

Exercise: Units of the wave equation

mass  $\times$  acceleration = forces

$$[kg] \quad \left[ \frac{m}{s^2} \right] \quad [N] = \left[ \frac{kg \cdot m}{s^2} \right] \text{ Newton}$$

We mostly use the wave equation written as

$$\rho \frac{\partial^2 u}{\partial t^2} - \nabla \cdot \underline{T} = \underline{f}$$

What are the corresponding units?

The material properties are given by

- density  $\rho$

- bulk & shear modulus, Young modulus,  
Lamé parameters

→ what follows for the elastic  
tensor  $\underline{\underline{C}}$ ?

Consider Hooke's law

$$\underline{\underline{T}} = \underline{\underline{C}} : \underline{\underline{\epsilon}} \quad \text{with strain } \underline{\underline{\epsilon}} \\ \text{and stress } \underline{\underline{T}}$$

What are the units of  $\underline{\underline{T}}$  and  $\underline{\underline{\epsilon}}$ ?