

name: Solution

1. Find the derivatives for the following functions (3 points each)

(a) $g(x) = 6x - 2xe^x$

(b) $f(x) = \frac{2e^x - 1}{2e^x + 1}$

(c) $h(w) = \frac{w^2 - 1}{w^2 + 1}$

$$\begin{aligned} (a) \quad g'(x) &= \frac{d}{dx}(6x) + \frac{d}{dx}(-2xe^x) \\ &= 6 - \left(\frac{d}{dx}(2x) \cdot e^x + 2x \frac{d}{dx}(e^x) \right) \\ &= 6 - 2e^x - 2xe^x \end{aligned}$$

$$\begin{aligned} (b) \quad f'(x) &= \left(\frac{\frac{d}{dx}(2e^x - 1)(2e^x + 1) - (2e^x + 1) \frac{d}{dx}(2e^x - 1)}{(2e^x + 1)^2} \right) \\ &= \left(\frac{2e^x(2e^x + 1) - 2e^x(2e^x - 1)}{(2e^x + 1)^2} \right) = \left(\frac{4e^x}{(2e^x + 1)^2} \right) \end{aligned}$$

$$\begin{aligned} (c) \quad h'(w) &= \left(\frac{\frac{d}{dw}(w^2 - 1)(w^2 + 1) - (w^2 - 1) \frac{d}{dw}(w^2 + 1)}{(w^2 + 1)^2} \right) \\ &= \left(\frac{(2w)(w^2 + 1) - (w^2 - 1)(2w)}{(w^2 + 1)^2} \right) = \left(\frac{4w}{(w^2 + 1)^2} \right) \end{aligned}$$