

# Observing floe-scale sea ice motion in the Greenland Sea marginal ice zone during summer

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## Abstract

The Fram Strait is a key region for ice export, linking the Arctic with the world ocean. We present floe-scale observations of sea ice motion in the Fram Strait marginal ice zone (MIZ) derived from moderate-scale optical imagery spanning the 2003-2020 period. Tracked ice floes provide Lagrangian measures of ice motion during the spring and summer. We show that the floe size distribution affects the rotation rates and fluctuating velocities of sea ice floes. Using simulations based on a quasi-geostrophic ocean model and a discrete element sea ice model, we show that ocean eddy forcing alone can produce the distinct non-Gaussian velocity anomaly distributions seen in observations. The scale of the velocity distributions decreases with increasing floe size and with increasing distance from the ice edge. Similarly, we show that the rotation rate distribution in both observations and simulations narrows with increasing floe size. Finally, we show that the deformation rates measured from tracked MIZ ice floes reproduce the power law scaling seen in the central Arctic, with the deformation rate decreasing as the scale of observations increases. The observations presented here provide a new avenue for sea ice model development and validation in the summer MIZ.



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**ABSTRACT.** Sea ice dynamics in the marginal ice zone are complex, resulting from coupled motions of the atmosphere and ocean interacting with a heterogeneous sea ice surface. The distribution of sea ice floe shapes and sizes affects the spatial coherence of ice motion and the response of ice to stresses. The Fram Strait is a key region for ice export, linking the Arctic with the world ocean. Complex currents, strong deformation, and low spatial correlation result in high uncertainty in sea ice drift observations. We present floe-scale observations of sea ice motion in the Fram Strait marginal ice zone (MIZ) derived from moderate-scale optical imagery spanning the 2003-2020 period. Tracked ice floes provide Lagrangian measures of ice motion during the spring and summer. We show that the floe size distribution affects the rotation rates and fluctuating velocities of sea ice floes. Simulations using a quasi-geostrophic ocean model and a discrete element model show that ocean eddy forcing alone can produce the distinct non-Gaussian velocity anomaly distributions seen in observations. The scale of the velocity distributions decreases with increasing floe size and with increasing distance from the ice edge. Similarly, we show that the rotation rate distribution in both observations and simulations narrows with increasing floe size. Finally, we show that the deformation rates measured from tracked MIZ ice floes reproduce the power law scaling seen in the central Arctic, with the deformation rate decreasing as the scale of observations increases. The observations presented here provide a new avenue for sea ice model development and validation in the summer MIZ.

INTRODUCTION

Sea ice dynamics occur across a continuum of time and space scales (McNutt and Overland, 2003), while sea ice observation systems are constrained by their minimum spatial resolution and reporting frequency (Lee and others, 2022). Advances in computational capability enable modeling centers to run Earth system models on ever-finer spatial grids. Traditional models of sea ice motion rely on a continuum approximation of sea ice dynamics (e.g., Hibler (1979)). Such models successfully reproduce many aspects of sea ice dynamics and thermodynamics (Hutter and others, 2018; Zhang, 2021). However, in the marginal ice zone (MIZ), and in other regions with high sub-grid variability, alternative approaches are needed (Herman, 2022). Validation and development of models capable of simulating small-scale sea ice variability requires observations of multi-scale sea ice motion, including observations of motion at the floe scale.

Sea ice motion in the Fram Strait and Greenland Sea is highly variable, and uncertainty in drift observations is high (e.g., Sumata and others (2014)). Ice motion results from a complex balance of forces, including atmospheric, oceanic, and internal ice stresses, Coriolis acceleration, surface tilt, and surface waves (Dumont, 2022; Dai and others, 2019; Hibler, 1979). Atmospheric and oceanic forcing are tightly coupled to the evolving sea ice interface. The effect of sharp contrasts in boundary conditions between ice-covered and open seas at the sea ice edge results in the formation of atmospheric jets (Guest and others, 2018), affecting ice motion (Heorton and others, 2014). Ocean currents (including tides) respond to seafloor topography, which can imprint on sea ice dynamics (Hakkinen, 1987; Watkins and others, 2023).

The imprint of ocean eddies on sea ice can be seen with in situ measurements (Timmermans and others, 2008) and remote sensing imagery (Manley, 1987; Johannessen and others, 1987; Kozlov and Atadzhanova, 2021). Near-surface eddies have been observed throughout the Arctic Ocean (Kozlov and others, 2019); eddy kinetic energy is particularly high in the Greenland Shelf and Fram Strait region (Von Appen and others, 2022; Armitage and others, 2017). The presence of a rich eddy field imparts a vorticity signal into ice floe motion, inducing rotation of ice floes (Manucharyan and others, 2022) and producing deformation (Zhang and others, 1999).

Spatial variability in ice motion is directly related to the floe size and the geometry of floe-floe interactions, which can lead to multifloe and aggregate motions (McNutt and Overland, 2003). The size of ice floes in the MIZ displays fractal-like power-law scaling, with bounds on minimum and maximum floe sizes determined by wave properties and coastal geometry. Floes become larger due to pieces of ice interlocking,

57 rafting, ridging and fusing, or decrease in size due to fracture (such as through collision with other floes,  
 58 wave interaction, or interaction with coastal features) and melt.

The floe size distribution (FSD) is a probability distribution characterizing the likelihood of finding ice floes of a given size in a region. The FSD affects the melt rate of ice, the spatial correlation of the sea ice response to atmospheric and oceanic stresses, and the partitioning of solar heat into the upper ocean. Rothrock and Thorndike (1984) introduced the idea of fitting a power law to the FSD such that the probability  $p(x)$  of a floe with area  $x$  is given by

$$p(x) = cx^{-\alpha} \quad (1)$$

59 where  $c$  is a normalization constant. The parameter  $\alpha$  is the slope of the power law distribution. Numerous  
 60 physical reasons cause FSD slopes to vary, including the seasonal cycle, storms and wave events, and  
 61 geographic differences (Inoue, 2004; Perovich and Jones, 2014; Geise and others, 2017; Hwang and others,  
 62 2017). Not all FSDs can be described with Equation 1, as acknowledged by Rothrock and Thorndike  
 63 (1984), and statistical issues can lead to varying  $\alpha$  estimates (Clauset and others, 2009). Nevertheless,  
 64 power laws have been frequently applied in the literature, producing a wide range of estimates for the  $\alpha$   
 65 parameter (c.f. Stern and others (2018b) comparing studies from 1984-2018).

66 Ice deformation, too, shows fractal-like properties across moderate to large scales, including scale invari-  
 67 ance in space and time (Marsan and others, 2004; Martin and Thorndike, 1985; Thorndike, 1986; Rampal  
 68 and others, 2008, 2019). Properties of the exponential relationships between deformation and the time  
 69 and space scales of measurements vary regionally and seasonally (Kwok, 2006; Stern and Lindsay, 2009;  
 70 Oikkonen and others, 2017). Spectral characteristics of sea ice deformation transition from red noise to  
 71 increasingly white noise as averaging length scales decrease (Hutchings and others, 2012). The appropriate  
 72 rheology to describe ice deformation depends on sea ice conditions, such that deformation in central Arctic  
 73 pack ice given stress from the atmosphere and ocean will be very different from deformation in the MIZ  
 74 (Herman, 2022). In particular, as the role of internal ice stress decreases, and ice floes are able to move  
 75 more freely, the time and space scales of sea ice motion are more likely to reflect the scales of atmosphere  
 76 and ocean forcing (Hutchings and others, 2012).

77 Numerous methods exist for characterizing ice properties and dynamics in the MIZ, yet gaps in the  
 78 observation network remain (Gerland and others, 2019; Lee and others, 2022). High resolution images  
 79 allow a larger portion of the FSD to be resolved (Wang and others, 2016; Stern and others, 2018a), but

have limited spatial and temporal availability; differences in spatial resolution and other data limitations make intercomparison challenging (Petty and others, 2021). Standard methods for observing ocean eddies in the world ocean (e.g., Chelton and others (2011)) are unavailable in the Arctic due to gaps in satellite coverage and the presence of sea ice; alternative approaches include manual eddy identification in synthetic aperture radar (SAR) imagery (Kozlov and others, 2019) and using sea surface topography (Kubryakov and others, 2021). Complications with melt onset in summer and subscale grid variability increase the uncertainty of remote sensing measurements of sea ice motion (Meier and others, 2000; Tschudi and others, 2020). Drifting buoy observations provide local estimates with high confidence (Webster and others, 2022), however observations in the Fram Strait and other marginal sea ice regions are sparse (Brunette and others, 2022; Gerland and others, 2019), and low spatial correlation reduces the representiveness of buoy observations.

In this article, we present sea ice observations from the Fram Strait region spanning spring and summer seasons from 2003-2020 derived from daily snapshots from optical satellite imagery using the Ice Floe Tracker algorithm (Lopez-Acosta and others, 2019). These floe-scale, Lagrangian measurements of sea ice motion address a major data gap for sea ice dynamics in the summer marginal ice zone (MIZ). Our focus is on how unique properties of the MIZ contribute to the temporal and spatial scales of sea ice motion, including effects of an evolving floe size distribution (FSD), proximity of the sea ice edge, and the presence of a rich upper ocean eddy field.

The remainder of the paper is as follows. In section 2, we describe the observational data sources and our model setup. In section 3, we describe the analysis methods. Results are presented and discussed in section 4. The paper is concluded in section 5.

## DATA

### Observations

We obtained Moderate Resolution Imaging Spectroradiometer (MODIS) imagery of the Fram Strait region from the from NASA Earthdata Worldview for April-September of each year from 2003 to 2020. We used mosaic imagery from the ascending passes (approximately local noon) for both the Aqua and Terra satellites. For each mosaic image, we assigned an overpass time using the Satellite Overpass Identification Tool (Hatcher and others, 2022).

We obtain floe-scale sea ice motion from the Ice Floe Tracker (IFT) algorithm. The IFT algorithm

is described in Lopez-Acosta and others (2019) and consists of three components: image processing, feature extraction, and floe tracking. The image processing step applies land and cloud masks, increases the contrast between water and ice, and normalizes the image. The processed image is then segmented using  $k$ -means clustering and watershed methods. Feature extraction collects shape properties (e.g., area, perimeter, best fit ellipse, centroid) from potential floes. Here we consider only potential floes with at least 300 pixels and at most 90,000 pixels (18.75 km<sup>2</sup> to 5,625 km<sup>2</sup>). False positives, including clouds and ice filaments, are removed using a circularity criterion  $C$

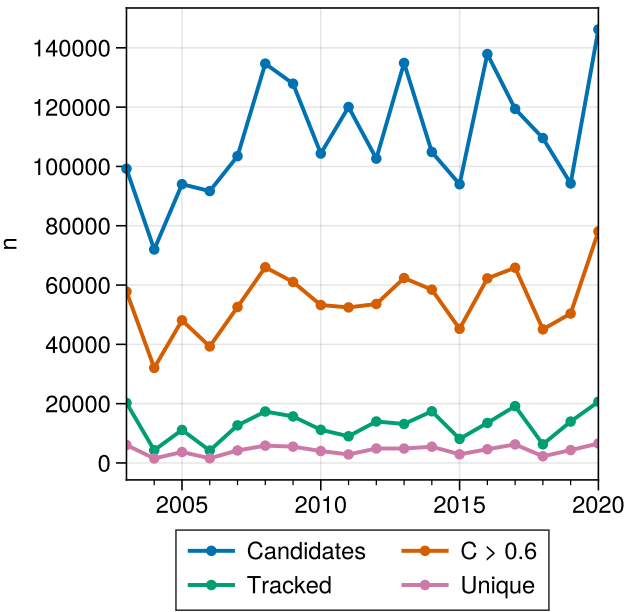
$$C = \frac{4\pi A}{P^2}, \quad (2)$$

where  $A$  is the floe area and  $P$  is the floe perimeter. The maximum circularity value is 1 (a perfect circle). Examining the distribution of  $C$  and the library of potential floe shapes from the feature extraction algorithm, we identify a local minimum of 0.6 separating false positives and ice floes. Shapes with  $C < 0.6$  are flagged and excluded from the analysis. The total number of floe shapes used in the floe size distribution analysis is marked in orange in Figure 1. On average, 55,000 floes are identified per year; variance year-to-year is related both to the sea ice extent and to varying cloud cover.

The floe tracking component links floe shapes between image pairs. For each floe, candidate matches in subsequent images are first filtered by travel distance and floe area. Potential floe matches are rotated until the area difference is minimized. If the area differences is sufficiently small after rotation,  $\psi$ -s curves (Kwok and others, 1990) are calculated for each floe. These curves summarize the tangent angle and perimeter of each floe. If the  $\psi$ -s correlation is higher than 0.7, the floes are linked. Whether a floe can be tracked depends on error in the algorithm, varying cloud cover, and on whether the floe remains intact. The green line in Figure 1 shows the number of floe shapes with at least one match. Finally, the purple line in Figure 1 indicates the number of unique floes in the set of floe trajectories. On average, 4,300 unique floes are observed each year.

Daily ascending images from Aqua and Terra are separated in time by between 20 and 90 minutes, typically. Both images are analyzed. Daily rotation rates are calculated separately for the two satellites. We use the mean daily rotation across the two satellites when both are available, otherwise we use rotation from a single satellite. Rotation rates are then normalized to radians per day. Floe positions are regridded to local noon, which is typically less than 2 hours away from the two satellite overpass times. Daily displacements are estimated via forward differences. Displacements are converted into velocity units ( $m/s$ ).





**Fig. 1.** Sample size of floe observations by year. Blue shows the number of candidate shapes, orange the number of shapes passing the circularity criterion (and thus considered to be ice floes), and green shows the number of tracked floes.

Note that this measure of velocity is not identical with instantaneous velocity, as daily observations only allow measurement of net displacements rather than total path distance traveled per day.

Following the daily displacement velocity estimation we apply an additional set of quality control steps. We flag (a) drift speeds larger than 1.5 m/s (b) floes with maximum drift speed throughout the full trajectory of less than 0.005 m/s (i.e., two pixels per day) and (c) floes with total travel distance of less than 250 m (one pixel) per day.

We use the National Snow and Ice Data Center (NSIDC) Daily Ice Motion Vectors (Tschudi and others, 2020) data product to estimate the time-average sea ice velocity. The ice motion vectors are on a 25 km grid, though the effective resolution is generally coarser. The NSIDC Ice Motion Vectors daily velocity estimates are interpolated linearly to floe positions. We then calculated the centered 5, 15, and 31-day average velocity from the Ice Motion Vectors and interpolate these averages to floe positions.

Sea ice concentration (SIC) data comes from the NSIDC Climate Data Record of Sea Ice Concentration (SIC CDR, Meier and others (2021)). We apply nearest neighbor interpolation to find the sea ice concentration in the nearest grid cell to the IFT floe positions. The distance to the ice edge is approximated by finding the minimum distance between a floe and the set of pixels in the SIC CDR with concentrations

144 between 0 and 30%.

## 145 Simulations

146 We examine the effects of mesoscale and submesoscale oceanic eddies on ice motion using a discrete element  
 147 sea ice model (SubZero, Manucharyan and Montemuro (2022)) forced by a two-layer quasi-geostrophic (QG)  
 148 ocean model. We use circular sea ice floes with radii  $R_{ice} = 1, 2, \dots, 29$  km. For each  $R_{ice}$ , we randomly  
 149 place  $n = 4,000$  floes onto the QG ocean flow field and allow the floes to be advected by the ocean currents  
 150 for 30 model days. The main adjustable parameters of the QG model are the bulk vertical shear  $\Delta U$ ,  
 151 the Rossby deformation radius,  $R_d$ , and the top/bottom ocean layer depth ratio  $\delta$ . Best-fit values of the  
 152 model  $\Delta U = 1.8$  m/s,  $R_d = 5.2$  km, and  $\delta=1$  were obtained using a loss function based on observed and  
 153 modeled floe rotation rates with data from the western Arctic Ocean (Beaufort Sea). Ocean model tuning  
 154 is described in Manucharyan and others (2022). The ocean flow fields were acquired after a simulation  
 155 year, ensuring statistical equilibration and a constant energy spectrum. Ocean fields were updated daily  
 156 in the simulation to align the simulation resolution with the temporal resolution of the observed sea ice  
 157 data. The time step for sea ice floes is set at 0.01 simulation day. 256 Fourier modes were used to simulate  
 158 domains of  $400 \times 400$  km in space. While we do not expect the ocean eddy field in the Greenland Sea to be  
 159 identical to the Beaufort Sea, the model allows us to compare observations to purely eddy-driven sea ice  
 160 motion.

## 161 METHODS

### 162 Floe size distribution

A common approach to estimating power law fits from empirical data is to apply a log-transform to the data and fit a line using least squares. However, Clauset and others (2009) point out that this method can be inaccurate due to the effect of sparse but impactful fluctuations in the tail of the distribution, and because the least squares fit is not testing whether the data are following a power law (see also Bauke (2007); Goldstein and others (2004)). By definition,  $x$  follows a power law if its probability distribution  $p(x)$  is proportional to  $x^{-\beta}$ , where  $\beta$  is constant; i.e.

$$p(x) \propto x^{-\beta} \quad (3)$$

Physical systems typically are bounded, e.g. there exists power law-like behavior between  $x_{min}$  and  $x_{max}$  so it is more precise to say that a power law describes the tail of the distribution. In statistics a power law is rigorously defined. We follow the approach of Clauset and others (2009), as implemented in the Python `powerlaw` package (Alstott and others, 2014). The method has three main steps. (1) Estimate  $x_{min}$  and  $\beta$ . (2) Calculate goodness of fit - if  $p > 0.1$ , a power law is a plausible hypothesis for the data. (3) Compare the power law with alternative hypothesis using a likelihood ratio test. ‘

## Velocity vector decomposition

The sea ice velocity can be expressed in reference to a mean flow  $\bar{u}, \bar{v}$  such that it contains an along-track (longitudinal) component  $u_L$  and cross-track (transverse) component  $u_T$ , with positive values indicating the direction of mean flow and  $90^\circ$  to the right of the mean flow, respectively. The longitudinal and transverse perturbation velocities  $u'_L$  and  $u'_T$  can then be computed by subtracting the mean flow from the individual floe velocities, and then calculating the longitudinal and transverse components of the velocity anomalies. Following Gabrielski and others (2015), we use centered-time averages of the NSIDC Ice Motion Vectors product to represent the mean flow. The transverse velocity component is often termed the *perturbation velocity*. Properties of  $u_T$  likely depend on the choice of the mean flow (e.g., Rampal and others (2009)), here we consider the effects of different time-average windows  $\tau \in (5, 10, 15)$  where  $\tau$  is time in days.

## Strain rate estimation

Area-averaged strain rates can be calculated from sets of point estimates of sea ice velocities by application of Green's theorem (e.g. Kwok and others (2003); Hutchings and others (2012); Rampal and others (2019); Dierking and others (2020)). Given a set of  $N$  ice floe positions and velocity estimates  $x, u(x)$ , we iterate over all possible triangles formed by subsets of floe positions and retain all triangles with minimum interior angle of  $20^\circ$  or greater. This results in 6.6 million polygons; since the number of available polygons is bounded above by a combinatorial function, the number of polygons varies widely per year. We calculate the area of the triangle via

$$A = \frac{1}{2} \sum_{i=1}^n [x_i y_{i+1} - y_i x_{i+1}]. \quad (4)$$

Note that in the summation notation above, the calculation wraps around the polygon to the origin, so for the triangles used here,  $x_4 = x_1$ . The latitude and longitude coordinates for each floe is projected into Cartesian space via the Lambert Azimuthal Equal Area projection for the area calculation. Interior

angles are calculated using the law of cosines. For angle and velocity calculations, we first transform the latitude and longitude coordinates into North Polar Stereographic coordinates. The area-averaged velocity gradients are calculated as

$$u_x = \frac{1}{A} \oint u dy \approx \frac{1}{2A} \sum_{i=1}^N [(u_{i+1} + u_i)(y_{i+1} - y_i)] \quad (5)$$

and similarly

$$v_x \approx \frac{1}{2A} \sum_{i=1}^N [(v_{i+1} + v_i)(y_{i+1} - y_i)] \quad (6)$$

$$u_y \approx -\frac{1}{2A} \sum_{i=1}^N [(u_{i+1} + u_i)(x_{i+1} - x_i)] \quad (7)$$

$$v_y \approx -\frac{1}{2A} \sum_{i=1}^N [(v_{i+1} + v_i)(x_{i+1} - x_i)]. \quad (8)$$

From these velocity gradients we calculate the strain rate components

$$\dot{\epsilon}_{shear} = \sqrt{(u_x - v_y)^2 + (u_y + v_x)^2} \quad (9)$$

$$\dot{\epsilon}_{div} = u_x + v_y \quad (10)$$

$$\dot{\epsilon}_{vort} = v_x - u_y \quad (11)$$

$$\dot{\epsilon}_{tot} = \sqrt{\dot{\epsilon}_{shear}^2 + \dot{\epsilon}_{div}^2}. \quad (12)$$

Uncertainty in the strain rate calculations depends on the uncertainty in position  $\sigma_X$  and area  $\sigma_A$ , and on the velocities. Triangle area uncertainty depends on the side lengths, so for a triangle with sides  $a, b, c$ , the uncertainty in area  $\sigma_A$  is given by

$$\sigma_A^2 = \frac{\sigma_X^2}{4}(a^2 + b^2 + c^2) \quad (13)$$

and relative uncertainty in a strain rate component  $\epsilon$  is given by

$$\frac{\delta_\epsilon}{\epsilon} = 2 \left( 4 \frac{\delta_x^2}{A} + 2 \frac{\delta_x^2}{U^2 T^2} + \delta_T^2 / T^2 + \frac{\delta_A^2}{A^2} \right)^{1/2} \quad (14)$$

From Lopez-Acosta and others (2019), the position error for ice floes is comparable to the resolution of the MODIS imagery, so  $\sigma_x \approx 255$  m, and velocity error  $\approx 0.65$  cm/s. For a right triangle with minimum angle 20, relative area uncertainty is 14% for a 10 km<sup>2</sup> triangle, dropping to 5% for triangles larger than 50 km<sup>2</sup>. For the polygons and floe velocities in our data, strain rate relative uncertainties of 10% are typical for individual measurements.

## Length scale parameter estimation

Our next task is to estimate the length scale dependence of deformation

$$\dot{\epsilon}_{tot} \sim L^{-\beta} \quad (15)$$

where  $L$  is the length scale of the observation; here, we use  $L = \sqrt{A}$ . We hypothesize that scaled total deformation

$$\dot{\epsilon}_{tot}^*(\beta) = \dot{\epsilon}_{tot}/L^{-\beta} = \dot{\epsilon}_{tot}L^{\beta} \quad (16)$$

is lognormally distributed. Lognormal distributions arise due to the central limit theorem in the case that independent random variables are combined multiplicatively rather than additively; lognormal distributions are observed in the plastic deformation of numerous materials. Under this assumption, the logarithm of the scaled total deformation is normally distributed

$$\log \dot{\epsilon}_{tot}^* \sim \mathcal{N}(\mu, \sigma^2) \quad (17)$$

with parameters  $\mu$  and  $\sigma^2$  dependent on the parameter  $\beta$

$$\mu(\beta) = \frac{1}{N} \sum_{i=1}^N \log \dot{\epsilon}_{tot,i}^*(\beta) \quad (18)$$

$$\sigma^2(\beta) = \frac{1}{N} \sum_{i=1}^N [\log \dot{\epsilon}_{tot,i}^*(\beta) - \mu(\beta)]^2 \quad (19)$$

where  $N$  is the total number of triangles. These are, of course, the standard maximum likelihood estimates for the parameters of a normal distribution. However at this stage the  $\beta$  parameter needed to calculate  $\dot{\epsilon}_{tot}^*$  is unknown. Our approach is to numerically find the maximum of the log likelihood function for  $\mathcal{N}(\mu, \sigma)$ .

The log likelihood function given  $n$  observations of deformation  $\dot{\epsilon}_{tot,i}$  and length scale  $L_i$  is

$$\begin{aligned} \log \mathcal{L}(\beta | \dot{\epsilon}_{tot}, L) = & -\frac{n}{2} \log(2\pi\sigma(\beta)^2) \\ & - \frac{1}{\sigma(\beta)^2} \sum_i^n [\dot{\epsilon}_{tot,i} - \mu(\beta)]^2 \end{aligned} \quad (20)$$

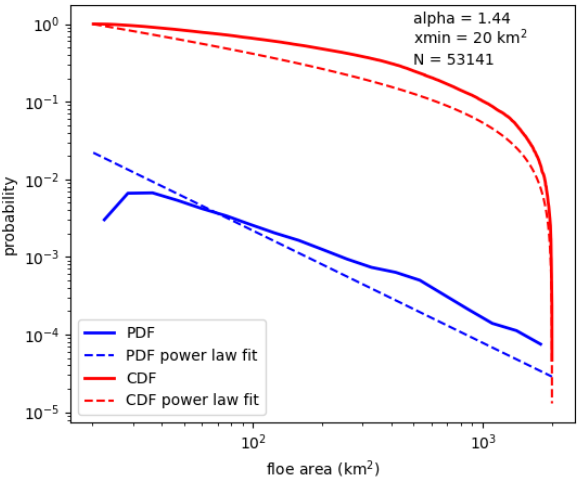
While the ice floe observations from Ice Floe Tracker are a random sample, they are not a uniform random sample in space or time. For example, ice floes cannot be detected when optically thick clouds are present. Furthermore, as the ice melts and evolves through the year, it is likely that the number of floes will change. Hence the number of floes detected will vary over time.

In order to prevent representation bias from affecting our estimates of  $\beta$  we take a stratified sampling approach. We sort the observations into 10 length scale bins ranging in size from 10 km to 300 km. The bin edges are regular in logarithmic space consistent with the parameter being based on the log-transformed data. We consider each month separately and pool all years together. Finally, we take a random sample of 1,000 observations from each length scale bin to form a sample of size 10,000. We emphasize that the bins are used for stratified sampling, and we do not average data within bins prior to estimating the length scale parameter. The parameter  $\beta$  is then estimated numerically by maximizing  $\log \mathcal{L}(\beta | \dot{\epsilon}_{tot}, L)$  over  $\beta \in (0, 1]$ . We calculate a bootstrap confidence interval for  $\beta$  using the quantile method with 1,000 bootstrap replicates.

## RESULTS

### Floe size distribution

The power law fit to the floe size distribution reveals a negative slope ( $\alpha$ ) of 1.44 (Figure 2). The  $\alpha$  is on the low range of typical alpha values for previously observed FSDs (Stern and others, 2018b). This could be because the ice exiting the Fram Strait is the thickest and oldest ice in the Arctic, and may be more resilient to break up due to its structural integrity. Uncertainty in floe area depends on the image resolution, and thus small floes have a much higher relative uncertainty. The deviation from the best fit line at floe sizes lower than  $\approx 100 \text{ km}^2$  may indicate a bias in the retrieval rate of small floes compared to large floes. Nevertheless, the empirical distributions show that sampled floes cover a wide range of sizes. While the lack of small floes needs to be addressed prior to investigating, for example, seasonal or interannual variability in the floe size distribution, the data do allow investigation of the effects of floe size on sea ice



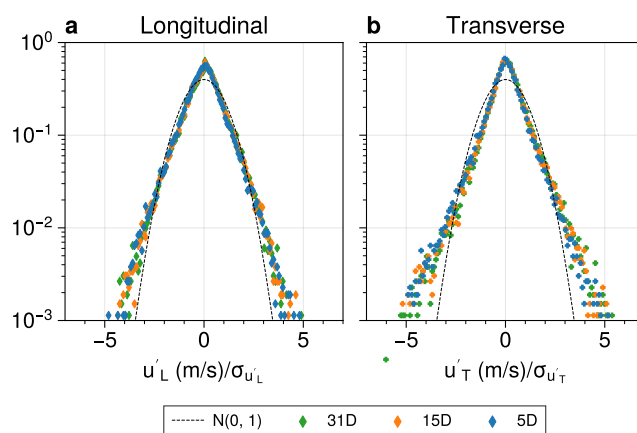
**Fig. 2.** Floe size distribution for floes identified in the Fram Strait with the Ice Floe Tracker. The probability distribution function (blue) and the complementary cumulative distribution function (red) for the data (solid line) and best fit (dashed line).

motion.

**Velocity distribution**

The distributions of the scaled velocity perturbations  $u'_L$  and  $u'_T$  are non-Gaussian (Figure 3). The shape of the distribution is relatively insensitive to the choice of averaging timescale  $\tau$  used for computing the background flow field. Differences in standard deviations between the three  $\tau$  values are  $O(0.1)$  cm/s, ranging from 8.8-9.1 cm/s for the longitudinal component and from 6.5-6.9 cm/s for the transverse component. As the fluctuating velocity distributions show little  $\tau$  dependence, we focus on results for  $\tau = 5D$  hereafter.

We now consider the role of ocean eddies, floe size, and distance to the ice edge on the velocity anomaly distributions. Non-Gaussian velocity anomaly distributions have been observed in sea ice in the central Arctic have been noted by Rampal and others (2009), and for open ocean drifters by Bracco and others (2000). The physical reasons for non-Gaussian velocity distributions may differ in the MIZ compared to the central Arctic. The QG model simulations test whether an ocean eddy field could produce the observed velocity characteristics. We find that the simulated velocity distributions show excellent agreement with the observations (Figure 4a-b). From this, we see that in the absence of winds, a turbulent ocean alone can produce sea ice velocity anomalies with the observed non-Gaussian distribution. Considering the standard



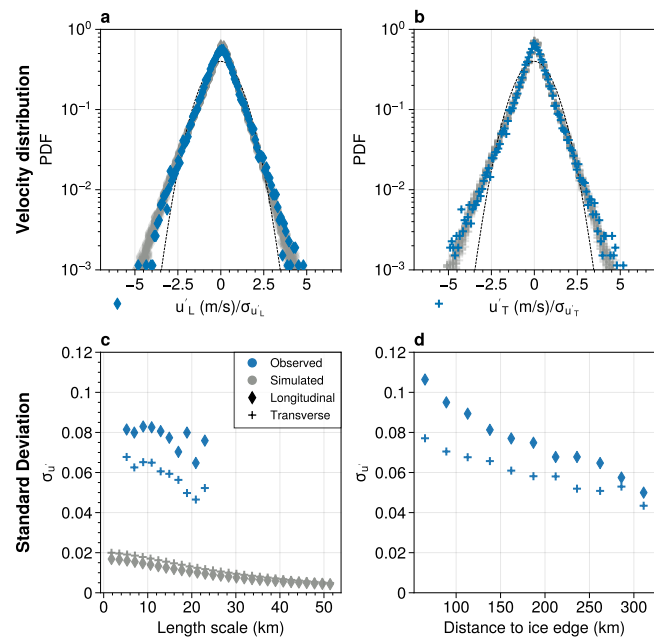
**Fig. 3.** Empirical probability distribution functions (PDFs) of scaled longitudinal (a) and transverse (b) velocity perturbations of Ice Floe Tracker floe displacements with respect to the 5-day (blue circles), 15-day (orange crosses), and 31-day (green squares) centered mean NSIDC gridded ice motion. Black lines show the PDF of a normal distribution with mean 0 and standard deviation 1.

deviations  $\sigma_{u'}$  of observations (within 2 km length bins) against the simulation results, we find in both cases that  $\sigma_{u'}$  decreases as the floe size increases (Figure 4c). However, the observed  $\sigma_{u'}$  is much larger than in the simulations. While there is a difference between longitudinal and transverse components in the simulations, with simulated transverse  $\sigma_{u'}$  slightly larger, we find the observed longitudinal  $\sigma_{u'}$  to be notably larger than transverse  $\sigma_{u'}$ .

The Beaufort Sea is known to have a less energetic eddy field than the Greenland Sea (Armitage and others (2017), e.g.). A QG-model tuned to the Greenland Sea would likely have different properties than the model we used. Secondly, the simulations are showing the velocity distribution in the absence of floe interactions, large-scale currents, and wind forcing. It is likely the case that the presence of a rapidly varying wind field would amplify the sea ice velocity perturbations. Model results presented by Rallabandi and others (2023) suggest that a stochastic wind field and interacting sea ice floes can also produce non-Gaussian sea ice velocity distributions. In any case, the results underscore the need for eddy-resolving ocean currents to correctly simulate ice motion in the MIZ.

The QG model simulates a homogeneous ocean. The position of the ice edge, coast interactions, and highly variable, shallow bathymetry produce a heterogeneous seascape in the Greenland Sea. From Figure 4d, we see a strong dependence of  $\sigma_{u'}$  on the proximity of the sea ice edge. The proximity of the ice edge reduces internal ice stress. More important, however, may be the effects of coupled air-ice-ocean interactions.





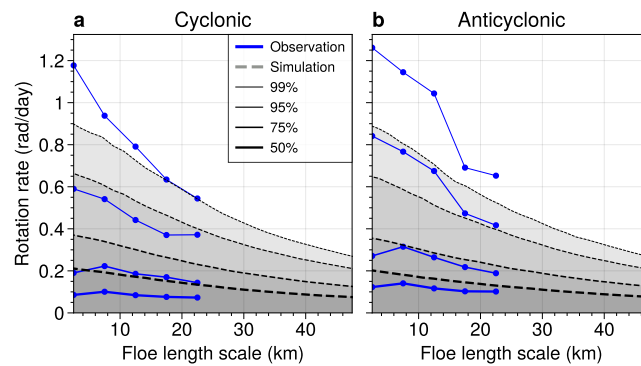
**Fig. 4.** Observed (blue) and simulated (gray) scaled velocity distributions (top) and standard deviations (bottom). As in Figure 3, a reference  $N(0,1)$  distribution is shown in panels a and b with a dotted line. Observed  $\sigma_{u'}$  in (c) and (d) are bin averages. In (c), 2 km bins are used, while in (d), 25 km bins are used. Only bins with at least 300 observations are shown. Length scale is the square root of floe area.

The FSD affects the velocity field by determining the scales of local velocity correlations. While the dependence is not as strong as with the distance to ice edge, we find higher standard deviations of the fluctuating velocities for small floes relative to large floes (Figure 4b), indicating larger departures from the local mean flow field.

### Rotation rates

The ability of Ice Floe Tracker to resolve sea ice rotation is a key advancement for remote sensing of sea ice motion. However, in the current version of the algorithm, the number of measured rotation rates is much smaller than the number of resolved floes, as a rotation rate can only be calculated for tracked floes where the floe is observed by the same satellite on two consecutive days. Nevertheless, enough rotation rates were calculated to examine the relationship between floe size and rotation rates.

In both the simulations and the observations, we see a narrowing of the rotation rate distribution as floe size increases (Figure 5). The highest rotation rates are seen in the smallest floes. Since a sea ice floe moves as a solid body, ocean stresses are integrated across the full floe. The lower rotation rates of



**Fig. 5.** Observed (blue lines) and simulated (gray shading, black dashed lines) rotation rate percentiles versus floe length scale. Observation percentiles are calculated within 5 km length scale bins. Only bins with at least 100 observations are shown. Lines from thickest to thinnest indicates the 50th, 75th, 95th, and 99th percentiles.

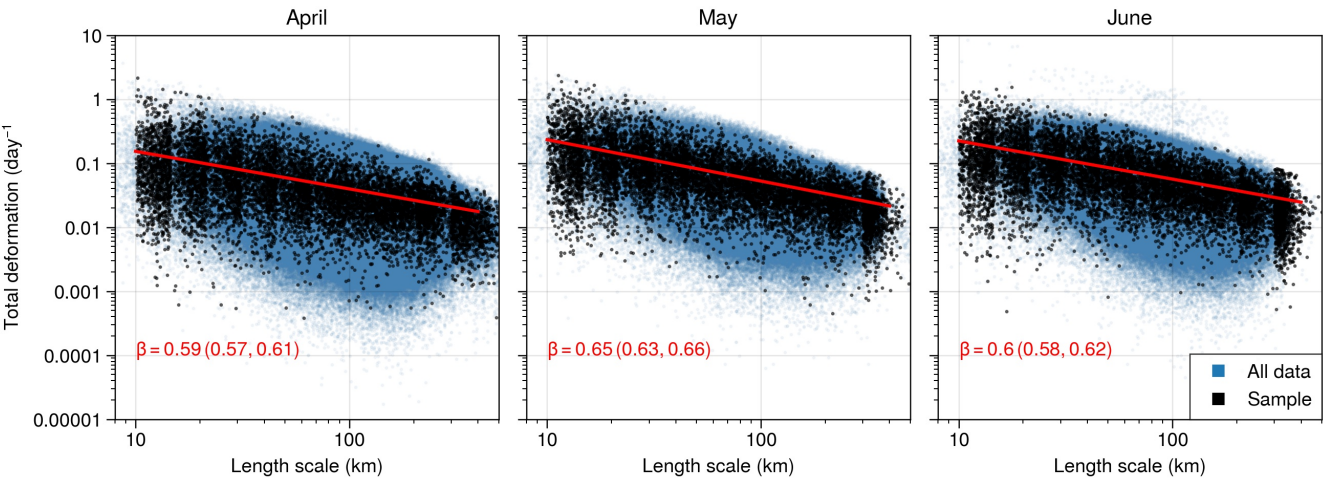
large floes may then reflect the ocean currents varying over smaller scales than the size of the floe. The relationship between ocean vorticity and floe shape depends on the size scales of ocean eddies and sea ice floes. The detailed kinematics of the eddy-floe size relationship will be addressed in a future publication.

The observed rotation rate distributions, while showing a similar scale dependence as the simulations, have narrower peaks and wider tails. The floe observations are not limited to low sea ice concentrations. The narrow peak may therefore indicate constraints on the rotation rate from floe interactions, while the wider tails may arise from the more energetic eddy field in the Greenland Sea compared to the simulations.

## Deformation length scales

Total deformation decreases with increasing length scale (Figure 6). Estimated length scale parameters range from  $\beta = 0.59$  in April to  $\beta = 0.65$  in May; based on the bootstrap confidence intervals, the May parameter is highest, however the practical difference is not large. These scaling parameters are much steeper than has been observed in the central Arctic winter pack ice (e.g.,  $\beta = 0.21$  in Hutchings and others (2012) and  $\beta = 0.2$  in Marsan and others (2004)), and is similar to the values found for small length scales by Oikkonen and others (2017). They found  $\beta$  increasing from 0.52 to 0.82 as the time interval decreased from 24 hours to 10 minutes. They further found lower deformation rates as the distance from the ice edge increased.

Comparison of the log-transformed scaled deformation rates with a normal distribution in a probability plot (not shown) indicates that the deformation rates are left-skewed, i.e., small deformation rates are more frequent than would be expected given the  $\mu$  and  $\sigma^2$  parameters given in equations 18 and 19. Given the



**Fig. 6.** Total deformation as a function of length scale for all polygons (blue) and for the stratified sample (black) for (a) May, (b) June, and (c) July. The maximum likelihood estimate for  $\beta$  assuming a lognormal distribution is shown with the red line. The length scale parameter  $\beta$  and corresponding bootstrap 95% confidence intervals are provided in the lower left of each panel.

known strong gradients in the East Greenland Sea ice velocity field it is likely that the skewed distributions are a result of including regions with different deformation properties. We can expect stronger deformation where sea ice concentration is lower, and we can expect there to be stronger deformation near the sea ice edge.

## CONCLUSIONS

The floe-scale observations presented here represent a new category of observations for the summer marginal ice zone. These observations complement existing in situ and remote sensing techniques by increasing the sample size of floe-scale displacement observations in the MIZ relative to available drifting buoy observations, by linking floe shapes with ice dynamics, and by producing floe rotation rates. The observations provide point estimates of ice displacements in a season and location where other observations are lacking or have high uncertainty: during the melt season and in the marginal ice zone.

We showed observational and model-based evidence that the both sea ice velocity anomalies and rotation rates are related to the floe size. In particular, as floe size increases, the scale of the velocity anomaly and rotation rate distributions decreases. The simulations show that the observed scale dependence can arise from ocean turbulence in the absence of winds and large-scale currents. This study marks the first time, to our knowledge, that the deformation length scales parameter in the MIZ has been calculated using floe-

scale remote sensing observations. Further work will examine the interannual variability in the deformation length scale.

A major motivation of the work presented here is to enable model development, including new parameterizations of FSD effects in sea ice models and representation of mesoscale and submesoscale sea ice-ocean interactions. Work toward improved metrics for discrete element sea ice models is underway.

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