

# Feature Indexing

CSE 40537/60537 Biometrics

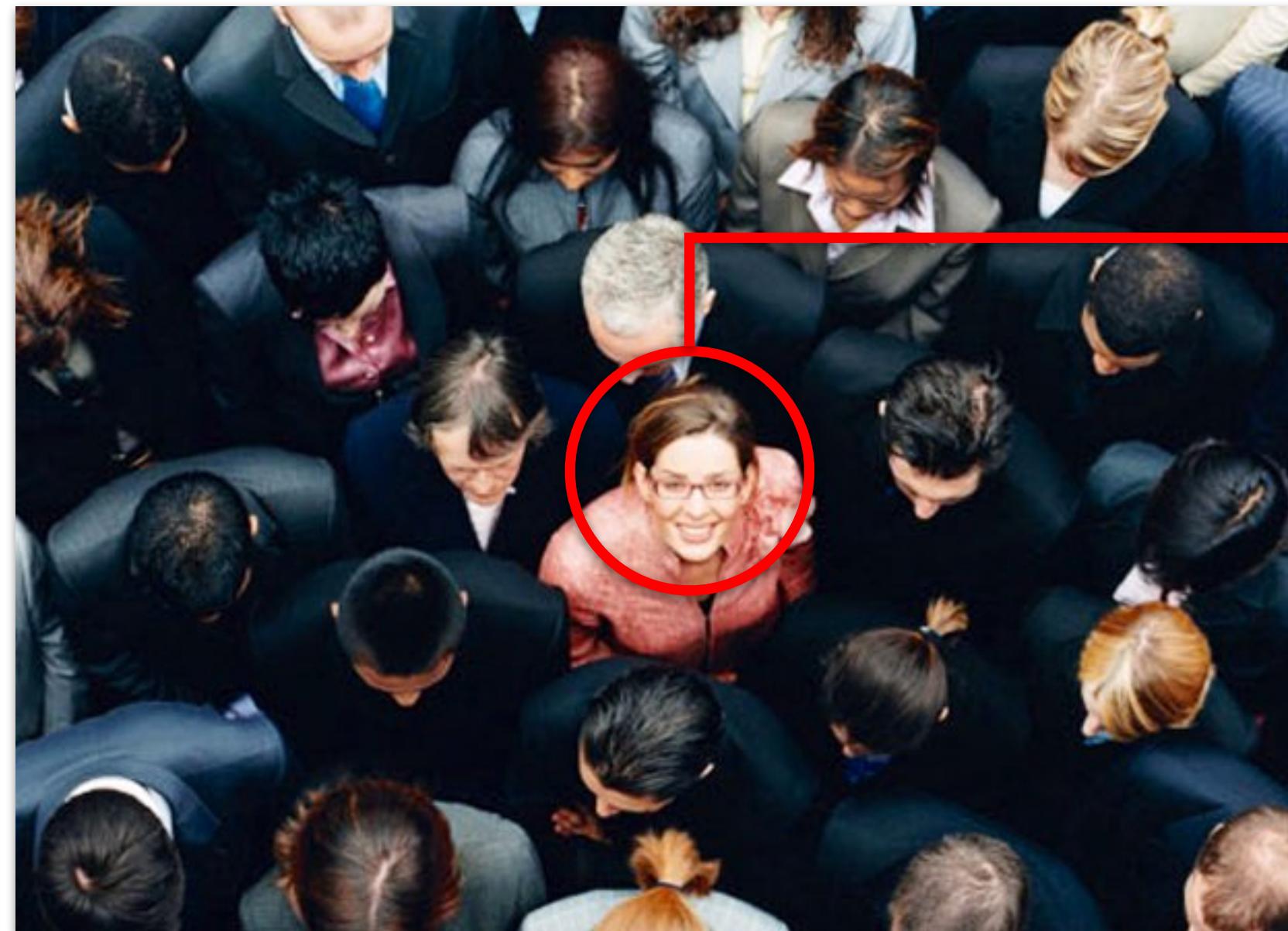
**Daniel Moreira**  
Spring 2022



# Today you will...

*Get to know*  
Methods of feature indexing for  
Biometric identification.

# What is Biometrics?

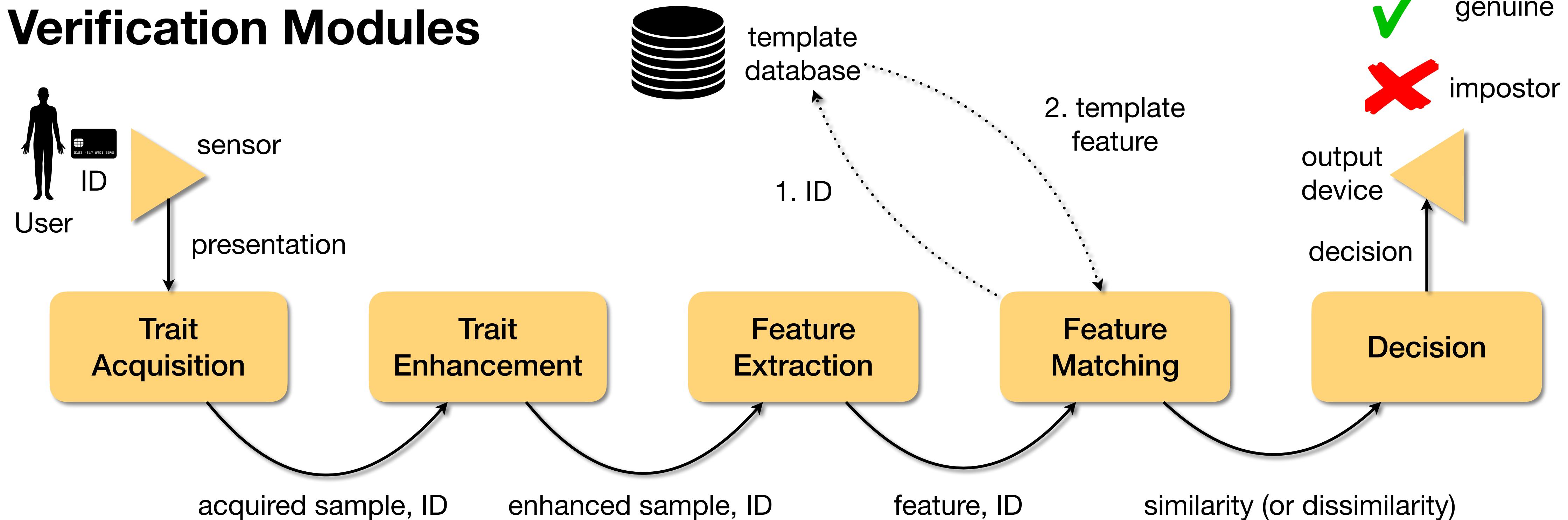


- **7 billion people**  
Who is this person? (*Identification*)  
Is this person Jane Doe? (*Verification*)

Biometrics aims at ***identifying*** or ***verifying*** the claimed or denied identity of an individual based on their ***physical***, ***chemical*** or ***behavioral*** traits.

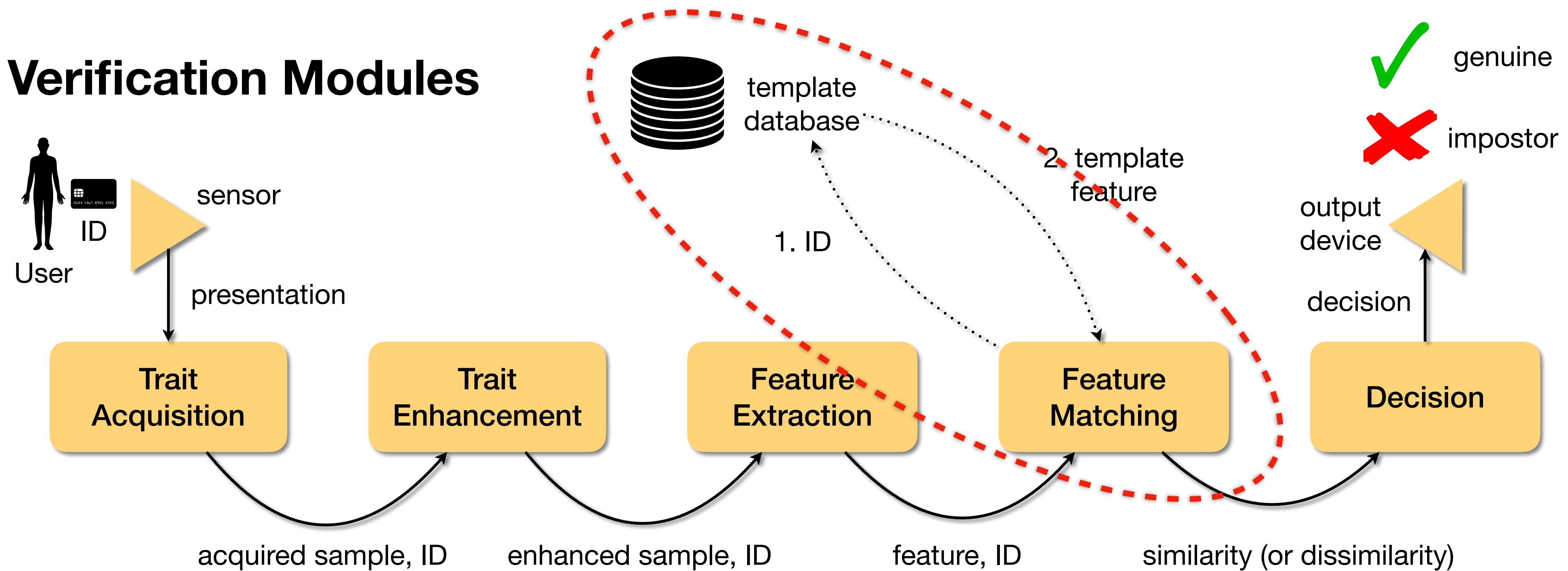
# Biometric Systems

## Verification Modules



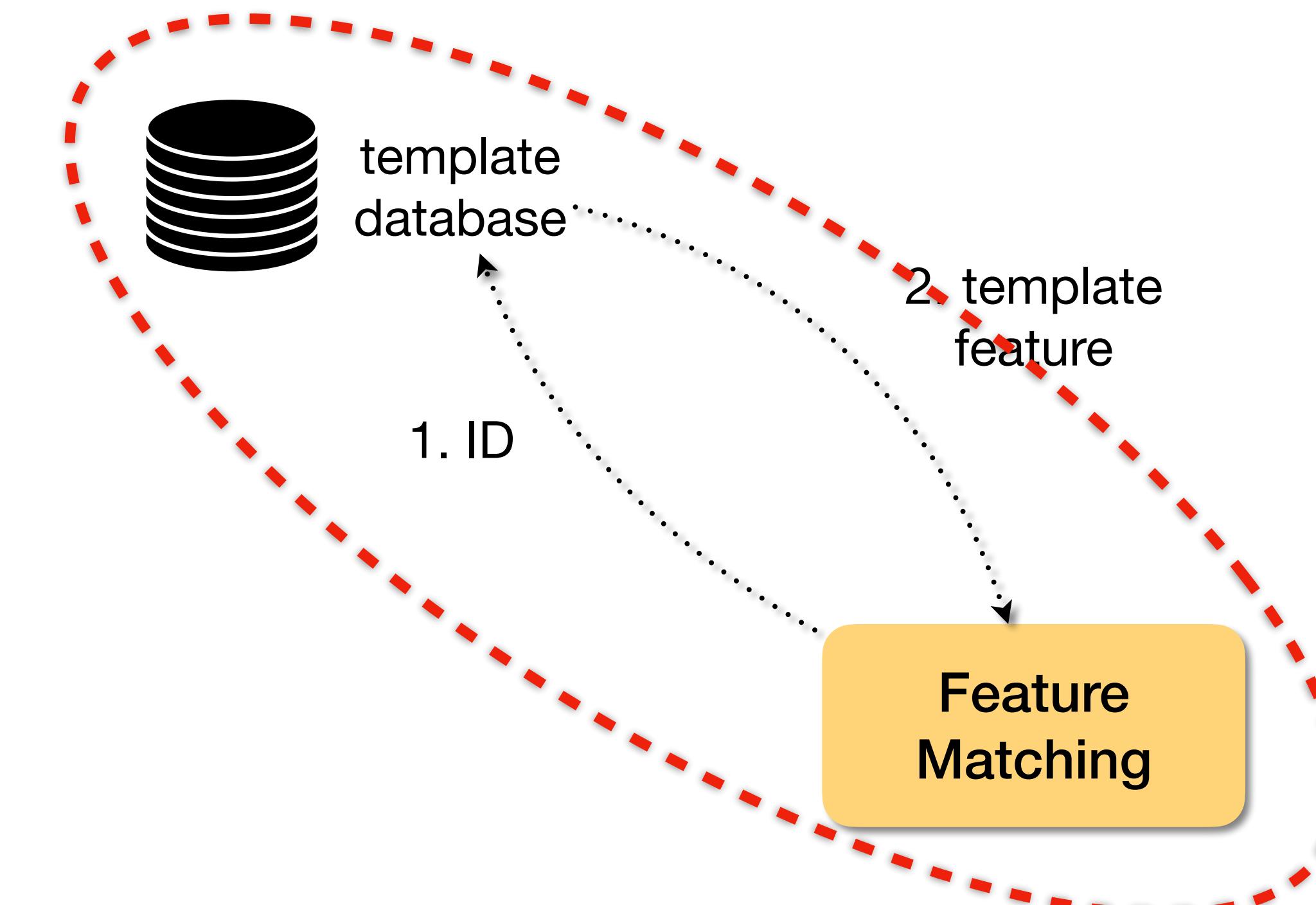
# Biometric Systems

## Verification Modules



# Biometric Verification

No need for complex feature indexing.

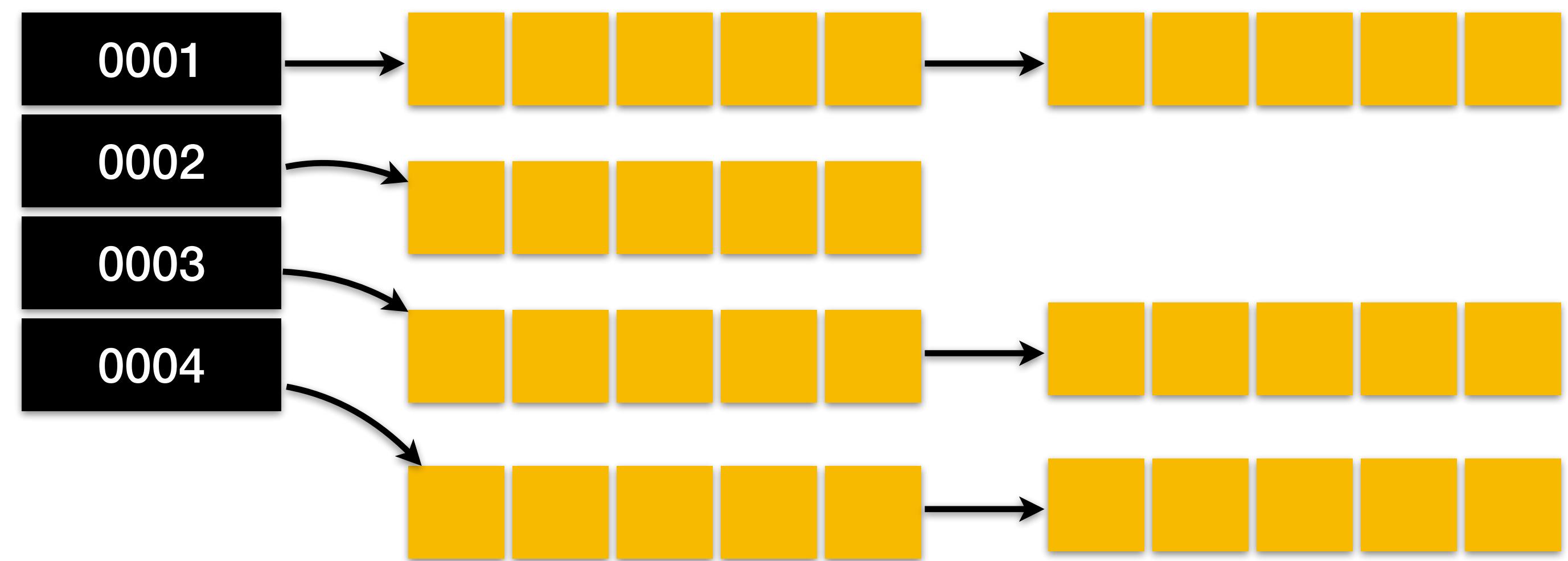


# Biometric Verification

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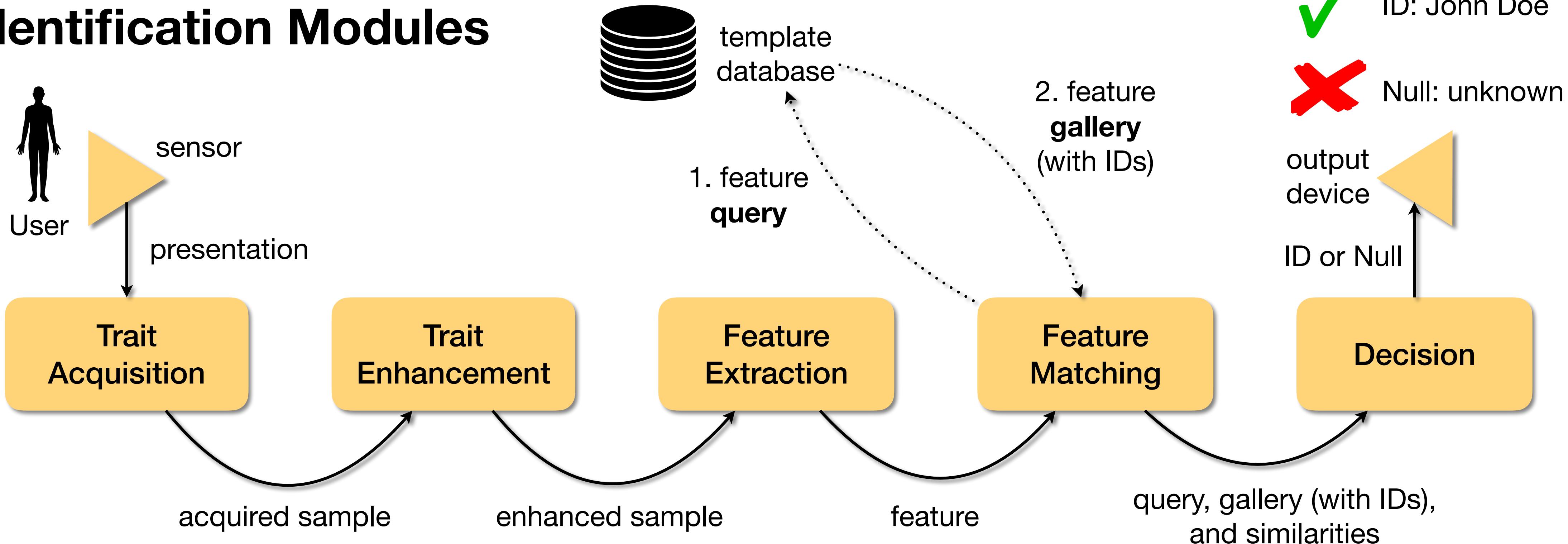
Use unique person's ID as index (or hash function input).

Retrieval of features in constant time.



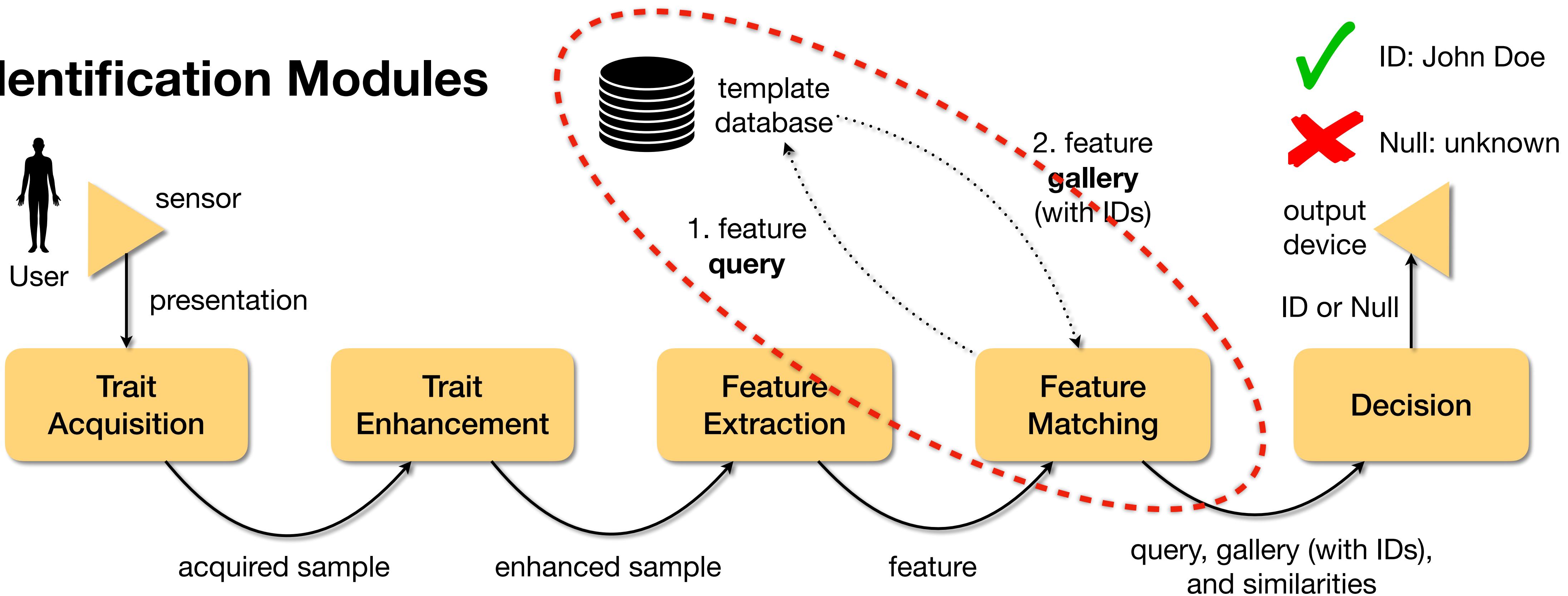
# Biometric Systems

## Identification Modules



# Biometric Systems

## Identification Modules

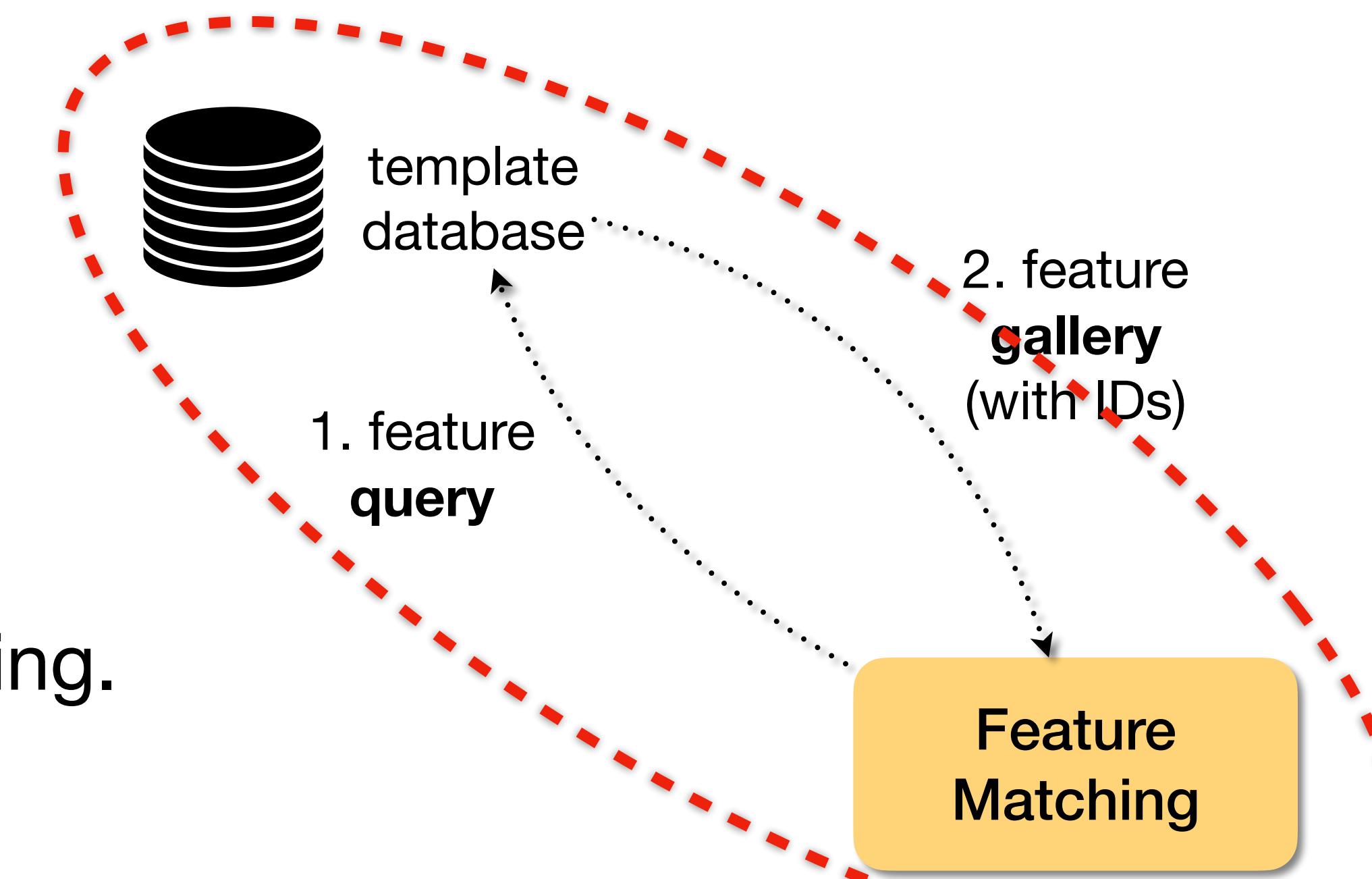


# Biometric Identification

How to retrieve  $k$ -nearest features to compose gallery?

Need for more complex indexing.

Retrieval of features as quick as possible.



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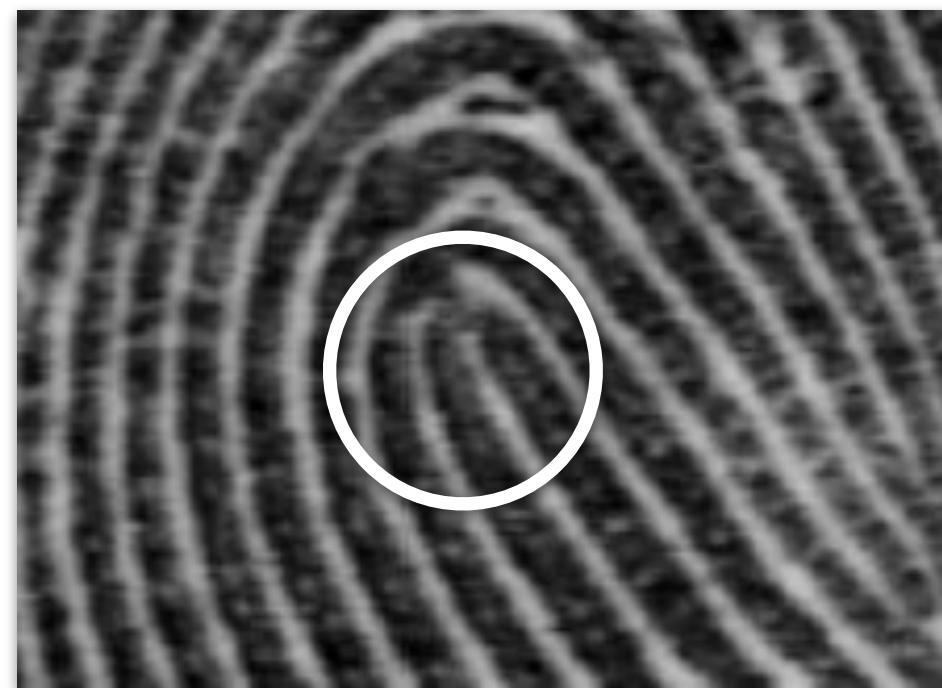
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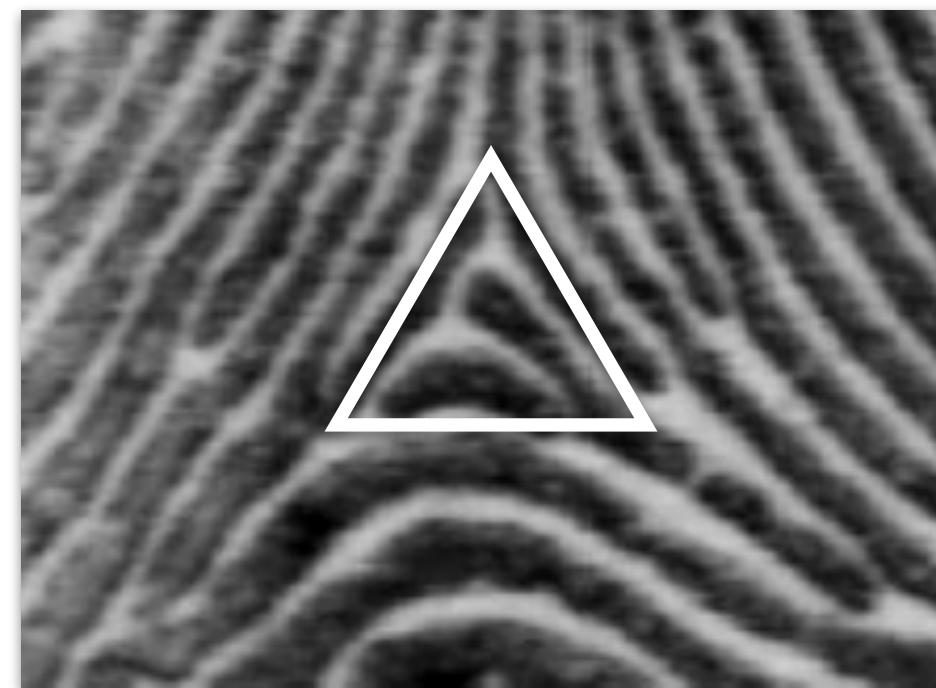
# Fingerprint Indexing

## Level-1 Features

### Usage of Singular Points and Core



loop



delta

Jain, Ross, and Nandakumar  
*Introduction to Biometrics*  
Springer Books, 2011

# Fingerprint Indexing

## Level-1 Features

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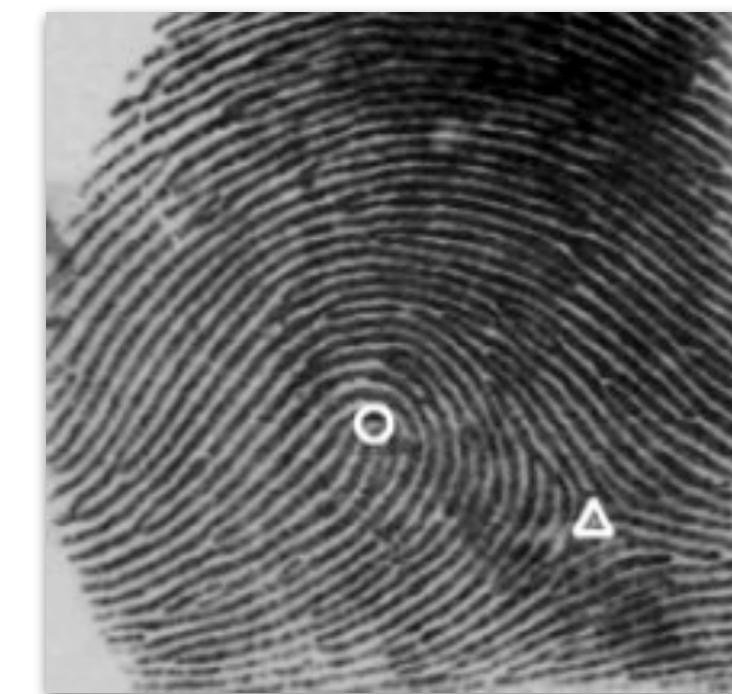
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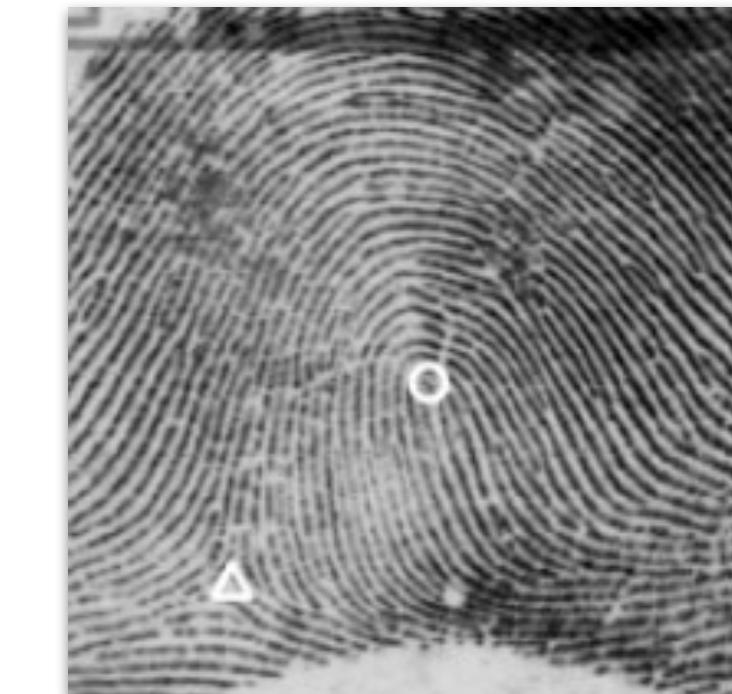
plain arch



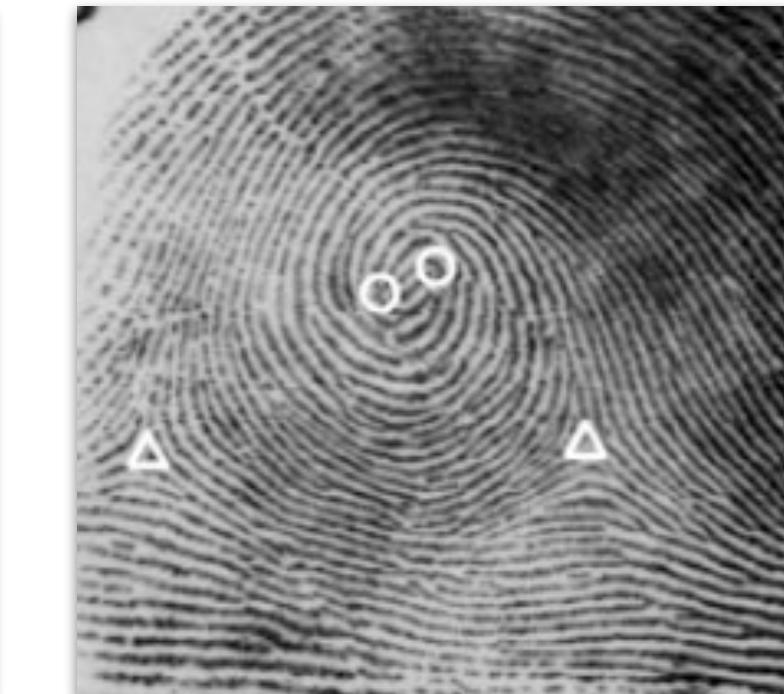
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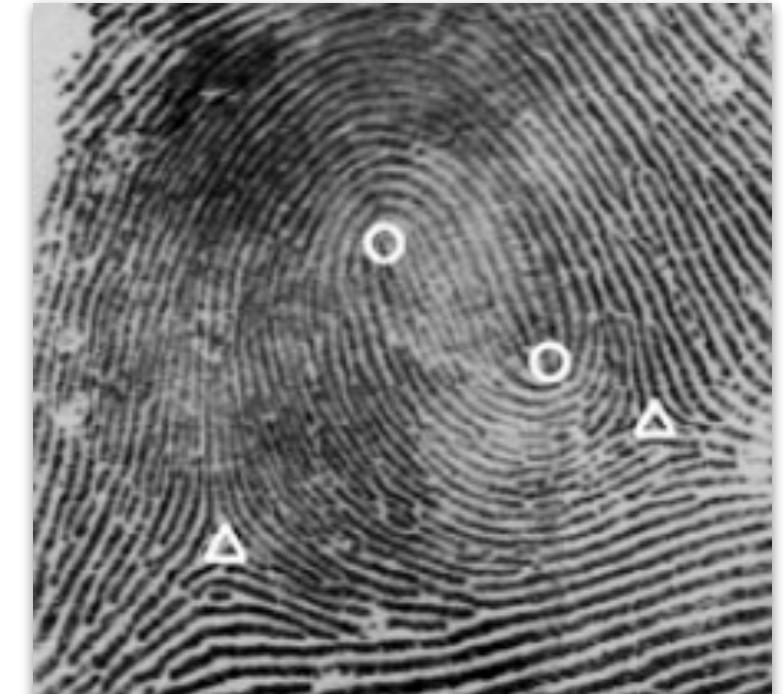
left loop



right loop



whorl



twin loop

# Fingerprint Indexing

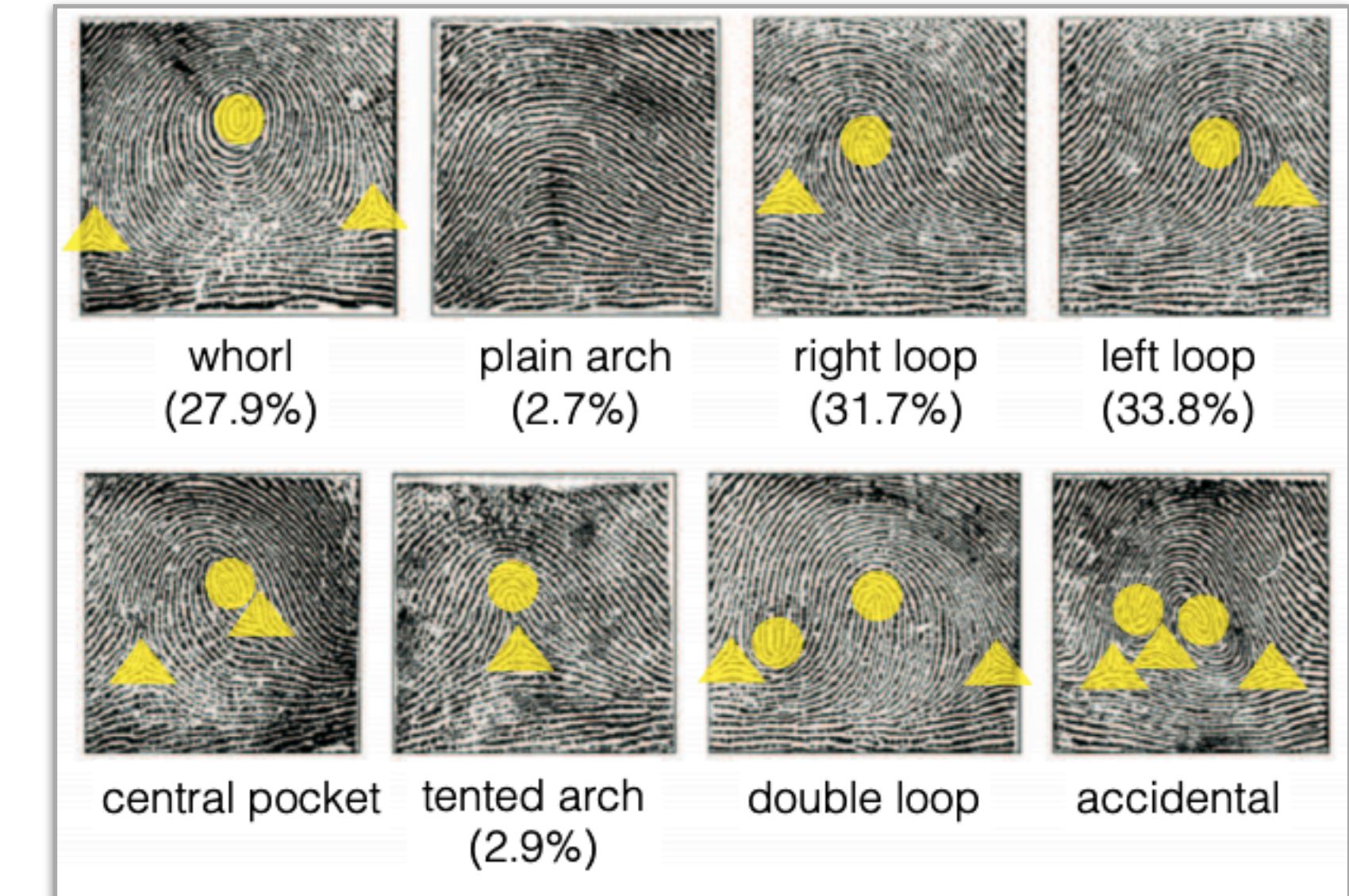
## Level-1 Features

### FBI Automated Fingerprint Identification system (AFIS)

More than 200 million dactyloscopy cards.

Varied quality of samples.

Thanks to fingerprint classification through level-1 features, this time is reduced to **20 min.**



Henry's features, an alternative classification of level-1 features with 8 classes.

# Fingerprint Indexing

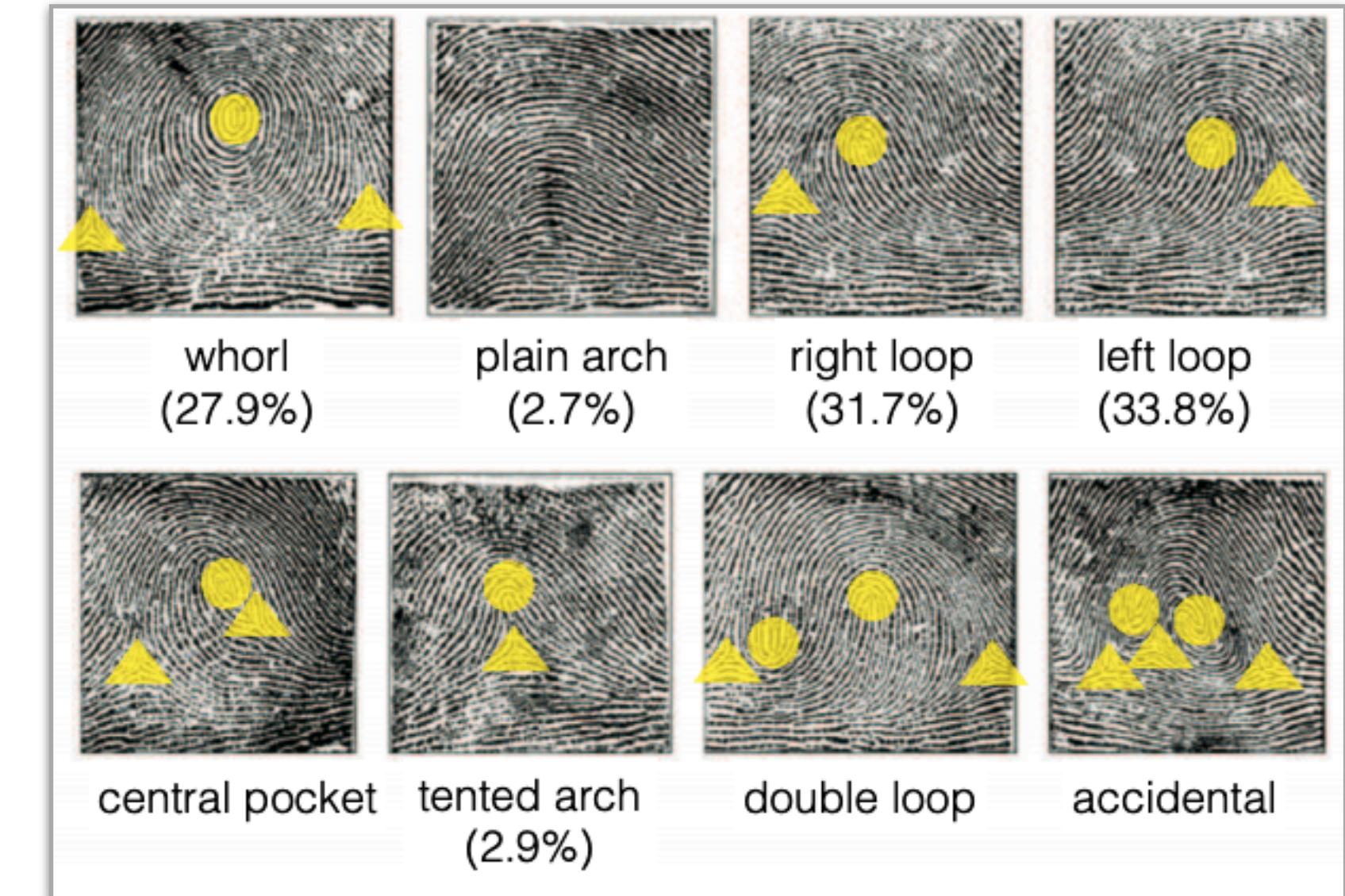
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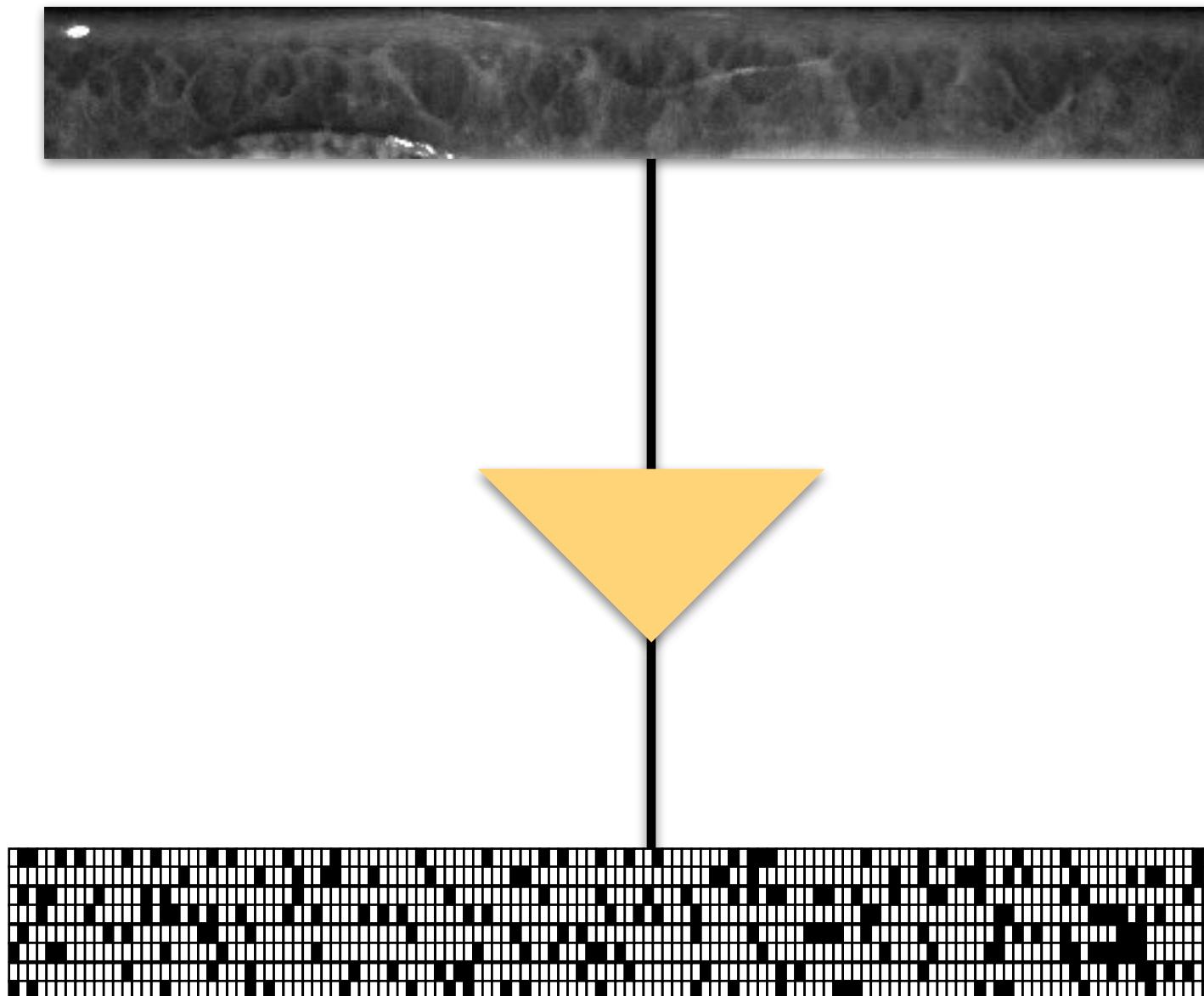
And a computer-based solution can do it in seconds, benefitting from the same features.



Henry's features, an alternative classification of level-1 features with 8 classes.

# Feature Indexing

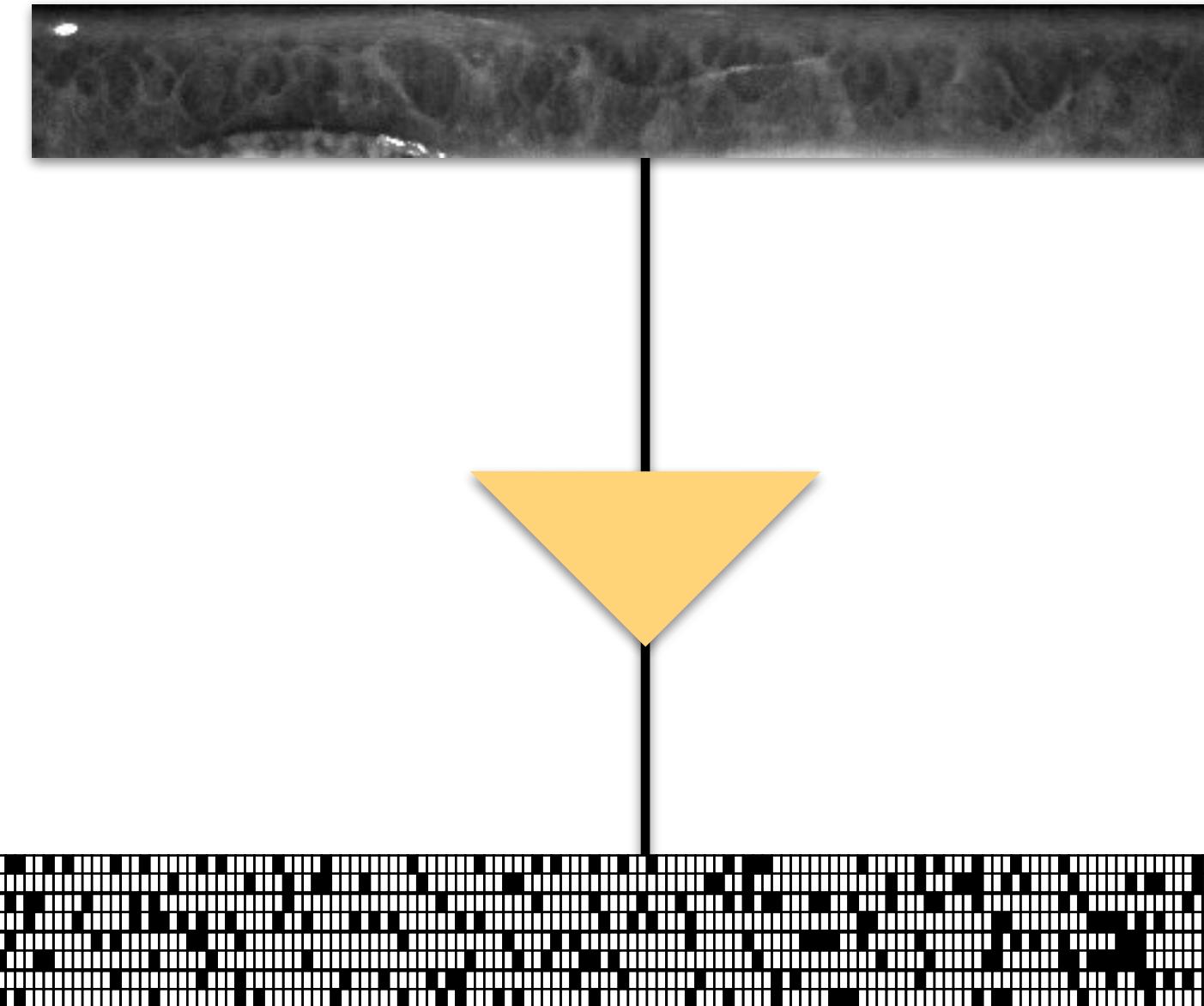
## Iris Identification



2048 bits IrisCode

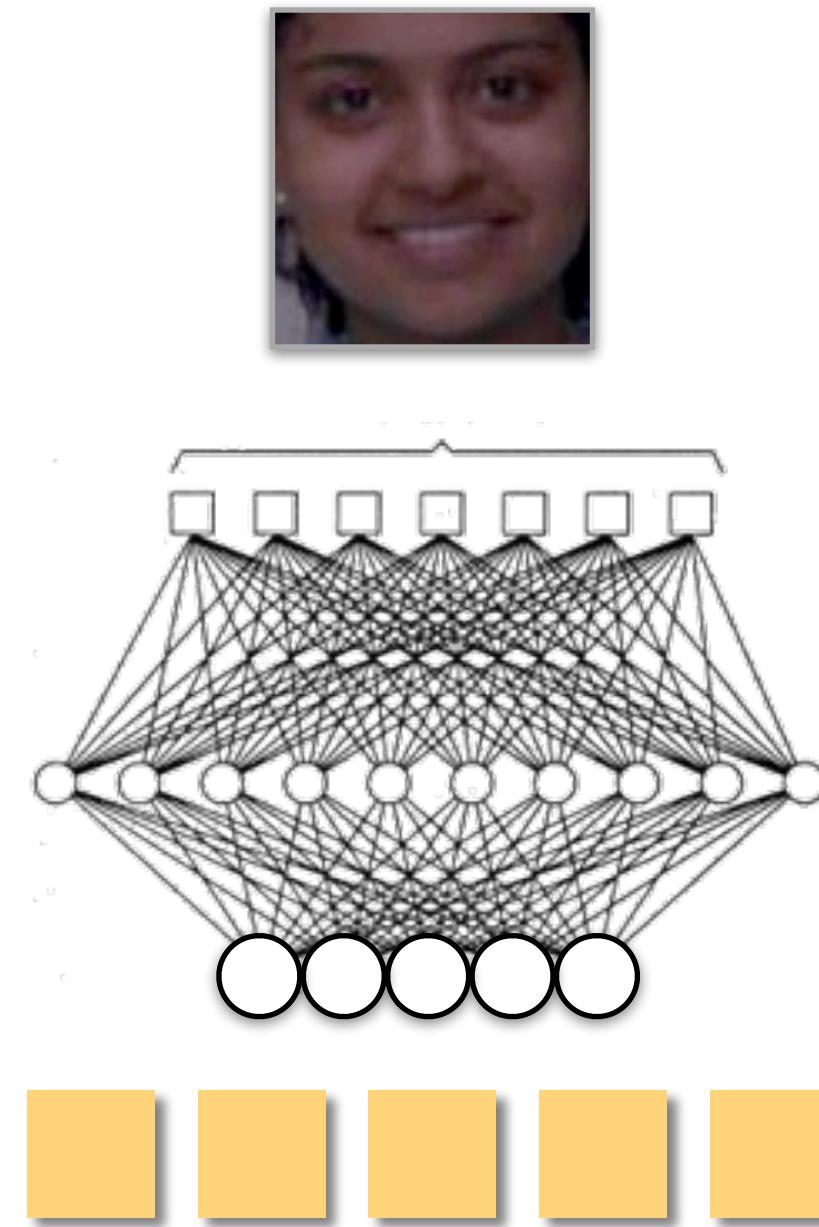
# Feature Indexing

Iris Identification



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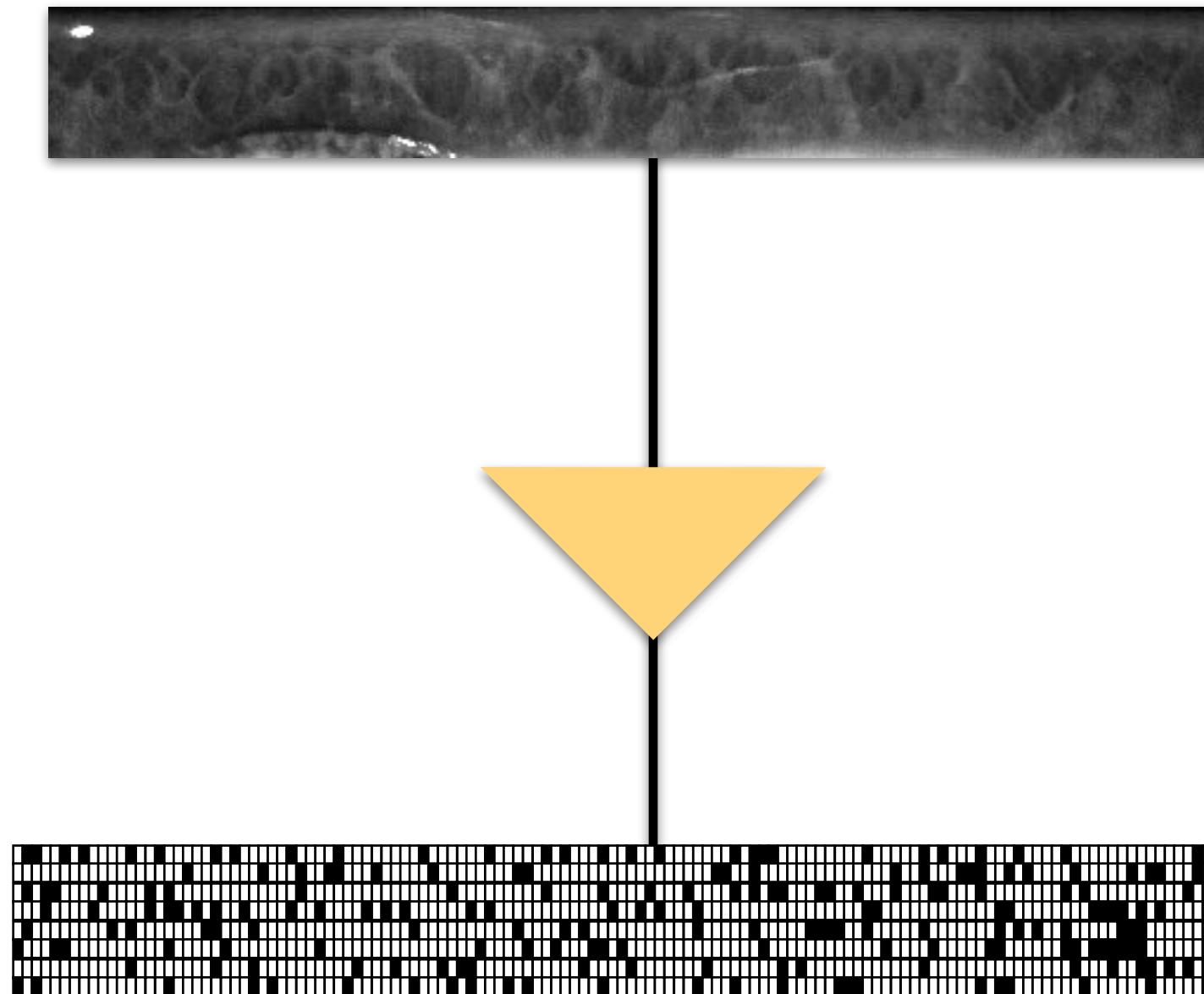
Face Identification



512D ArcFace embedding

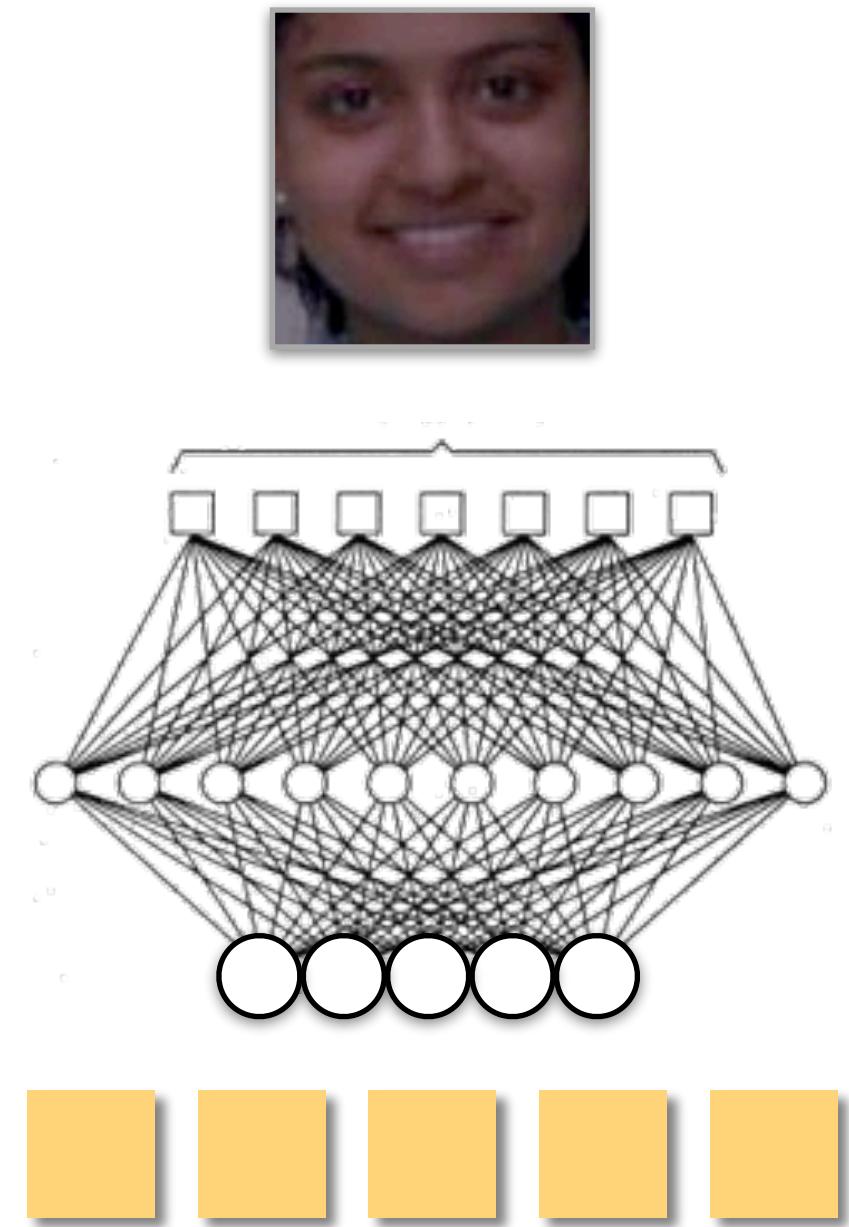
# Feature Indexing

Iris Identification



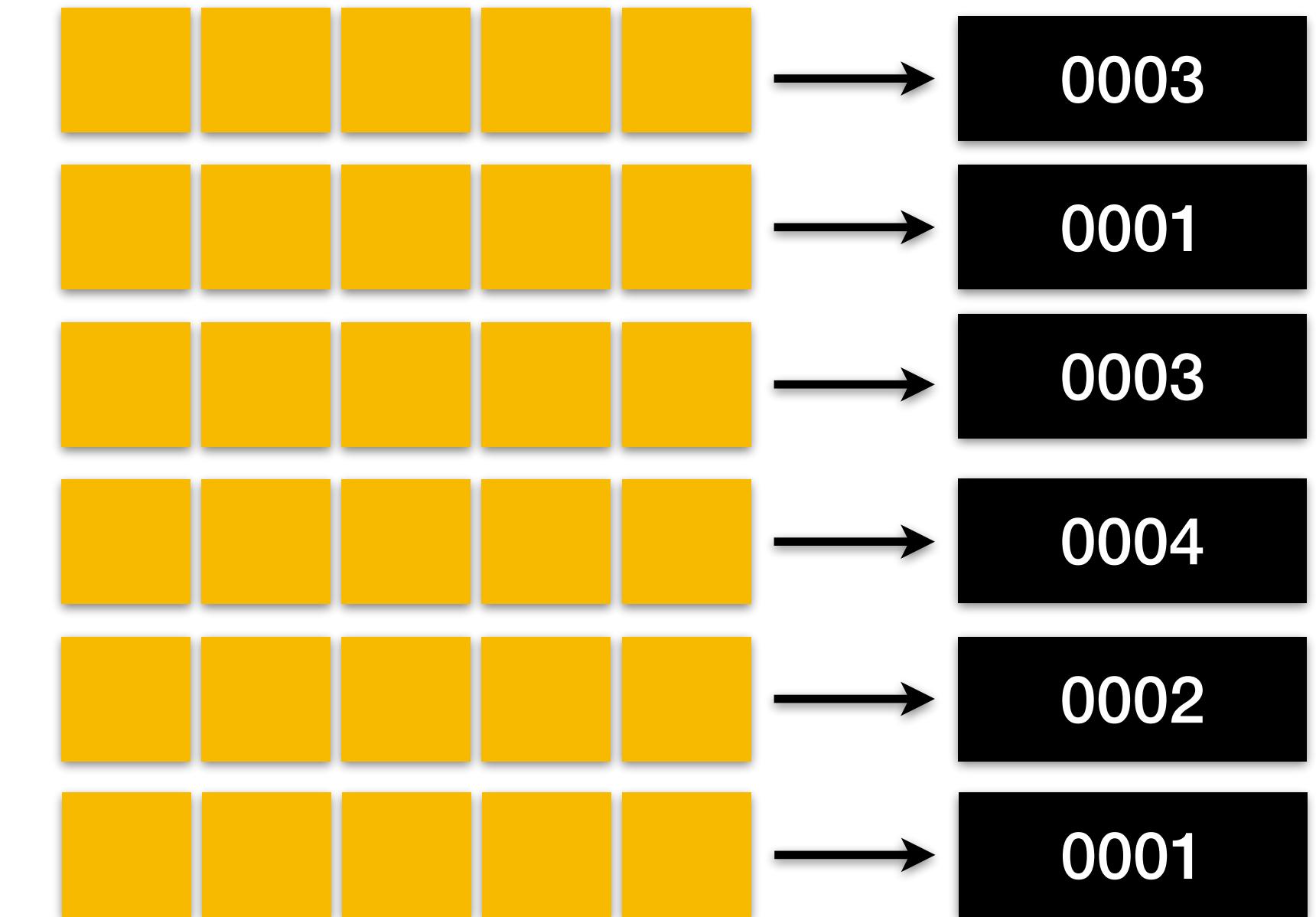
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Face Identification



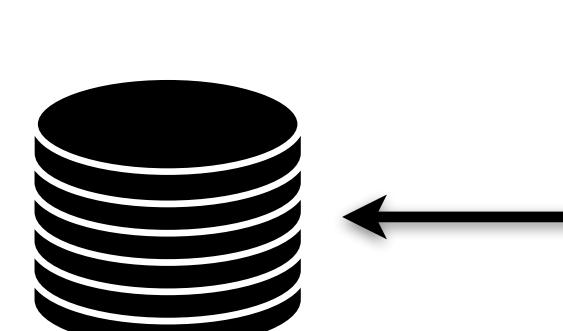
512D ArcFace embedding

Inverted Index



Feature space

Person's IDs

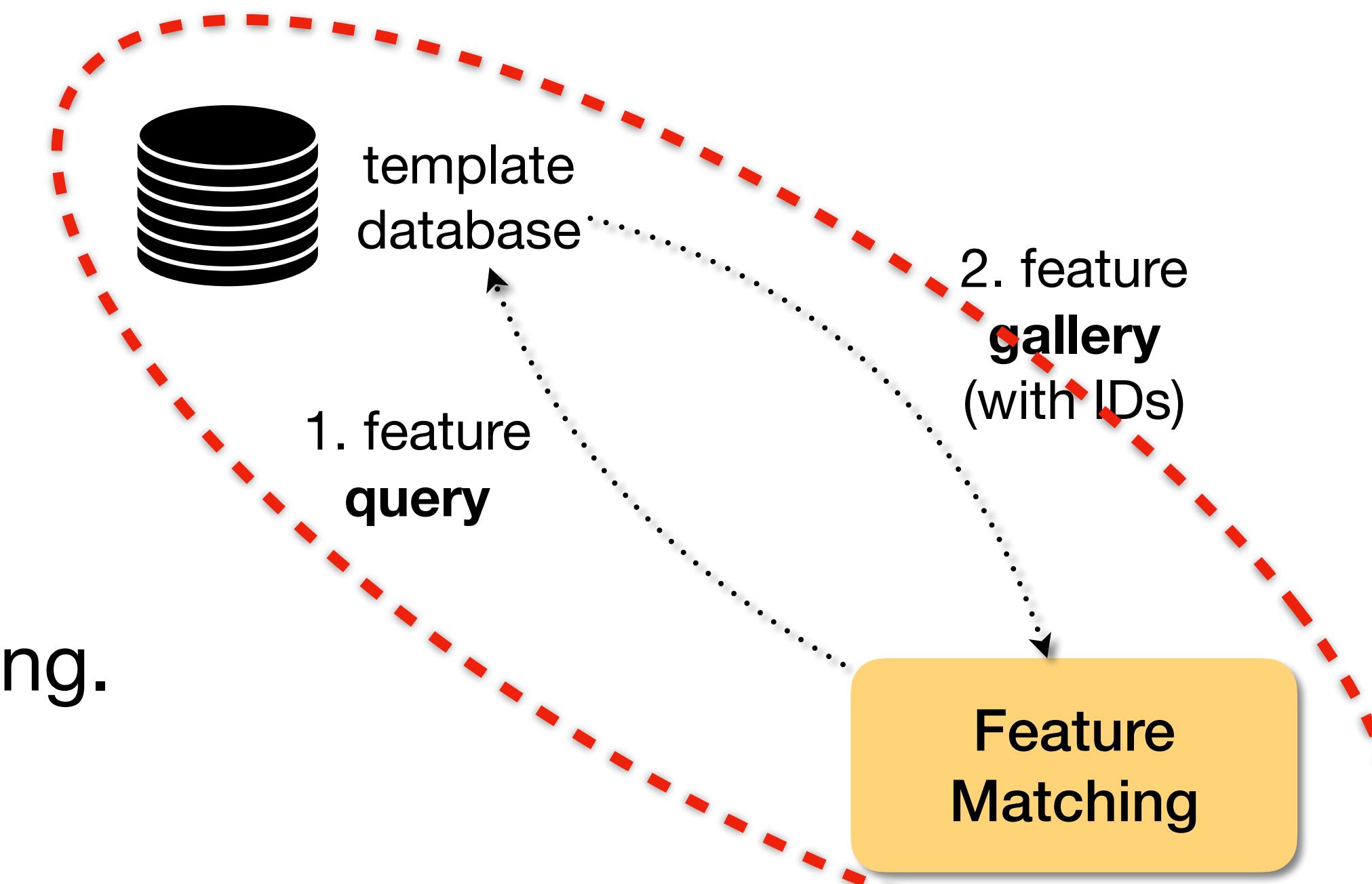


# Feature Indexing

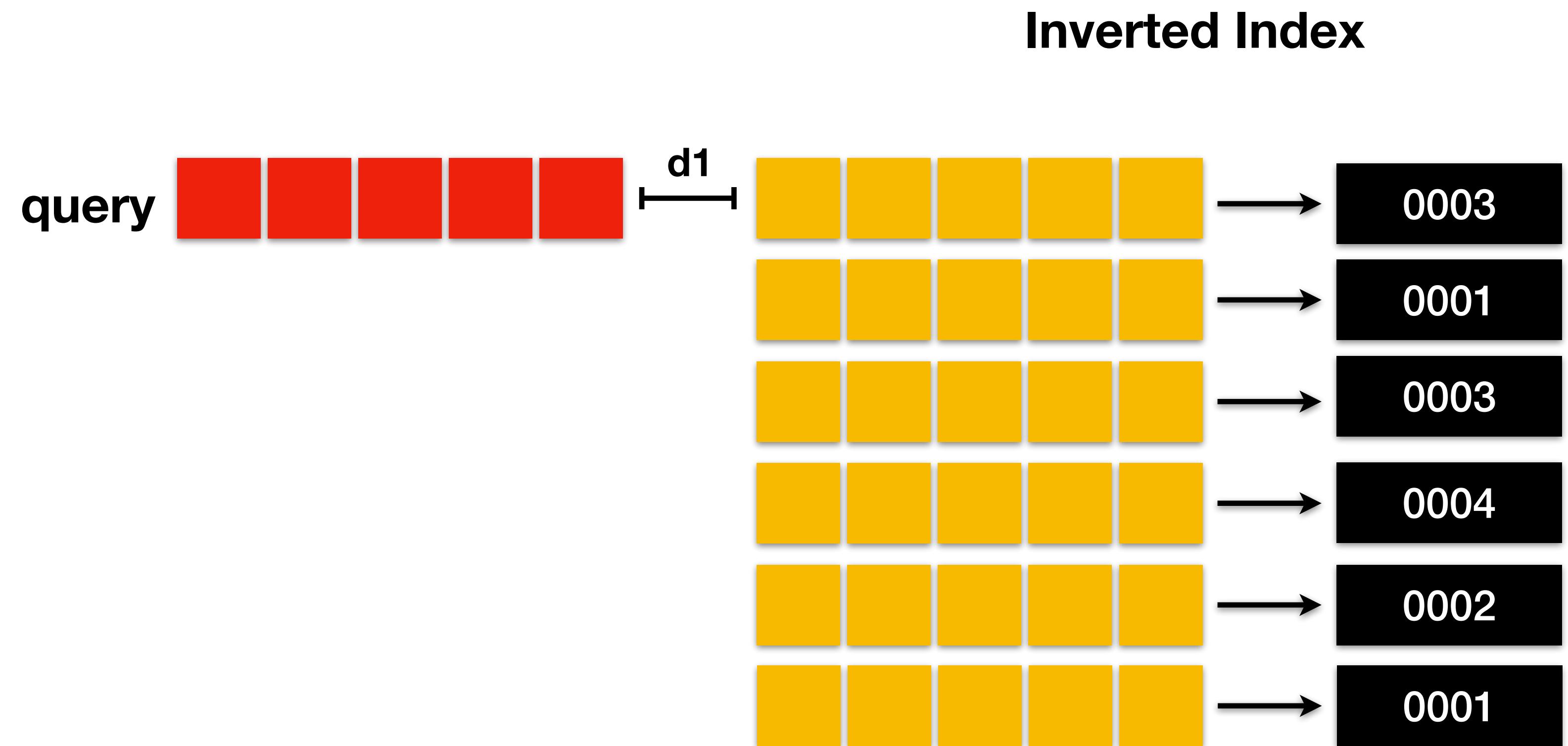
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Need for more complex indexing.

Retrieval of features as quick as possible.



# Brute Force Search

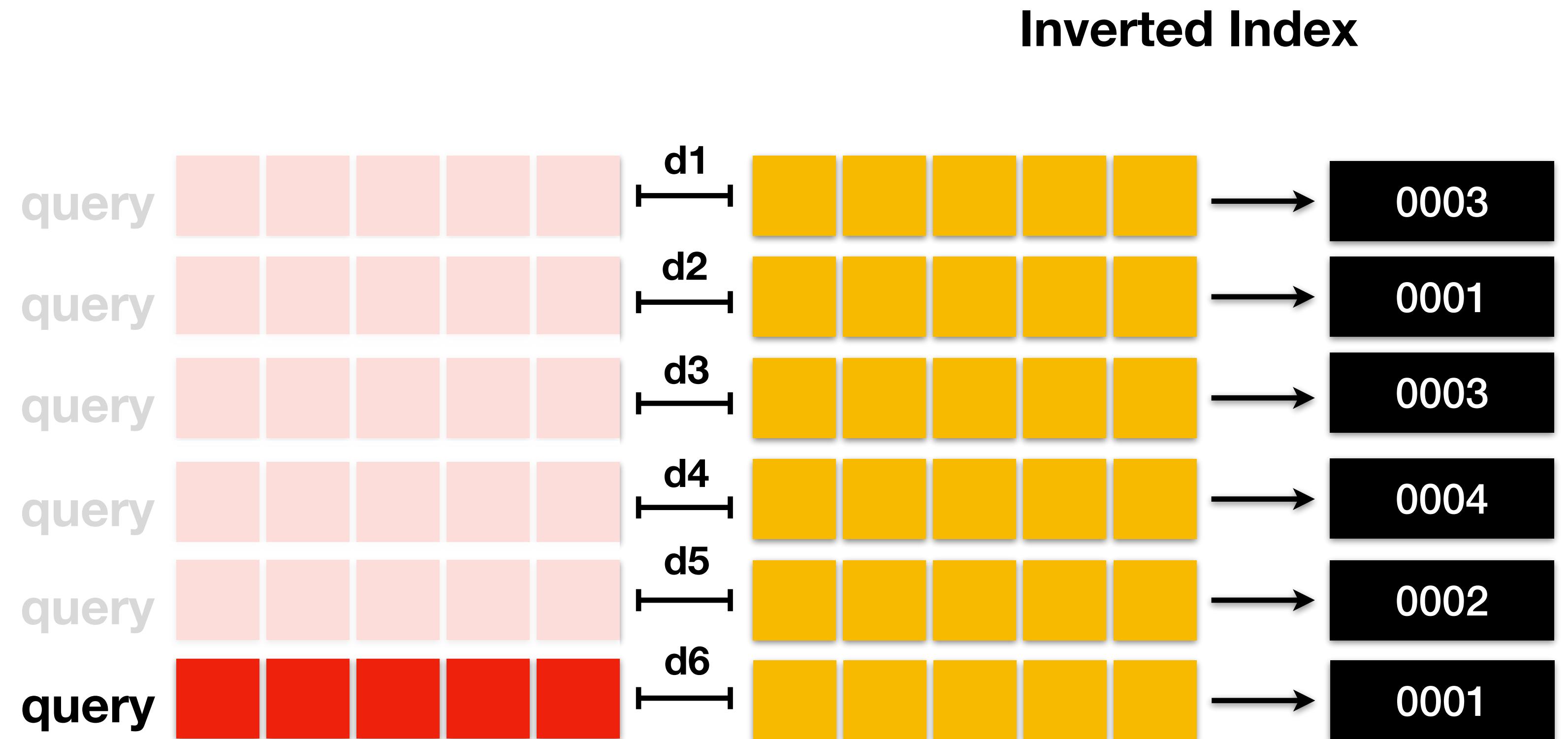


# Brute Force Search

What is the computational complexity?

Linear:  $O(n)$ , where  $n$  is the number of features.

How to reduce it?



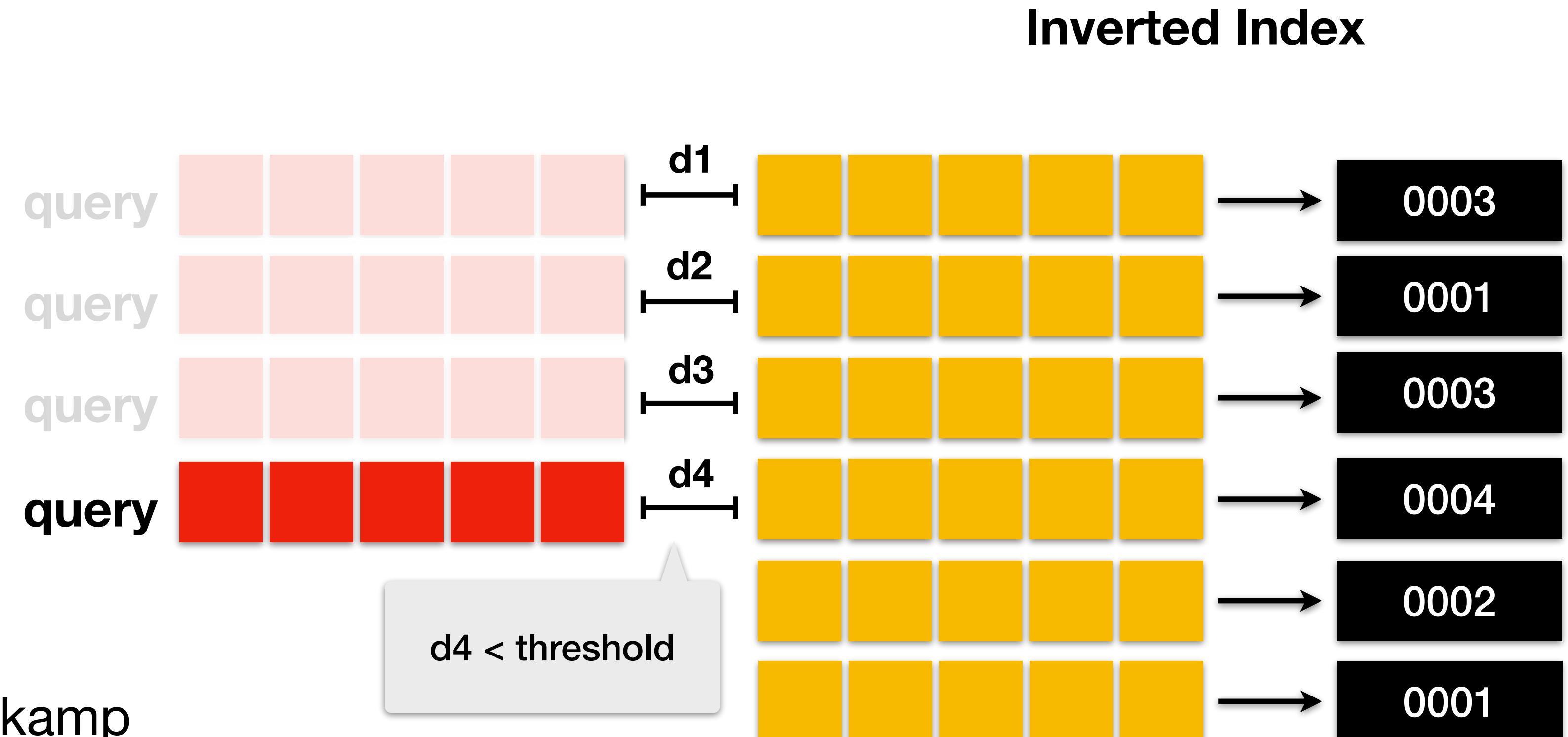
# Early Stop Search

How to reduce complexity?

Stop when you find a feature that is close enough.



Dr. Andrey Kuehlkamp mentioned this for iris identification.

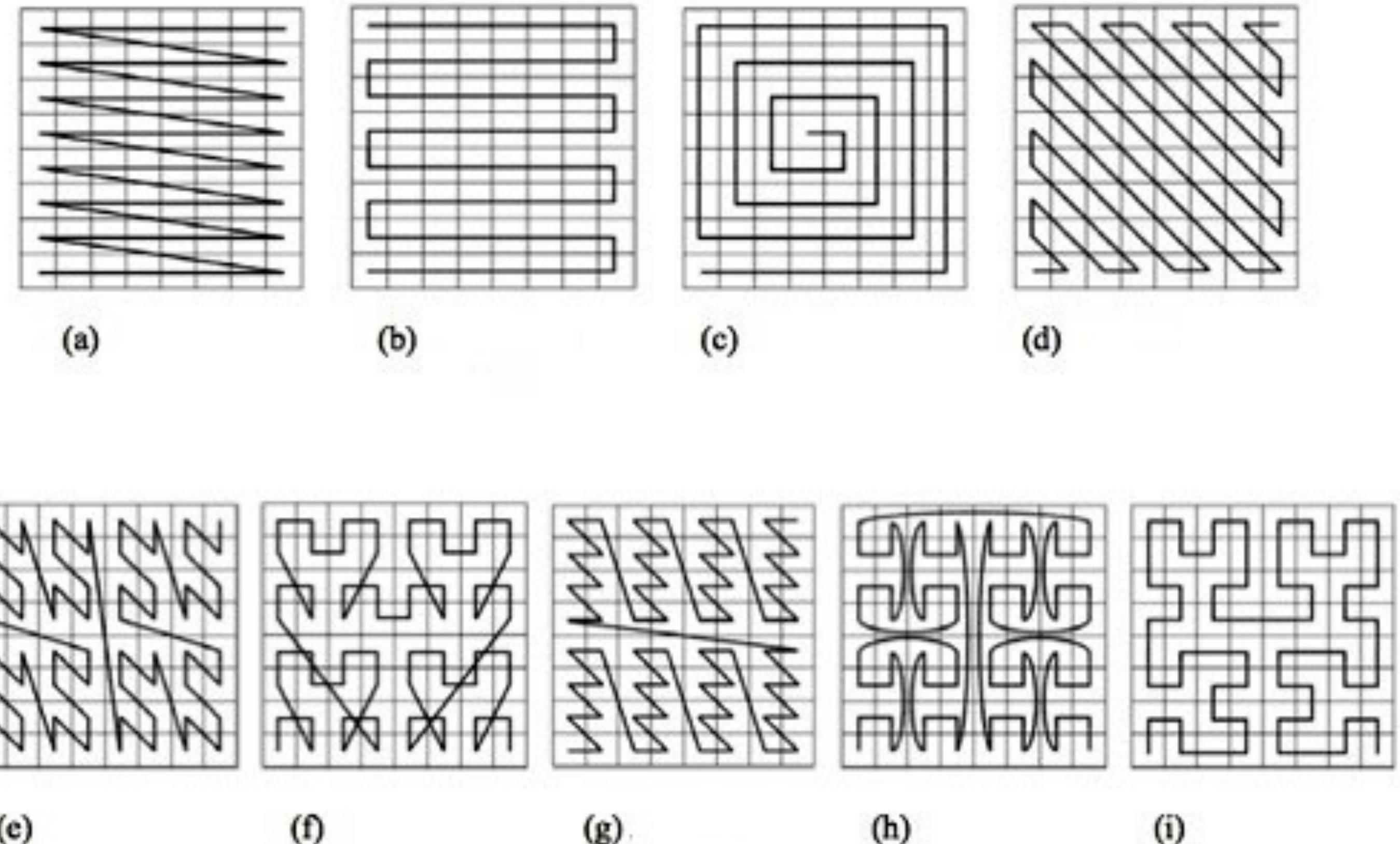


# Space Filling Curves

How to reduce complexity?

Curves determined by index mapping functions that pass once through every point of an  $N$ -dimensional space.

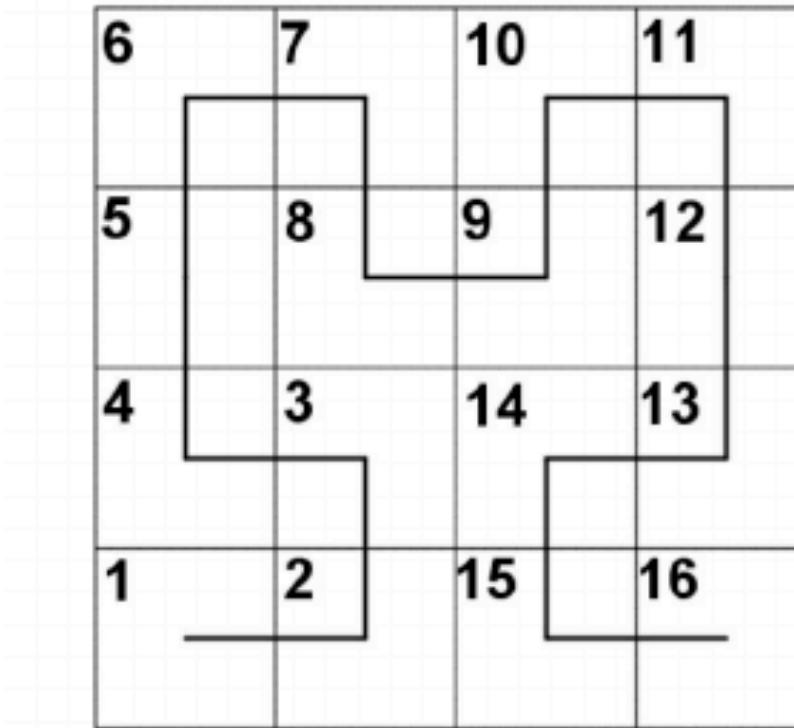
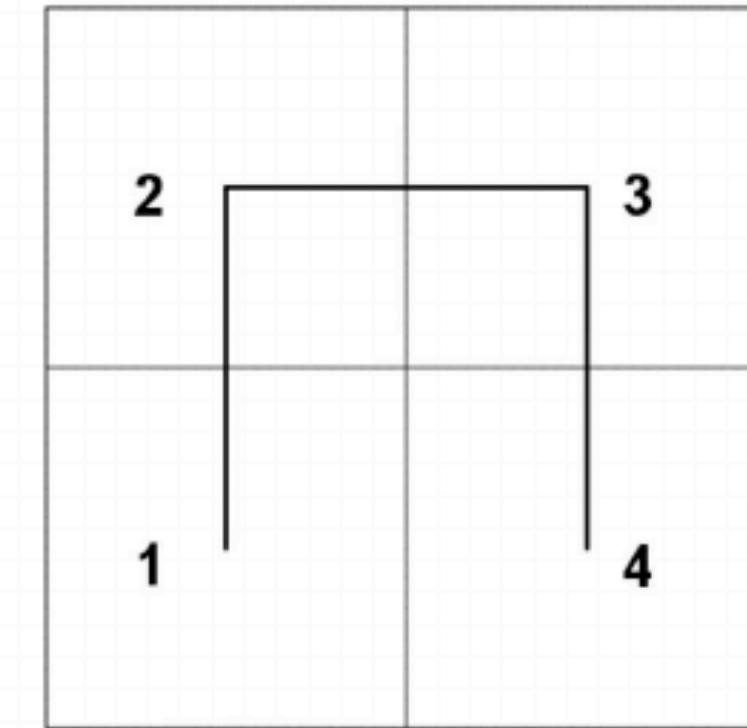
2D space examples



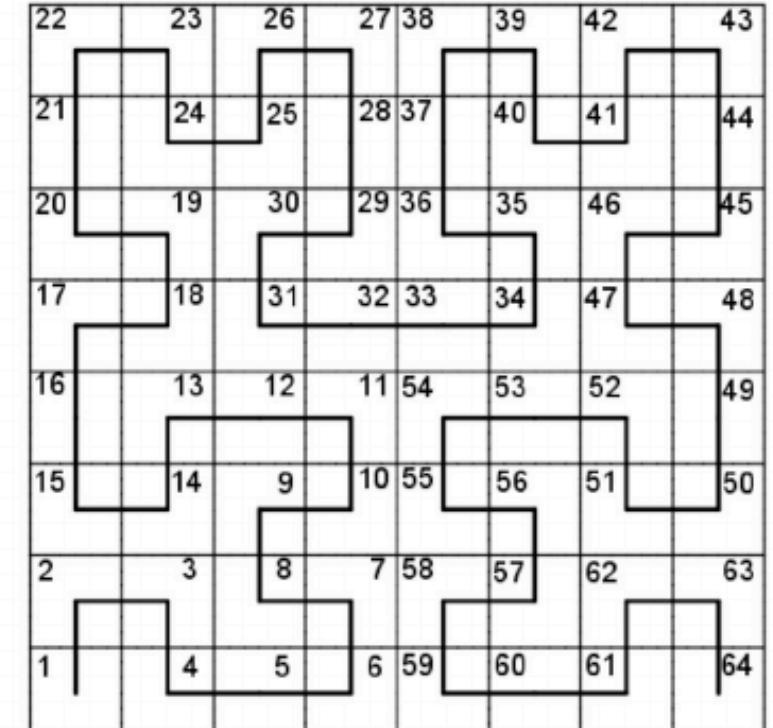
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2D space examples



Hilbert curves

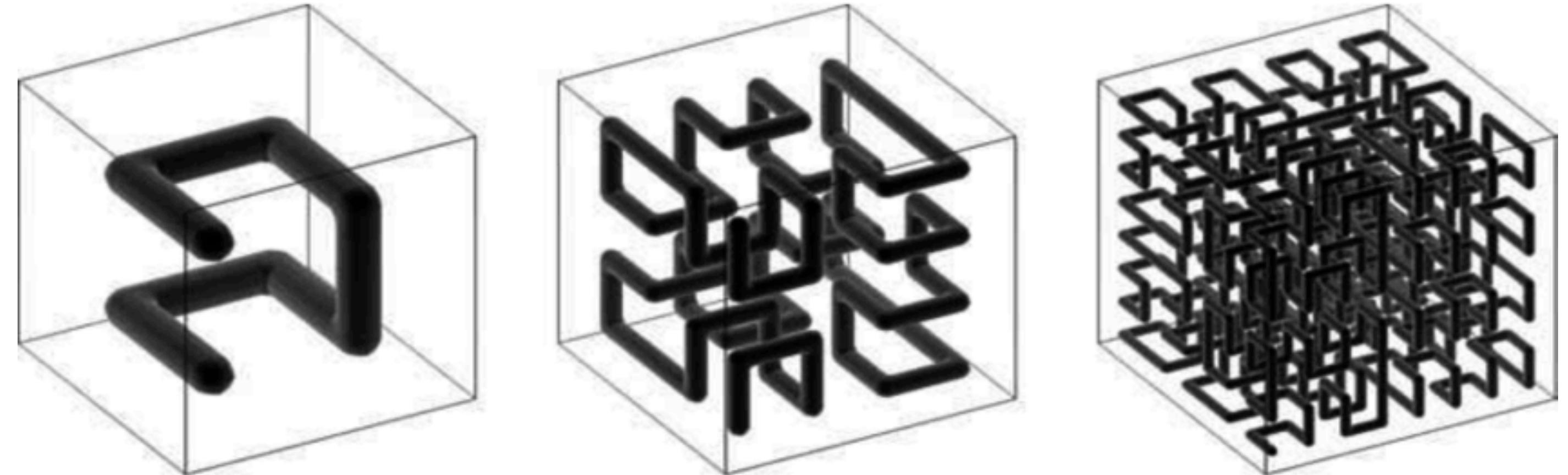
# Space Filling Curves

How to reduce complexity?

Curves determined by index mapping functions that pass once through every point of an  $N$ -dimensional space.

The mapping functions are executed in constant time, w.r.t. the number of features.

3D space examples



Hilbert curves

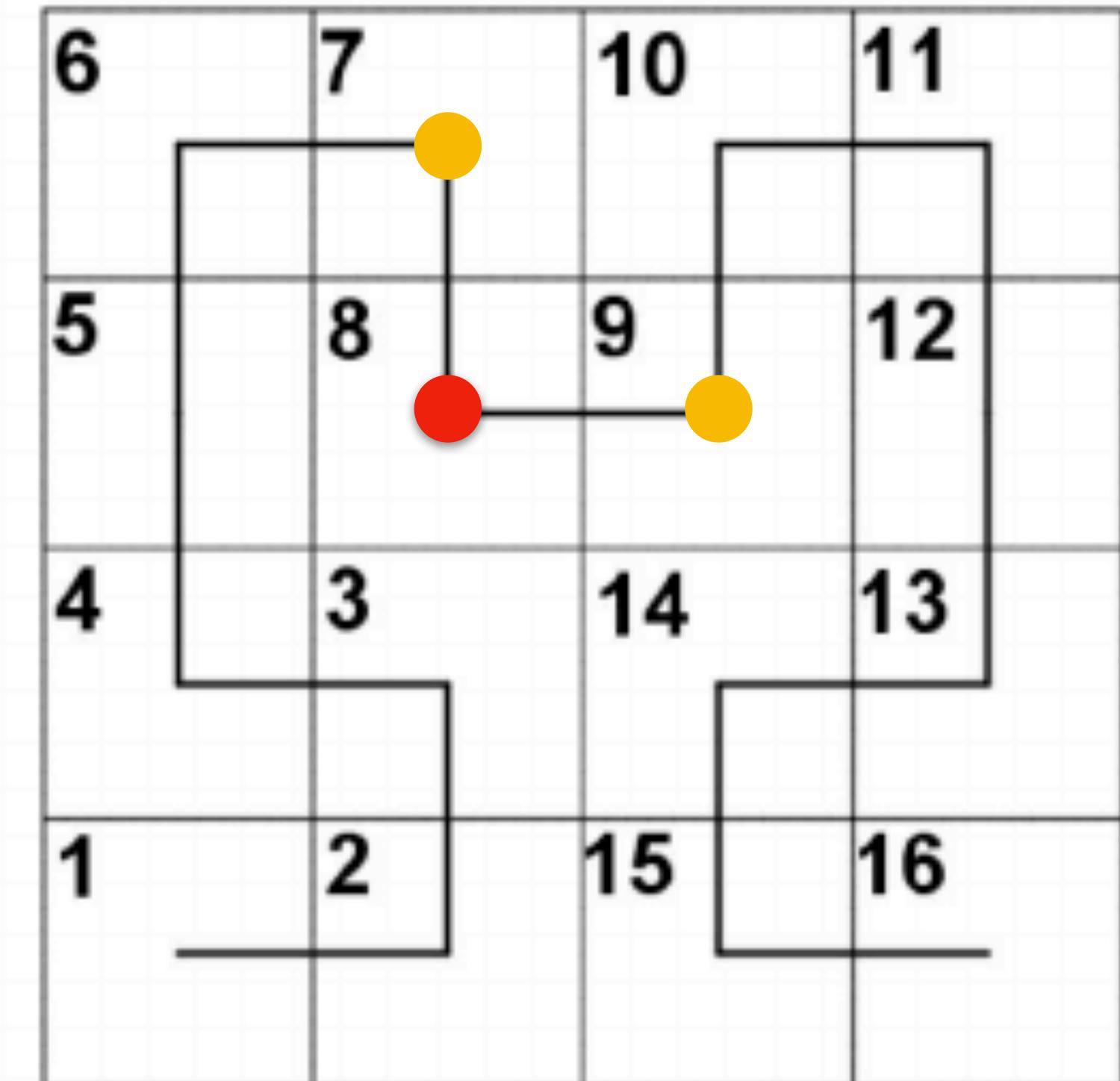
# Space Filling Curves

How to reduce complexity?

The curves are 1D and the elements indexed by them are “sorted” in an *approximation* of their distances in the original space.

If the curve is used as a binary tree, an approximation of the  $k$ -nearest elements can be obtained in  $O(\log(n))$ , where  $n$  is the number of features.

Example:  
2-nearest elements



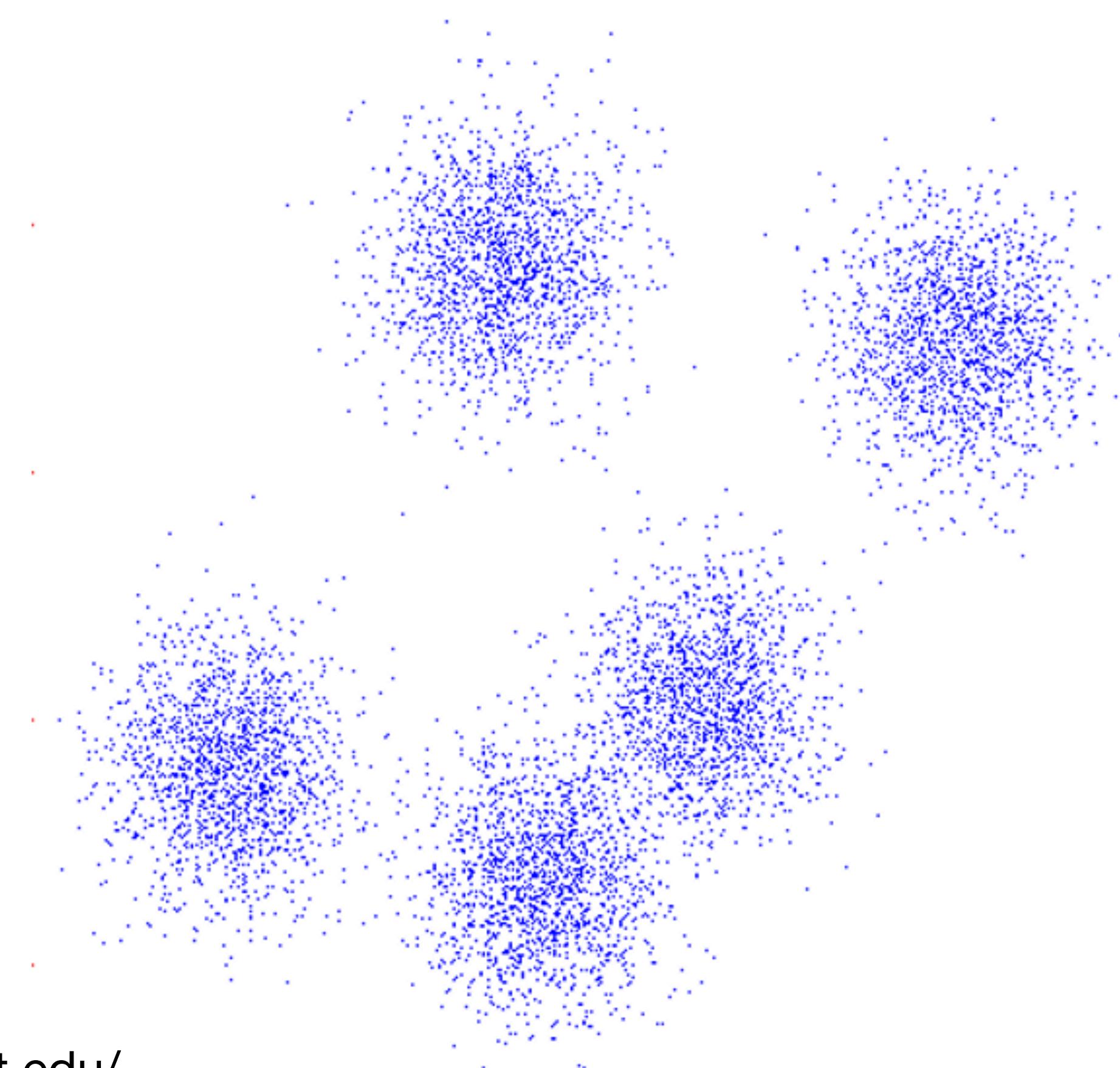
# Clustering

How to reduce complexity?

Cluster the features and limit the k-nearest search to one or a couple of clusters.

There will be less elements to consider

Source: <https://people.csail.mit.edu/dsontag/courses/ml12/slides/lecture14.pdf>



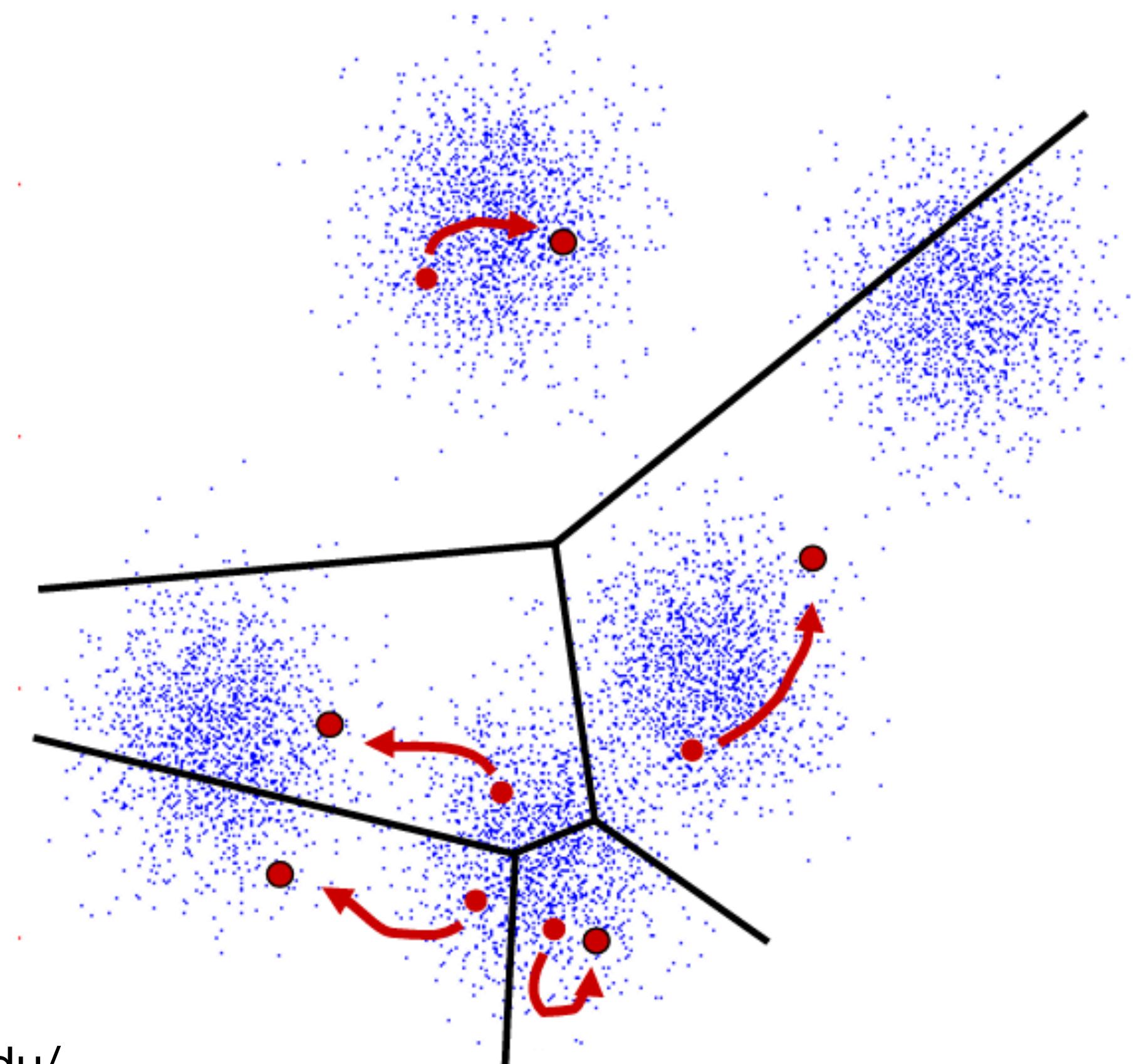
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## K-Means

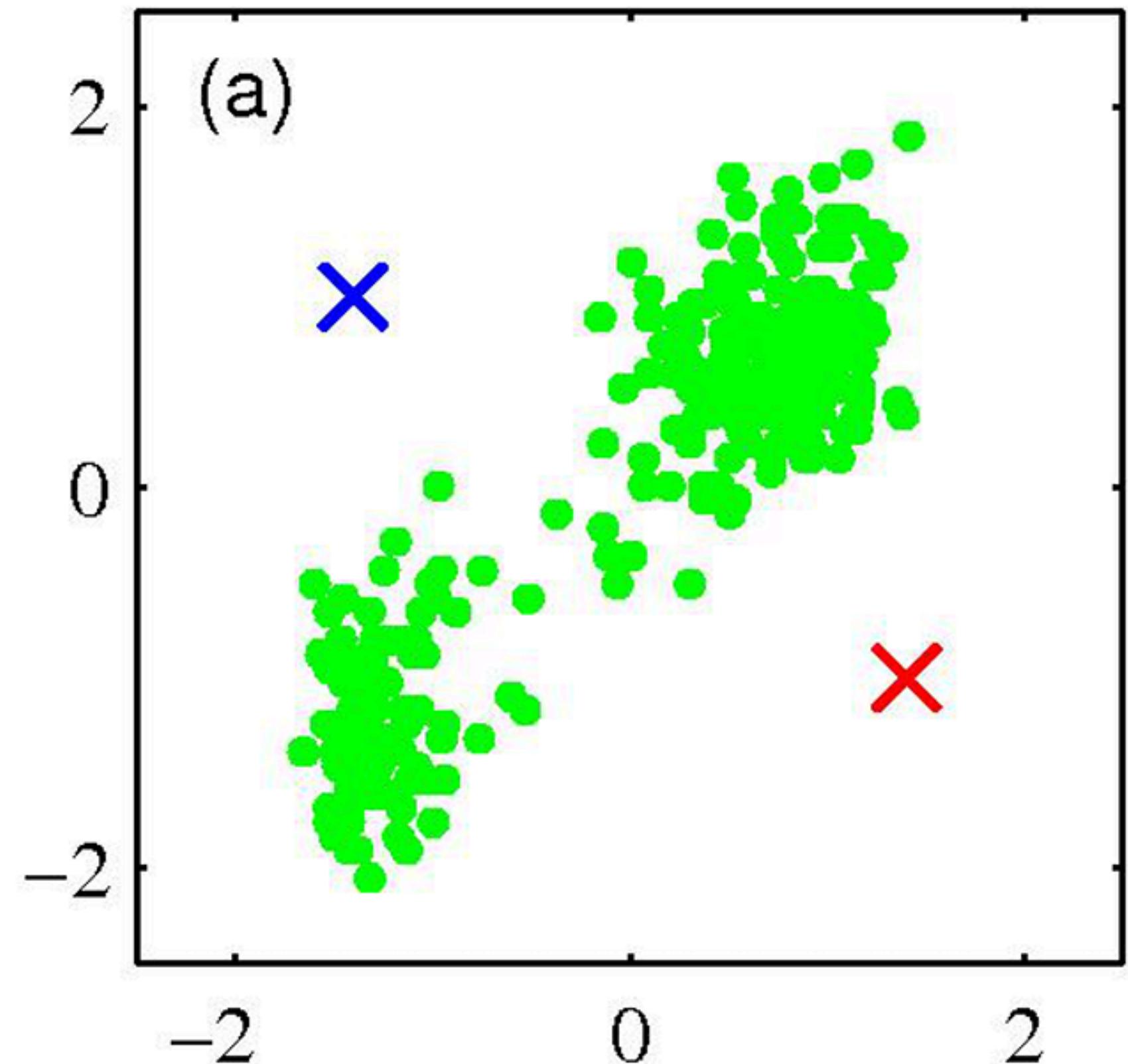


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# Clustering

## K-Means

Select K random features as cluster centers.

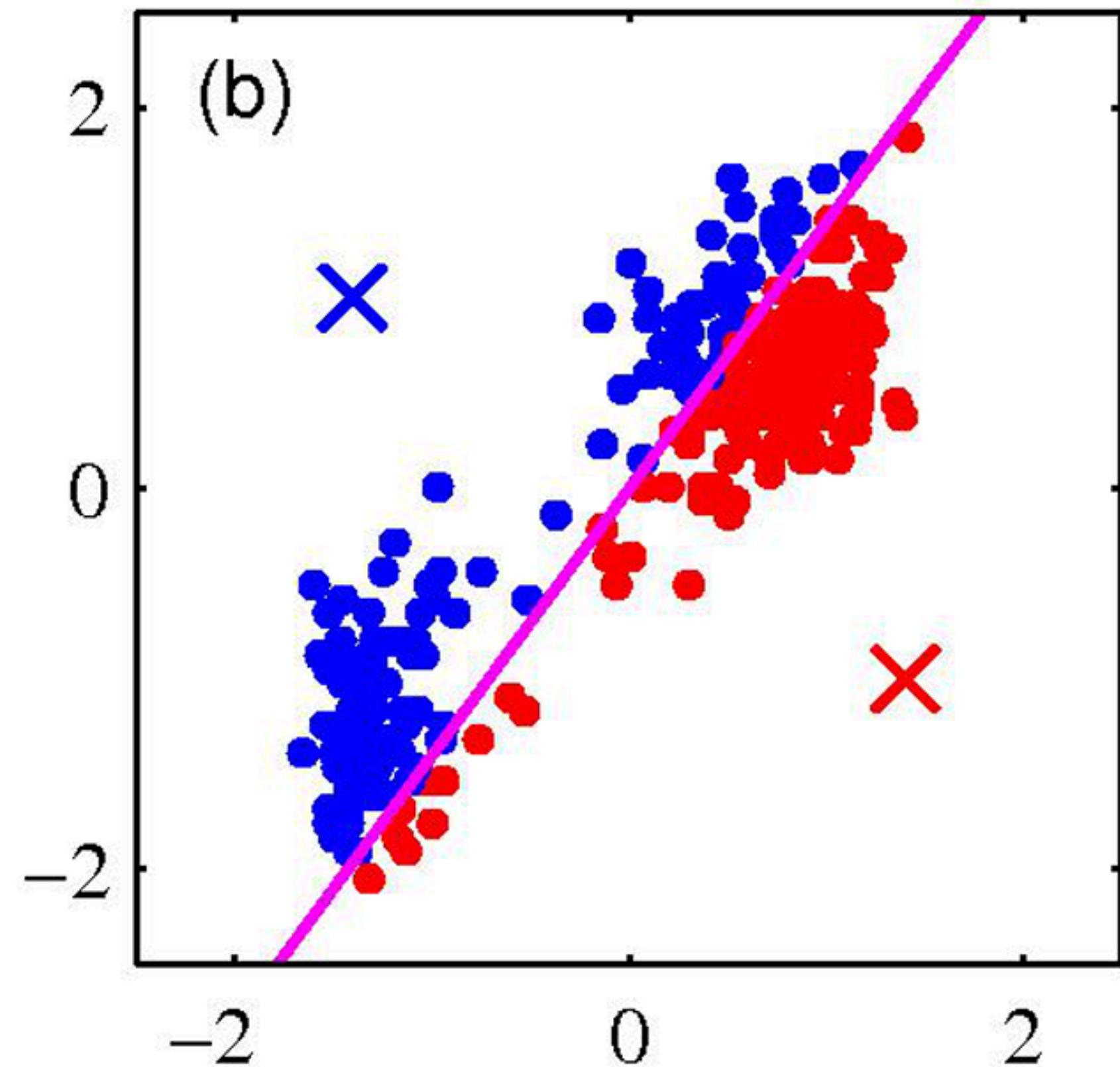


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# Clustering

## K-Means

Assign features to closes cluster centers.

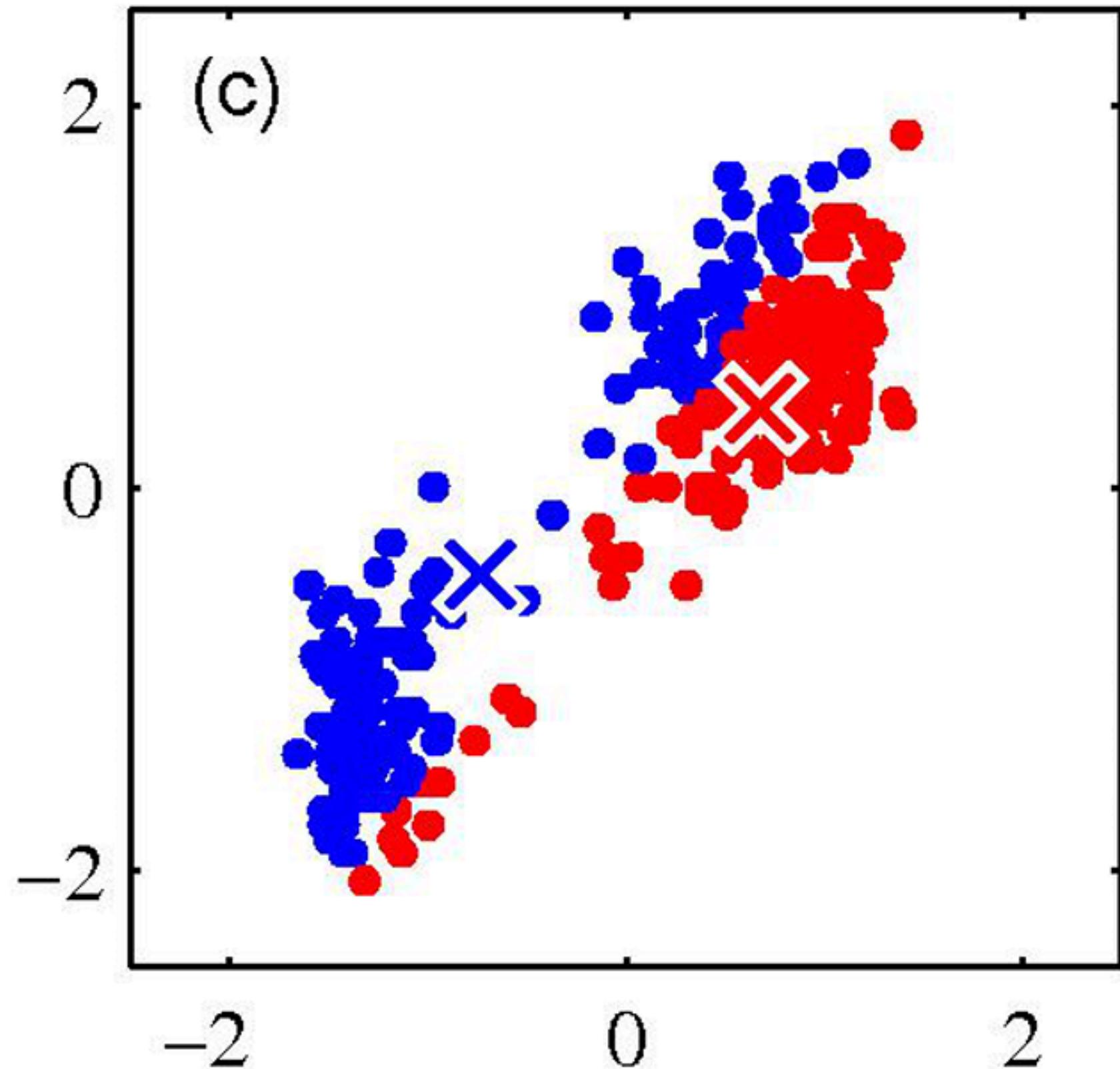


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# Clustering

## K-Means

Update the cluster centers by taking the **means** of each cluster.

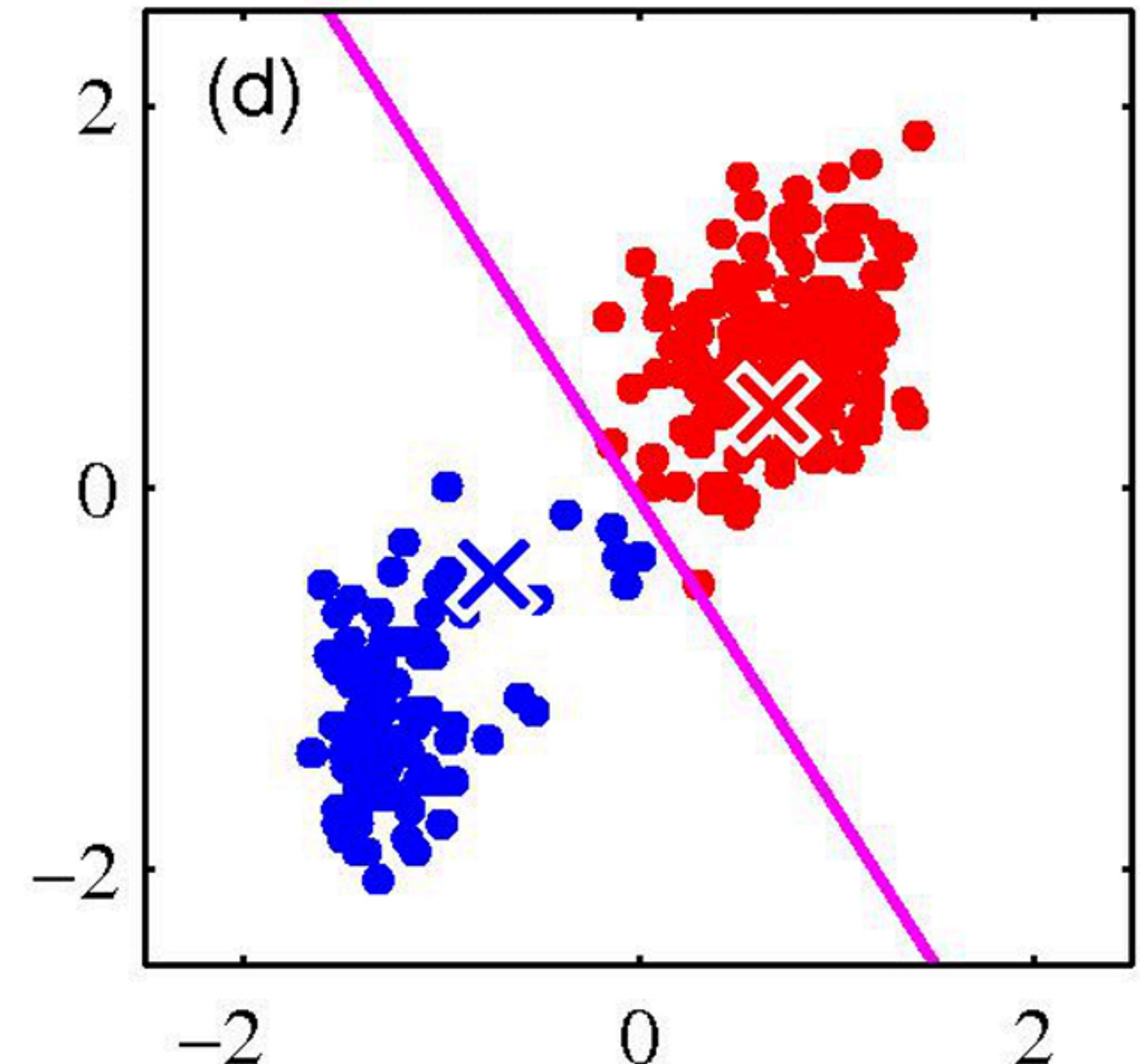


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# Clustering

K-Means

Repeat until convergence.



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# Clustering

## K-Means

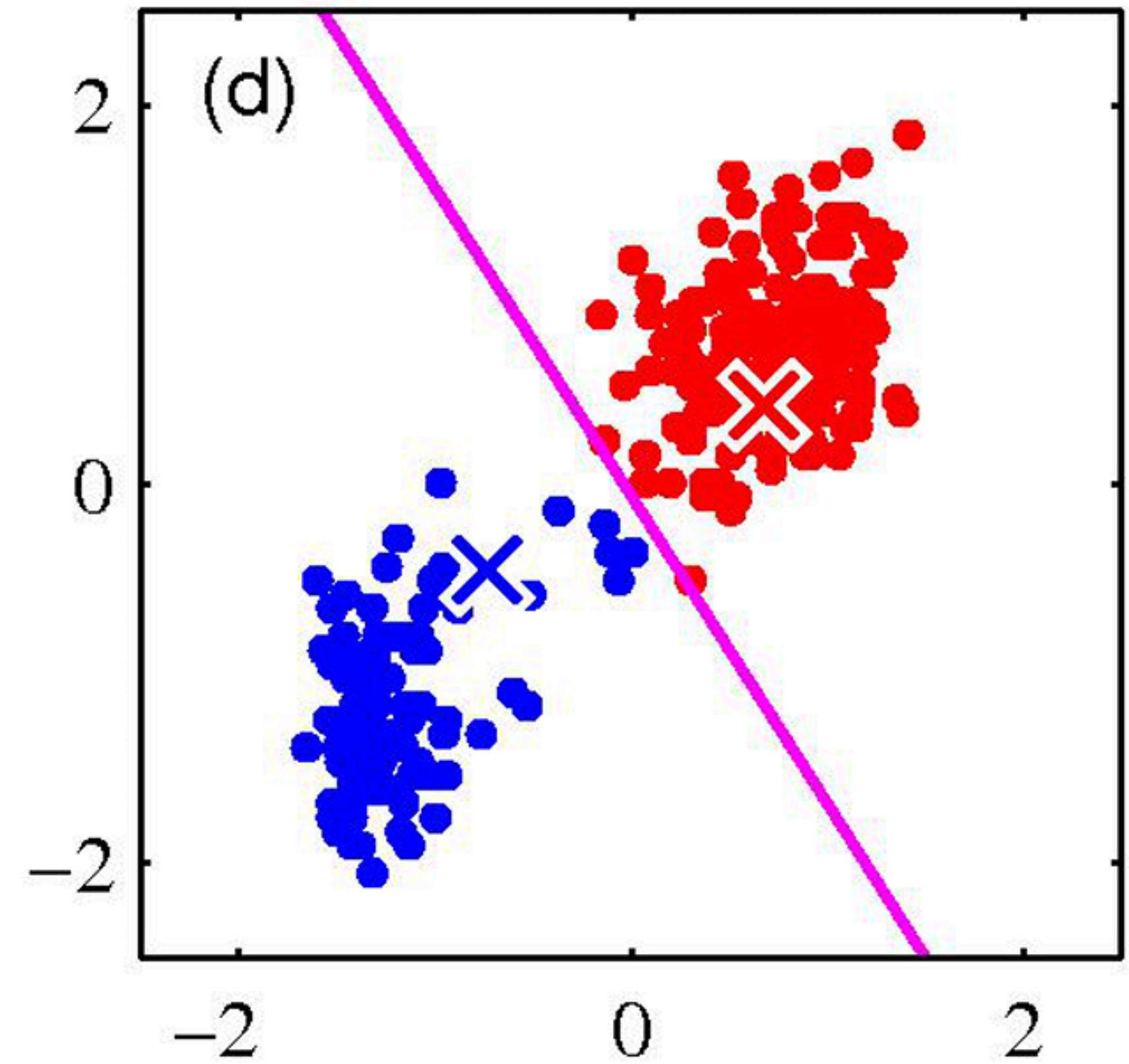
What are the limitations of this approach?

What is the ideal number of clusters?

Complexity of building clusters:  
 $O(Kn)$  in each step until convergence.

K: #clusters  
n: #features

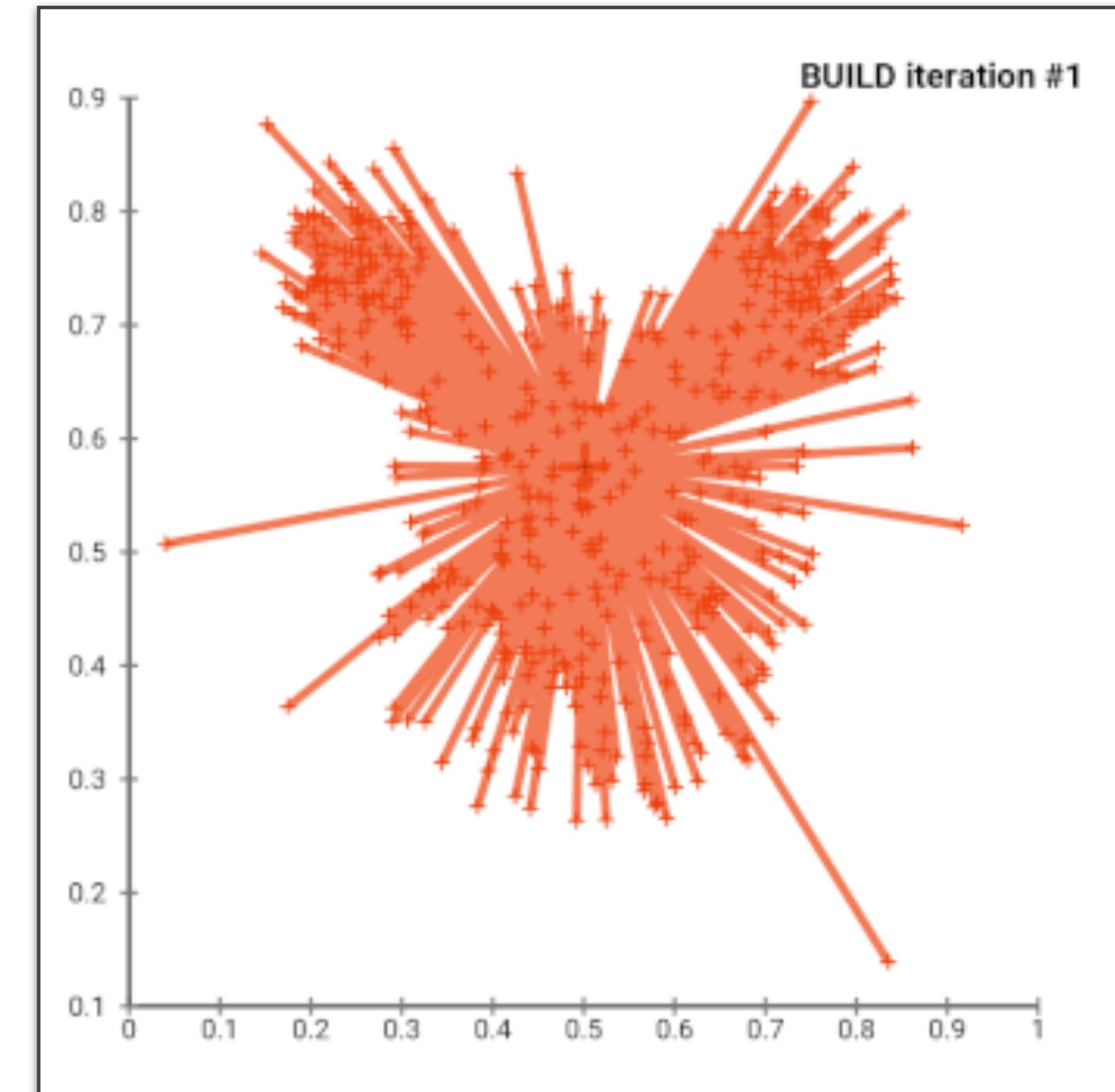
Clustering is *offline*: i.e., it does not happen at feature querying time.



# Clustering

Variation: K-medoids

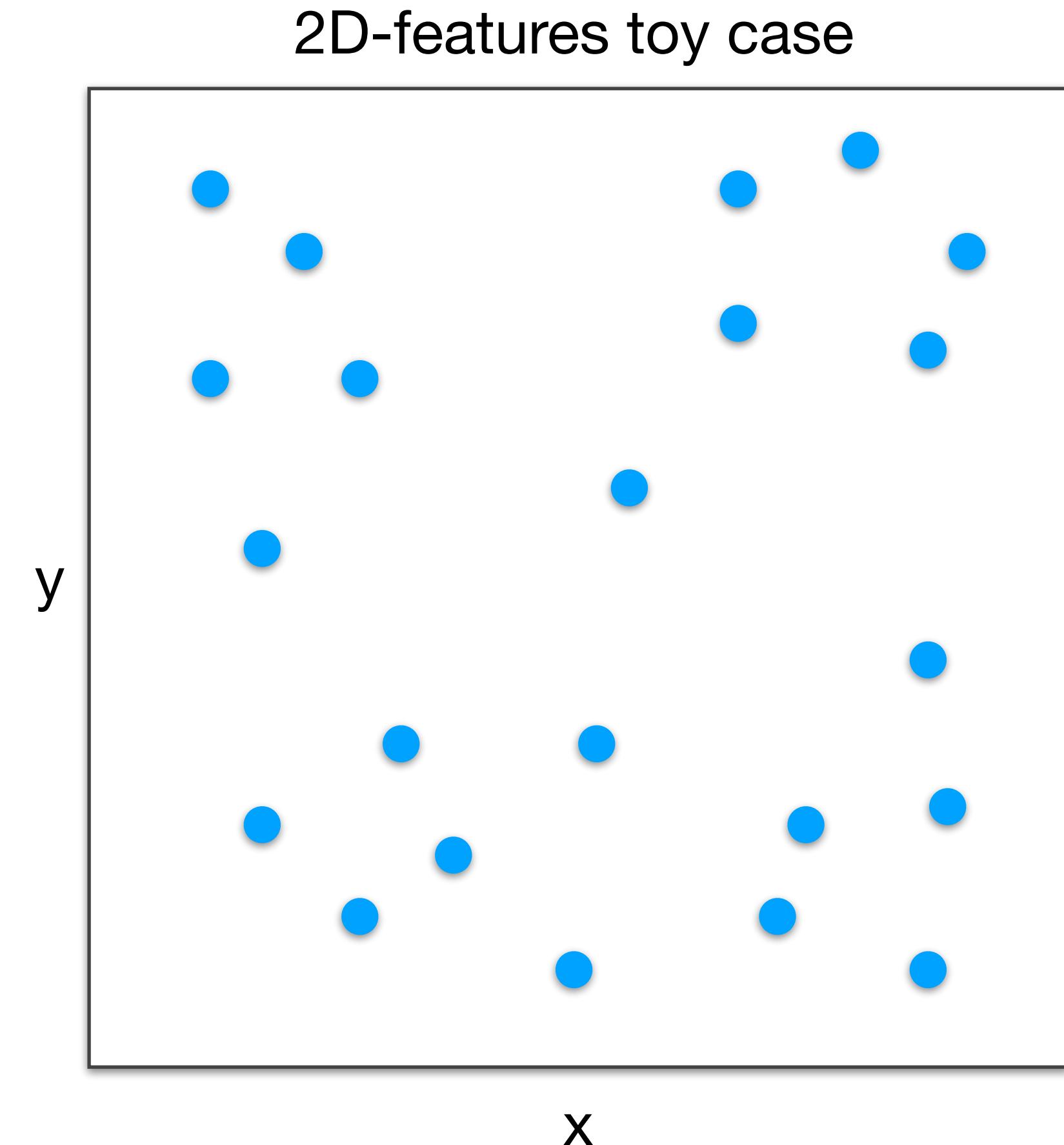
Instead of using *means* as the cluster centers, use *medians*, which are actual existing features.



# KD Trees

How to reduce complexity?

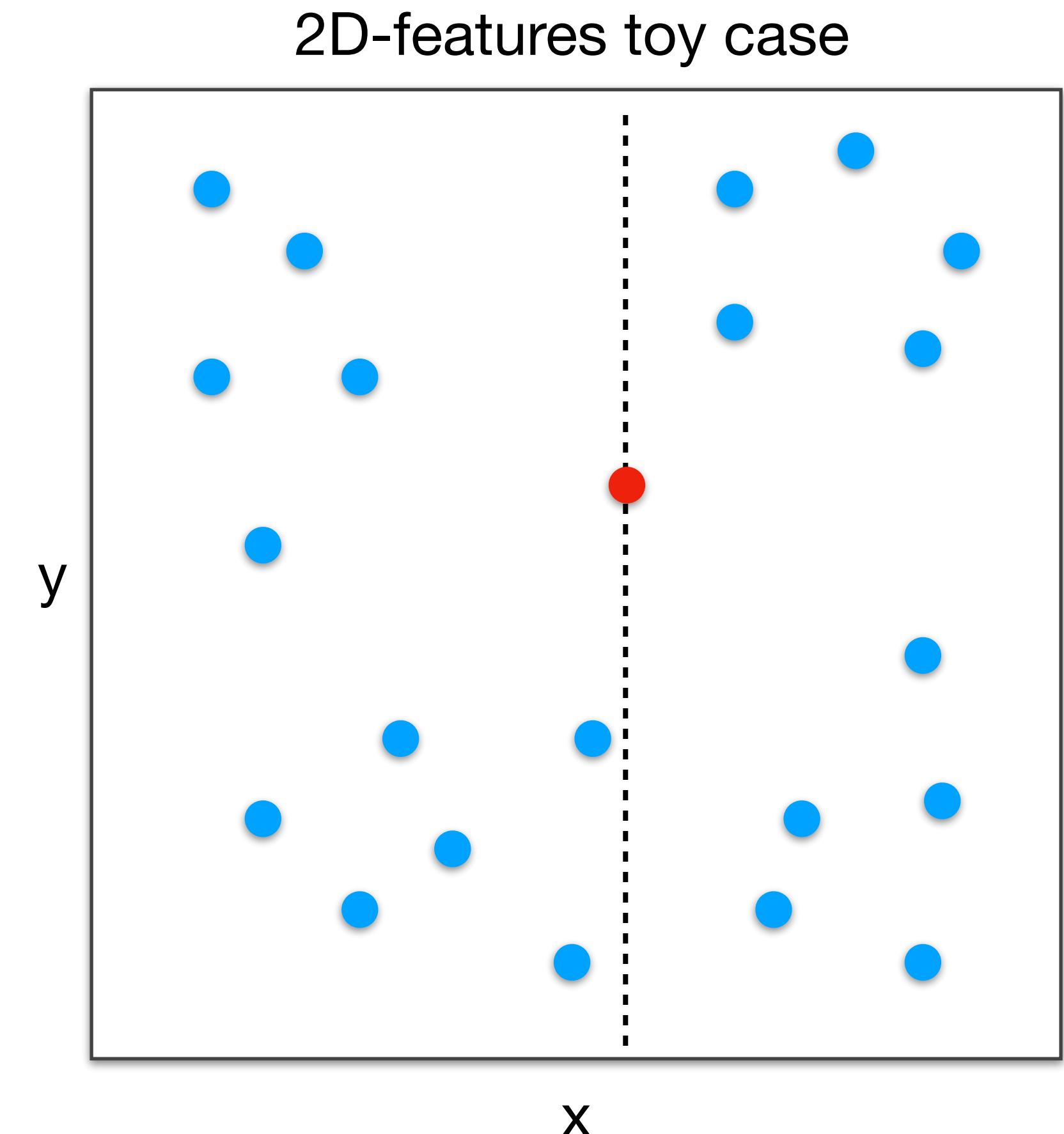
K-dimensional trees:  
*For K times*  
*Split one feature dimension into two halves.*



# KD Trees

How to reduce complexity?

K-dimensional trees:  
*For K times*  
*Split one feature dimension into two partitions using medians.*

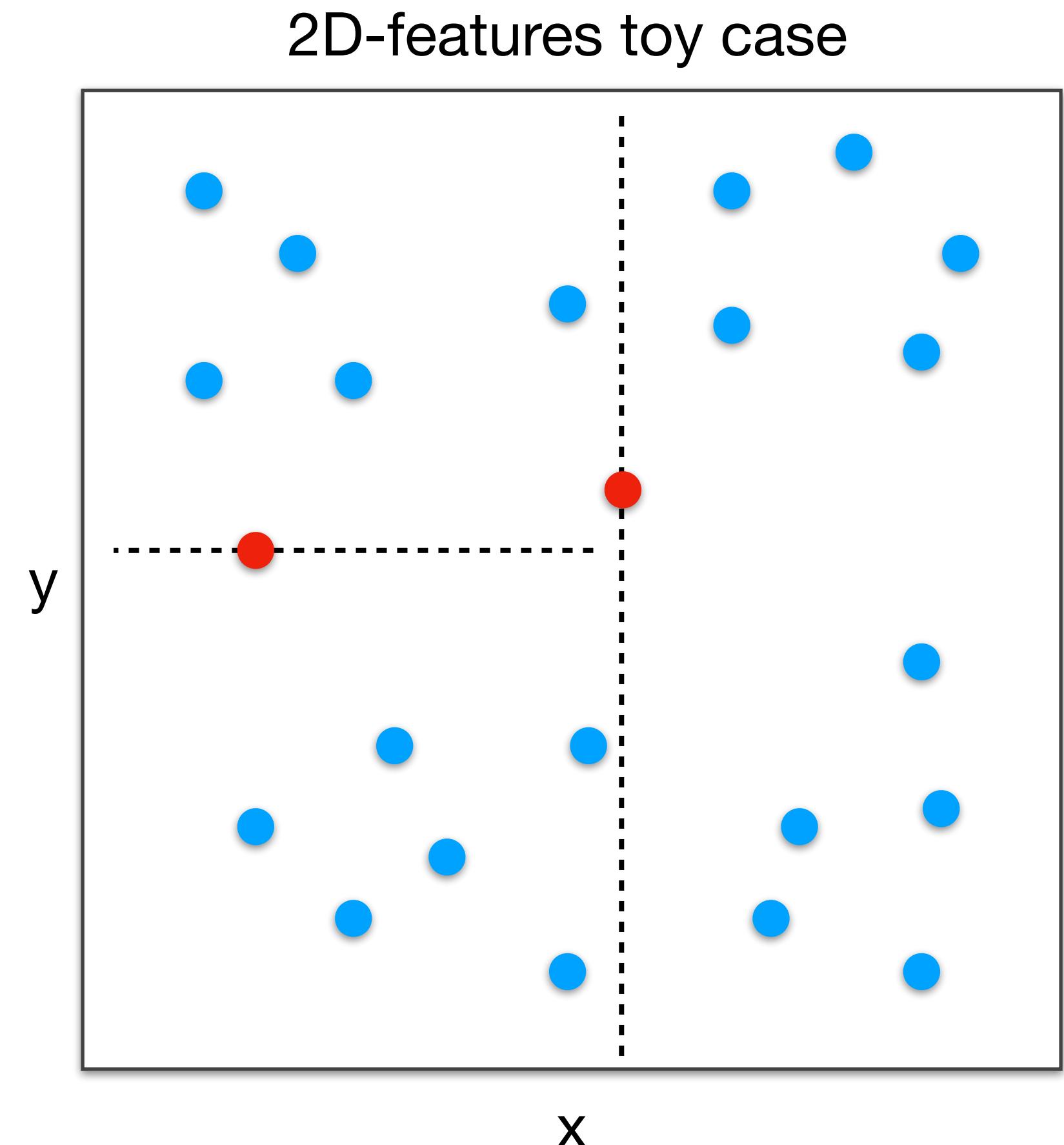


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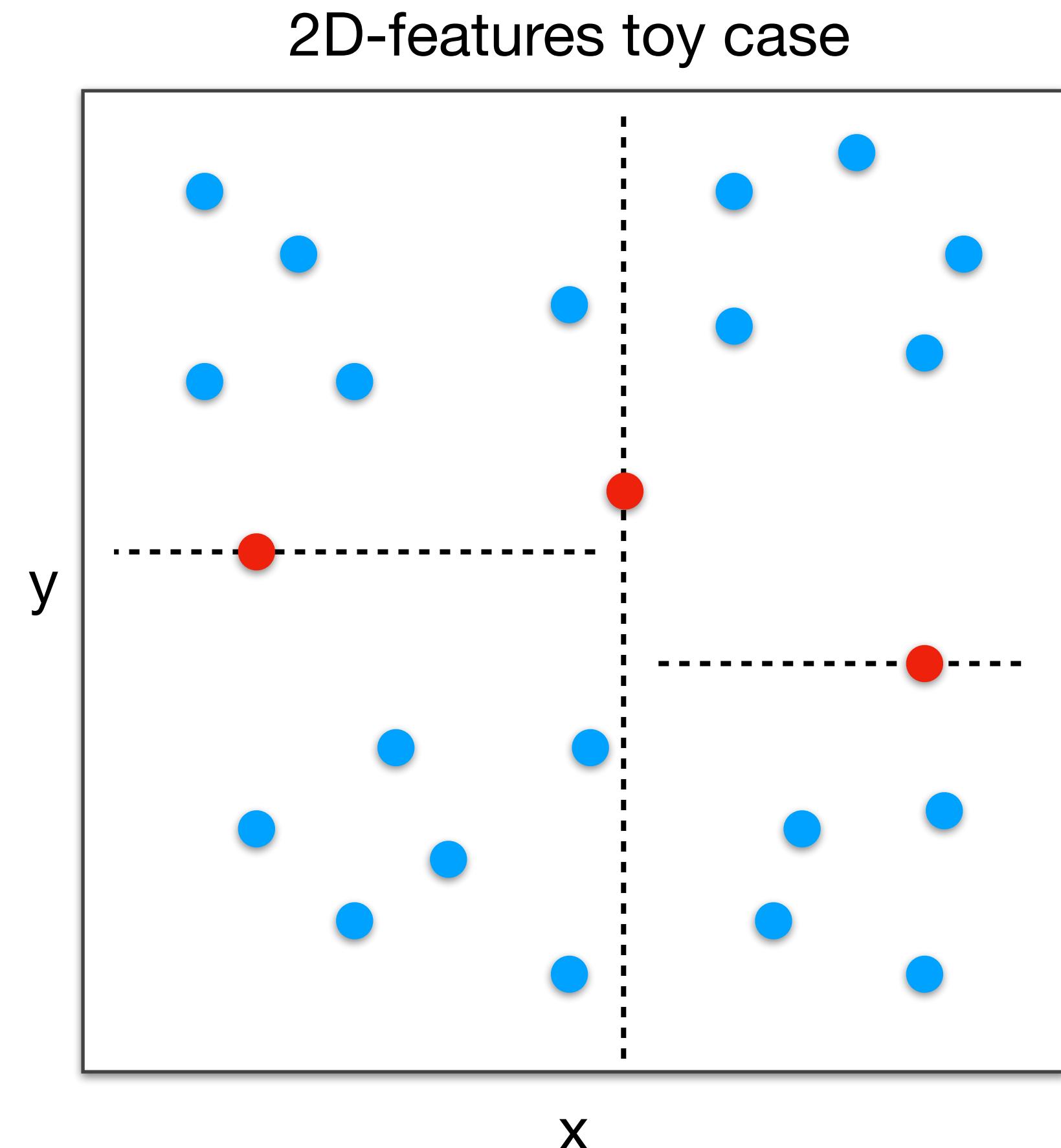


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# KD Trees

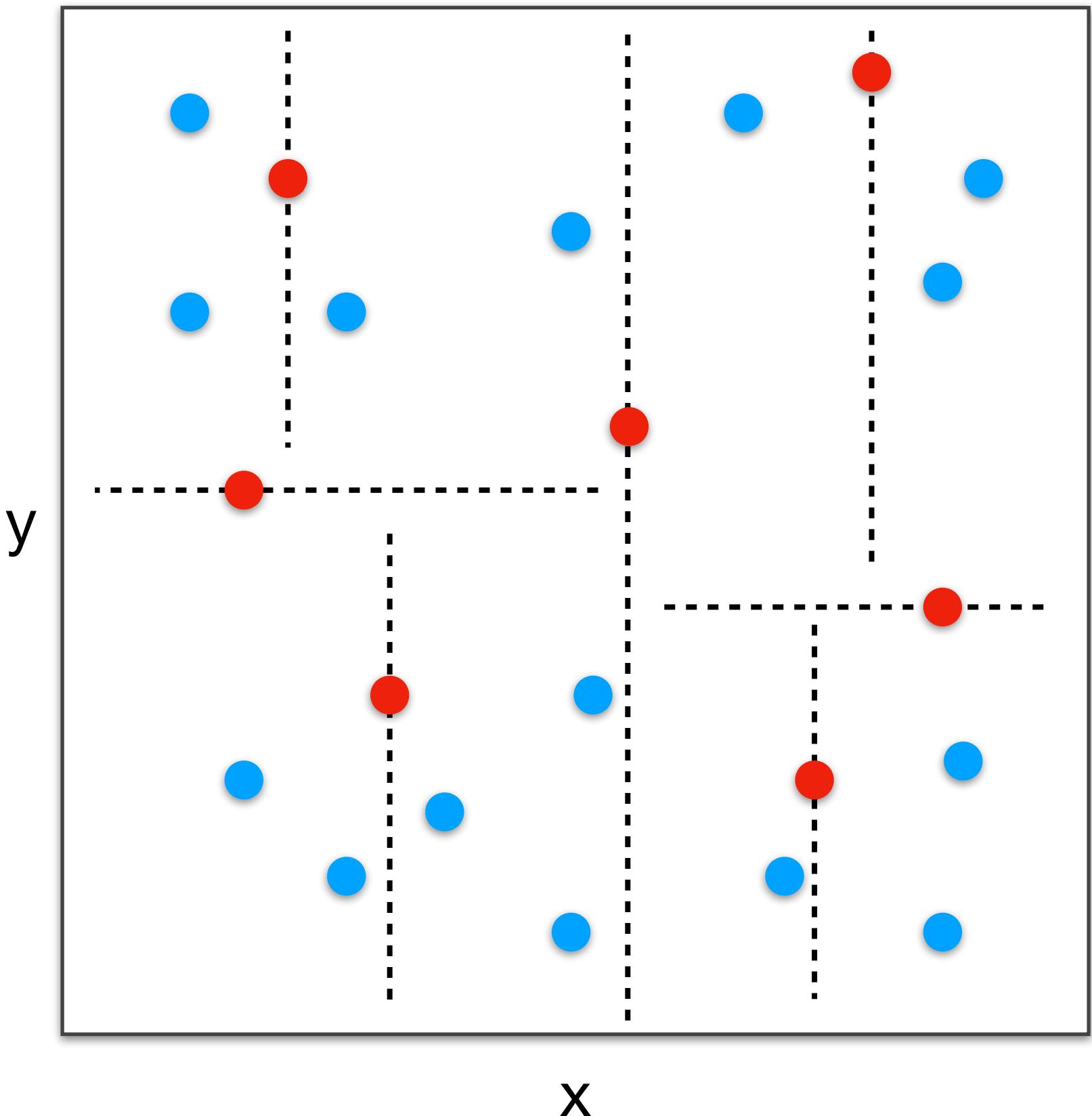
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2D-features toy case



$K = 3$

# KD Trees

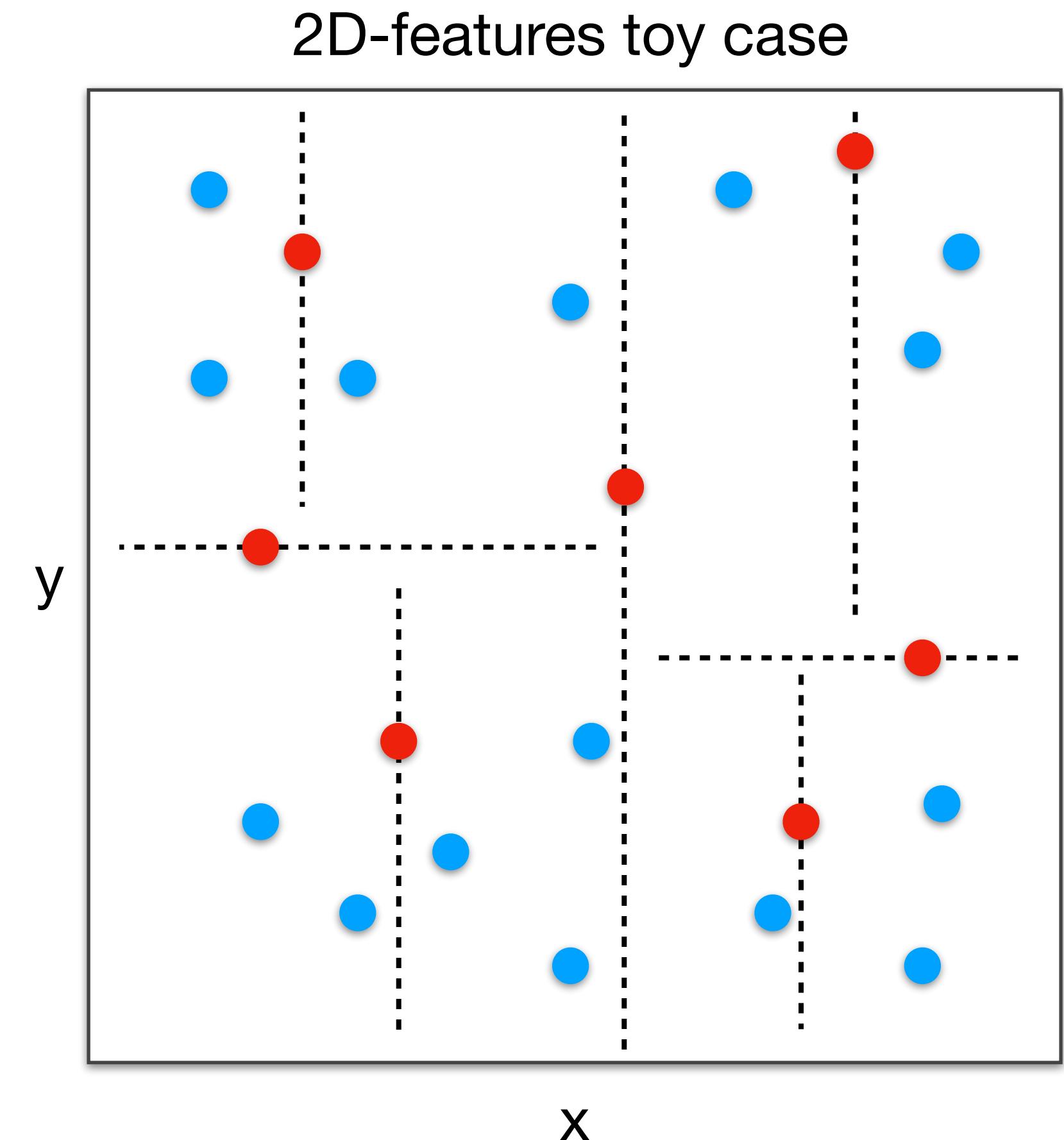
How to reduce complexity?

K-dimensional trees:  
*For K times*

*Split one feature dimension into two partitions using medians.*

Complexity to build:  $O(n \log(n))$

Building is *offline*: i.e., it does not happen at feature querying time.



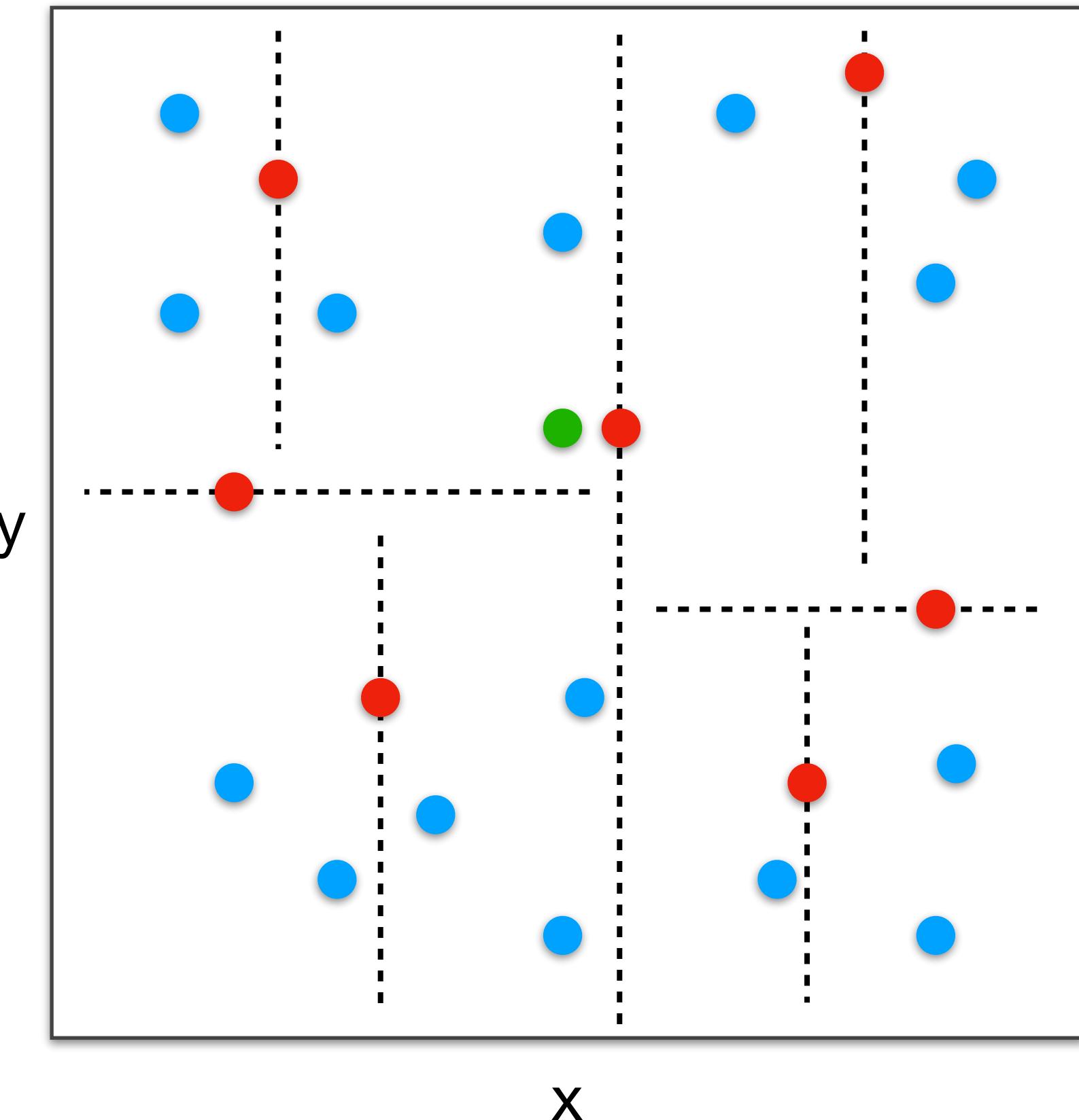
# KD Trees

How to reduce complexity?

How to obtain 3-nearest neighbors?

query

2D-features toy case



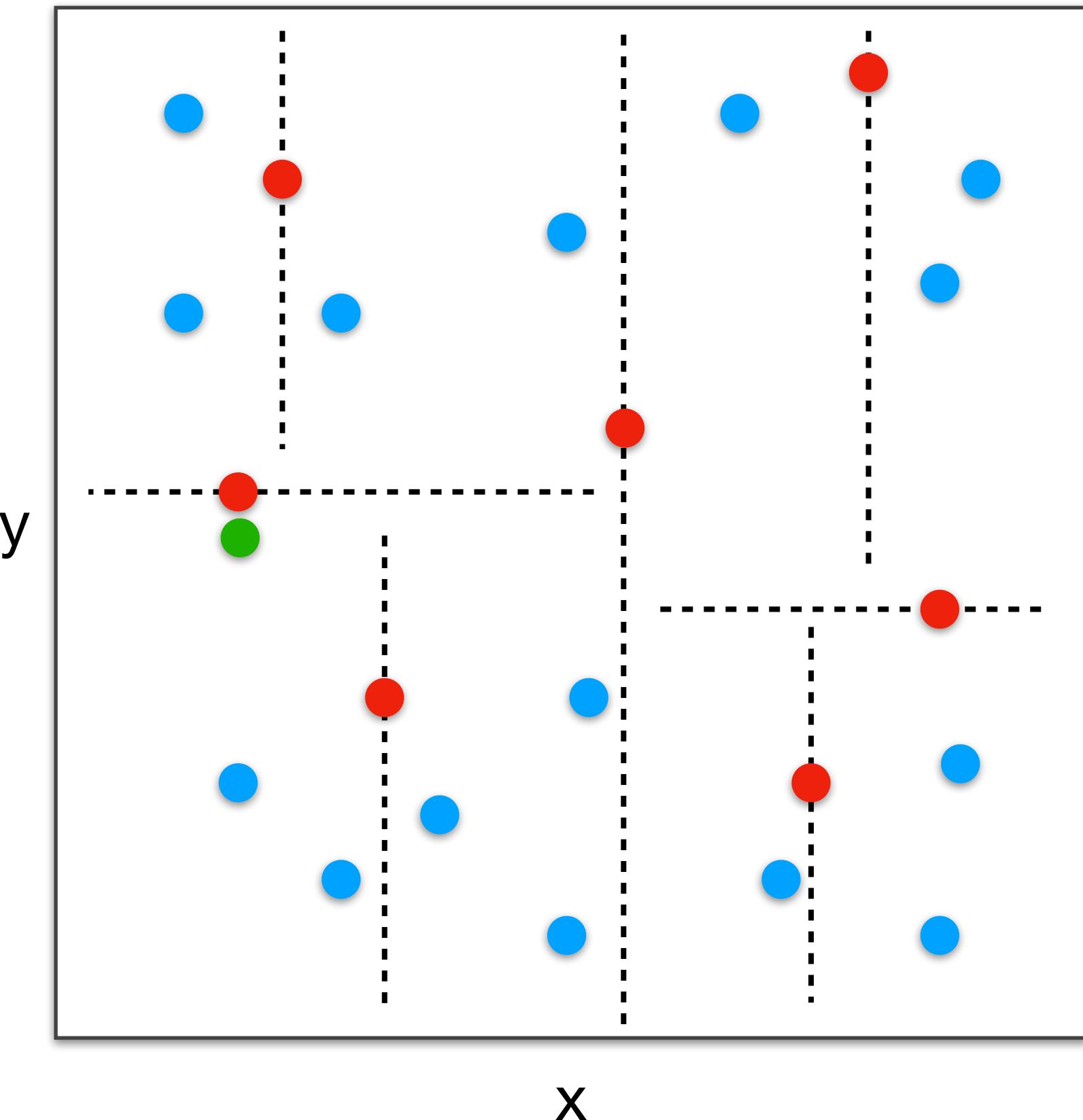
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How to reduce complexity?

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2D-features toy case



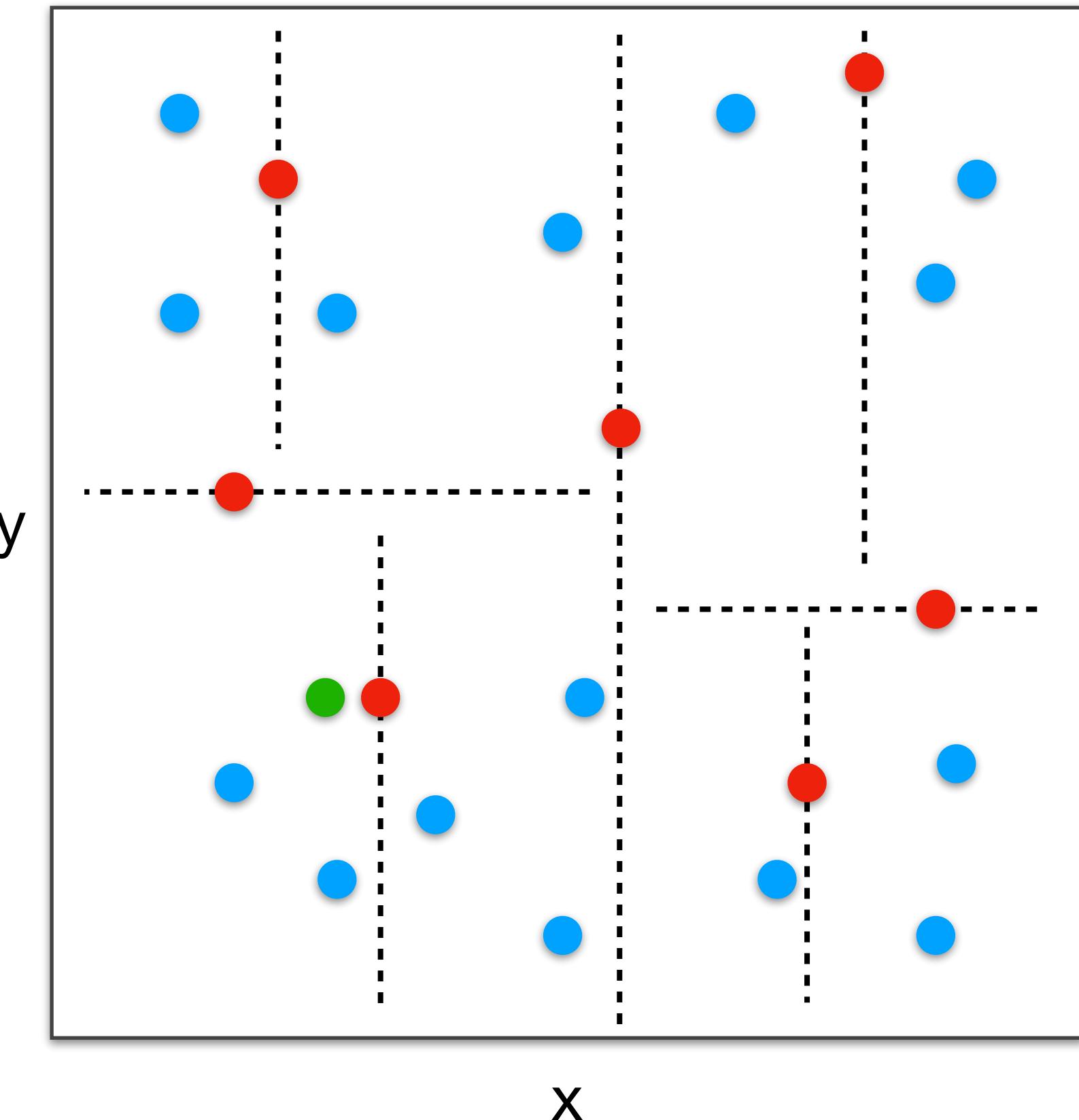
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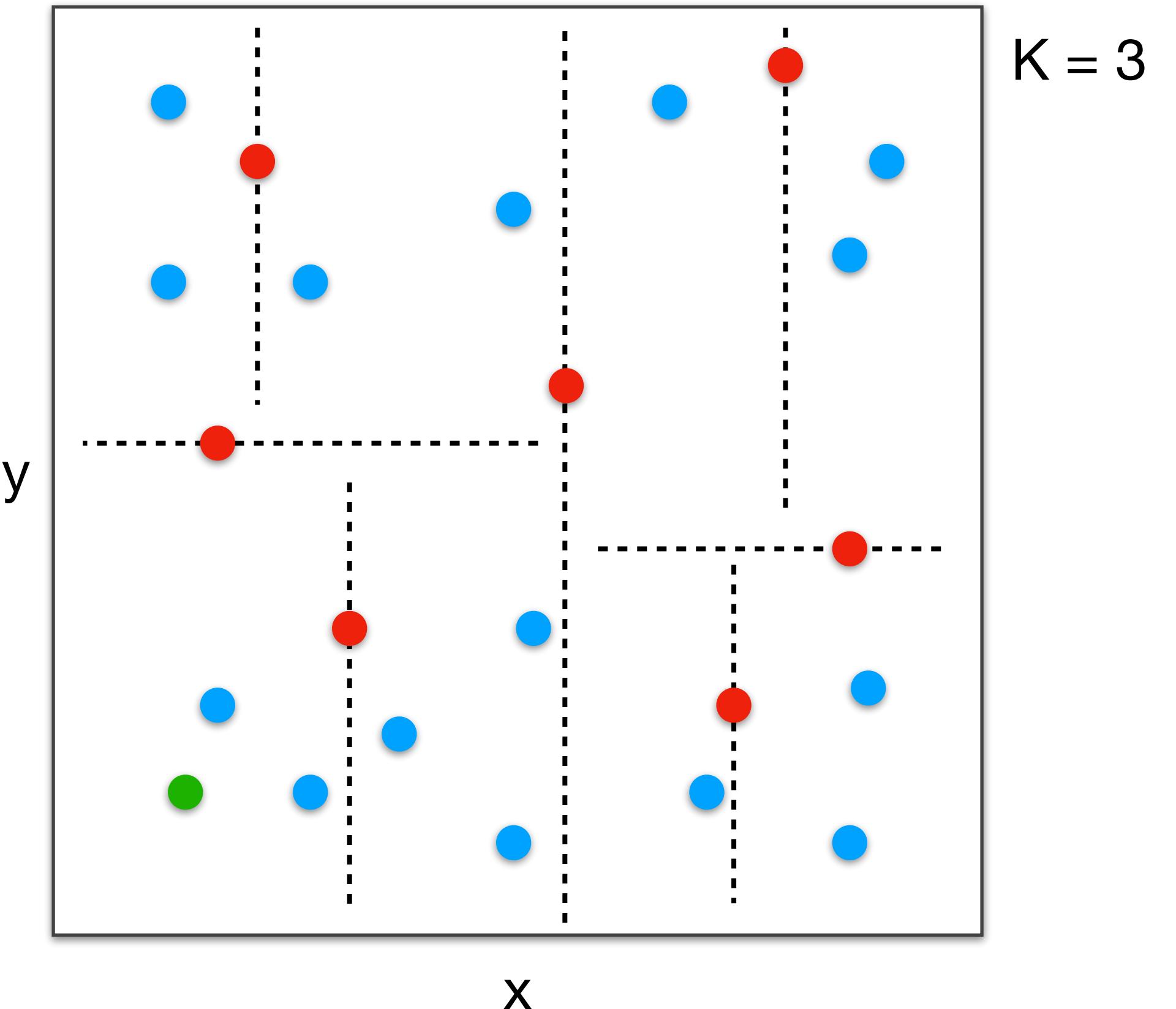
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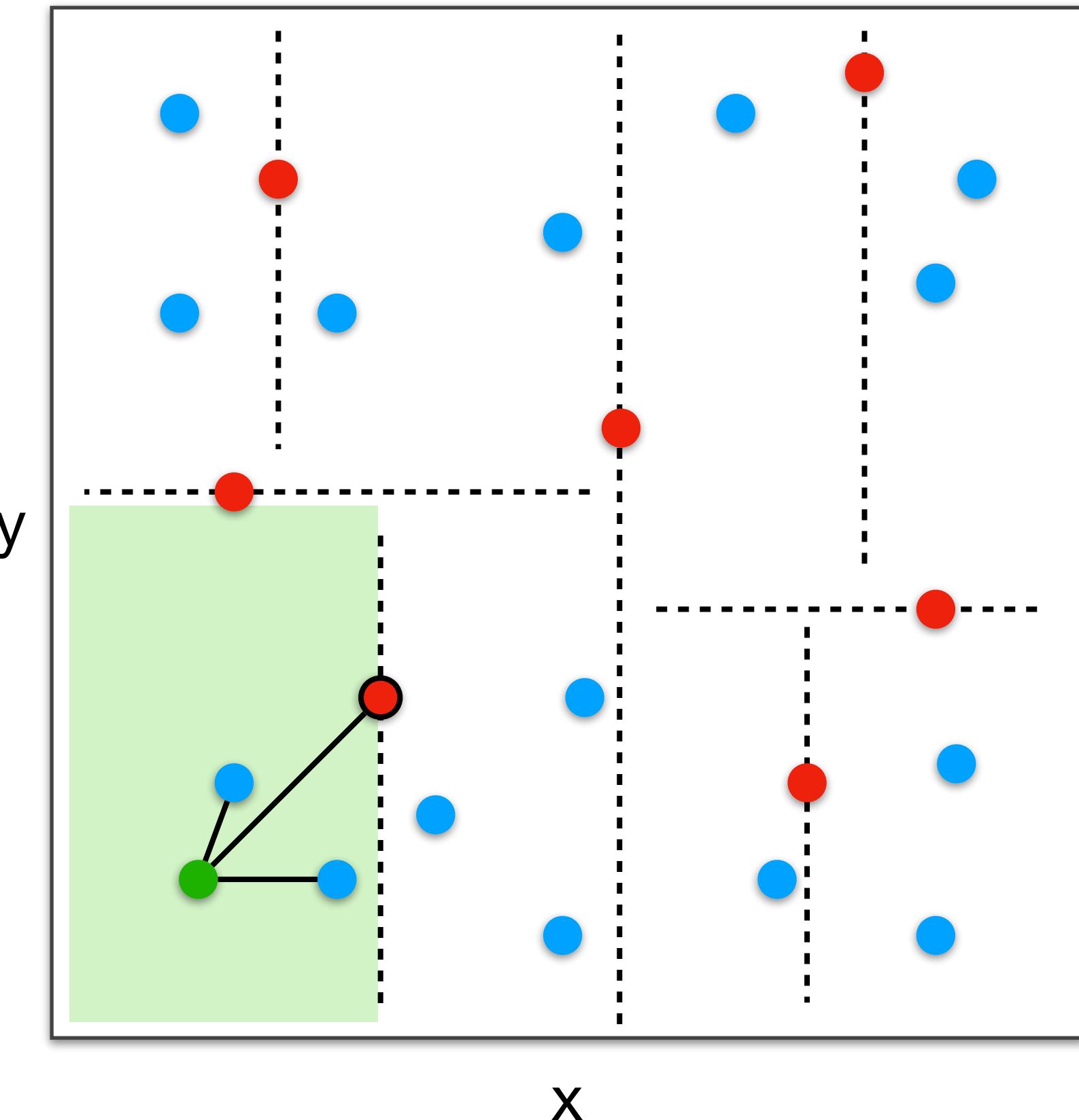
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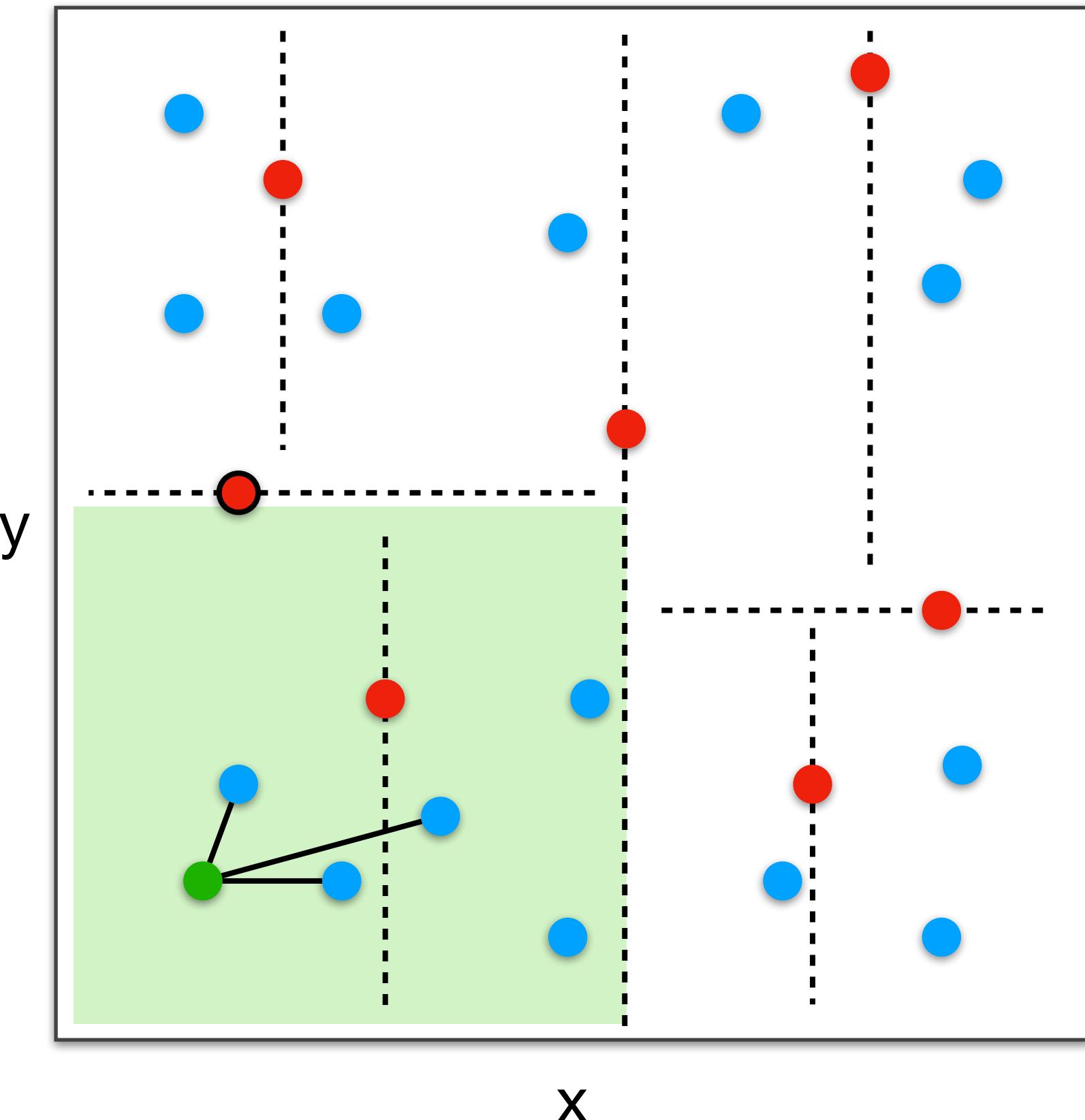
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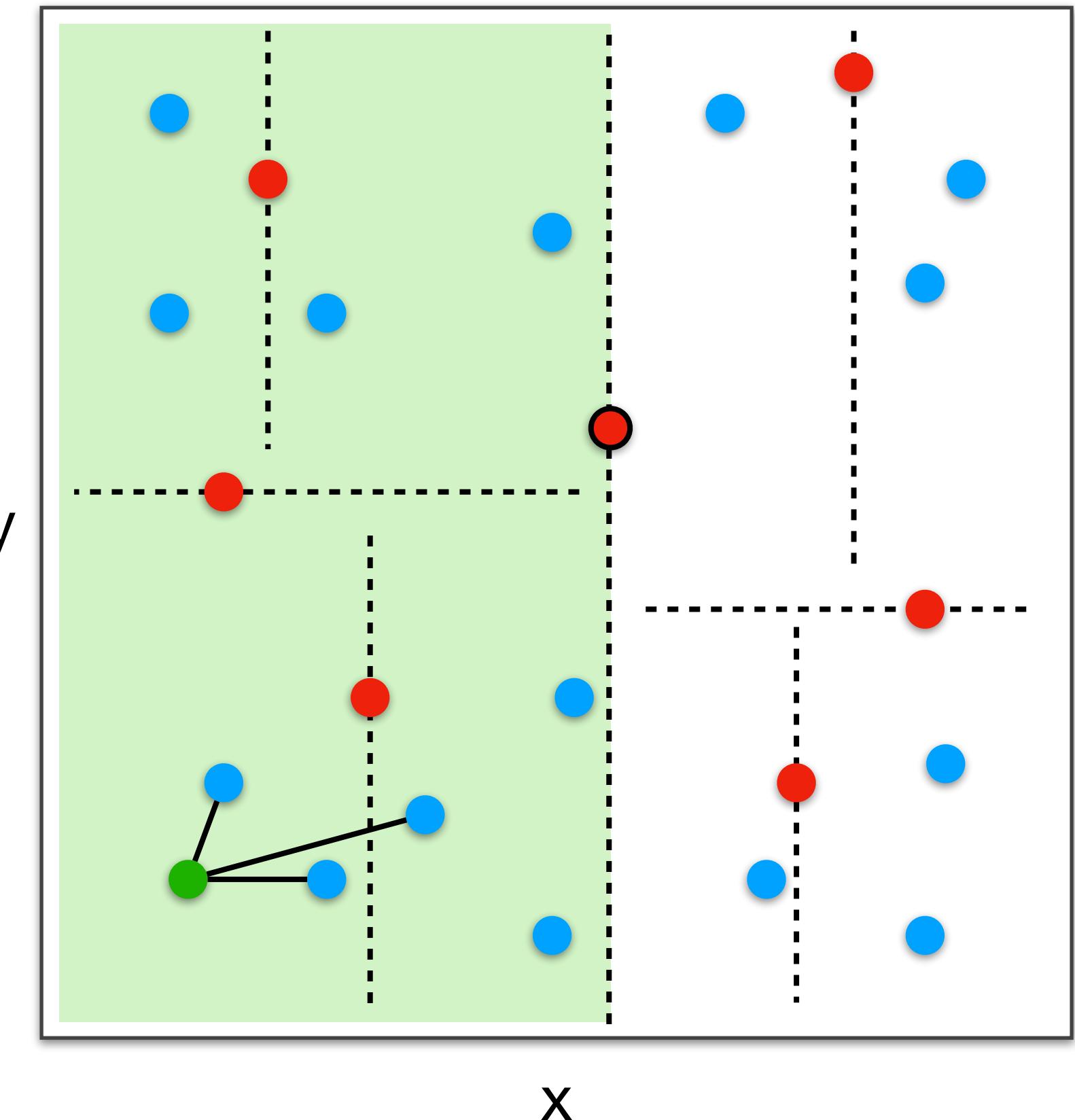
How to reduce complexity?

How to obtain 3-nearest neighbors?



No changes in 3-nearest, so stop.

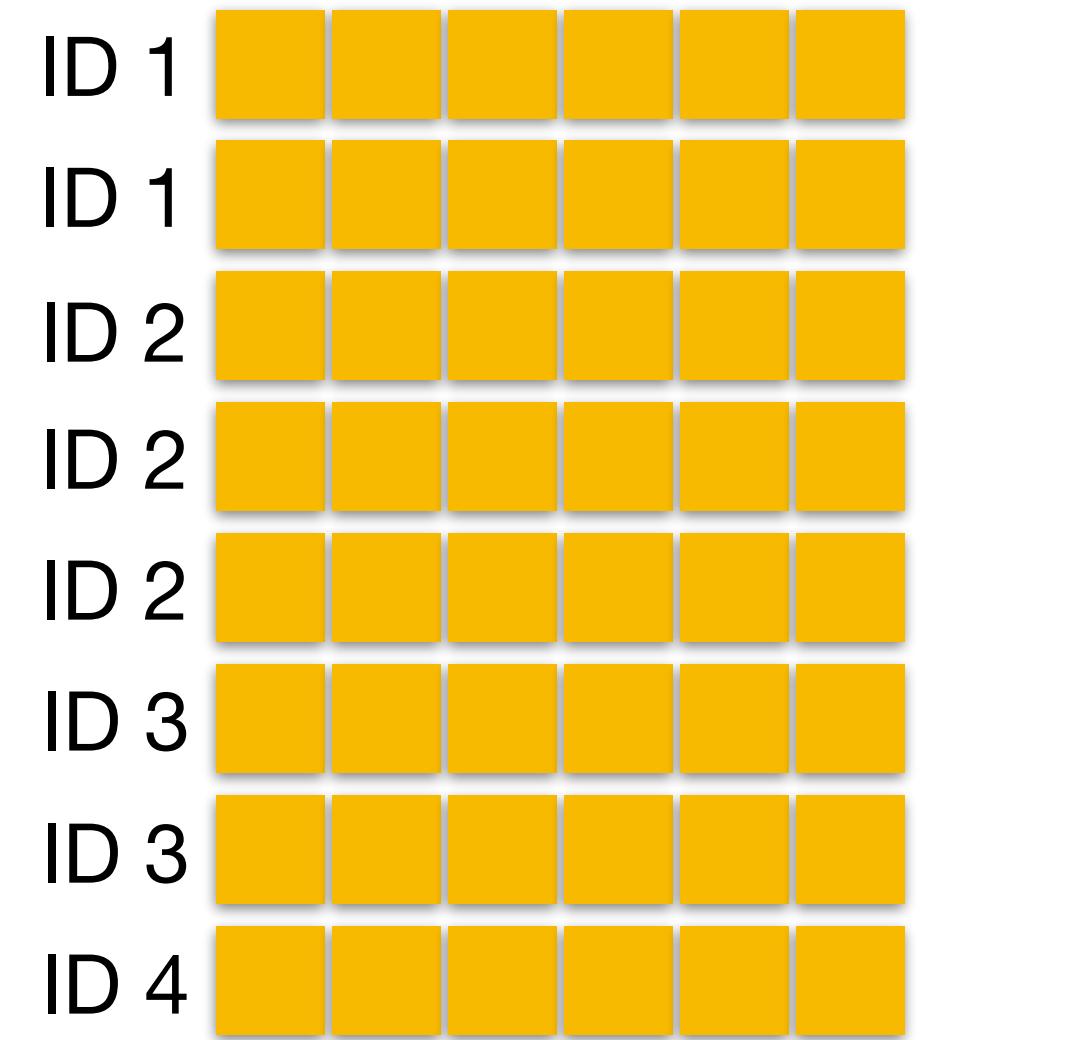
2D-features toy case



# Product Quantization

How to reduce size?

Toy Case (6D features, reality: 512D for faces)

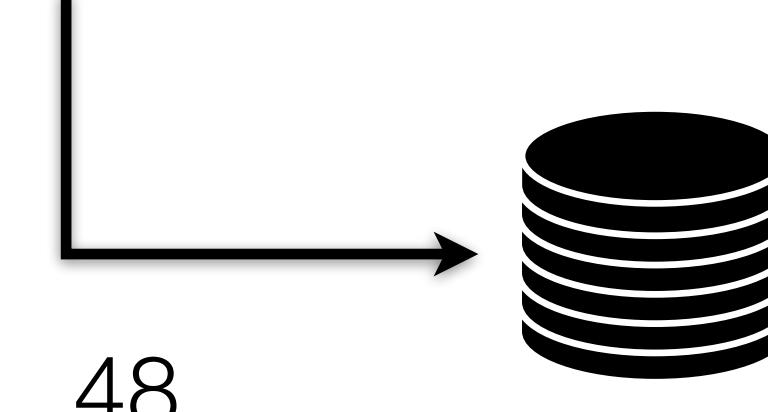


...



$P$  people

$M$  features



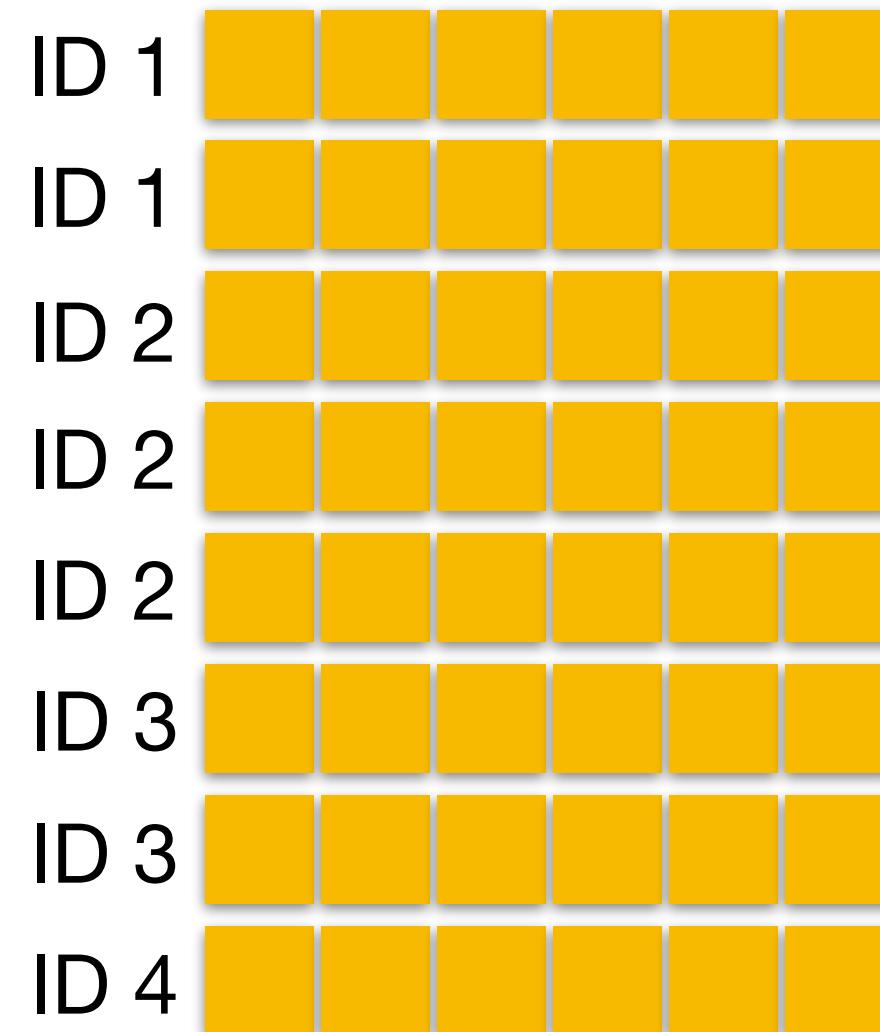
# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

1. Start with a **coarse quantizer**.

Toy Case (6D features, reality: 512D for faces)

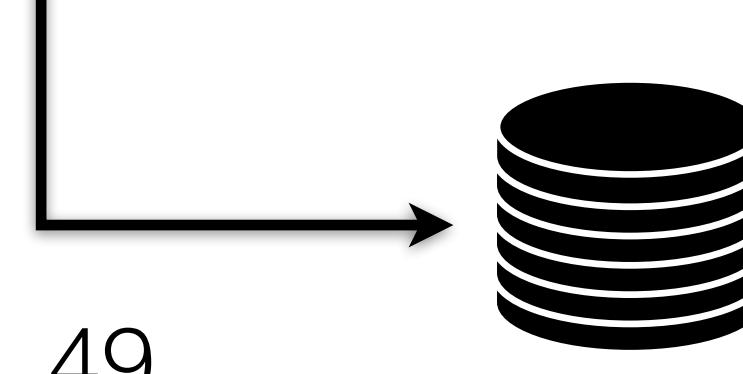


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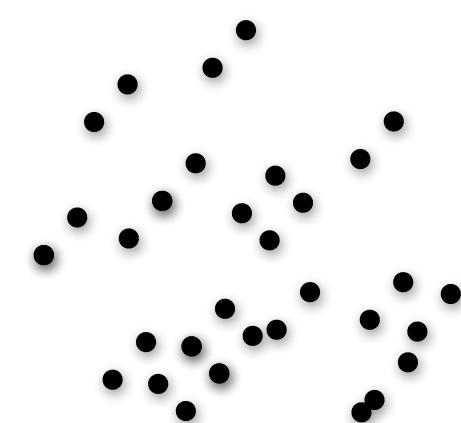
$P$  people

$M$  features



49

coarse quantizer



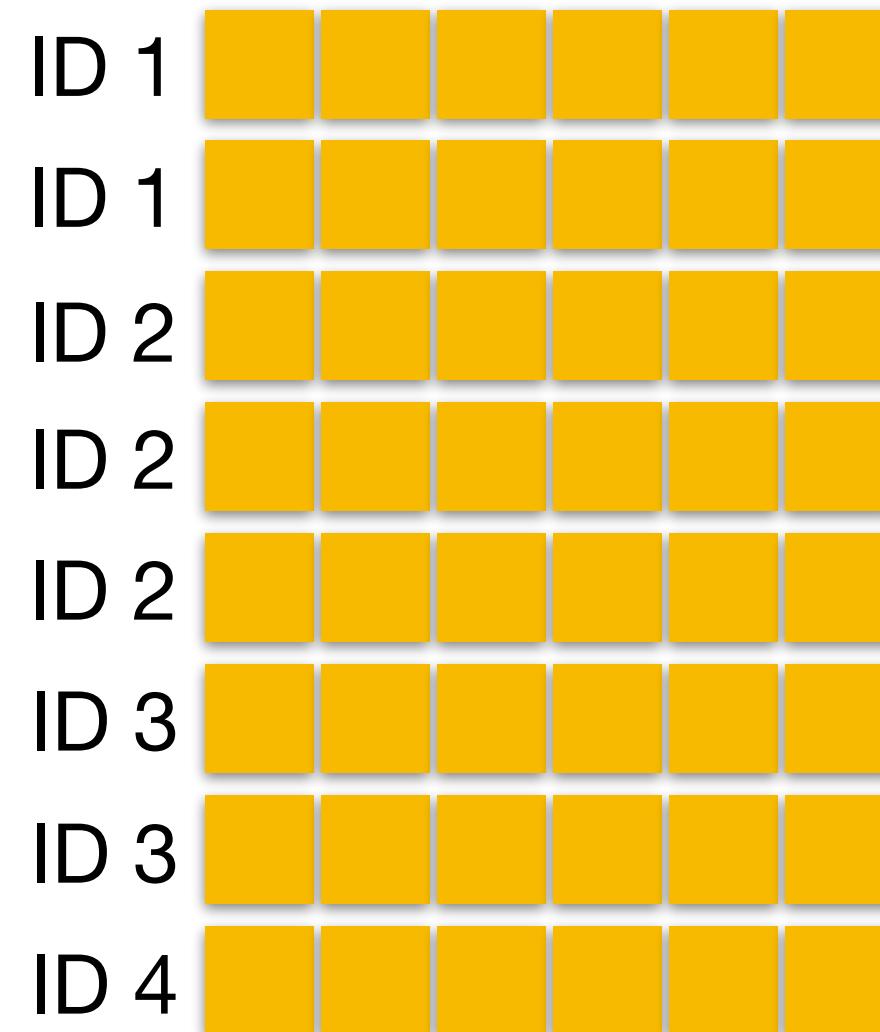
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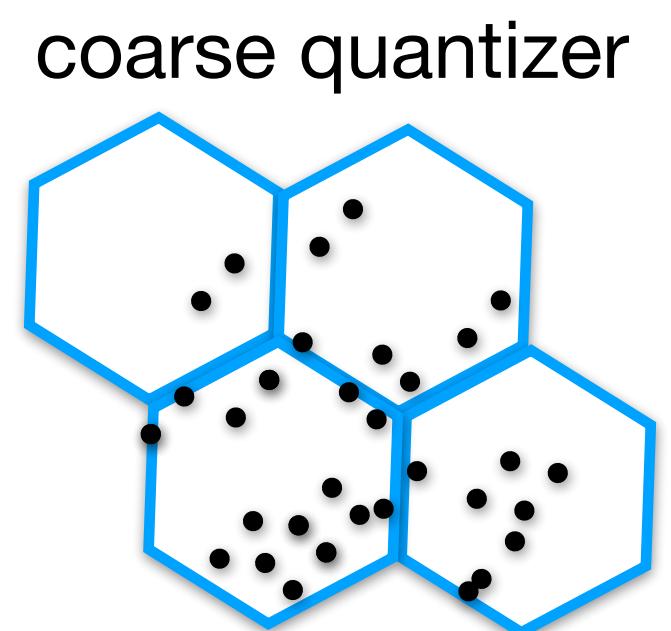
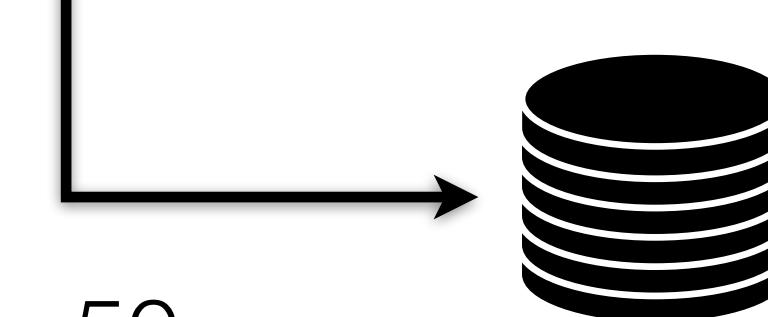


ID  $P$

$P$  people

$M$  features

50



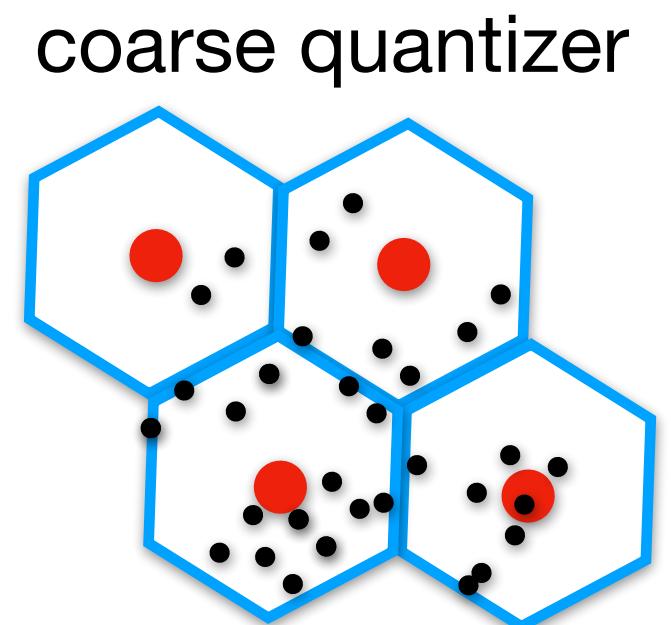
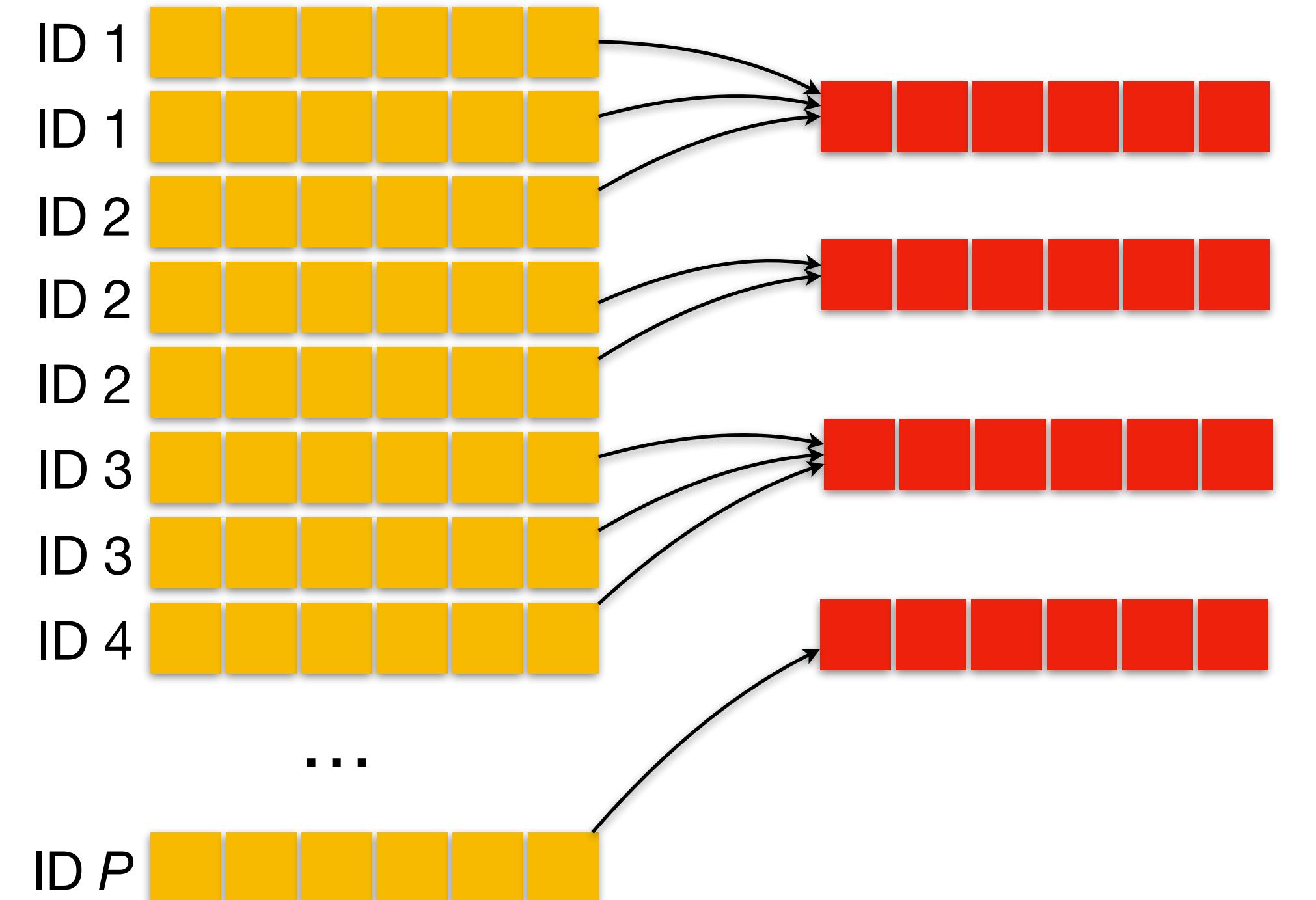
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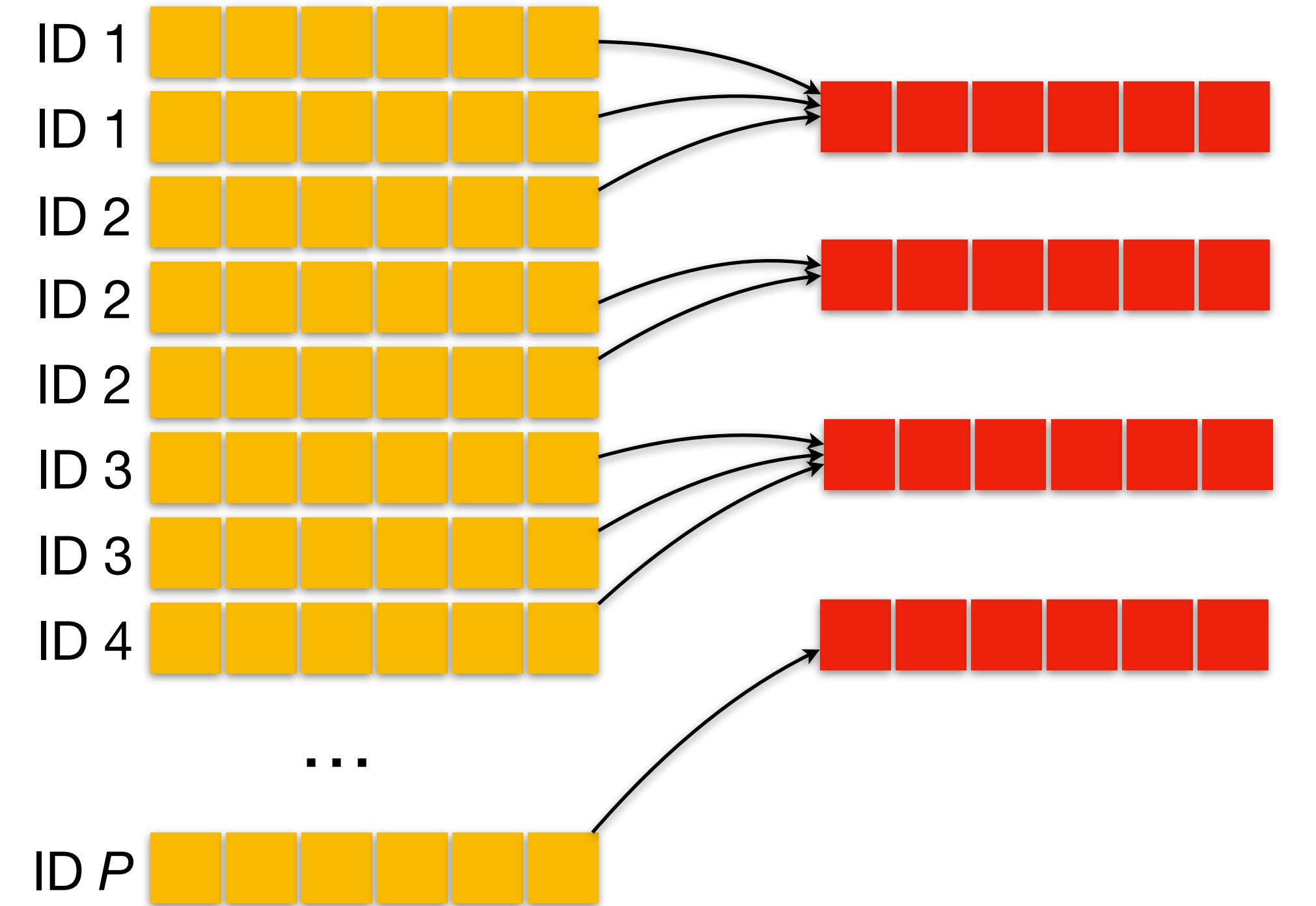
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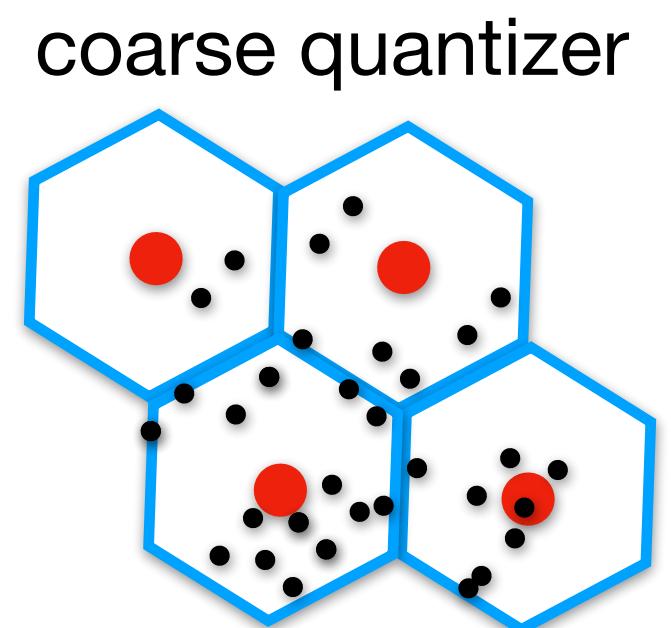


$P$  people

$M$  features

$M \gg N$

$N$  coarse centroids

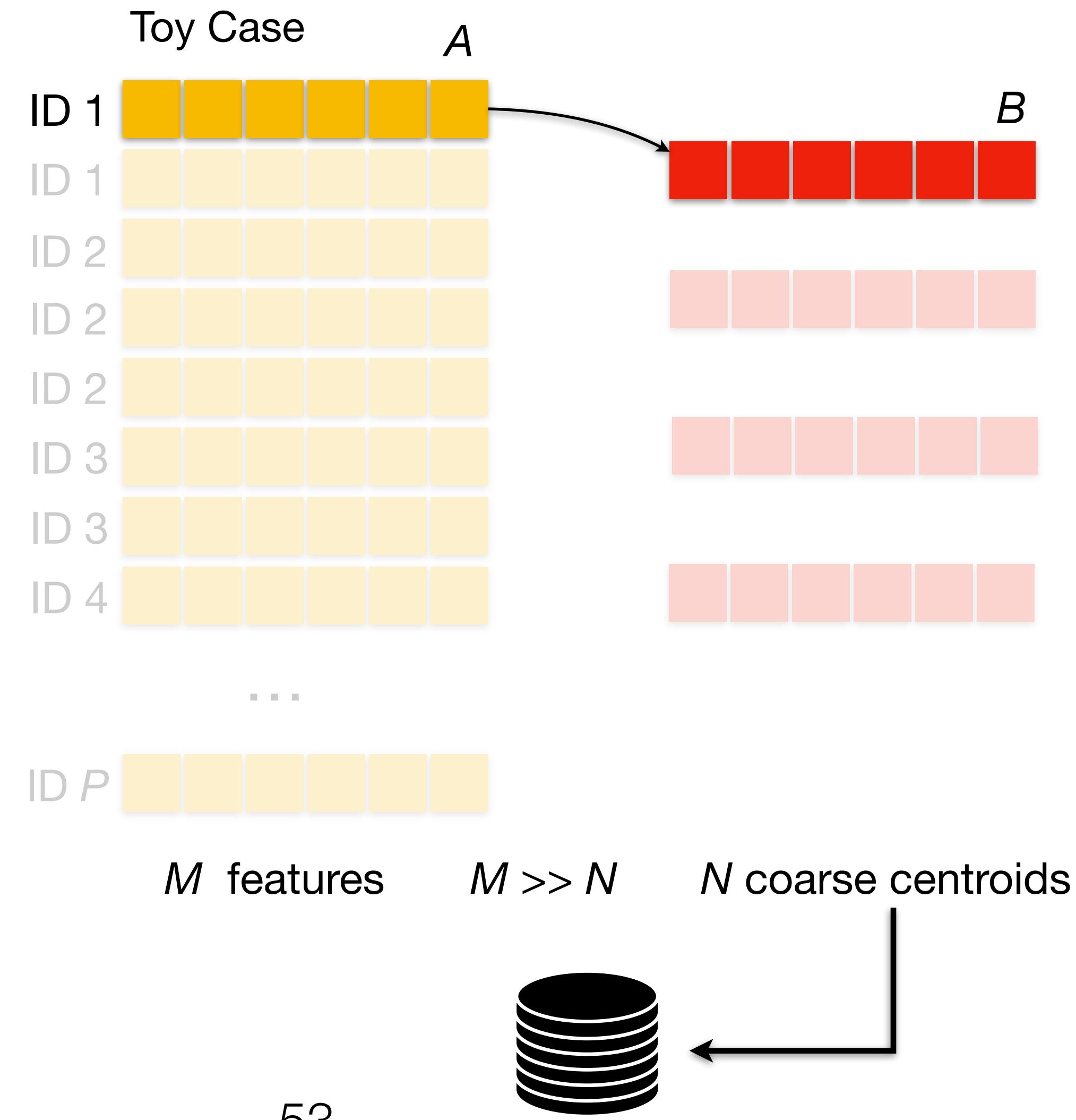


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

2. Compute **residuals** (differences) between features and their respective coarse centroids.

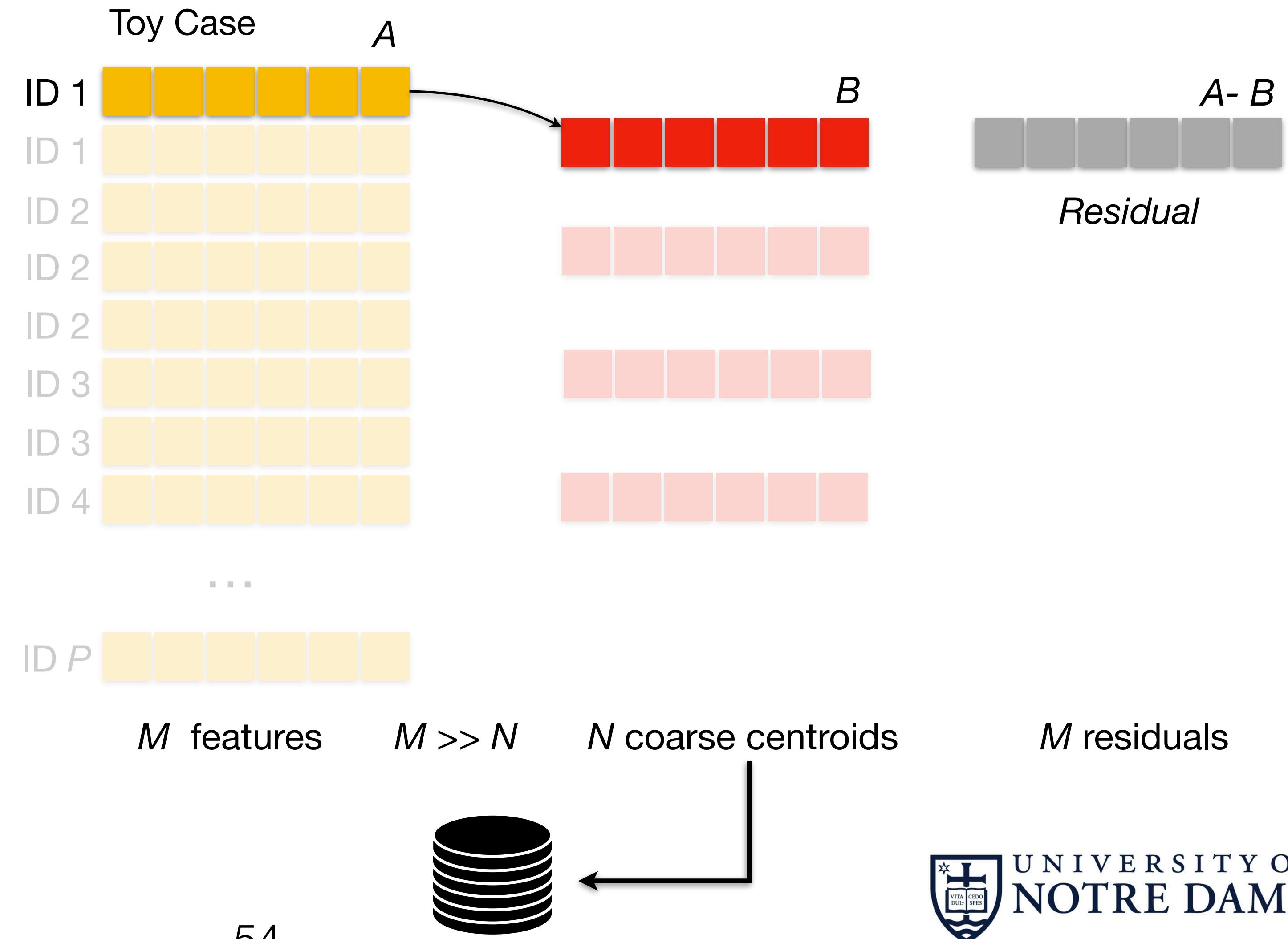


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State-of-the-art feature indexing.

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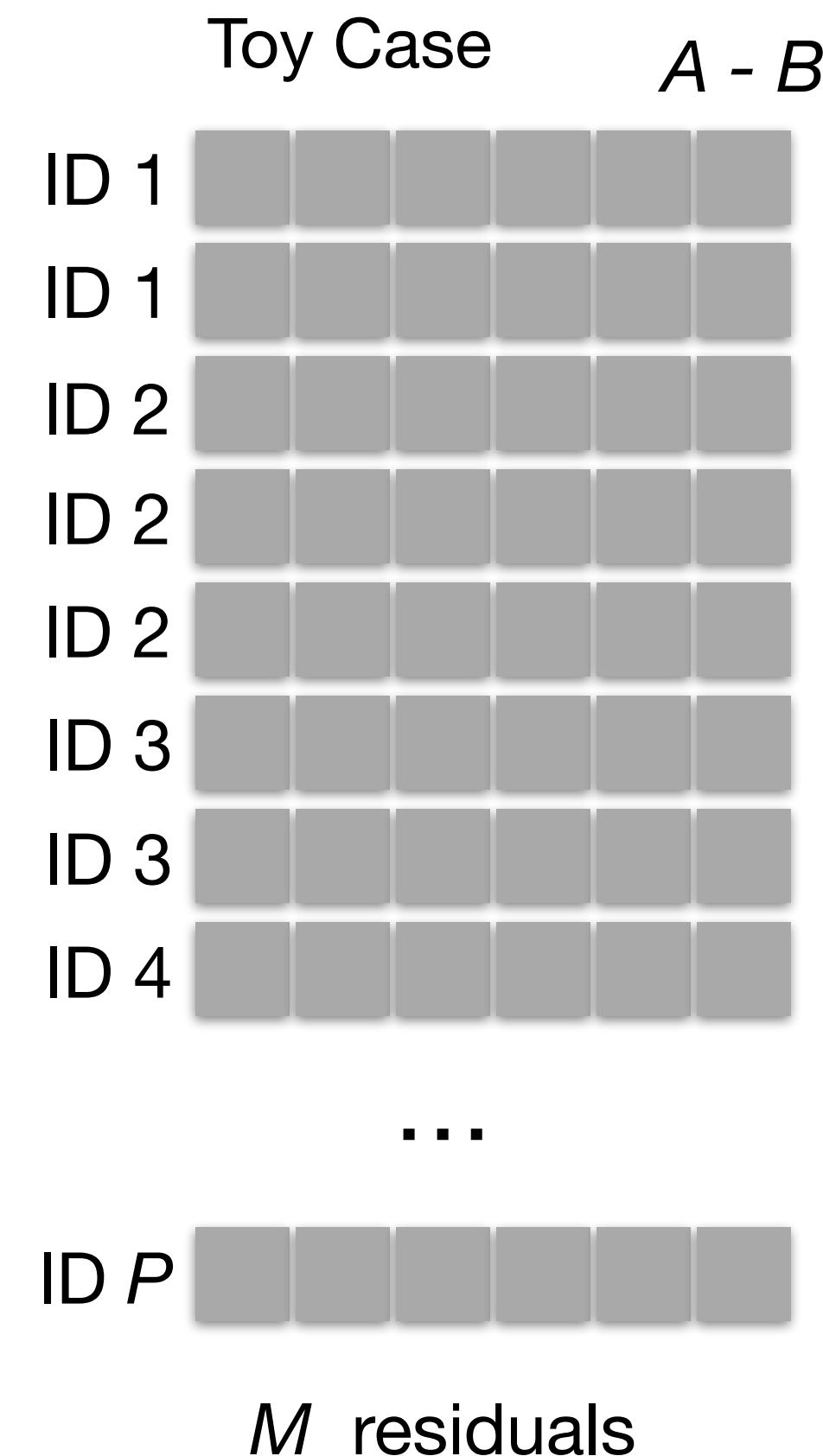


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

3. Reduce the dimensionality of residuals with **Product Quantization**.

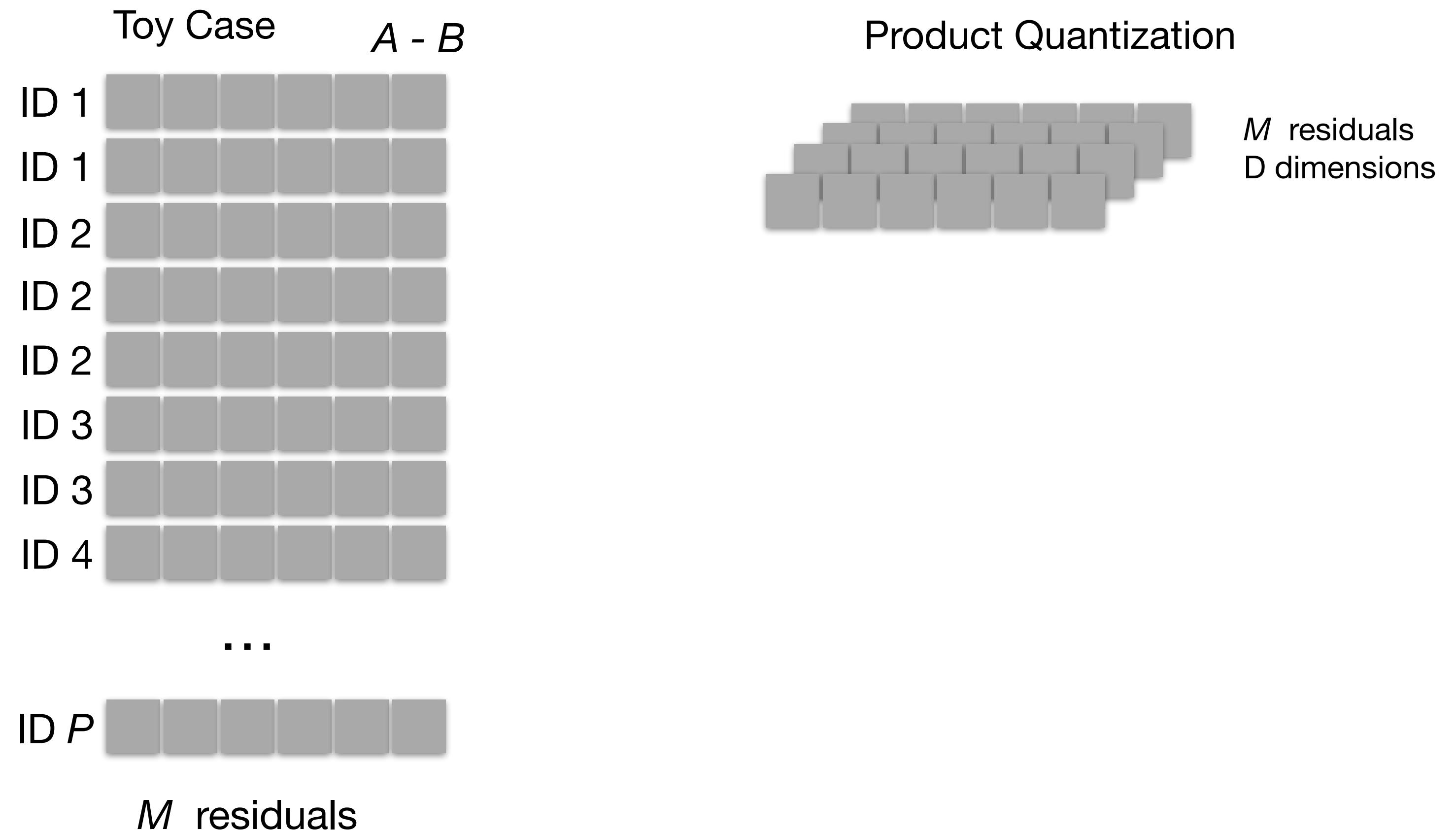


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State-of-the-art feature indexing.

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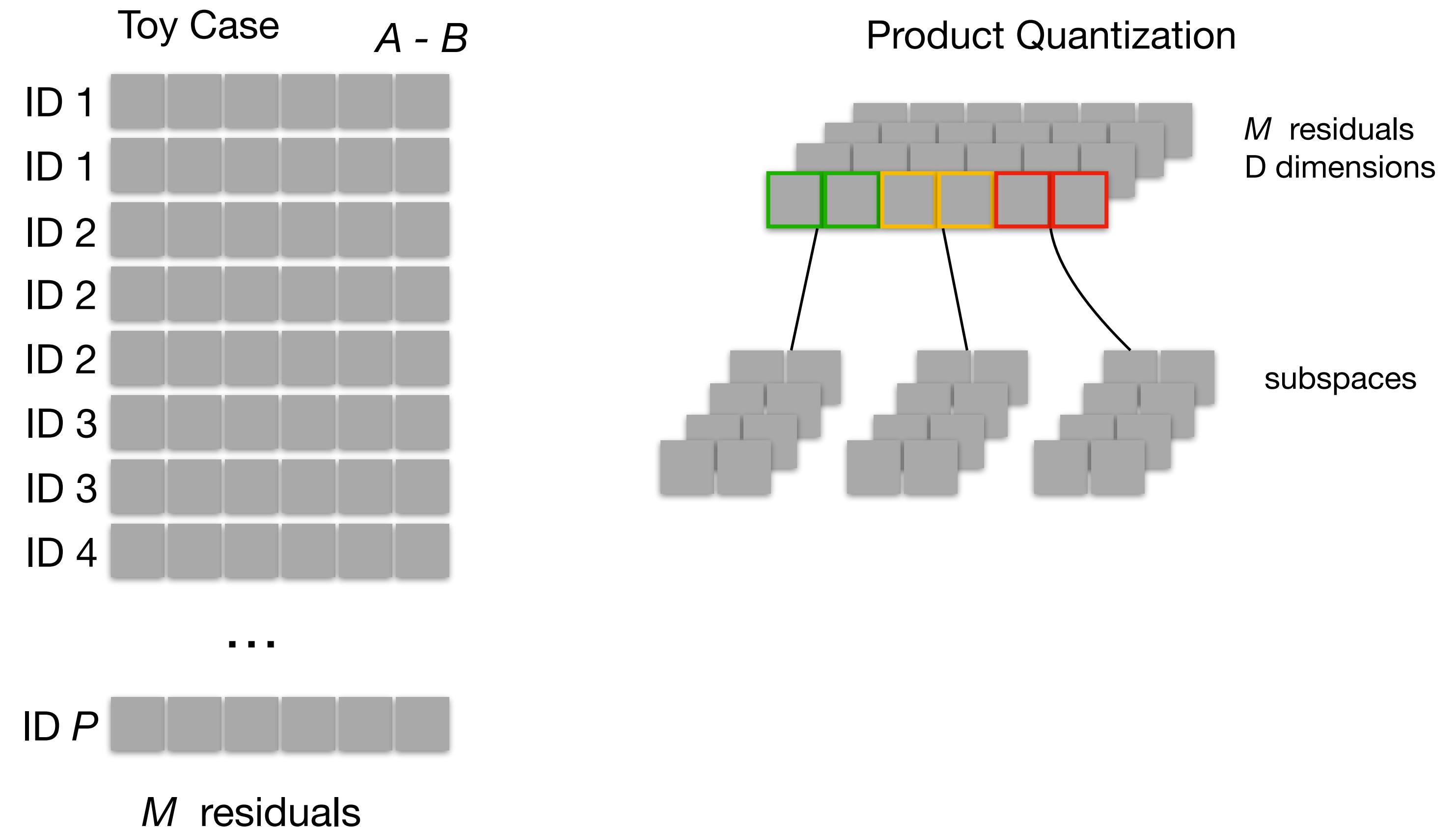


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How to reduce size?

State-of-the-art feature indexing.

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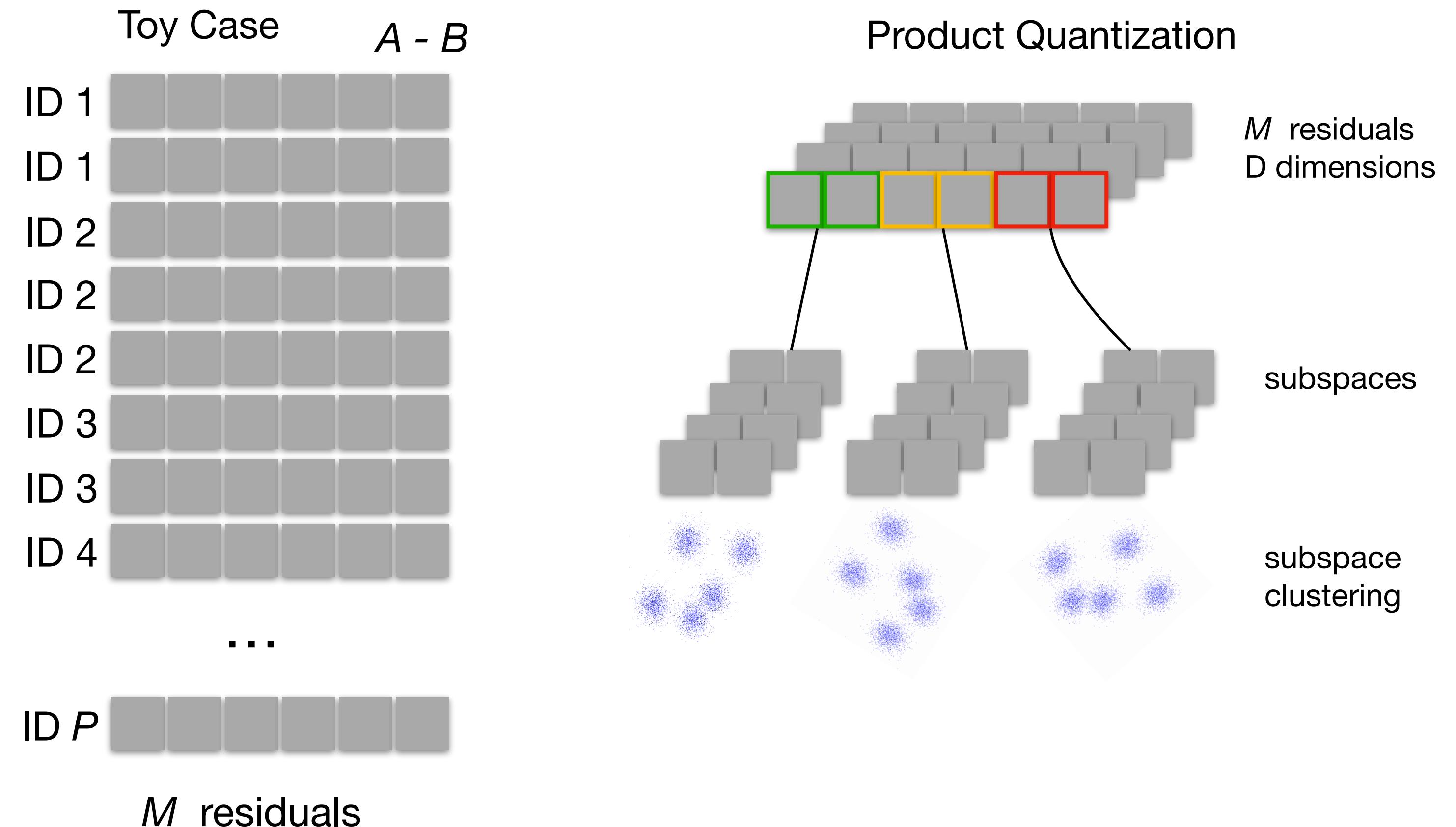


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How to reduce size?

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3. Reduce the dimensionality of residuals with **Product Quantization**.

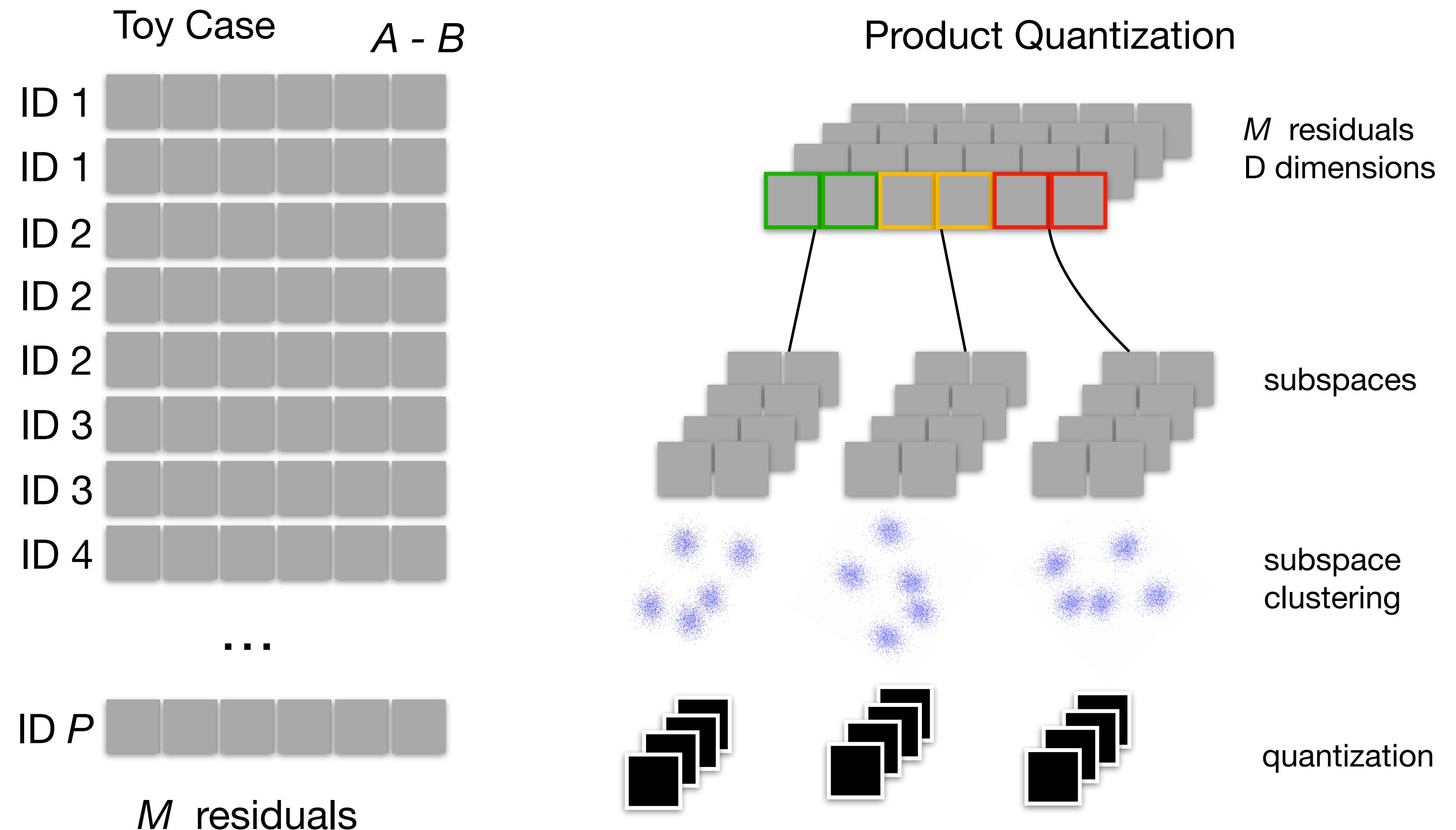


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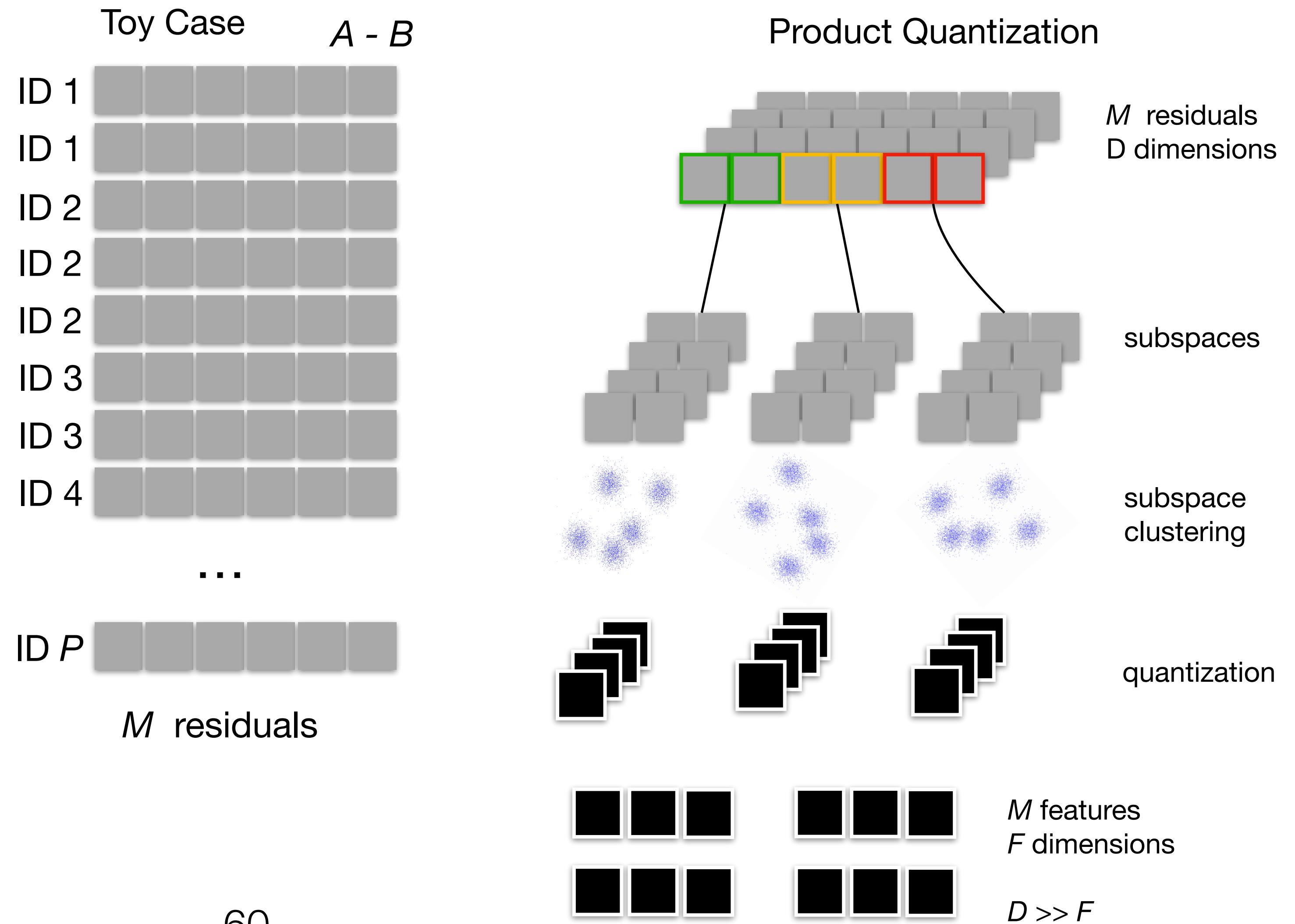


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How to reduce size?

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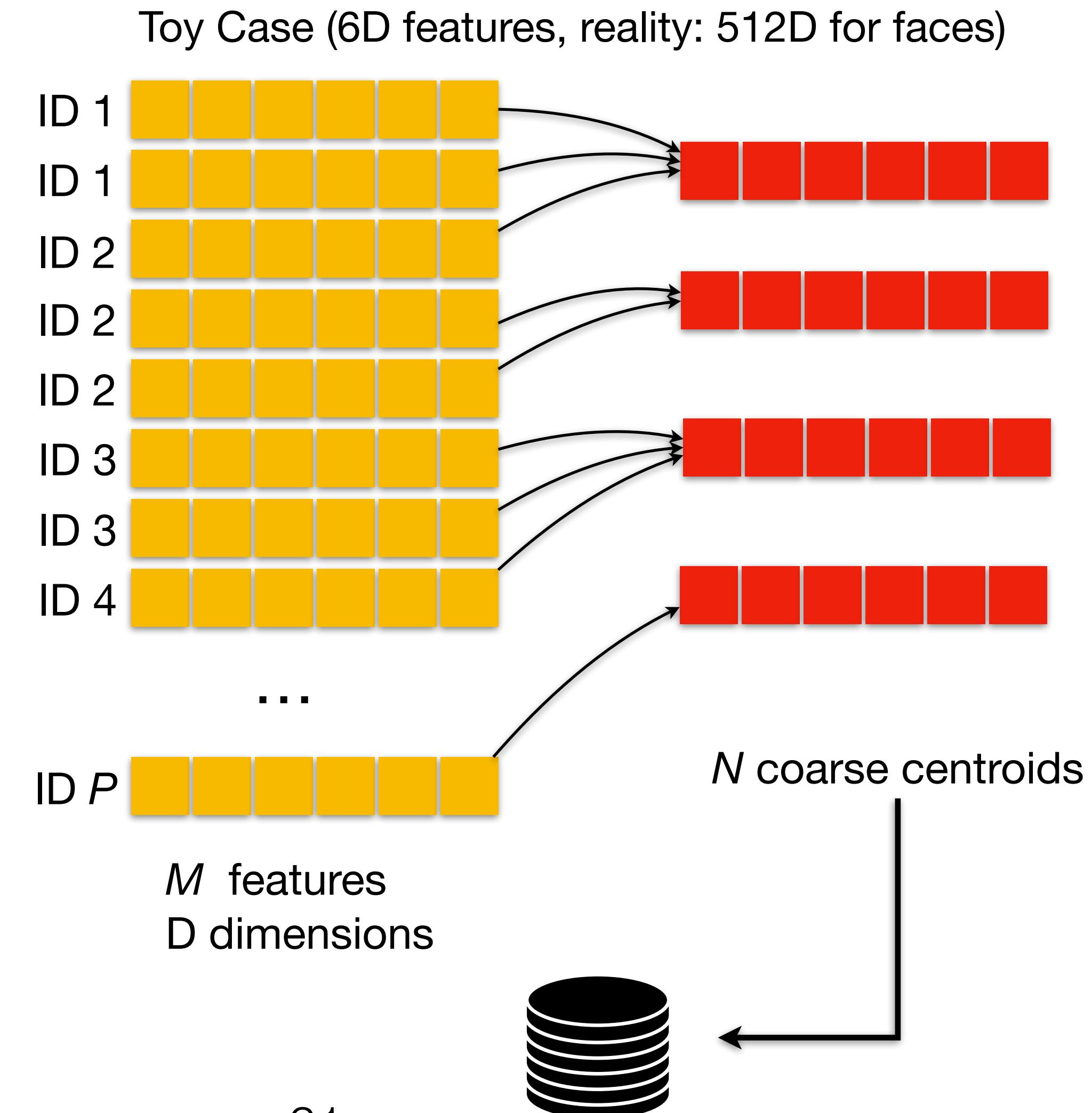


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

4. Append the product quantized residuals to an **inverted file index**.

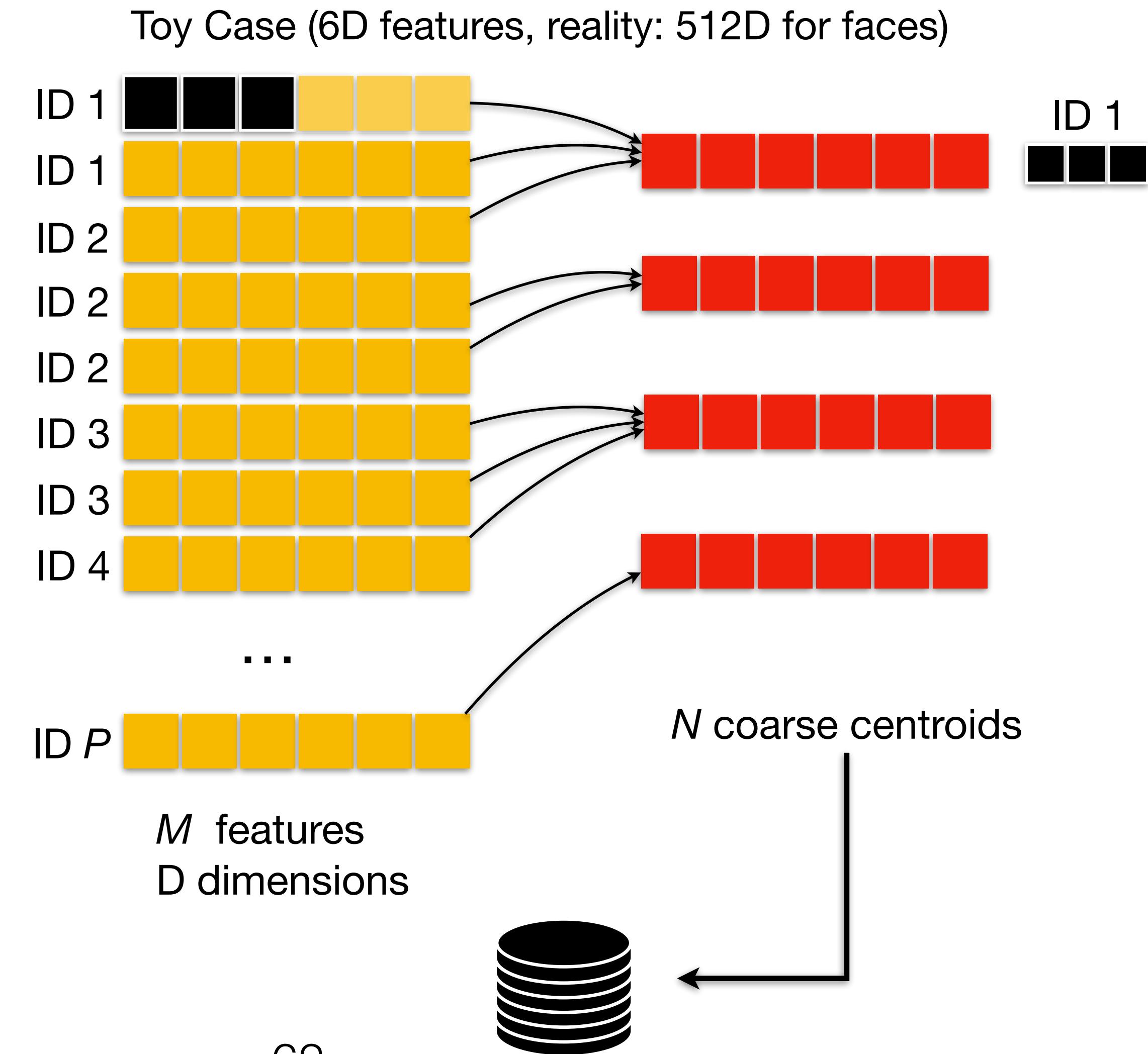


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# State-of-the-art feature indexing.

4. Append the product quantized residuals to an inverted file index.

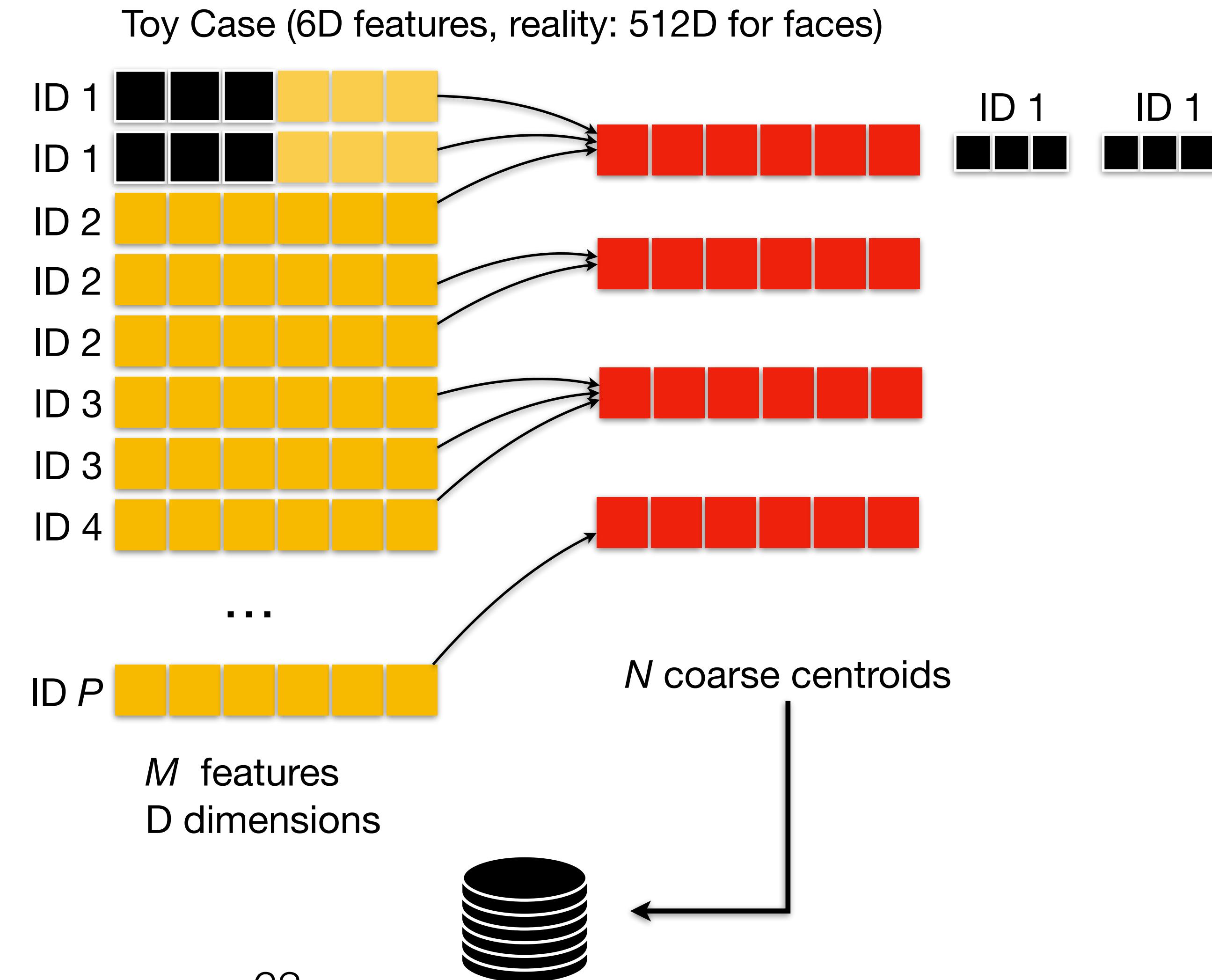


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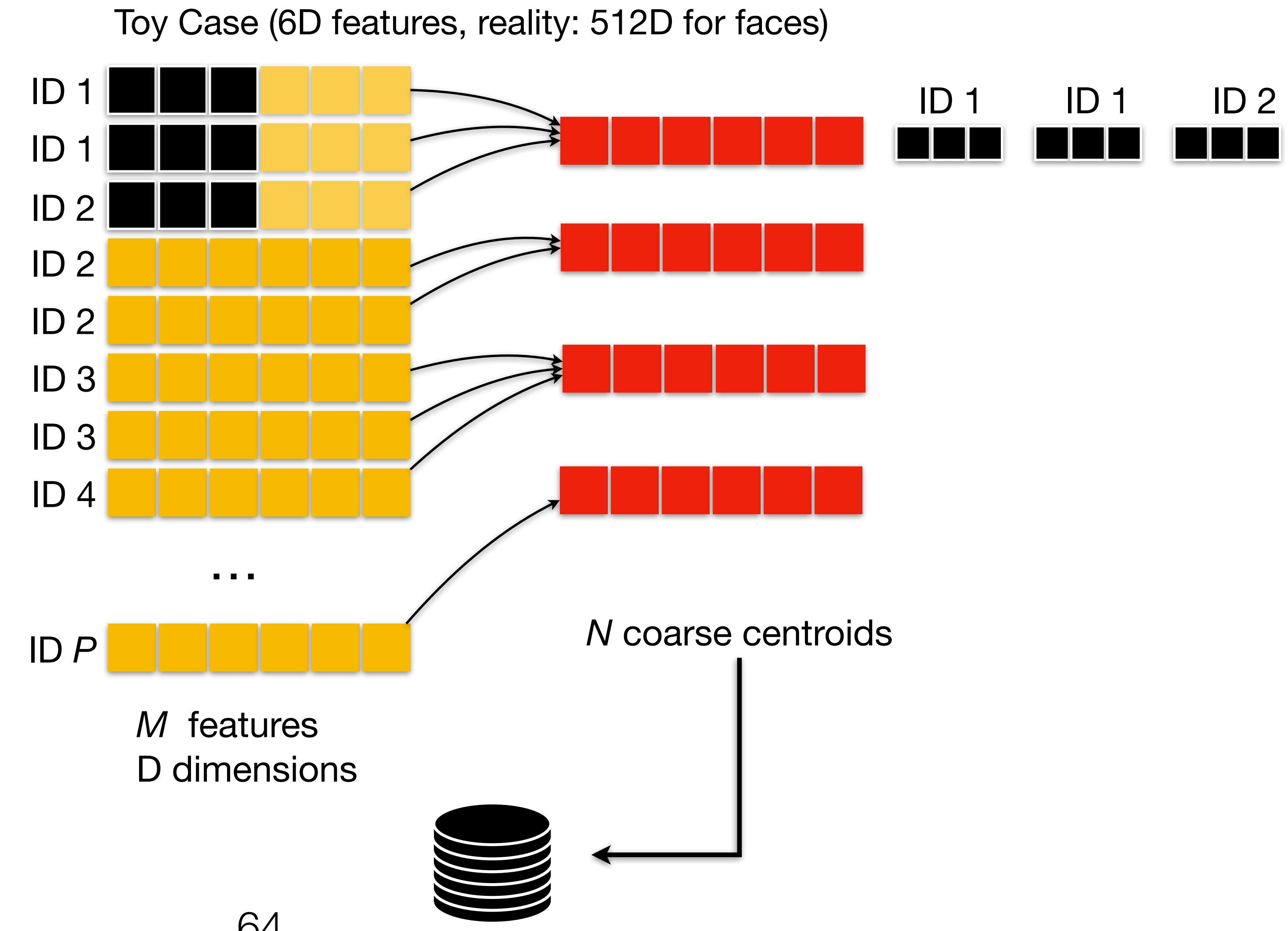


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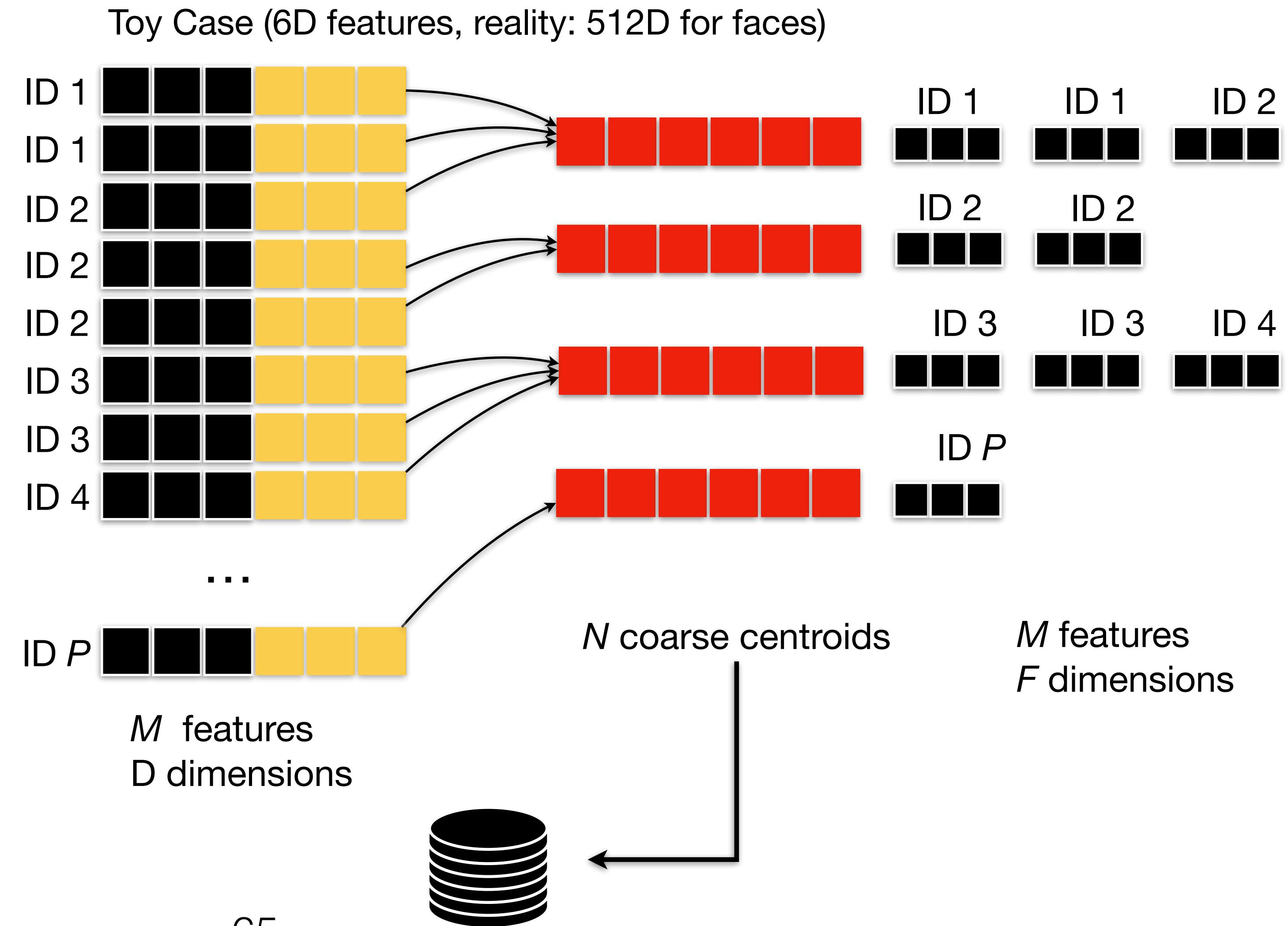


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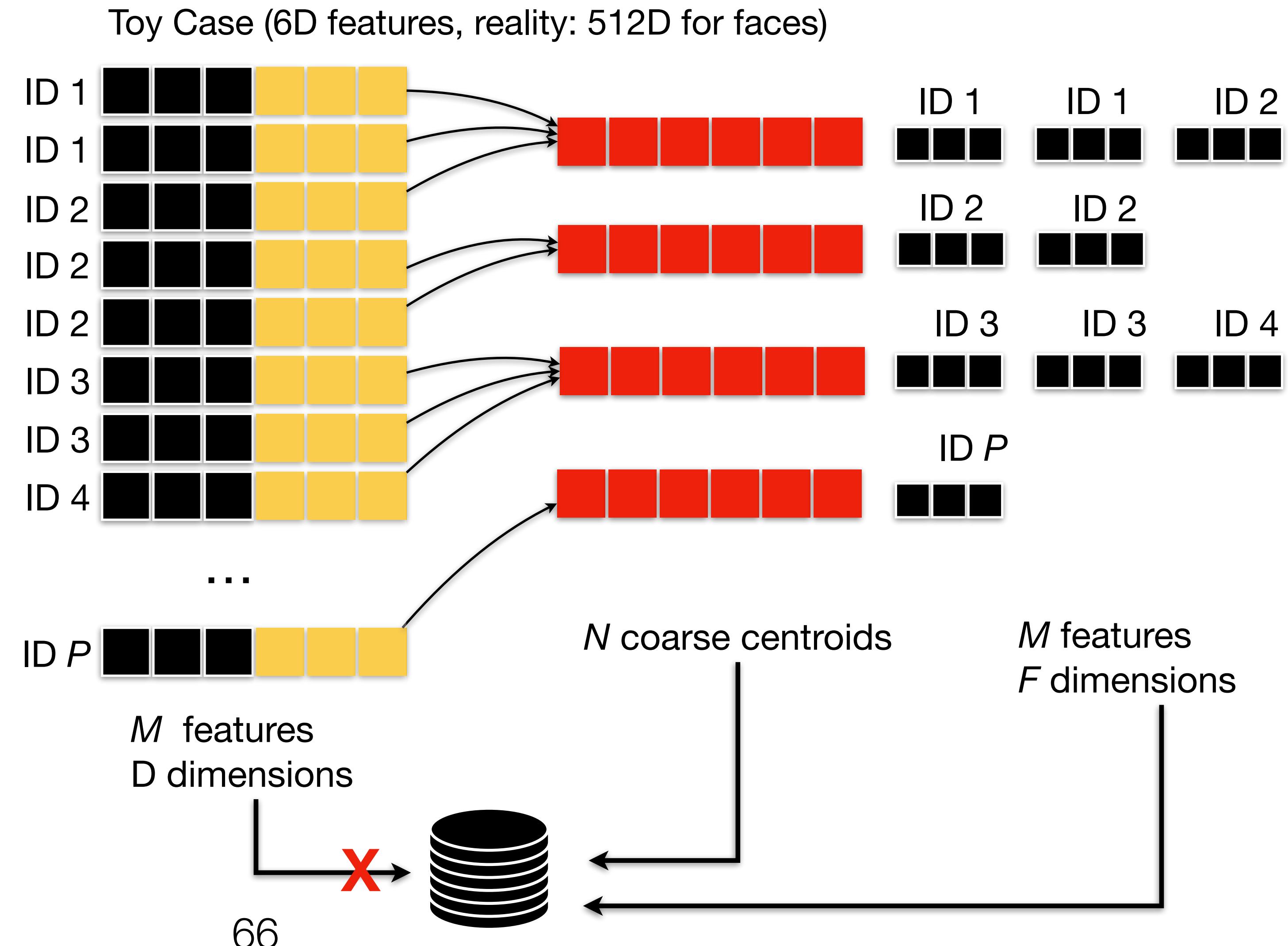


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How to reduce size?

State-of-the-art feature indexing.

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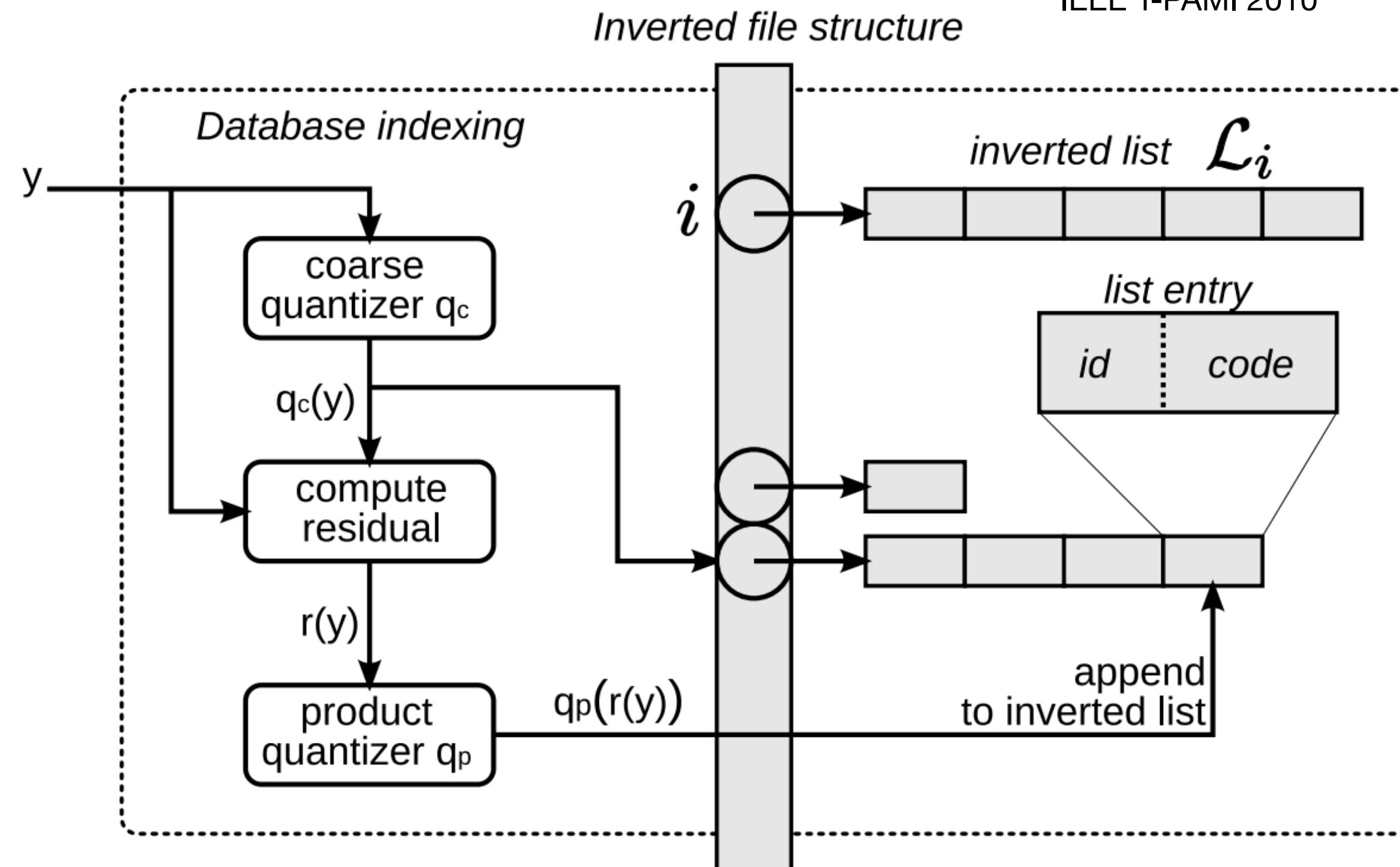
# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

Usage example:  
**Indexing.**

Source: Jegou et al.  
*Product quantization for nearest neighbor search*  
IEEE T-PAMI 2010



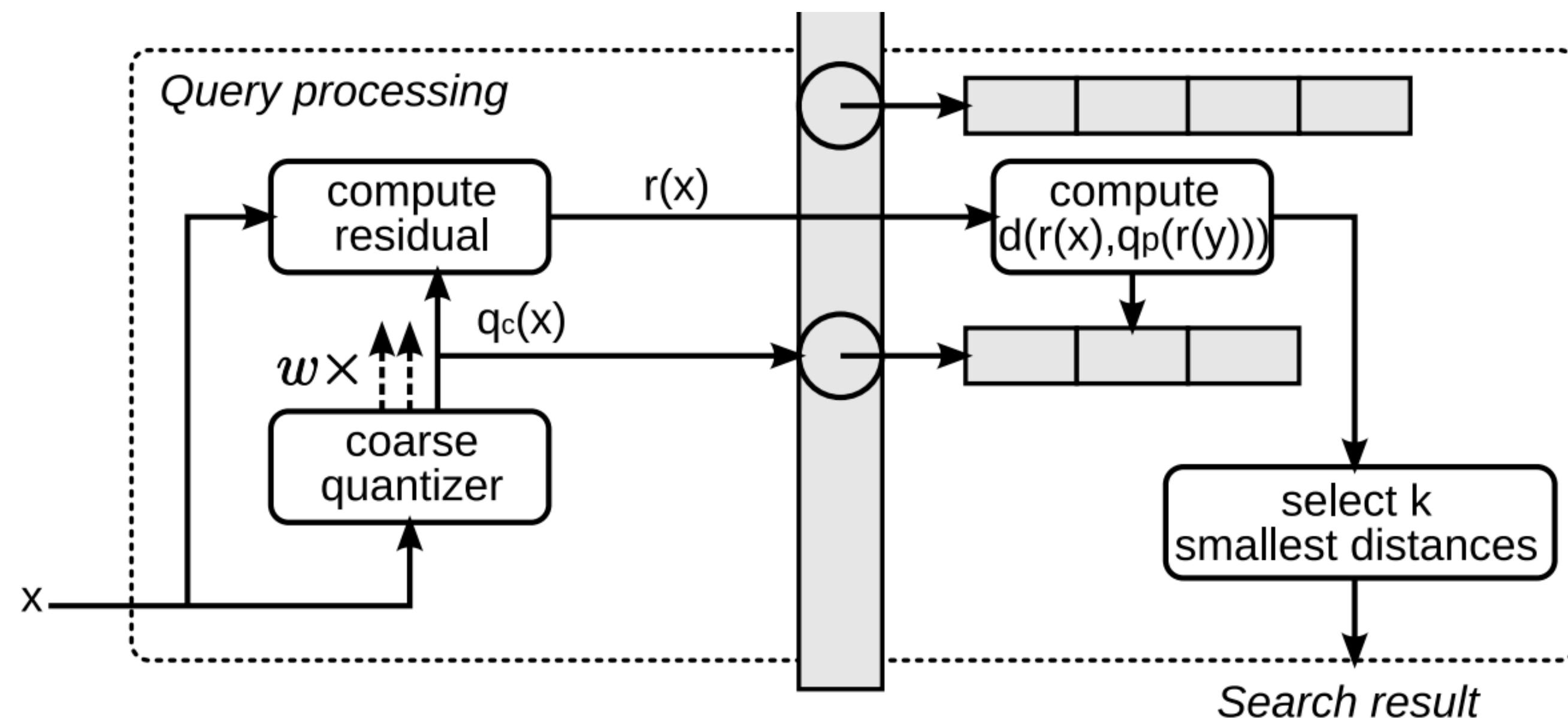
# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

Usage example:  
**Retrieving k-nearest.**

Source: Jegou et al.  
*Product quantization for nearest neighbor search*  
IEEE T-PAMI 2010



# Product Quantization

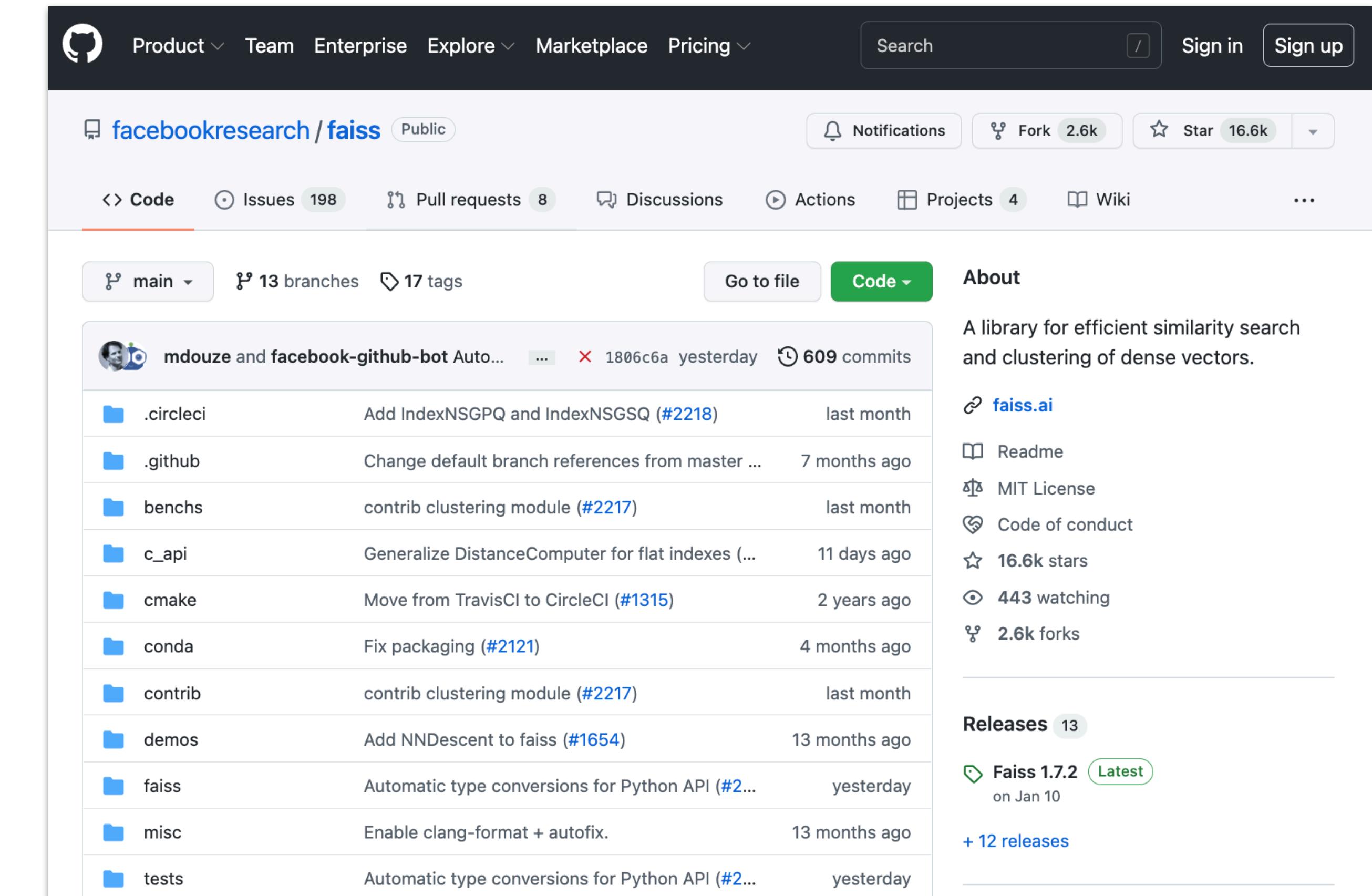
How to reduce size?

State-of-the-art feature indexing.

Available implementation.

## Faiss

Faiss is a library for efficient similarity search and clustering of dense vectors. It contains algorithms that search in sets of vectors of any size, up to ones that possibly do not fit in RAM. It also contains supporting code for evaluation and parameter tuning. Faiss is written in C++ with complete wrappers for Python/numpy. Some of the most useful algorithms are implemented on the GPU. It is developed primarily at [Facebook AI Research](#).



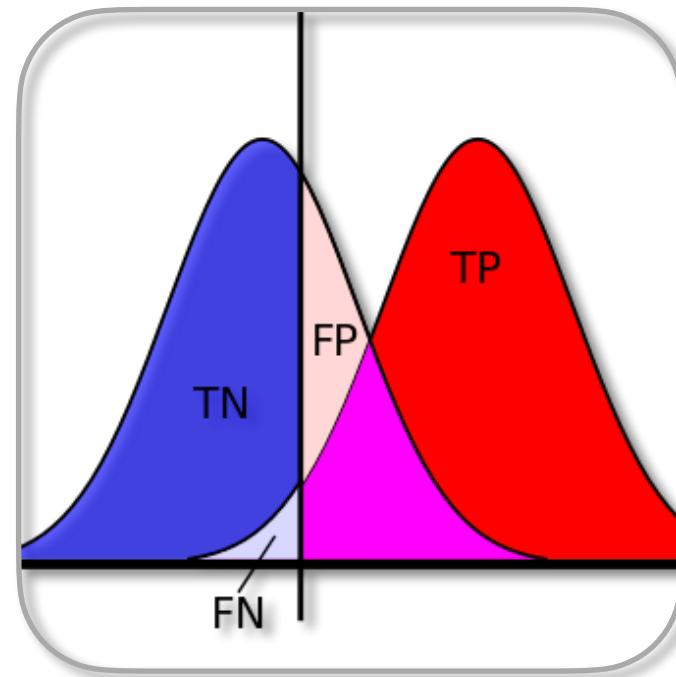
The screenshot shows the GitHub repository page for `facebookresearch/faiss`. The repository is public, has 198 issues, 8 pull requests, and 4 projects. The main branch is `main`, which has 13 branches and 17 tags. There are 609 commits from mdouze and facebook-github-bot. The repository is described as a library for efficient similarity search and clustering of dense vectors. It includes links to faiss.ai, Readme, MIT License, Code of conduct, 16.6k stars, 443 watching, and 2.6k forks. The releases section shows Faiss 1.7.2 as the latest version, released on Jan 10, with 13 releases in total.

Commit	Message	Date
<code>.circleci</code>	Add IndexNSGPQ and IndexNSGSQ (#2218)	last month
<code>.github</code>	Change default branch references from master ...	7 months ago
<code>benchs</code>	contrib clustering module (#2217)	last month
<code>c_api</code>	Generalize DistanceComputer for flat indexes ...	11 days ago
<code>cmake</code>	Move from TravisCI to CircleCI (#1315)	2 years ago
<code>conda</code>	Fix packaging (#2121)	4 months ago
<code>contrib</code>	contrib clustering module (#2217)	last month
<code>demos</code>	Add NNDescent to faiss (#1654)	13 months ago
<code>faiss</code>	Automatic type conversions for Python API (#2...	yesterday
<code>misc</code>	Enable clang-format + autofix.	13 months ago
<code>tests</code>	Automatic type conversions for Python API (#2...	yesterday

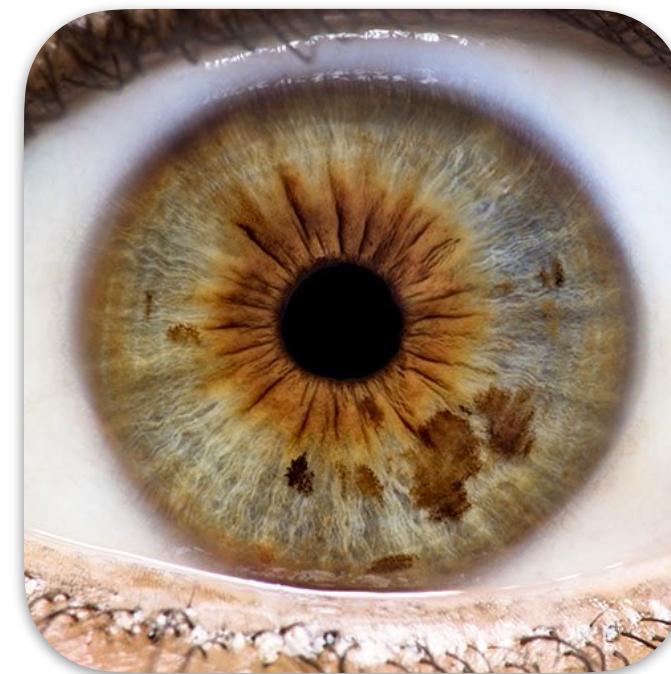
<https://github.com/facebookresearch/faiss>

# S'up Next?

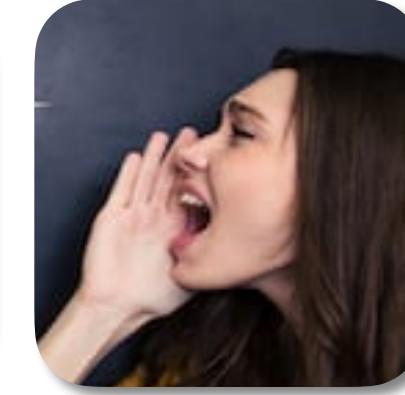
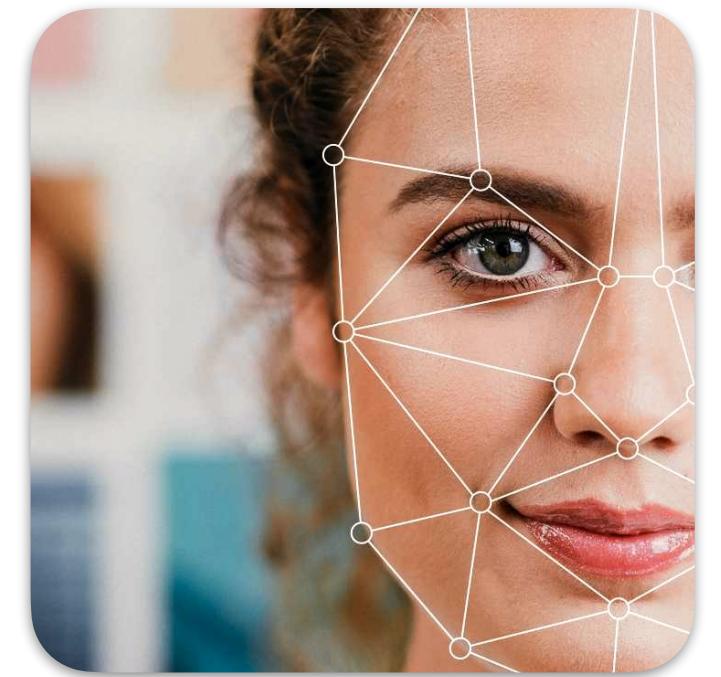
## Content



**Basics**  
Concepts  
Metrics  
Metric implementation



**Core Traits (3)**  
Concepts  
Baseline implementation  
Evaluation  
Assignments



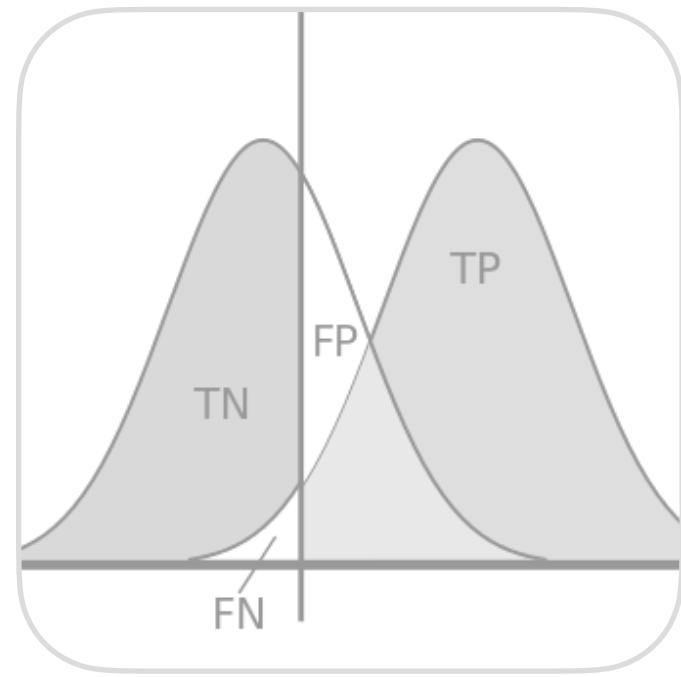
**Alternative Traits and Fusion Concepts**



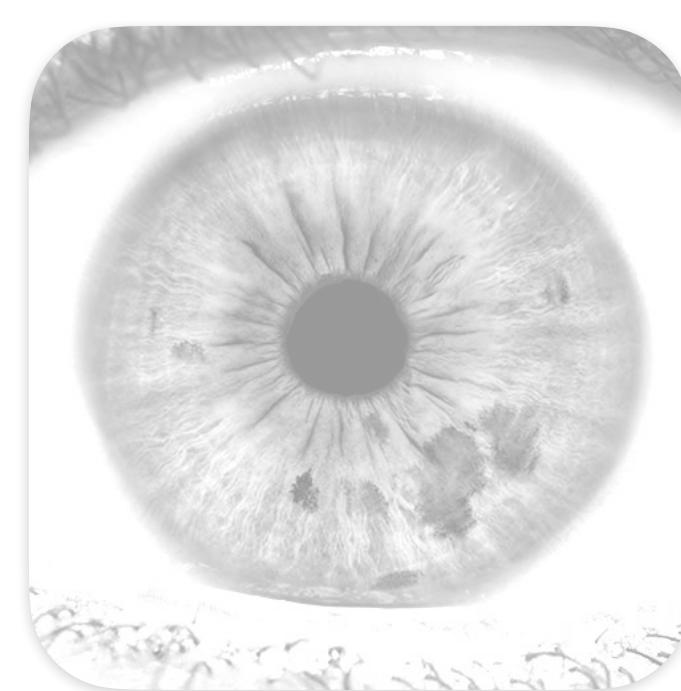
**Invited Talks (2)**  
State of the art  
Future work

# S'up Next?

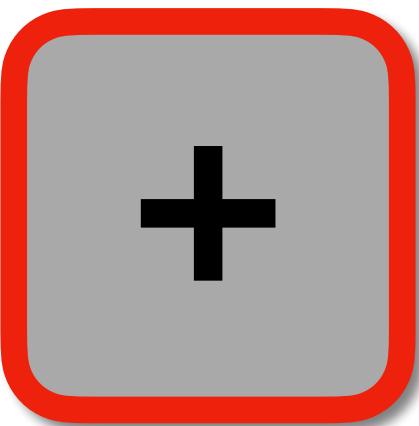
## Content



Basics  
Concepts  
Metrics  
Metric implementation



Core Traits (3)  
Concepts  
Baseline implementation  
Evaluation  
Assignments



Alternative Traits and  
Fusion  
Concepts



Invited Talks (2)  
State of the art  
Future work