

name: Solution

1. Compute the derivatives for the following functions (2 points each)

(a) $y = \cos(5t)$

(b) $y = \sin(\cos(z))$

(c) $g(x) = \frac{x}{e^{3x}}$

(d) $(y = \cos(4x^3))^{\frac{7}{4}}$

$$a) y' = -5 \sin(5t)$$

$$b) y' = \cos(\cos(z)) \frac{d}{dz}(\cos(z)) \\ = -\cos(\cos(z)) \sin(z)$$

$$c) g'(x) = \frac{\frac{d}{dx}(x) e^{3x} - x \frac{d}{dx}(e^{3x})}{(e^{3x})^2} = \frac{e^{3x} - 3x e^{3x}}{e^{6x}}$$

$$d) y' = \frac{7}{4} (\cos(4x^3))^{\frac{3}{4}} \frac{d}{dx}(\cos(4x^3)) \\ = \frac{7}{4} (\cos(4x^3))^{\frac{3}{4}} (-\sin(4x^3) \frac{d}{dx}(4x^3)) \\ = -\frac{7}{4} (\cos(4x^3))^{\frac{3}{4}} \sin(4x^3) \cdot 12x^2 \\ = -21x^2 \sin(4x^3) (\cos(4x^3))^{\frac{3}{4}}$$