row q. In other words, the call to placeQueen (4) places a queen in row 4. At this stage we are just going to place them all in the first column (column 0) of each row. Since we want them to be placed in order (starting at 0), do you want to make the call to addQueen (row, col) immediately before or after the recursive step?

Once you have determined where it should go, then add the code to placeQueen that will add a queen in the appropriate location. Compile and run your code (enter 0 then step then -1) to see that the queens appear properly (starting at the top left corner, and going down in a straight line all the way to the bottom of the board). Make sure this is working correctly before proceeding any further.

- 4. In a similar fashion, after all of the queens have been placed, we want to now remove them, one-at-atime, except in reverse order (last one first). Think about where in the placeQueen method you will want to make the call to removeQueen (row, col). Will it be immediately before or after the recursive step? When you have determined where it should go, then add the code to placeQueen that will remove a queen from the appropriate location.
  - Compile and run your code to see that all of the queens appear and then disappear properly. *Make sure this is working correctly before proceeding any further.*
- 5. We need to have placeQueen check the isForbidden method before going ahead and adding a queen to a given location. Write an if statement that checks the isForbidden before doing anything else (use row and col as the parameters). The current version of isForbidden should not have any effect on the current placement of queens, so that means a queen will still be added to the first column of each row. *Make sure this is working correctly before proceeding any further.*

6. Now we need to deal with placing the queen in a column other than the first one. Immediately after checking if q is within size (the number of rows), write a for loop that iterates through each column number (using size – also the number of columns).

Next should come the call to see if the location isForbidden. The queen should be added to the first location (column) that returns false (the location is not forbidden). If for some reason isForbidden should return true for every column in a given row, then addQueen, removeQueen and the recursive step would not get called for that row, and placeQueen should return false (because a queen did not get placed).

You should now notice that now after all of the queens are placed in the first column of each row, the last queen is removed, and then added to the next column to the right, and so on. If left alone, the program will now display each of the N! unique ways to display N queens on a board. You probably don't have time to watch them all, but you should see that it appears to be working correctly for the bottom rows before stopping the program. *Make sure this is working correctly before proceeding any further.* 

- 7. The final steps involve modifying the isForbidden method to return true if any other queens are in a position to attack the location where we are considering putting another queen. When you have this working you should see the queens initially fill in the diagonal from location (0, 0) to location (n-1, n-1). Make sure this is working correctly before proceeding any further.
- 8. The last thing we need is Forbidden to check for is any queens that may be on a diagonal from the given location.
  - If working properly, isForbidden should now only return true if and only if there are other queens in the same column, or on either 45 degree diagonal line from the given location.
- 9. Finally, properly stop the recursion after we have found a solution.
- 10. If everything is working correctly, your program should now continue to run until it places all of the queens properly. It may take several minutes for the program to find a solution, but it should eventually. Verify that it does so. Have fun experimenting with the different options you were provided with. Try a different board size, mode, or delay. Demonstrate your work for me to observe.