Exercise: Units of the wave equation mass x acceleration = forces  $\begin{bmatrix} \frac{m}{s^2} \end{bmatrix}$   $\begin{bmatrix} N \end{bmatrix} = \begin{bmatrix} \frac{k_g}{s} \\ \frac{m}{s^2} \end{bmatrix}$  Newton

We mostly use the wave equation written as

 $S \partial_{\ell}^{2} u - \nabla \cdot T = f$ 

What are the corresponding units?

The material properties are given by

- density 9

- bulk & shear modulus, Young modulus, Lamé parameters

- what follows for the clastic tusor  $\leq$  ?

Consider Hocke's law

and stress T

What are the units of I and E?

Response:  $\int \frac{\lambda_2}{\lambda_1} u - \nabla \cdot \vec{l} = f$   $\begin{bmatrix} \frac{\lambda_2}{m_3} \end{bmatrix} \begin{bmatrix} \frac{m}{m_2} \end{bmatrix} \begin{bmatrix} \frac{N}{m_2} \end{bmatrix} \begin{bmatrix} \frac{N}{m_3} \end{bmatrix}$ with f: force per unit volume- bulk 8 shear modulus, Young modulus,

Lamé parameter  $\begin{bmatrix} GP_0 \end{bmatrix} = \begin{bmatrix} 10^9 P_0 \end{bmatrix} \text{ with } \begin{bmatrix} P_0 \end{bmatrix} = \begin{bmatrix} \frac{N}{m_2} \end{bmatrix}$ Paseol

unit of pressure

typical values for rocke:  $\lambda_1 u \sim 20 - 120 GP_0$ 

For isotropic media

Cijki = 2 fij ske + M(sik sjut fie sik)

has units [Pa]

Considering Hooke's law  $T = C = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \left[ \nabla_{n} + (\nabla_{n}) \right]^{\frac{1}{2}}$   $= \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \left[ \nabla_{n} + (\nabla_{n}) \right]^{\frac{1}{2}}$   $= \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \left[ \nabla_{n} + (\nabla_{n}) \right]^{\frac{1}{2}}$ as dimensionless

Stroin is the change in length Example on strain: compared to original length En change of length original length 2s estimate & v 4A - max.

amplitude displacement Let's assume à harmanie wave  $u(x, t) = A \sin(\omega t - kx)$ χ W: Insular frequency k: warenember wavelergh with warrlength 2 = vT, period T = 2TT and thus  $a = \frac{2\pi}{6}$ Given  $(\lambda, v)$ : period  $T = \frac{\lambda}{v}$ = 8 hm = 1.6s 5 km/s frequency w= 2TT 23.9 (ad) wavenumber h = 2TT

~0.8 (km)

Harmonic wave

$$u(x,t) = A \sin(\omega t - kx)$$

$$= A \sin(\frac{2\pi}{\lambda}(\omega t - x))$$

$$\frac{\partial}{\partial x} u = -\frac{2\pi}{3} A \cos\left(\frac{2\pi t}{T} - \frac{2\pi x}{3}\right)$$

leads to 
$$\varepsilon_{max} \sim \frac{2\pi A}{\lambda} = \frac{2\pi 0.04m}{8 \text{ km}}$$