

name: Solution

1 (8 points). Graph the function  $f(x) = 3x - x^3$ . Be sure to label all intervals where  $f$  is increasing and decreasing, the intervals where  $f$  is concave up and down, and list local extrema.

Increasing/Decreasing

$$f'(x) = 3 - 3x^2$$

$$\text{C.P.} = \pm 1$$

-1	+1
$f'(x) < 0$	$f'(x) > 0$

- increasing on  $(-\infty, -1), (1, \infty)$
- decreasing on  $(-1, 1)$

Concave Up/Down

$$f''(x) = -6x$$

$$\text{C.P.} = 0$$

0	
$f''(x) > 0$	$f''(x) < 0$

- concave up  $(-\infty, 0)$
- concave down  $(0, \infty)$

Extrema

The critical points are

$$x = \pm 1.$$

•  $x = -1$  is a minimum  
b/c  $f$  is concave up

•  $x = 1$  is a maximum b/c  $f$  is concave down

