PROBLEM A

February 4, 2023

0.1 Problem A

0.2 A1

```
[3]: #import dependencies

import numpy as np
import pandas as pd
from pandas import Series, DataFrame
import matplotlib.pyplot as plt

import scipy
from scipy import stats
% matplotlib inline
```

UsageError: Line magic function `%` not found.

```
[4]: # load the data

ford_model = pd.read_excel(r'/home/dsm/PART_A/FORD.csv')
  tesla_model = pd.read_excel(r'/home/dsm/PART_A/TESLA.csv')

f = ford_model.head(252)
  t = tesla_model.head(252)
```

```
[5]: #print ford entries
print(f)
```

```
Date
                Open
                           High
                                       Low
                                                Close
                                                       Adj Close
                                                                     Volume
0
    44592
          19.580000
                      20.330000 19.370001
                                            20.299999
                                                       19.760141
                                                                   91361900
    44593 20.610001
                      20.850000
                                 19.920000
                                            20.660000
                                                       20.110567
1
                                                                  117651800
2
    44594 20.809999
                      21.049999
                                 20.180000
                                            20.629999
                                                       20.081366
                                                                   95377600
3
    44595 20.170000
                      20.620001
                                19.870001
                                            19.889999
                                                       19.361044
                                                                  103016000
4
    44596 18.520000
                      18.590000 17.520000
                                            17.959999
                                                       17.482370
                                                                  211100500
247
    44951
          12.600000
                      12.850000
                                 12.490000 12.790000
                                                       12.790000
                                                                   37739000
    44952 12.990000
                      13.070000 12.710000 12.920000
                                                       12.920000
                                                                   48970900
```

```
249
         44953
               12.880000
                            13.370000 12.870000
                                                   13.270000
                                                              13.270000
                                                                           62066500
         44956
    250
               13.010000
                            13.200000 12.860000
                                                   12.890000
                                                              12.890000
                                                                           64463300
    251
         44957
                 13.390000
                            13.570000
                                       13.250000
                                                   13.445000
                                                              13.445000
                                                                           50203979
    [252 rows x 7 columns]
[6]: #print tesla entries
     print(t)
                                                                   Adj Close
          Date
                       Open
                                   High
                                                 Low
                                                           Close
    0
         44592
                290.903320
                             312.663330
                                         287.350006
                                                      312.239990
                                                                  312.239990
    1
         44593
                311.736664
                             314.566681
                                         301.666656
                                                      310.416656
                                                                  310.416656
    2
         44594
                309.393341
                             310.500000
                                         296.470001
                                                      301.886658
                                                                  301.886658
    3
         44595
                294.000000
                             312.333344
                                         293.506653
                                                      297.046661
                                                                   297.046661
    4
         44596
                299.073334
                                                                  307.773346
                             312.166656
                                         293.723328
                                                      307.773346
    247
         44951
                 141.910004
                             146.410004
                                         138.070007
                                                      144.429993
                                                                  144.429993
    248
         44952
                159.970001
                             161.419998
                                                      160.270004
                                                                   160.270004
                                         154.759995
    249
         44953
                162.429993
                             180.679993
                                          161.169998
                                                      177.899994
                                                                   177.899994
    250
         44956
                178.050003
                             179.770004
                                         166.500000
                                                      166.660004
                                                                  166.660004
    251
         44957
                164.570007
                             173.748398
                                         162.779999
                                                      171.285004
                                                                  171.285004
            Volume
    0
         104436000
    1
          73138200
```

- 2 66792900
- 3 78855600
- 4 73625400
-
- 247 192734300248 234815100
- 249 305632100
- 210 000002100
- 250 230203200251 143541028
- [252 rows x 7 columns]

[40]: # describe properties f.describe()

```
「40]:
                                                                       Close
                      Date
                                  Open
                                               High
                                                             Low
               252.000000
                            252.000000
                                         252.000000
                                                     252.000000
                                                                  252,000000
      count
      mean
             44773.039683
                             14.114206
                                          14.362817
                                                       13.856746
                                                                   14.114702
      std
               105.714597
                              2.080363
                                           2.114100
                                                        2.033197
                                                                    2.070480
             44592.000000
      min
                             11.050000
                                          11.210000
                                                       10.610000
                                                                   10.950000
      25%
             44682.250000
                             12.375000
                                          12.742500
                                                       12.187500
                                                                   12.495000
```

```
50%
             44774.500000
                             13.745000
                                         13.875000
                                                      13.375000
                                                                  13.655000
      75%
             44862.750000
                             15.577500
                                         15.775000
                                                      15.332500
                                                                  15.512500
      max
             44957.000000
                             20.809999
                                         21.049999
                                                      20.180000
                                                                  20.660000
              Adj Close
                                Volume
             252.000000
                         2.520000e+02
      count
      mean
              13.895848
                         6.544592e+07
      std
               1.962912
                         2.449133e+07
      min
              10.837501
                         1.298090e+07
      25%
              12.347353 5.077075e+07
      50%
              13.471792
                         5.956675e+07
      75%
              15.295121 7.603990e+07
      max
              20.110567
                         2.111005e+08
[41]: # describe properties
      t.describe()
[41]:
                                  Open
                                              High
                                                                      Close \
                     Date
                                                            Low
               252.000000
                            252.000000
                                        252.000000
                                                     252.000000
                                                                 252.000000
      count
      mean
             44773.039683
                            247.776852
                                        253.925483
                                                     240.908320
                                                                 247.206872
      std
               105.714597
                             62.848254
                                         63.835486
                                                      61.767233
                                                                  62.741874
                                        111.750000
                                                     101.809998
      min
             44592.000000
                            103.000000
                                                                 108.099998
      25%
             44682.250000
                            209.692493
                                        220.552502
                                                     205.705002
                                                                 212.637505
      50%
             44774.500000
                            251.911667
                                        257.413330
                                                     242.483330
                                                                 251.758331
      75%
             44862.750000
                            296.651672
                                        302.702499
                                                     288.214173
                                                                 293.966667
      max
             44957.000000
                            378.766663
                                        384.290009
                                                     362.433319
                                                                 381.816681
              Adj Close
                                Volume
             252.000000
                         2.520000e+02
      count
      mean
             247.206872
                         9.464496e+07
      std
              62.741874
                         4.181675e+07
             108.099998 4.186470e+07
      min
      25%
             212.637505
                         6.702772e+07
      50%
             251.758331
                         8.411670e+07
      75%
             293.966667
                          1.025714e+08
      max
             381.816681
                          3.056321e+08
 [8]: f.sum()
 [8]: Date
                   1.128281e+07
      Open
                   3.556780e+03
      High
                   3.619430e+03
      Low
                   3.491900e+03
      Close
                   3.556905e+03
      Adj Close
                   3.501754e+03
      Volume
                   1.649237e+10
      dtype: float64
```

```
[9]: t.sum()
 [9]: Date
                    1.128281e+07
      Open
                   6.243977e+04
      High
                   6.398922e+04
      Low
                   6.070890e+04
      Close
                   6.229613e+04
      Adj Close
                   6.229613e+04
      Volume
                   2.385053e+10
      dtype: float64
[10]: f.sum(axis=1)
[10]: 0
             9.140659e+07
             1.176965e+08
      2
             9.542230e+07
      3
             1.030607e+08
             2.111452e+08
      247
             3.778401e+07
      248
             4.901592e+07
      249
             6.211152e+07
      250
             6.450832e+07
      251
             5.024900e+07
      Length: 252, dtype: float64
[11]: t.sum(axis=1)
[11]: 0
             1.044821e+08
      1
             7.318434e+07
      2
             6.683901e+07
      3
             7.890169e+07
             7.367152e+07
      247
             1.927800e+08
      248
             2.348608e+08
      249
             3.056779e+08
      250
             2.302490e+08
      251
             1.435868e+08
      Length: 252, dtype: float64
[12]: # median
      f.median()
[12]: Date
                   4.477450e+04
      Open
                   1.374500e+01
      High
                    1.387500e+01
```

```
Adj Close
                   1.347179e+01
      Volume
                   5.956675e+07
      dtype: float64
[13]: # median
      t.median()
[13]: Date
                   4.477450e+04
      Open
                   2.519117e+02
      High
                   2.574133e+02
                   2.424833e+02
      Low
      Close
                   2.517583e+02
      Adj Close
                   2.517583e+02
      Volume
                   8.411670e+07
      dtype: float64
[14]: # mean
      f.mean()
[14]: Date
                   4.477304e+04
      Open
                   1.411421e+01
      High
                   1.436282e+01
     Low
                   1.385675e+01
      Close
                   1.411470e+01
      Adj Close
                   1.389585e+01
      Volume
                   6.544592e+07
      dtype: float64
[15]: # mean
      f.mean()
[15]: Date
                   4.477304e+04
      Open
                   1.411421e+01
      High
                   1.436282e+01
     Low
                   1.385675e+01
      Close
                   1.411470e+01
      Adj Close
                   1.389585e+01
      Volume
                   6.544592e+07
      dtype: float64
[16]: # media
      t.mean()
[16]: Date
                   4.477304e+04
      Open
                   2.477769e+02
```

Low

Close

1.337500e+01

1.365500e+01

```
High
                   2.539255e+02
      Low
                   2.409083e+02
      Close
                   2.472069e+02
      Adj Close
                   2.472069e+02
      Volume
                   9.464496e+07
      dtype: float64
[17]: # standard deviation
      f.std()
[17]: Date
                   1.057146e+02
      Open
                   2.080363e+00
      High
                   2.114100e+00
      Low
                   2.033197e+00
      Close
                   2.070480e+00
      Adj Close
                   1.962912e+00
      Volume
                   2.449133e+07
      dtype: float64
[18]: # standard deviation
      t.std()
[18]: Date
                   1.057146e+02
      Open
                   6.284825e+01
      High
                   6.383549e+01
     Low
                   6.176723e+01
      Close
                   6.274187e+01
      Adj Close
                   6.274187e+01
      Volume
                   4.181675e+07
      dtype: float64
[19]: # skewness
      f.skew()
[19]: Date
                  -0.000113
      Open
                   0.627788
      High
                   0.641640
      Low
                   0.591521
      Close
                   0.640540
      Adj Close
                   0.582377
      Volume
                   2.021585
      dtype: float64
[20]: # skewness
      t.skew()
```

```
[20]: Date
                  -0.000113
      Open
                  -0.405063
      High
                  -0.422329
     Low
                  -0.388196
      Close
                  -0.401201
      Adj Close
                  -0.401201
      Volume
                   1.862001
      dtype: float64
[21]: # Kurtosis
      f.kurtosis()
[21]: Date
                  -1.192528
      Open
                  -0.155128
      High
                  -0.132661
     Low
                  -0.246695
      Close
                  -0.110457
      Adj Close
                  -0.123741
      Volume
                   7.840863
      dtype: float64
[22]: # kurtosisi
      t.kurtosis()
[22]: Date
                  -1.192528
      Open
                  -0.483477
                  -0.477637
      High
      Low
                  -0.499871
      Close
                  -0.491002
      Adj Close
                  -0.491002
      Volume
                   3.985554
      dtype: float64
[23]: # correlation coefficient of ford
      f.corr()
[23]:
                     Date
                               Open
                                          High
                                                     Low
                                                             Close
                                                                     Adj Close \
      Date
                 1.000000 -0.641805 -0.650803 -0.625817 -0.634419
                                                                     -0.590937
      Open
                           1.000000
                -0.641805
                                     0.995655
                                                0.994575 0.988481
                                                                     0.986130
      High
                -0.650803
                           0.995655
                                      1.000000
                                                0.996067
                                                          0.995167
                                                                      0.992172
      Low
                -0.625817
                           0.994575
                                      0.996067
                                                1.000000
                                                          0.995775
                                                                      0.994726
      Close
                -0.634419
                           0.988481
                                      0.995167
                                                0.995775
                                                          1.000000
                                                                     0.998316
      Adj Close -0.590937
                           0.986130
                                      0.992172
                                                0.994726
                                                          0.998316
                                                                      1.000000
      Volume
                -0.353874
                           0.310933
                                     0.322564 0.267250
                                                          0.291683
                                                                      0.276329
                   Volume
                -0.353874
      Date
```

```
Low
                0.267250
      Close
                0.291683
      Adj Close
                0.276329
     Volume
                 1.000000
[24]: # correlation coefficient of testt
      t.corr()
[24]:
                     Date
                               Open
                                                            Close
                                                                   Adj Close \
                                         High
                                                    Low
      Date
                1.000000 -0.770786 -0.782781 -0.764027 -0.774274
                                                                   -0.774274
      Open
                -0.770786 1.000000 0.996463 0.995588 0.989473
                                                                    0.989473
     High
                -0.782781
                          0.996463 1.000000
                                                                    0.995556
                                              0.996513 0.995556
     Low
                -0.764027 0.995588 0.996513
                                               1.000000 0.996384
                                                                    0.996384
      Close
                -0.774274 0.989473 0.995556 0.996384 1.000000
                                                                    1.000000
     Adj Close -0.774274 0.989473 0.995556 0.996384 1.000000
                                                                    1.000000
     Volume
                0.516943 - 0.696407 - 0.683205 - 0.708456 - 0.693845 - 0.693845
                  Volume
     Date
                0.516943
      Open
                -0.696407
     High
                -0.683205
     Low
                -0.708456
      Close
                -0.693845
      Adj Close -0.693845
      Volume
                 1.000000
     0.2.1 A2
[25]: import matplotlib.pyplot as plt
[26]: # Discard unneeded data
      f_close = pd.DataFrame(f.Close)
[27]: # Discard unneeded data
      t_close = pd.DataFrame(t.Close)
[28]: # use rolling method to calculate and plot MOVING AVERAGE
      f_close['MA_9'] = f_close.Close.rolling(9).mean().shift()
      f_close['MA_20'] = f_close.Close.rolling(20).mean()
```

Open

High

0.310933

0.322564

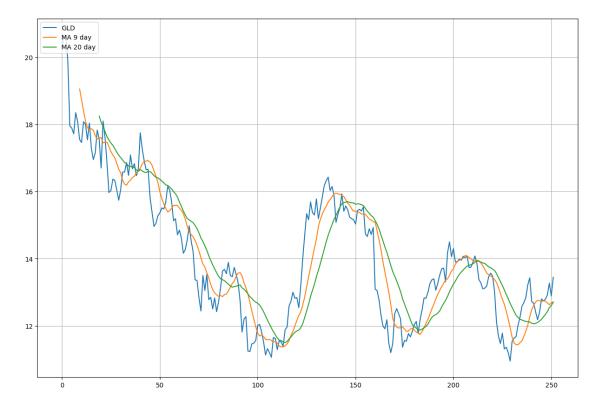
```
t_close['MA_9'] = t_close.Close.rolling(9).mean().shift()
       t_close['MA_20'] = t_close.Close.rolling(20).mean()
[29]: f_close['MA_20'].head(20)
[29]: 0
                   {\tt NaN}
        1
                   NaN
       2
                   NaN
        3
                   NaN
        4
                   NaN
                   NaN
        5
                   NaN
        6
        7
                   NaN
        8
                   {\tt NaN}
        9
                   NaN
        10
                   NaN
        11
                   NaN
        12
                   NaN
                   NaN
        13
        14
                   NaN
        15
                   NaN
        16
                   NaN
        17
                   {\tt NaN}
        18
                   NaN
        19
               18.247
        Name: MA_20, dtype: float64
[30]: t_close['MA_20'].head(20)
[30]: 0
                        {\tt NaN}
        1
                        {\tt NaN}
        2
                        {\tt NaN}
        3
                        NaN
        4
                        {\tt NaN}
        5
                        NaN
        6
                        {\tt NaN}
        7
                        {\tt NaN}
                        {\tt NaN}
        8
        9
                        {\tt NaN}
        10
                        {\tt NaN}
                        NaN
        11
        12
                        {\tt NaN}
        13
                        {\tt NaN}
        14
                        NaN
        15
                        {\tt NaN}
        16
                        {\tt NaN}
        17
                        {\tt NaN}
```

18 NaN 19 293.925497

Name: MA_20, dtype: float64

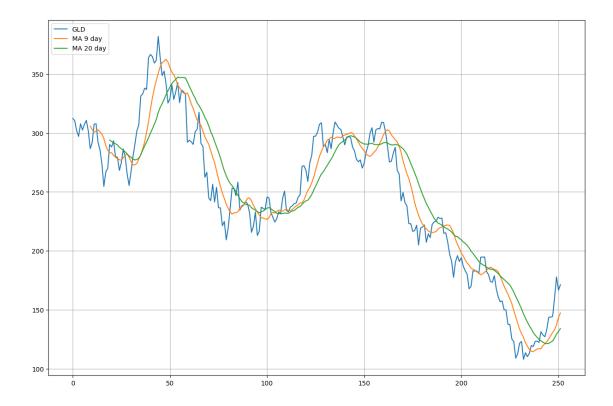
```
[31]: plt.figure(figsize=(15,10))
   plt.grid(True)
   plt.plot(f_close['Close'],label='GLD')
   plt.plot(f_close['MA_9'], label='MA 9 day')
   plt.plot(f_close['MA_20'], label='MA 20 day')
   plt.legend(loc=2)
```

[31]: <matplotlib.legend.Legend at 0x7fba8ca56d40>



```
[32]: plt.figure(figsize=(15,10))
   plt.grid(True)
   plt.plot(t_close['Close'],label='GLD')
   plt.plot(t_close['MA_9'], label='MA 9 day')
   plt.plot(t_close['MA_20'], label='MA 20 day')
   plt.legend(loc=2)
```

[32]: <matplotlib.legend.Legend at 0x7fba83bf4c70>



0.2.2 A3

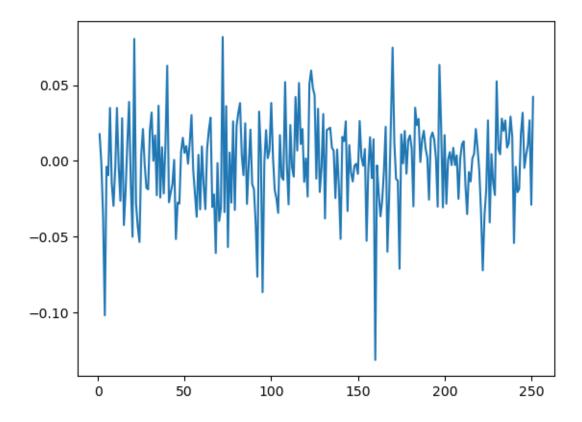
```
[33]: # Compute log change (instantaneous rate of return)
    f_close["change"] = np.log(f_close["Close"] / f_close["Close"].shift())

[34]: # Compute log change (instantaneous rate of return)
    t_close["change"] = np.log(t_close["Close"] / t_close["Close"].shift())

[35]: # Plot reveals noisy data centered around 0

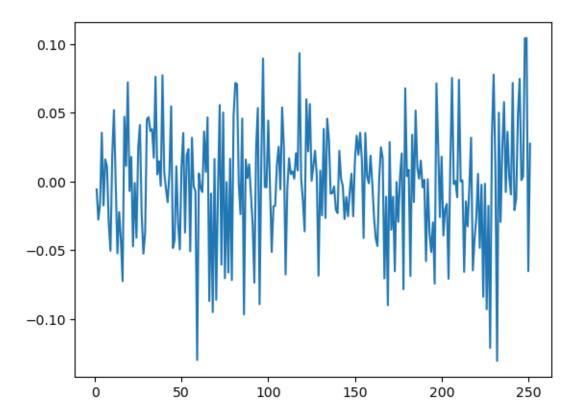
    plt.plot(f_close.change)
```

[35]: [<matplotlib.lines.Line2D at 0x7fba83c832e0>]



```
[36]: # Plot reveals noisy data centered around 0
plt.plot(t_close.change)
```

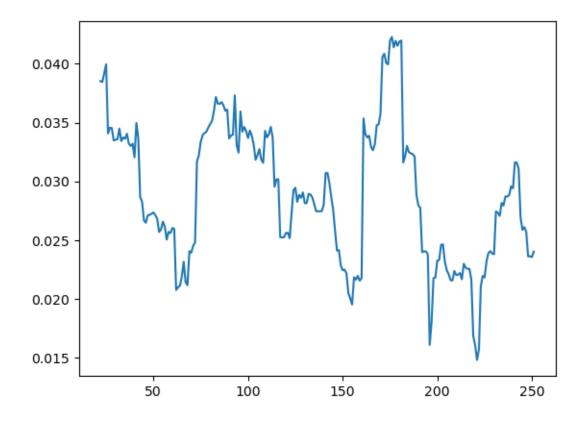
[36]: [<matplotlib.lines.Line2D at 0x7fba8492d870>]



```
[37]: # Compute rolling historical volatility, offset using .shift() method

f_close['Volatility'] = f_close.change.rolling(21).std().shift()
f_close['Volatility'].plot()
```

[37]: <AxesSubplot:>



```
[38]: # Compute rolling historical volatility, offset using .shift() method

t_close['Volatility'] = t_close.change.rolling(21).std().shift()

t_close['Volatility'].plot()
```

[38]: <AxesSubplot:>

