

Dear Dr. Azim Eskandarian,

My colleagues and I are grateful for the opportunity to revise our paper. The reviewers have provided excellent feedback which we have utilized to improve the quality of the manuscript. Our response to each reviewer comment appears below. The reviewer comments are given in the red format and our responses are in blue.

Reviewer 1

The comments for reviewer 1 are addressed here:

1. **Reviewer:** The motivation of this study is not well introduced. Two important related works [6] and [19] by the authors themselves are still under review and are inaccessible. It is suggested to remove these works from the reference list. Ignoring the above related works, the authors shall explore other motivation of this study.

Response: We have reorganized the first section to better outline the motivation of the paper which is discussed in paragraphs 7-9 of Section I. We have also removed reference [6]. Where reference 19 is in review for the same journal, we plan to work with the editor to get both papers published in the proper order so that the computational benefits in this paper can be properly illustrated.

2. **Reviewer:** The considered problem seems not clearly introduced. The authors need to carefully describe the charging activities for each BEB in a day. Generally one bus runs several times on its planned line everyday, and therefore it may be charged more than one time on the same charger. The established mathematical model in Sections II and III, however, does not depict this feature and no relevant subscript has been defined. Please explain it.

Response: We understand the reviewer to mean that the assumed bus activities throughout the day were not well defined and that the mathematical model in Sections II and III does not include multiple charge times for each bus throughout the day, or a corresponding subscript. In Section IIa paragraph 2 we define the subscripts i, j to represent the j^{th} stop for the i^{th} bus so that each bus may charge multiple times throughout the day which we understand to include the features and subscripts the reviewer has requested.

3. **Reviewer:** The presentation of this work needs improvement. Some formulae and explanation sentences are redundant and can be removed. For example, Formula (4) and even (5) are not necessary. The first line in Formula (9) is also redundant. Fig 1 seems unnecessary as we can use Fig 3. The sentences from Formula (11) to Formula (14) together with the formulae (11), (12), (14) are wordy, and Formulae (13) and (15) are enough to express the constraints.

Response: The reviewer is right in that our presentation contains redundancy. We wanted to write so that a less experienced audience could benefit from our work which lead to some of the smaller steps the reviewer has mentioned. We understand this may not be helpful for more experienced audiences and have carefully reviewed the presentation and removed less necessary steps including line 2 of equation 9, Fig. 1, and Eqn 13.

4. **Reviewer:** As the authors use matrix form to express the constraints of the mathematical model, it is suggested to explain the dimension sizes of some matrices such as A_4 in (16) and A_8 in (47).

Response: This is a good point, we have considered doing so but feel that many of the constraints are situation dependent. For example, A_4 depends on the number of scenarios where overlap is possible and would have to be determined for each set of routes. Additionally, A_8 also depends on the number of stops each bus makes throughout the day which would need to be given along with a specific route schedule.

5. **Reviewer:** In the numerical experiments, the authors only give results for one small-scale instance with 5 buses and 5 chargers. More computational experiments with larger scales are strongly suggested to verify the effectiveness of the proposed method. Moreover, the authors shall tell the name of solver used to solve the MILP model, and explain the maximum instance scale (on the number of buses and chargers) it can solve for the established model.

Response: This is great point, we have updated our results section to include plots that show how both the runtime and monthly cost increases with the number of buses. The solver (Gurobi) was listed in paragraph 2 of Section VI. The maximum instance scale will depend on the capacity of the solving hardware. The framework itself is general enough to handle an arbitrary number of buses and chargers. We have given an example of how the runtimes increase with the number of buses so that the reader may have a general idea of what to expect.

6. **Reviewer:** In the reference list, the information of issue, volume and pages for each reference shall be provided. Besides, there are many grammar errors and typos in the work. Below are some of them. The authors shall proofread the paper thoroughly.

(a) Page2 line 6-7 right column, an MILP

(b) Page 2 line 56-57 left column, is charging

- (c) Page 3 line 58-59 left column, delete a redundant word when
- (d) Page 4 line 28-29 right column, denoted as
- (e) Page 8 line 45-46 left column, on two
- (f) Page 8 line 52-53 left column, a user's

Response: We have updated the reference list to include the issue, volume and pages for each reference where applicable. We have also included the DOI for each item for ease of reference. We have also proofread the paper and worked with an editor to remove grammar errors and typos in the work.

Reviewer 2

The comments for reviewer 2 are addressed here:

1. **Reviewer:** The related work could be presented in more detail, possibly in a separate section

Response: The review brings up a good point. We have considered using a separate section, but the paper seemed to flow better if the literature review was included as part of the introduction. We have however extended the descriptions given in our literature search to include more details that explain how previous work relates to our proposed method.

2. **Reviewer:** The domain and range of all variables should be described. Also, a table summarizing the notations should be added to enhance the readability of the paper.

Response: None

3. **Reviewer:** A comment that applies to several parts of the paper is that several formulas are being presented the authors need to use a more detailed textual description because occasionally it becomes difficult to follow them.

Response: This is a great comment, we have reviewed our paper and updated several areas with additional textual description including Equations 11 and 12. We have also removed several redundant steps such as the step from Eqn. 12 to Eqn. 13 and line 2 of Eqn. 9.

4. **Reviewer:** In addition to the results presented in VI-B and given that MILP methods are used, it is important that the authors experiment execution time and scalability using a larger setting since 5 buses and 5 chargers can be considered to be a rather small setting.

Response: Good point, we have included a section on scalability that centers on two additional figures, Fig. 12 and 13. Figure 12 shows how the cost increases with the number of buses to demonstrate that the proposed method scales well in performance. Fig. 13 describes the runtime of a larger scenario with 5 – 30 buses to show how the runtime evolves as the number of buses increases.